

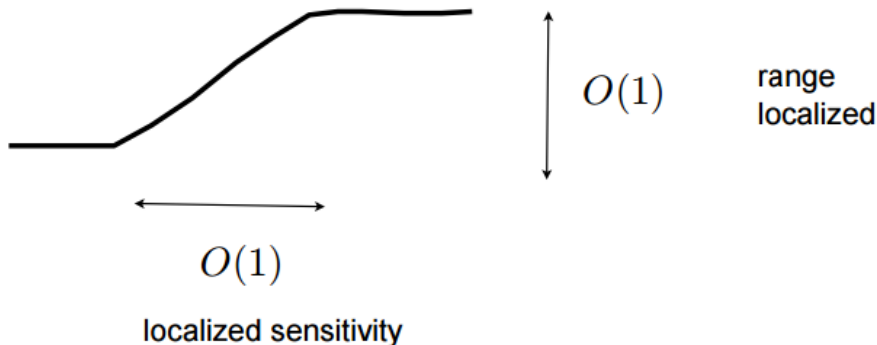
# Positive and negative feedback

Slides courtesy of prof. Rodolphe Sepulchre

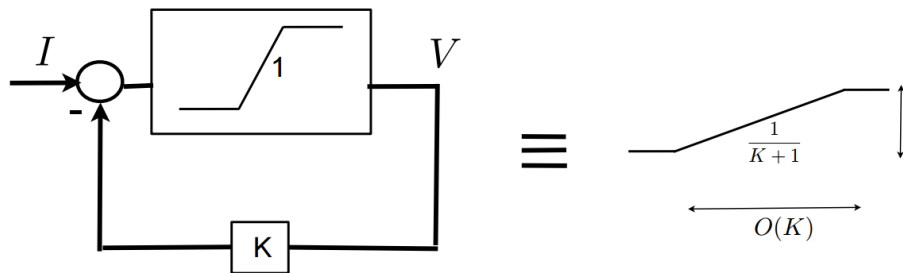
July 9, 2015

# Range-localized sensitivity is a nonlinear behavior

$$V = \text{sat}(I)$$



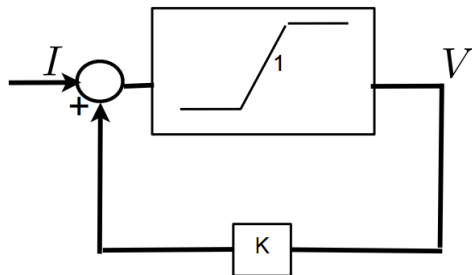
# Black principle: negative feedback 'linearizes'



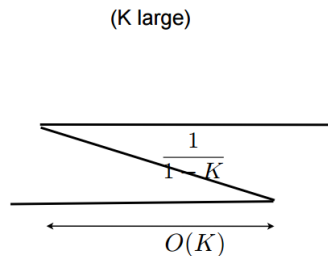
$$V = \text{sat}_1(I - KV) \equiv V = \text{sat}_{\frac{1}{1+K}}(I)$$

Sensitivity domain is spread by negative feedback  
(The essence of control theory)

# Black principle: positive feedback 'quantizes'



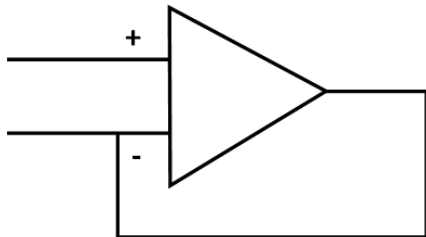
$\equiv$



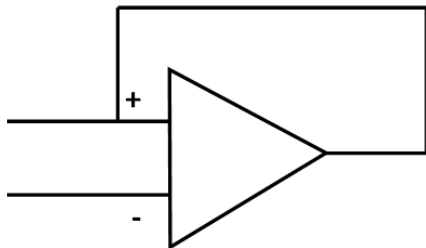
$$V = \text{sat}_1(I + KV) \equiv V = \begin{cases} +1 & I \geq -1 - K \\ -1 & I \leq K - 1 \end{cases}$$

Sensitivity domain is spread by negative feedback

# Black feedback principle

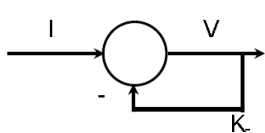


- ➊ Negative feedback linearizes
- ➋ Continuous behavior
- ➌ Analog technology
- ➍ Output primarily reflects the input
- ➎ Loops enhance or amplify the changes between input and output



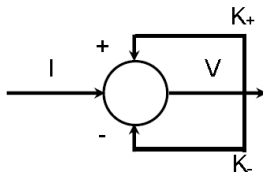
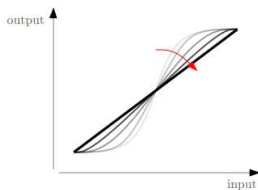
- ➊ Positive feedback quantizes
- ➋ On-Off behavior
- ➌ Digital Technology
- ➍ Output primarily reflects memory of the past
- ➎ Loops tend to dampen or buffer the changes between input and output

# Balanced feedback 'localizes'



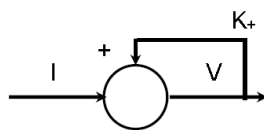
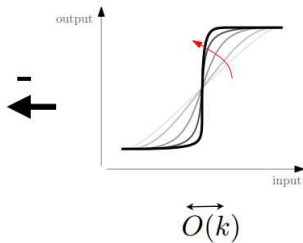
*'linear'*

$|k| \text{ large}$



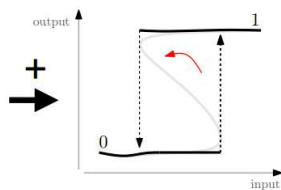
*'localized'*

$|k| \text{ small}$



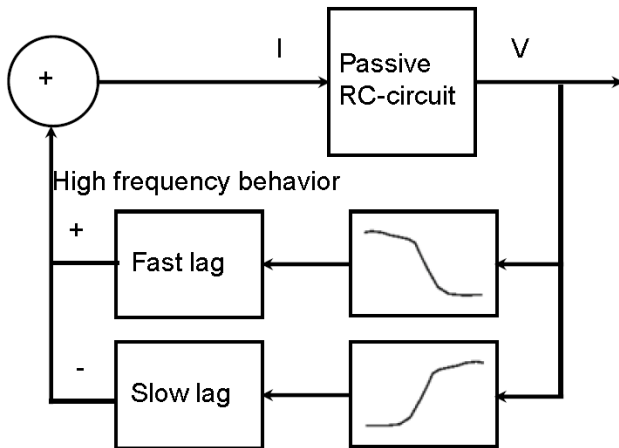
*'memory'*

$|k| \text{ large}$



$$k \approx K_+ - K_-$$

# Robust space + time localization by feedback



Low frequency behavior

Necessary localization in same frequency range!