Paraphrase Identification; Numpy; Scikit-Learn

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Paraphrase Identification

Paraphrase Identification

- Is a sentence (A) a paraphrase of another sentence (B)?
- Do two tweets contain the same information?
- This is a difficult problem
 - What is a paraphrase?
 - ▶ Do two exact paraphrases even exist? paraphrase ⇔ strong similarity, approximately equal meaning
 - Linguistic variation
 - ▶ Even more difficult in twitter: abbreviations, spelling errors, ...
- Examples:
 - (A) I hate Mario Chalmersdont know why
 - (B) idc idc chalmers be making me mad
 - (A) It fits the larger iPhone 5
 - (B) Should I get the iPhone 5 or an Android

SemEval-2015 Task 1: Paraphrase Similarity in Twitter

- ca. 19000 tweet pairs annotated with Amazon Mechanical Turk
- Binary classification: Pair is paraphrase (True) or not (False)
- Brainstorming: good features for recognizing paraphrases?

Strong baseline features¹

- Word overlap.
 - Most simple form: Number of common words that occur in both tweets (ignore frequency).

"overlap"

- ▶ Needs some normalization (so that there is no bias for longer tweets).
- Simple solution: Extra feature for number of unique tokens in text1 and text2.

"union"

- Word-Ngram overlap.
 - Accounts for some ordering information.
 - Otherwise same approach as for word overlap.
 - 3-grams perform well for this task
- Word-pair features
 - What if paraphrases use different, but semantically similar words?
 - Learn equivalences from tweets in training data!
 - ▶ Features for combinations: Word from text1 with word from text2.

¹Thanks to Kevin Falkner for providing extensive feature analysis. (■) (

Example: feature representation

- (A) happy Memorial Day have a happy weekend
- (B) wishing everyone a happy Memorial Day

```
{"word_overlap":4,
"three_gram_overlap":1,
"word_union":8,
"threegram_union":8,
"happy#wishing":1,
"memorial#everyone":1,
"happy#happy":1,
...}
```

Implementation

• What is the result of the follwing list comprehension?

```
l=["wishing", "everyone", "a", "happy", "memorial", "day"]
n=2
[l[i:i+n] for i in range(len(1)-n+1)]
```

• How to implement word-pair features?

Data Representation for Machine Learning

Data Representation

- Dataset: collection of instances
- Design matrix

$$\boldsymbol{X} \in \mathbb{R}^{n \times m}$$

- n: number of instances
- ▶ *m*: number of features (also called *feature space*)
- For example: $X_{i,j}$ count of feature j (e.g. a stem form) in document i.
- Unsupervised learning:
 - Model X, or find interesting properties of X.
 - Training data: only X.
- Supervised learning:
 - Predict specific additional properties from X.
 - ▶ Training data: Label vector $\mathbf{y} \in \mathbb{R}^n$ (or label matrix $\mathbf{Y} \in \mathbb{R}^{n \times k}$) together with \mathbf{X}



ullet Use matrix $oldsymbol{X}$ and vector $oldsymbol{y}$ to stack instances on top of each other.

$$\mathbf{X} = \begin{bmatrix} x_{12} & x_{13} & \dots & x_{1n} \\ x_{22} & x_{23} & \dots & x_{2n} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ x_{m2} & x_{m3} & \dots & x_{mn} \end{bmatrix} \quad \mathbf{y} = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_m \end{bmatrix}$$

Binary classification:

$$\mathbf{y} = \begin{bmatrix} 0 \\ 1 \\ \vdots \\ 0 \end{bmatrix} \dots \text{ or } \dots \begin{bmatrix} -1 \\ 1 \\ \vdots \\ -1 \end{bmatrix}$$

• Multi-class classification (one-hot-encoding):

$$m{Y} = egin{bmatrix} 0 & 0 & 1 \ 1 & 0 & 0 \ dots & & \ 0 & 1 & 0 \ \end{bmatrix}$$

Data Representation

- For performance reasons, machine-learning toolkits (scikit-learn, Keras, ...) use matrix representations (rather than e.g. string-to-count dictionaries).
- These matrix classes usually contain efficient implementations of
 - ▶ mathematical operations (matrix multiplication, vector addition ...)
 - data access and transformation (getting a certain row/column, inverting a matrix)
- What would be an appropriate underlying data-structures for the following feature sets:
 - \blacktriangleright Each feature is the grey-scale value of a pixel in a 100 \times 100 gray-scale image?
 - ► Each feature is the indicator whether a particular word (vocab size 10000) occurs in a document or not?

Data Representation

- What would be an appropriate underlying data-structures for the following feature sets:
 - \blacktriangleright Each feature is the grey-scale value of a pixel in a 100×100 gray-scale image?
 - Most of the features have a distinct value $\neq 0$. The appropriate data structure is similar to a nested list (list-of-lists). \Rightarrow Numpy Arrays
 - ► Each feature is the indicator whether a particular word (vocab size 10000) occurs in a document or not?
 - Most of the features have a value equal to 0. The appropriate data structure only stores those entries that are different than 0. (E.g with a dictionary: (row, col) \rightarrow value.) \Rightarrow SciPy Sparse Matrices

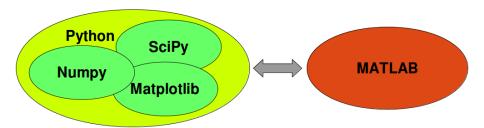
Introduction to Numpy

What is NumPy?

- Acronym for "Numeric Python"
- Open source extension module for Python.
- Powerful data structures for efficient computation of multi-dimensional arrays and matrices.
- Fast precompiled functions for mathematical and numerical routines.
- Used by many scientific computing and machine learning packages.
 For example
 - Scipy (Scientific Python): Useful functions for minimization, regression, Fourier-transformation and many others.
 - Similar datastructures exist in *Tensorflow*, *Pytorch*: Deep learning, mimimization of custom objective functions, auto-gradients.
- Downloading and installing numpy: www.numpy.org

The Python Alternative to Matlab

- Python in combination with Numpy, Scipy and Matplotlib can be used as a replacement for MATLAB.
- Matplotlib provides MATLAB-like plotting functionality.



Comparison between Core Python and Numpy

- "Core Python": Python without any special modules, i.e. especially without NumPy.
- Advantages of Core Python:
 - high-level number objects: integers, floating point
 - containers: lists with cheap insertion and append methods, dictionaries with fast lookup
- Advantages of using Numpy with Python:
 - array oriented computing
 - efficiently implemented multi-dimensional arrays
 - designed for scientific computation

A simple numpy Example

- NumPy needs to be imported. Convention: use short name np import numpy as np
- Turn a list of temperatures in Celsius into a one-dimensional numpy array:

```
>>> cvalues = [25.3, 24.8, 26.9, 23.9]

>>> np.array(cvalues)

[ 25.3 24.8 26.9 23.9]
```

Turn temperature values into degrees Fahrenheit:

Compare to using core python only:

>>> [
$$x*9/5 + 32$$
 for x in cvalues] [77.54, 76.64, 80.42, 75.02]



Creation of evenly spaced values (given stepsize)

- Useful for plotting: Generate values for x and compute y = f(x)
- Syntax:

```
arange([start ,] stop[, step ,], dtype=None)
```

- Similar to core python range, but returns ndarray rather than a list iterator.
- Defaults for start and step: 0 and 1
- dtype: If it is not given, the type will be automatically inferred from the other input arguments.
- Don't use non-integer step sizes (use linspace instead).
- Examples:

```
>>> np.arange(3.0)
array([ 0., 1., 2.])
>>> np.arange(1,5,2)
array([1, 3])
```

Creation of evenly spaced values (given number of values)

```
linspace(start, stop, num=50, endpoint=True, \
    retstep=False)
```

- Creates ndarray with num values equally distributed between start (included) and stop).
- If endpoint=True (default), the end point is included, otherwise (endpoint=False) it is excluded.

```
>>> np.linspace (1, 3, 5) array ([ 1. , 1.5, 2. , 2.5, 3. ]) >>> np.linspace (1, 3, 4, endpoint=False) array ([ 1. , 1.5, 2. , 2.5])
```

• If retstep=True, the stepsize is returned additionally:

```
>>> np.linspace(1, 3, 4, endpoint=False, \ retstep=True) (array([ 1. , 1.5, 2. , 2.5]), 0.5)
```

Exercise

Compare the speed of vector addition in core Python and Numpy

Multidimensional Arrays

- NumPy arrays can be of arbitrary dimension.
- 0 dimensions (scalar): np.array(42)
- 1 dimension (vector): np.array([3.4, 6.9, 99.8, 12.8])
- 2 dimensions (matrix):

```
np.array([ [3.4, 8.7, 9.9], [1.1, -7.8, -0.7], [4.1, 12.3, 4.8])
```

3 or more dimensions (tensor):

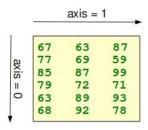
```
np.array([ [[111, 112], [121, 122]], [[211, 212], [221, 222]], [[311, 312], [321, 322]] ])
```

Question

• When can a 3 dimensional array be an appropriate representation?

Shape of an array

```
>>> x = np.array([ [67, 63, 87],
... [77, 69, 59],
... [85, 87, 99],
... [79, 72, 71],
... [63, 89, 93],
... [68, 92, 78]])
>>> np.shape(x)
(6, 3)
```



Changing the shape

• reshape creates new array:

```
>>> a = np.arange(12).reshape(3, 4)

>>> a

array([[ 0, 1, 2, 3],

      [ 4, 5, 6, 7],

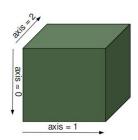
      [ 8, 9, 10, 11]])
```

Changing shape value (for existing array):

```
>>> a.shape = (2, 6)
>>> a
array([[ 0, 1, 2, 3, 4, 5],
       [ 6, 7, 8, 9, 10, 11]])
```

- Obviously, product of shape sizes must match number of elements!
- If a dimension is given as -1 in a reshaping operation, the other dimensions are automatically calculated.

Shape of 3D Array



Transposing an Array

• 2D case:

Multidimensional case:

- a.transpose(...) takes tuple of indices, indicating which axis of the old (input) array is used for each axis of the new (output) array.
- ▶ 3D example: b = a.transpose(1,0,2)
- \Rightarrow axis 1 in a is used as axis 0 for b, axis 0 (a) becomes 1 (b), and axis 2 (a) stays axis 2 (b).

Basic Operations

• By default, arithmetic operators on arrays apply *elementwise*:

```
>>> a = np.array( [20,30,40,50] )
>>> b = np.array( [0,1,2,3] )
>>> c = a-b
array([20, 29, 38, 47])
>>> b**2
array([0, 1, 4, 9])
>>> a<35
array([ True, True, False, False], dtype=bool)
```

• In particular, the elementwise multiplication ...

```
>>> a * b
array([ 0, 30, 80, 150])
```

• ... is not to be confused with the *dot product*:

Unary Operators

Numpy implements many standard unary (elementwise) operators:

```
>>> np.exp(b)
>>> np.sqrt(b)
>>> np.log(b)
```

• For some operators, an axis can be specified:

Indexing elements

• Indexing single elements:

```
>>> B = np.array([ [[111, 112], [121, 122]],
... [[211, 212], [221, 222]],
... [[311, 312], [321, 322]] ])
>>> B[2][1][0]
321
>>> B[2,1,0]
321
```

Indexing entire sub-array:

Indexing starting from the end:

$$>>> B[-1,-1]$$
 array([321, 322])



Indexing with Arrays/Lists of Indices

```
>>> a = np.arange(12)**2

>>> i = np.array([1,1,3,8,5])

>>> # This also works:

>>> # i = [1,1,3,8,5]

>>> a[i]

array([1, 1, 9, 64, 25])
```

Indexing with Boolean Arrays

Boolean indexing is done with a boolean matrix of the *same shape* (rather than of providing a list of integer indices).

```
>>> a = np.arange(12).reshape(3,4)
>>> b = a > 4
array ([[False, False, False, False],
       [False, True, True, True],
       [ True, True, True, True]], dtype=bool)
>>> a[b]
array ([ 5, 6, 7, 8, 9, 10, 11])
>>> a[b] = 0
array([[0, 1, 2, 3],
     [4, 0, 0, 0],
       [0, 0, 0, 0]
```

Slicing

- Syntax for slicing lists and tuples can be applied to multiple dimensions in NumPy.
- Syntax:

```
A[start0:stop0:step0, start1:stop1:step1, ...]
```

• Example in 1 dimension:

```
>>> S = np.array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> S[3:6:2]
array([3, 5])
>>> S[:4]
array([0, 1, 2, 3])
>>> S[4:]
array([4, 5, 6, 7, 8, 9])
>>> S[:]
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
```

Slicing 2D

$$A = np. arange (25). reshape (5,5)$$

 $B = A[:3,2:]$

$$B = A[3:,:]$$

$$X = np.arange(28).reshape(4,7)$$

 $V = X[...2 ...3]$

$$Y = X[::2, ::3]$$

$$Y = X[:, ::3]$$









Slicing: Caveat

 Slicing only creates a new view: the underlying data is shared with the original array.

```
>>> A = np.array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9]) 
>>> S = A[2:6] 
>>> S[0] = 22 
>>> S[1] = 23 
>>> A 
array([ 0, 1, 22, 23, 4, 5, 6, 7, 8, 9])
```

If you want a deep copy that does not share elements with A, use:
 A[2:6].copy()

Quiz

• What is the value of b?

```
>>> a = np.arange(4)
>>> b = a[:]
>>> a *= b
```

Arrays of Ones and of Zeros

```
>>> np.ones((2,3))
array([[ 1., 1., 1.],
      [ 1., 1., 1.]])
>>> a = np.ones((3,4),dtype=int)
array ([[1, 1, 1, 1],
       [1, 1, 1, 1],
       [1, 1, 1, 1]
>>> np.zeros((2,4))
array([[ 0., 0., 0., 0.],
       [0., 0., 0.. 0.11)
>>> np.zeros_like(a)
array([[0, 0, 0, 0].
       [0, 0, 0, 0]
       [0.0.0.0]
```

Creating Random Matrices

• Array of floats uniformly drawn from the interval [0, 1):

• Generate floats drawn from standard normal distribution $\mathcal{N}(0,1)$:

- For repeatability of your experiment, initialize the seed at the beginning of your script:
 - \triangleright >>> np.random.seed = 0
 - Otherwise, it will be initialized differently at every run (from system clock).
 - ▶ If you use core python random numbers, also initialize the seed there:

```
>>> import random >>> random.seed (9001)
```

Creating Diagonal Matrices

- eye(N, M=None, k=0, dtype=float)
 - N Number of rows.
 - M Number of columns.
 - k Diagonal position.
 - 0: main diagonal, starting at (0,0)+n, -n: move diagonal n up/down

dtype Data type (e.g. int or float)



• \Rightarrow To create an identity matrix (symmetric $N=M,\ k=1$) the size N is the only argument.

Iterating

Iterating over rows:

```
>>> for row in b:
... print(row)
...
[0 1 2 3]
[10 11 12 13]
[20 21 22 23]
[30 31 32 33]
[40 41 42 43]
```

• \Rightarrow but (!) prefer matrix operations over iterating, if possible.

Stacking of arrays

Vertical stacking:

```
>>> a = np.array([[1,2],[3,4]])

>>> b = np.array([[11,22],[33,44]])

>>> np.vstack((a,b))

array([[1, 2],

       [3, 4],

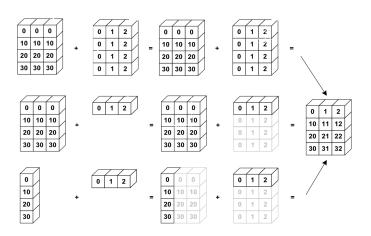
       [11, 22],

       [33, 44]])
```

Horizontal stacking:

Broadcasting

Operations can work on arrays of different sizes if Numpy can **transform** them so that they all have the **same size**!

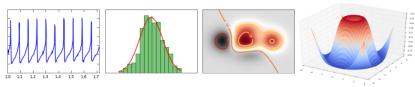


Plotting data

- Often it is a good idea to plot some properties of the data.
 - Verify expectations that you have about the data.
 - ► Spot trends, maxima/minima, (ir-)regularities and outliers.
 - similiratities / dissimilarities between two data sets.
- Recommended package: Matplotlib/Pyplot

Pyplot

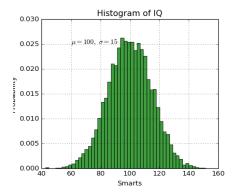
Plotting data and functions with Python.



- Package of the matplotlib library.
- Uses numpy data structures
- Inspired by the matlab plotting commands
- Import pyplot as: import matplotlib.pyplot as plt

Example: Histograms

- Show the empirical distribution of one variable.
- Frequency of values with equally-spaced intervals.



x = 100 + 15 * np.random.randn(10000)
plt.hist(x, 50)

Ressources

• NumPy Quickstart:
 http:
 //docs.scipy.org/doc/numpy-dev/user/quickstart.html

• http://www.python-course.eu/numpy.php

Scipy Sparse Matrices

Scipy Sparse Matrices

- **SciPy** is another package of the Python scientific computing stack. (NumPy+SciPy+Matplotlib~Matlab)
- scipy.sparse contains a range of sparse matrix implementations
 - Different underlying datastructures
 - slightly different use-cases
- All implementations
 - inherit from the same base class
 - provide basic matrix operations, e.g.:

get_shape()	Get shape of a matrix.
getnnz()	Number of stored values, including
	explicit zeros.
transpose ([axes, copy])	Reverses the dimensions of the sparse
	matrix.
+,add(other)	Add two matrices.
*,mul(other), dot(other)	Matrix (vector) multiplication
	4 D S 4 D S 4 D S 5

Types of Sparse Matrices

scipy . sparse . csr_matrix	Compressed Sparse Row matrix (default).
	Very efficient format for arithmetic operations.
	(Less efficient for column slicing or
	inserting/removing values)
scipy . sparse . lil_matrix	Row-based linked list sparse matrix.
	Efficient changes to matrix structure.
	(Less efficient for column slicing or arithmetic)
scipy . sparse . coo_matrix	A sparse matrix in COOrdinate format.
	Triples of row, column and value.
	Good (only) for building matrices from
	coordinates. For any operations convert to
	CSR or LIL.
scipy . sparse . dia_matrix	Sparse matrix with DIAgonal storage

What is the result?

```
import numpy as np
from scipy.sparse import csr_matrix
A = csr_matrix([[1, 2, 0], [0, 0, 3], [4, 0, 5]])
v = np.array([1, 0, -1])
A.dot(v)
```

Memory Saving

- Given:
 - ▶ 1000 docs
 - ▶ 100 unique words per doc
 - ▶ 10000 vocabulary size
- What is the expected percentage of memory used by sparse matrix (compared to dense)?

Time Saving

```
from timeit import default_timer as timer
from scipy import sparse
import numpy as np
rnd = np.random.RandomState(seed=123)
X = \text{rnd.uniform(low=0.0, high=1.0, size=(200000, 1000))}
v = rnd.uniform(low=0.0, high=1.0, size=(1000,1))
X[X<0.99]=0
v [v < 0.99] = 0
X_csr = sparse.csr_matrix(X)
v_csr = sparse.csr_matrix(v)
start = timer()
X 2 = X.dot(v)
time_dense = timer() - start
start = timer()
X_2 = X_csr.dot(v_csr)
time_sparse = timer() - start
```

 \Rightarrow 0.16 seconds (time_dense) vs. 0.01 seconds (time_sparse)

Scikit-learn Data Structures

 Now that we know about Numpy (dense) matrices, and Scipy (sparse) matrices, let's see how we can use them for machine learning with Scikit-learn.

Scikit-learn Vectorizers

- For efficiency, Scikit-learn uses matrices for its algorithms.
- However, data is often present in different forms (text; dictionaries: feature → count; ...)
- Scikit-learn provides Vectorizers to convert other data-types into matrices.
- A vectorizer object provides a mapping (e.g. from vocabulary to column indices): it is important that the same mapping is used for training, test and dev data!
- For most vectorizers, one can choose whether Dense or Sparse representation is preferred.

Loading features from dicts

- DictVectorizer can be used to convert feature arrays represented as lists of dict objects to the NumPy/SciPy representation
- Input: one dict per instance (feature counts)
 - key: feature
 - value: observed value of that feature
- Output: Design matrix
- The vectorizer constructs a feature map use the same feature map for new data! (I.e. do not create a new feature map).
- Values of the dictionary can be:
 - Numerical: the numerical value is stored in the resulting matrix in the column for that feature.
 - ▶ Boolean: two columns are created in the matrix for that feature.
 - String: several columns are created in the matrix, one for each possible value for that feature.

DictVectorizer: Example

```
>>> measurements = \Gamma
... {'city': 'Dubai', 'temperature': 33.},
... {'city': 'London', 'temperature': 12.},
... {'city': 'San Fransisco', 'temperature': 18.},
. . . ]
>>> from sklearn.feature_extraction import DictVectorizer
>>> v = DictVectorizer()
>>> v.fit_transform(measurements).toarray()
array([[ 1., 0., 0., 33.],
      [ 0., 1., 0., 12.],
      Γ 0.. 0., 1., 18.]])
>>> v.get_feature_names()
['city=Dubai', 'city=London', 'city=San Fransisco', 'temperature']
```

DictVectorizer

- Creates sparse matrices by default, can be changed to dense.
- v.fit(list_of_dicts): Creates and stores a mapping from features to matrix columns.
- v.transform(list_of_other_dicts): Applies the stored mapping to (potentially new) dictionaries.
- v.fit_transform(list_of_dicts): fit and transform in one step.

>>> v = DictVectorizer(sparse=False)

Feature hashing

- Hash function (not a rigorous definition, but sufficient for our purposes):
 - ► Function that maps every object from input space to an integer in pre-specified range
 - Regularities (e.g. sequential order) from input space are not preserved in output space, assignment looks random (for properties of interest)
- Hash collision: Two different values from input space are mapped to same output
- Applications of hash functions?

Feature hashing

- Large amounts of features also means many model parameters to learn and store (no sparsity here)
- One way of fighting amount of features: sort and take most frequent.
- Another way: use hash function to "randomly" group features together
- Hashing trick:
 - Input space: features
 - Output space: columns in design matrix
- FeatureHasher: Vectorizer that uses the hashing trick.
 - ⇒ inverse_transform is not possible

CountVectorizer: Transforming text into a design matrix

- SciPy CountVectorizer provides some functionality to create feature matrices from raw text
 - tokenization
 - lowercasing
 - ngram creation
 - occurrence counting
 - filtering by minimum word length (default=2)
 - filtering by minimum and maximum document frequency.
 - **...**
- Use cases:
 - ► CountVectorizer: Very convenient for standard usage!
 - ▶ **DictVectorizer:** You have more control if you create the features (dictionaries) yourself and use DictVectorizer

CountVectorizer

```
>>> from sklearn.feature_extraction.text import CountVectorizer
>>> corpus = [
       'This is the first document.',
... 'This is the second second document.',
... 'And the third one.',
... 'Is this the first document?',
. . . 1
>>> vectorizer = CountVectorizer()
>>> X = vectorizer.fit_transform(corpus)
>>> vectorizer.get_feature_names()
['and', 'document', 'first', 'is', 'one', 'second', 'the', 'third',
 'this'l
>>> X.toarray()
array([[0, 1, 1, 1, 0, 0, 1, 0, 1],
       [0. 1. 0. 1. 0. 2. 1. 0. 1].
       [1, 0, 0, 0, 1, 0, 1, 1, 0].
       [0, 1, 1, 1, 0, 0, 1, 0, 1]], dtype=int64)
```

CountVectorizer: unigrams, bigrams, document frequency

Summary

- Features for Paraphrase identification
 - Number of overlapping words and ngrams
 - Normalization for tweet length
 - Word pair features
- Dense and Sparse Matrices
 - Numpy arrays docs.scipy.org/doc/numpy-dev/user/quickstart.html
 - Scipy sparse matrices docs.scipy.org/doc/scipy-0.18.1/reference/sparse.html
- Scikit-learn Vecorizers
 http://scikit-learn.org/stable/modules/feature_extraction.html
- Questions?