

Physical Chemistry Problems and Why We Care

September 13, 2016

1 Introduction

There are several concepts in *physical chemistry* that turn out to have wide applications and we are going to explore some of them here.

First, we should acknowledge that the early history is filled with people who had the luxury to explore rather esoteric topics, while we might be learning these as a matter of our own ‘development’ and with a sense of what for! I’ll try to make an argument that this stuff really does matter, but for now, let’s start the problem set!

Second, we also need to understand that these assignments have been developed as hurdles that have almost nothing to do with the end-goal of being a health-care professional. Instead, it’s better to reflect that being able to think about problem solving is actually the real goal here and we need to learn to problem solve in a systematic way.

2 Problem #2

2.1 Background

Neutron radiation is a kind of ionizing radiation which consists of free neutrons. A result of nuclear fission or nuclear fusion, it consists of the release of free neutrons from atoms, and these free neutrons react with nuclei of other atoms to form new isotopes, which, in turn, may produce radiation.

Cold, thermal and hot neutron radiation is most commonly used for scattering and diffraction experiments in order to assess the properties and the structure of materials in crystallography, condensed matter physics, biology, solid state chemistry, materials science, geology, mineralogy and related sciences. Neutron radiation is also used in select facilities to treat cancerous tumors due to its highly penetrating and damaging nature to cellular structure. Neutrons can also be used for imaging of industrial parts termed neutron radiography when using film, neutron radioscopy when taking a digital image, such as through image plates, and neutron tomography for three-dimensional images. Neutron imaging is commonly used in the nuclear industry, the space and aerospace industry, as well as the high reliability explosives industry.

The imaging is a function of the particles wavelength, λ , where higher frequencies resolve higher resolution. It's rare that one would ever have to calculate this from scratch, but the value of the exercise is ???

2.2 de Broglie Wavelength

In 1923, Louis de Broglie, a French physicist, proposed a hypothesis to explain the theory of the atomic structure. By using a series of substitution de Broglie hypothesizes particles to hold properties of waves. Within a few years, de Broglie's hypothesis was tested by scientists shooting electrons and rays of lights through slits. What scientists discovered was the electron stream acted the same as light proving de Broglie correct.

Thus, for this problem, we will determine the wavelength of a particle (neutron), which also has a mass – one of the strangest scientific theories!

In this problem we are trying to determine (calculate) the 'de Broglie' wavelength. So, let's first determine the units of a wavelength, so we have a clue where we are heading! In general, wavelength is measured as length per time, in SI units, we often see this as m/s, but for atomic particle scales, the units are often Å/second, where an Angstrom (Å) is $1 \cdot 10^{-10}$ meters, i.e very short distances! Note: an Å is not an SI unit, which is terribly lame. But let's let that go for now, I think $1 \cdot 10^{-9}$ is the SI units, which is nanometers. Whatever!

We are given the a number that includes temperature, as measured in Kelvin. Okay, that seems to be a weird parameter to be given! But let's back up. We are told that a particle accelerator generate neutrons at 2500K, where K is degrees Kelvin, i.e. a temperature. By knowing temperature, we are supposed to figure out a wavelength, weird!!!

We are given the following equation to determine velocity of the neutron

$$\mu_{rms} = \sqrt{(3k_B T/m)} \quad (1)$$

where μ_{rms} is room-mean-speed (m/s), k_B is Boltzmann's Constant ($1.38e^{-23}$ J/K) and T is temperature (degrees K) and m is the mass of the particle (kg). This equation is the root-mean square of speed (velocity) of particles – I think it's a kind of a measure of variation of speed, see http://www.studyphysics.ca/2007/20/ap_thermodynamics/42a_ap_kinetic_theory_gases.pdf for a decent explanation. For now, we'll use μ_{rms} as root-mean-square speed defined as the square root of mean square (the arithmetic mean of the squares of a set of numbers). The RMS is also known as the quadratic mean and is a particular case of the generalized mean with exponent.

Thus, the μ_{rms} is

```
> k_B = 1.38e-23
> T = 2500
> m = 1.6750e-24; m
```

```
[1] 1.675e-24
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```
> mu = sqrt(3*k_B*T/m); mu
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```
[1] 248.578
```

Thus, we have now calculated the speed as 248.58. However, I am not sure this is right. Did you get this as a intermediate answer with your prof? I need to figure out the units too!

Next, what do we do with the velocity?

Using this site: http://chem.libretexts.org/Core/Physical_and_Theoretical_Chemistry/Quantum_Mechanics/02._Fundamental_Concepts_of_Quantum_Mechanics/De_Broglie_Wavelength, we might be able to evaluate the question with some sense that we understand what in the world is happening:

$$\lambda = hp = hmv \quad (2)$$

where h is planck's constant, p is the particle momentum and m is the particle's mass and μ is the particles' velocity.

Based on this equation, we have velocity, μ , and we know the mass of the neutron, which is 0. Thankfully, h , or Planck's Constant is a known quantity, although we derive it in problem #4!

```
> h = 6.626e-34
```

```
> lambda = h * m * mu; lambda
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```
[1] 2.758856e-55
```

At this point, I am doing something wrong, because it's hard to believe that this wavelength is so small, 0. I suspect I didn't calculate the velocity correctly, seems way too slow!

3 On Planck's Constant

https://en.wikipedia.org/wiki/Planck_constant

$\lambda/\text{\AA}$ is in the units of wavelength per meter or meter/second/meter thus we are left with a time unit! Neat. I am not sure why they can tell us that! Whatever...

V_s/V so velocity of something over another velocity. Okay, this seems weird – what is the s ?

Finally, the hint is anything but a real hint – basically driving more questions that it answers.

The equation given is

$$KE = EV_s \quad (3)$$

where KE is kinetic energy (units?) and E is the charge of an electron (volts) and V_s is velocity of ??.

We can use the photo-electric equation,

$$E = h\nu \quad (4)$$

```

> one=c(2536, 2830, 3039, 3302, 3663, 4358)
> two=c(2.6, 2.11, 1.81, 1.47, 1.1, .57)
> coef(lm(one~two))

(Intercept)          two
  4713.1565    -885.1904

> plot(one,two)

```

