# Introduction to NumPy

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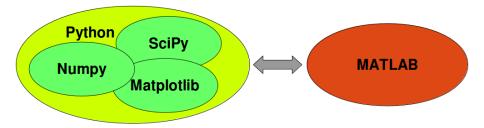
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## What is NumPy?

- Acronym for "Numeric Python"
- Open source extension module for Python.
- Powerful data structures for efficient computation of multi-dimensional arrays and matrices.
- Fast precompiled functions for mathematical and numerical routines.
- Used by many scientific computing and machine learning packages.
   For example
  - Scipy (Scientific Python): Useful functions for minimization, regression, Fourier-transformation and many others.
  - ► *Theano*: Deep learning, mimimization of custom objective functions, auto-gradients.
- Downloading and installing numpy: www.numpy.org

### The Python Alternative to Matlab

- Python in combination with Numpy, Scipy and Matplotlib can be used as a replacement for MATLAB.
- Matplotlib provides MATLAB-like plotting functionality.



## Comparison between Core Python and Numpy

- "Core Python": Python without any special modules, i.e. especially without NumPy.
- Advantages of Core Python:
  - high-level number objects: integers, floating point
  - containers: lists with cheap insertion and append methods, dictionaries with fast lookup
- Advantages of using Numpy with Python:
  - array oriented computing
  - efficiently implemented multi-dimensional arrays
  - designed for scientific computation

## A simple numpy Example

- NumPy needs to be imported. Convention: use short name np import numpy as np
- Turn a list of temperatures in Celsius into a one-dimensional numpy array:

```
>>> cvalues = [25.3, 24.8, 26.9, 23.9]
>>> np.array(cvalues)
[ 25.3 24.8 26.9 23.9]
```

Turn temperature values into degrees Fahrenheit:

• Compare to using core python only:

>>> [ 
$$x*9/5 + 32$$
 for x in cvalues] [77.54, 76.64, 80.42, 75.02]

## Creation of evenly spaced values (given stepsize)

- Useful for plotting: Generate values for x and compute y = f(x)
- Syntax:

```
arange\left( \left[\,start\,\,,\right]\,\,stop\left[\,,\,\,step\,\,,\right]\,,\,\,dtype\!\!=\!\!None\right)
```

- Similar to core python range, but returns ndarray rather than a list iterator.
- Defaults for start and step: 0 and 1
- dtype: If it is not given, the type will be automatically inferred from the other input arguments.
- Don't use non-integer step sizes (use linspace instead).
- Examples:

```
>>> np.arange(3.0)
array([ 0., 1., 2.])
>>> np.arange(1,5,2)
array([1, 3])
```

## Creation of evenly spaced values (given number of values)

```
linspace(start, stop, num=50, endpoint=True, \
    retstep=False)
```

- Creates ndarray with num values equally distributed between start (included) and stop (excluded).
- If endpoint=True, the end point is included additionally.

```
>>> np.linspace(1, 3, 5)
array([ 1. , 1.5, 2. , 2.5, 3. ])
>>> np.linspace(1, 3, 4, endpoint=False)
array([ 1. , 1.5, 2. , 2.5])
```

• If retstep=True, the stepsize is returned additionally:

```
>>> np.linspace(1, 3, 4, endpoint=False, \
    retstep=True)
(array([ 1. , 1.5, 2. , 2.5]), 0.5)
```

#### Exercise

• Compare the speed of vector addition in core Python and Numpy

### Multidimensional Arrays

- NumPy arrays can be of arbitrary dimension.
- 0 dimensions (scalar): np.array(42)
- 1 dimension (vector): np.array([3.4, 6.9, 99.8, 12.8])
- 2 dimensions (matrix):

```
np.array([ [3.4, 8.7, 9.9], [1.1, -7.8, -0.7], [4.1, 12.3, 4.8])
```

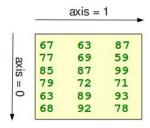
• 3 or more dimensions (tensor):

#### Question

• When can a 3 dimensional array be an appropriate representation?

### Shape of an array

```
>>> x = np.array([ [67, 63, 87],
...
[77, 69, 59],
...
[85, 87, 99],
...
[79, 72, 71],
...
[63, 89, 93],
...
[68, 92, 78]])
>>> np.shape(x)
(6, 3)
```



## Changing the shape

• reshape creates new array:

```
>>> a = np.arange(12).reshape(3, 4)

>>> a

array([[ 0, 1, 2, 3],

      [ 4, 5, 6, 7],

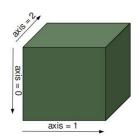
      [ 8, 9, 10, 11]])
```

Changing shape value (for existing array):

```
>>> a.shape = (2, 6)
>>> a
array([[ 0, 1, 2, 3, 4, 5],
        [ 6, 7, 8, 9, 10, 11]])
```

- Obviously, product of shape sizes must match number of elements!
- If a dimension is given as -1 in a reshaping operation, the other dimensions are automatically calculated.

## Shape of 3D Array



## Transposing an Array

• 2D case:

- Multidimensional case:
  - a.transpose(...) takes tuple of indices, indicating which axis of the old (input) array is used for each axis of the new (output) array.
  - D example:
    b = a.transpose(1,0,2)
  - $\Rightarrow$  axis 1 in a is used as axis 0 for b, axis 0 (a) becomes 1 (b), and axis 2 (a) stays axis 2 (b).

### **Basic Operations**

• By default, arithmetic operators on arrays apply *elementwise*:

```
>>> a = np.array( [20,30,40,50] )

>>> b = np.array( [0,1,2,3] )

>>> c = a-b

array([20, 29, 38, 47])

>>> b**2

array([0, 1, 4, 9])

>>> a<35

array([ True, True, False, False], dtype=bool)
```

• In particular, the elementwise multiplication ...

```
>>> a * b
array([ 20, 60, 120, 200])
```

• ... is not to be confused with the dot product:

```
>>> a.dot(b)
400
```

### **Unary Operators**

Numpy implements many standard unary (elementwise) operators:

```
>>> np.exp(b)
>>> np.sqrt(b)
>>> np.log(b)
```

• For some operators, an axis can be specified:

#### Indexing elements

• Indexing single elements:

Indexing entire sub-array:

Indexing starting from the end:

$$>>> B[-1,-1]$$
 array([321, 322])

## Indexing with Arrays/Lists of Indices

```
>>> a = np.arange(12)**2

>>> i = np.array([1,1,3,8,5])

>>> # This also works:

>>> # i = [1,1,3,8,5]

>>> a[i]

array([1, 1, 9, 64, 25])
```

## Indexing with Boolean Arrays

Boolean indexing is done with a boolean matrix of the *same shape* (rather than of providing a list of integer indices).

```
>>> a = np.arange(12).reshape(3,4)
>>> b = a > 4
array ([[False, False, False, False],
       [False, True, True, True],
       [ True, True, True, True]], dtype=bool)
>>> a[b]
array ([ 5, 6, 7, 8, 9, 10, 11])
>>> a[b] = 0
array([[0, 1, 2, 3],
     [4, 0, 0, 0],
       [0, 0, 0, 0]
```

### Slicing

- Syntax for slicing lists and tuples can be applied to multiple dimensions in NumPy.
- Syntax:

```
A[start0:stop0:step0, start1:stop1:step1, ...]
```

• Example in 1 dimension:

```
>>> S = np.array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])

>>> S[3:6:2]

array([3, 5])

>>> S[:4]

array([0, 1, 2, 3])

>>> S[4:]

array([4, 5, 6, 7, 8, 9])

>>> S[:]

array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
```

# Slicing 2D

$$A = np.arange(25).reshape(5,5)$$
  
 $B = A[:3,2:]$ 

$$B = A[3:,:]$$

$$X = np.arange(28).reshape(4,7)$$
  
 $Y = X[::2, ::3]$ 

$$Y = X[::2, ::3]$$

$$Y = X[:, ::3]$$









#### Slicing: Caveat

 Slicing only creates a new view: the underlying data is shared with the original array.

>>> A = np.array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])  
>>> 
$$S = A[2:6]$$
  
>>>  $S[0] = 22$   
>>>  $S[1] = 23$   
>>> A  
array([ 0, 1, 22, 23, 4, 5, 6, 7, 8, 9])

If you want a deep copy that does not share elements with A, use:
 A[2:6].copy()

#### Quiz

• What is the value of b?

```
>>> a = np.arange(4)
>>> b = a[:]
>>> a *= b
```

## Arrays of Ones and of Zeros

```
>>> np.ones((2,3))
array ([[ 1., 1., 1.],
       [1., 1., 1.]
>>> a = np.ones((3,4),dtype=int)
array ([[1, 1, 1, 1],
       [1, 1, 1, 1],
       [1, 1, 1, 1]
>>> np.zeros((2,4))
array([[ 0., 0., 0., 0.],
       [0., 0., 0., 0.]
>>> np.zeros_like(a)
array([[0, 0, 0, 0],
       [0, 0, 0, 0]
       [0.0,0.0]
```

## Creating Random Matrices

Array of floats uniformly drawn from the interval [0, 1):

• Generate floats drawn from standard normal distribution  $\mathcal{N}(0,1)$ :

- For repeatability of your experiment, initialize the seed at the beginning of your script:
  - $\triangleright$  >>> np.random.seed = 0
  - Otherwise, it will be initialized differently at every run (from system clock).
  - ▶ If you use core python random numbers, also initialize the seed there:

```
>>> import random
>>> random.seed (9001)
```

## Creating Diagonal Matrices

- eye(N, M=None, k=0, dtype=float)
  - N Number of rows.
  - M Number of columns.
  - k Diagonal position.
    - 0: main diagonal, starting at (0,0)
  - +n, -n: move diagonal n up/down

dtype Data type (e.g. int or float)



•  $\Rightarrow$  To create an identity matrix (symmetric  $N=M,\ k=1$ ) the size N is the only argument.

### **Iterating**

• Iterating over rows:

```
>>> for row in b:
... print(row)
...
[0 1 2 3]
[10 11 12 13]
[20 21 22 23]
[30 31 32 33]
[40 41 42 43]
```

•  $\Rightarrow$  but (!) prefer matrix operations over iterating, if possible.

## Stacking of arrays

Vertical stacking:

```
>>> a = np.array([[1,2],[3,4]])

>>> b = np.array([[11,22],[33,44]])

>>> np.vstack((a,b))

array([[1, 2],

       [3, 4],

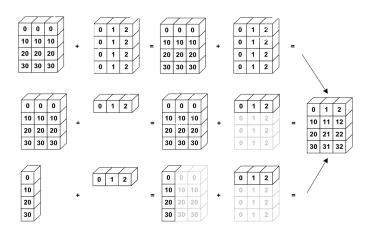
       [11, 22],

       [33, 44]])
```

Horizontal stacking:

#### Broadcasting

Operations can work on arrays of different sizes if Numpy can **transform** them so that they all have the **same size**!

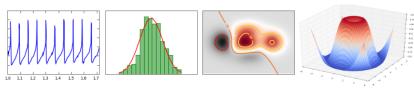


## Plotting data

- Often it is a good idea to plot some properties of the data.
  - Verify expectations that you have about the data.
  - ► Spot trends, maxima/minima, (ir-)regularities and outliers.
  - similiratities / dissimilarities between two data sets.
- Recommended package: Matplotlib/Pyplot

## **Pyplot**

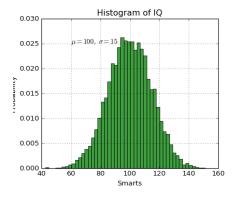
• Plotting data and functions with Python.



- Package of the matplotlib library.
- Uses numpy data structures
- Inspired by the matlab plotting commands
- Import pyplot as: import matplotlib.pyplot as plt

### Example: Histograms

- Show the empirical distribution of one variable.
- Frequency of values with equally-spaced intervals.



x = 100 + 15 \* np.random.randn(10000)
plt.hist(x, 50)

#### Ressources

• NumPy Quickstart:
 http:
 //docs.scipy.org/doc/numpy-dev/user/quickstart.html

• http://www.python-course.eu/numpy.php