

# Problem Set 3

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## 1 Problem Set 3

### 2 Question 1 part 1

```
incumbents_lm <- lm(voteshare ~ difflog, data = incumbents)
summary(incumbents_lm)
```

### 3 Question 1 part 2

```
ggplot(incumbents, aes(difflog, voteshare)) +
  geom_point(alpha = 0.5) + geom_smooth(method = "lm")
```

These two functions `geom_point` and `geom_smooth` add a scatterplot and a regression line

### 4 Question 1 part 3

```
resids1 <- resid(incumbents_lm)
resids1
class(resids1)
#> [1] "numeric"
```

## 5 Question 1 part 4

$$y = 0.041666 * x + 0.579031$$

$$\beta_0 = 0.579031 \quad \beta_1 = 0.041666 \quad x_1 = \text{difflog} \quad y = \text{voteshare}$$

$$\hat{y} = \beta_0 + \beta_1 x_1$$

$$\hat{y} = 0.579031 + 0.041666 x_1$$

## 6 Question 2 part 1

```
incumbents_lm2 <- lm(presvote ~ difflog, data = incumbents)
summary(incumbents_lm2)
```

## 7 Question 2 part 2

```
ggplot(incumbents, aes(difflog, presvote)) +
  geom_point(alpha = 0.5) +
  geom_smooth(method = "lm")
```

## 8 Question 2 part 3

```
resids2 <- resid(incumbents_lm2)
resids2
class(resids2)
#> [1] "numeric"
```

## 9 Question 2 part 4

$$y = 0.023837 * x + 0.0507583$$

$$\beta_0 = 0.0507583 \quad \beta_1 = 0.023837 \quad x_1 = \text{difflog} \quad y = \text{presvote}$$

$$\hat{y} = \beta_0 + \beta_1 x_1$$

$$\hat{y} = 0.507583 + 0.023837x_1$$

## 10 Question 3 part 1

`incumbents_lm3 <- lm(voteshare ~ presvote, data = incumbents)`

`summary(incumbents_lm3)`

## 11 Question 3 part 2

`ggplot(incumbents, aes(presvote, voteshare)) +  
geom_point(alpha = 0.5) +  
geom_smooth(method = "lm")`

## 12 Question 3 part 3

$$y = 0.388018 \cdot x + 0.441330$$

$$\beta_0 = 0.441330 \quad \beta_1 = 0.388018 \quad x_1 = \text{presvote} \quad y = \text{voteshare}$$

$$\hat{y} = \beta_0 + \beta_1 x_1$$

$$\hat{y} = 0.441330 + 0.388018x_1$$

## 13 Question 4 part 1

`incumbents_lm4 <- lm(resids1 ~ resids2, data = incumbents)`  
`summary(incumbents_lm4)`

## 14 Question 4 part 2

```
ggplot(incumbents, aes(resids2, resids1)) +  
geom-point(alpha = 0.5) +  
geom-smooth(method = "lm")
```

## 15 Question 4 part 3

$$y = -0.00000000000000000486 * x + 0.25687701270009788423$$

$$\beta_0 = 0.25687701270009788423$$

$$\beta_1 = -0.00000000000000000486$$

$$x_1 = \text{resids2} \quad y = \text{resids1}$$

$$\hat{y} = \beta_0 + \beta_1 x_1$$

$$\hat{y} = 0.25687701270009788423 + -0.00000000000000000486 x_1$$

## 16 Question 5 part 1

```
incumbents_lm5 <- lm(voteshare ~ difflog + presvote, data = incumbents)
```

```
summary(incumbents_lm5)
```

## 17 Question 5 part 2

```
x1 = difflog x2 = presvote
```

$$y = 0.0355431 * x_1 + 0.2568770 * x_2 + 0.4486442$$

$$\beta_0 = 0.4486442 \quad \beta_1 = 0.0355431 \quad \beta_2 = 0.2568770$$

$$x_1 = \text{difflog} \quad x_2 = \text{presvote} \quad y = \text{voteshare}$$

$$\hat{y} = \beta_0 + \beta_1 x_1 + \beta_2 x_2$$

$$\hat{y} = 0.4486442 + 0.0355431x_1 + 0.2568770x_2$$

## 18 Question 5 part 3

The residuals for the output of the lm of incumbents-lm4 and the residuals for the out of the lm of incumbents-lm5 returns the same values for min -0.25928, 1q -0.04737 median -0.00121, 3q 0.04618, max 0.33126.