

# Outline

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# Digital Implementation

The difference equations are typically implemented in a microcontroller or in an FPGA (field-programmable gate array) device:

$$u[k] = K_p e[k] + \frac{K_d}{T_s} (e[k] - e[k-1]) + u_i[k]$$

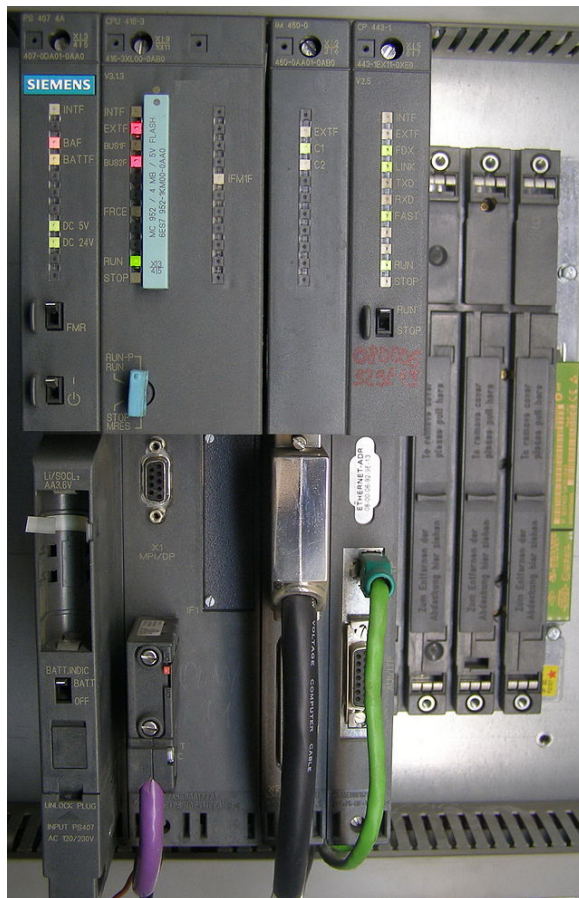
with  $u_i[k] = u_i[k-1] + K_i T_s e[k]$

## Pseudocode

```
previous_error = 0
integral = 0
Start:
error = setpoint - measured_value
proportional = KP * error
integral = integral + Ki*sampling_time*error
derivative = Kd*(error-previous_error)/sampling_time
output = proportional + integral + derivative
previous_error = error
wait (sampling_time)
goto Start
```

# Digital Implementation

PLC with a digital PID module:



Digital PID:



# PLC

A **P**rogrammable **L**ogic **C**ontroller (PLC) is a digital computer used for automation in process industry.

