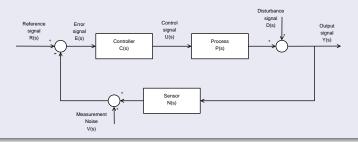
#### Outline

- Basics
  - Control Theory
  - Demo: Inverted Pendulum
- 2 Control Goals
  - Examples
  - Exercise
- Closed-loop systems
  - Sensitivity Robustness
  - Types of systems and Steady State Error
  - Noise and disturbance rejection

- Measurement noise is often modelled by zero-mean white noise.
- Disturbances are actual changes to the state of the system



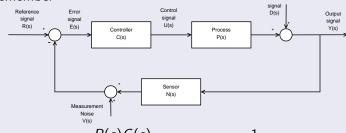
- Cruise control:
  - Measurement errors on the speed are noise
  - A change in slope is a disturbance



Disturbance

## Noise and disturbance rejection

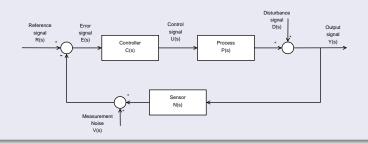




$$Y(s) = \frac{P(s)C(s)}{1 + P(s)C(s)}R(s) + \frac{1}{1 + P(s)C(s)}D(s)$$

• Setting  $M(s) = \frac{1}{1 + P(s)C(s)}$  sufficiently small results in the rejection of D. This can be achieved by choosing C(s) sufficiently high.

- What happens to the measurement noise?
  - It will be amplified and applied to the input of the plant which in turn leads to a nervous controller.



- Good disturbance rejection requires fast control actions to bring the system back to the desired state
- Good noise rejection requires slow control actions
- Note that a controller can not see the difference between measurement noise and disturbances. Slow controllers will be less sensitive to measurement noise but fast controllers will have better disturbance rejection

#### **Slow Controllers**

Not sensitive to noise Small control actions



#### **Fast Controllers**

Good disturbance rejection
Fast tracking

#### **Robust Controllers**

Model errors will not affect the behaviour of the system strongly



#### **Aggresive Controllers:**

Exchanges robustness for better performance