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An introduction to the vector database.

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Getting Started with Vector Databases - Introduction to Vector Similarity Search

Introduction

Hey there - welcome back to Milvus codelabs. In the previous tutorials, we took a look at unstructured data, vector databases, and Milvus - the world's most popular open-source vector database. We also briefly touched upon the idea of *embeddings*, high-dimensional vectors which serve as awesome semantic representations of unstructured data. One key note to remember - embeddings which are "close" to one another represent semantically similar pieces of data.

In this tutorial, we'll build on that knowledge by going over a word embedding example and seeing how semantically similar pieces of unstructured data are "near" one another while dissimlar pieces of unstructured data are "far" from one another. This will lead into a semi-deep dive into *nearest neighbor search*, a computing problem that involves finding the closest vector(s) to a query vector based on a unified *distance metric*. We'll go over some well-known methods for nearest neighbor search (including my favorite - ANNOY) in addition to commonly used *distance metrics*.

Excited yet? Great. Let's dive in.

Comparing embeddings

Some prep work

Before beginning, we'll need to install the gensim library and load a word2vec model.

```
1  % pip install gensim --disable-pip-version-check
2  % wget https://s3.amazonaws.com/dl4j-distribution/GoogleNews-vectors-
      negative300.bin.gz
3  % gunzip GoogleNews-vectors-negative300.bin
```

```
1  Requirement already satisfied: gensim in /Users/fzliu/.pyenv/lib/
      python3.8/site-packages (4.1.2)
2  Requirement already satisfied: smart-open>=1.8.1 in /Users/fzliu/.pyenv
      /lib/python3.8/site-packages (from gensim) (5.2.1)
3  Requirement already satisfied: numpy>=1.17.0 in /Users/fzliu/.pyenv/lib
      /python3.8/site-packages (from gensim) (1.19.5)
4  Requirement already satisfied: scipy>=0.18.1 in /Users/fzliu/.pyenv/lib
      /python3.8/site-packages (from gensim) (1.7.3)
5  --2022-02-22 00:30:34--  https://s3.amazonaws.com/dl4j-distribution/
      GoogleNews-vectors-negative300.bin.gz
```

```
 6  Resolving s3.amazonaws.com (s3.amazonaws.com)... 52.216.20.165
 7  Connecting to s3.amazonaws.com (s3.amazonaws.com)|52.216.20.165|:443...
        connected.
 8  HTTP request sent, awaiting response... 200 OK
 9  Length: 1647046227 (1.5G) [application/x-gzip]
10  Saving to: GoogleNews-vectors-negative300.bin.gz
11
12  GoogleNews-vectors- 100%[===================>]   1.53G  2.66MB/s    in
        11m 23s
13
14  2022-02-22 00:41:57 (2.30 MB/s) - GoogleNews-vectors-negative300.bin.gz
        saved [1647046227/1647046227]
15
16  gunzip: GoogleNews-vectors-negative300.bin: unknown suffix -- ignored
```

Now that we've done all the prep work required to generate word-to-vector embeddings, let's load the trained `word2vec` model.

```
1  >>> from gensim.models import KeyedVectors
2  >>> model = KeyedVectors.load_word2vec_format('GoogleNews-vectors-
       negative300.bin', binary=True)
```

Example 0: Marlon Brando

Let's take a look at how `word2vec` interprets the famous actor Marlon Brando.

```
1  >>> print(model.most_similar(positive=['Marlon_Brando']))
```

```
1  [('Brando', 0.757453978061676), ('Humphrey_Bogart', 0.6143958568572998)
      , ('actor_Marlon_Brando', 0.6016287207603455), ('Al_Pacino',
      0.5675410032272339), ('Elia_Kazan', 0.5594002604484558), ('
      Steve_McQueen', 0.5539456605911255), ('Marilyn_Monroe',
      0.5512186884880066), ('Jack_Nicholson', 0.5440199375152588), ('
      Shelley_Winters', 0.5432392954826355), ('Apocalypse_Now',
      0.5306933522224426)]
```

Marlon Brando worked with Al Pacino in The Godfather and Elia Kazan in A Streetcar Named Desire. He also starred in Apocalypse Now.

Example 1: If all of the kings had their queens on the throne

Vectors can be added and subtracted from each other to demo underlying semantic changes.

```
1  >>> print(model.most_similar(positive=['king', 'woman'], negative=['man
       '], topn=1))
```

```
1  [('queen', 0.7118193507194519)]
```

Who says engineers can't enjoy a bit of dance-pop now and then?

Example 2: Apple, the company, the fruit, . . . or both?

The word "apple" can refer to both the company as well as the delicious red fruit. In this example, we can see that Word2Vec retains both meanings.

```
1  >>> print(model.most_similar(positive=['samsung', 'iphone'], negative=[
       'apple'], topn=1))
2  >>> print(model.most_similar(positive=['fruit'], topn=10)[9:])
```

```
1  [('droid_x', 0.6324754953384399)]
2  [('apple', 0.6410146951675415)]
```

"Droid" refers to Samsung's first 4G LTE smartphone ("Samsung" + "iPhone" - "Apple" = "Droid"), while "apple" is the 10th closest word to "fruit".

Nearest neighbor search

Now that we've seen the power of embeddings, let's take a look at some of the ways we can perform exact nearest neighbor search.

Linear search

The simplest but most naïve nearest neighbor search algorithm is good old linear search: computing the distance from a query vector to all other vectors in the vector database. For obvious reasons, naïve search does not work when trying to scale our vector database to tens or hundreds of millions of vectors, but when the total number of elements in the database is small, this can actually be the most efficient way to perform vector search - a separate data structure for the index is not required, while inserts and deletes can be implemented fairly easily. Due to the lack of space complexity as well as constant space overhead associated with naïve search, this method can often outperform space partitioning even when querying across a moderate number of vectors. With all the talk nowadays about runtime complexity and horizontal scaling, remember the KISS principle for small applications and/or prototyping: Keep It Simple, Stupid.

Space partitioning

Like naïve search, space partitioning is a way of implementing NN search, guaranteeing that the closest neighbors to an input query vector are found. Space partitioning is not a single algorithm, but rather a family of algorithms that all use the same concept. KD-trees are the simplest algorithm in this family, and work by continuously bisecting the search space (splitting the vectors into "left" and "right" buckets) in a manner similar to binary search trees. Although space partitioning algorithms undoubtedly improve nearest neighbor search query tiems, performing the search can still be prohibitively expensive once database sizes become large.

Approximate nearest neighbor search

As we've seen in the previous section, exact nearest neighbor search can be pretty expensive once

Integer quantization

Quantization is a technique for reducing the total size of the database by reducing the precision of the vectors. Integer quantization works by multiplying high-precision floating point vectors with a scalar value, then casting the elements of the resultant vector to their nearest integers. This not only reduces the effective size of the entire database (e.g. by a factor of four for conversion from `float64_t` to `int16_t`), but also has the positive side-effect of speeding up vector-to-vector distance computations.

Product quantization

Product quantization is another quantization technique that works similar to dictionary compression. Imagine using a clustering algorithm such as k-means to cluster the vectors in the vector database. At query time, we can then fetch vectors that belong in the same cluster as the query vector. This cluster-based quantization method will may work well for small datasets and low- to medium-dimensional vectors, but large datasets will result in a more-than-manageable number of cluster centroids. This is where product quantization comes in – instead of computing centroids over all vector dimensions together, we can instead cluster subvectors, i.e. split each vector into 2 or more segments and perform clustering for each segment. A vector database indexed using subvector centroids is referred to as having an inverted multi-index. We won't dive too deep into the math and theory behind PQ since it is a fairly deep and well-studied topic, but if you're interested, you can check out the original PQ paper in addition to some of the extensions such as Optimized PQ and Locally Optimized PQ.

Hierarchical Navigable Small Worlds

Hierarchical Navigable Small Worlds (HNSW) is a graph-based indexing and retrieval algorithm. This works differently from product quantization: instead of improving the searchability of the database by reducing its effective size, HNSW creates a multi-layer graph from the original data. Upper layers contain only "long connections" while lower layers contain only "short connections" between vectors in the database (see the next section for an overview of vector distance metrics). Individual graph connections are created a-la skip lists. With this architecture in place, searching becomes fairly straightforward – we greedily traverse the uppermost graph (the one with the longest inter-vector connections) for the vector closest to our query vector. We then do the same for the second layer, using the result of the first layer search as the starting point. This continues until we complete the search at the bottommost layer, the result of which becomes the nearest neighbor of the query vector. You can check out the original HNSW paper here.

Approximate Nearest Neighbors Oh Yeah

This is probably my favorite ANN algorithm simply due to its playful and unintunitive name. Approximate Nearest Neighbors Oh Yeah (ANNOY) is a tree-based algorithm popularized by Spotify (it's used in their music recommendation system). Despite the strange name, the underlying concept behind ANNOY is actually fairly simple – binary trees. ANNOY works by first randomly selecting two vectors in the database and bisecting the search space along the hyperplane separating those two vectors. This is done iteratively until there are fewer than some predefined parameter `NUM_MAX_ELEMS` per node. Since the resulting index is essentially a binary tree, this allows us to do our search on O(log n) complexity.

Commonly used similarity metrics

The very best vector databases are useless without similarity metrics – methods for computing the distance between two vectors. Numerous metrics exist, so we will discuss only the most commonly used subset here.

Floating point vector similarity metrics

The most common floating point vector similarity metrics are, in no particular order, *L1 distance*, *L2 distance*, and *cosine similarity*. The first two values are *distance metrics* (lower values imply more similarity while higher values imply lower similarity), while cosine similarity is a *similarity metric* (higher values imply more simlarity).

1.
$$d_{l1}(\mathbf{a}, \mathbf{b}) = \sum_{i=1}^{N} |\mathbf{a}_i - \mathbf{b}_i|$$

2.
$$d_{l2}(\mathbf{a}, \mathbf{b}) = \sqrt{\sum_{i=1}^{N} (\mathbf{a}_i - \mathbf{b}_i)^2}$$

3.
$$d_{cos}(\mathbf{a}, \mathbf{b}) = \frac{\mathbf{a} \cdot \mathbf{b}}{|\mathbf{a}||\mathbf{b}|}$$

L1 distance is also commonly referred to as Manhattan distance, aptly named after the fact that getting from point A to point B in Manhattan requires moving along one of two fixed directions. The second equation, L2 distance, is simply the distance between two vectors in Euclidean space. The third and final equation is cosine distance, equivalent to the cosine of the angle between two vectors. Note the equation for cosine similarity works out to be the dot product between normalized versions of input vectors **a** and **b**.

With a bit of math, we can also show that L2 distance and cosine similarity are effectively equivalent when it comes to similarity ranking:

$$d_{l2}(\mathbf{a}, \mathbf{b}) = (\mathbf{a} - \mathbf{b})^T (\mathbf{a} - \mathbf{b})$$

$$= \mathbf{a}^T \mathbf{a} - 2\mathbf{a}^T \mathbf{b} + \mathbf{b}^T \mathbf{b}$$

$$= 2 - 2\mathbf{a}^T \mathbf{b}$$

$$= 2(1 - d_{cos}(\mathbf{a}, \mathbf{b}))$$

Essentially, if you have unit norm vectors

$$|\mathbf{a}| = |\mathbf{b}| = 1$$

, L2 distance and cosine similarity are functionally equivalent! Always remember to normalize your embeddings.

Binary vector similarity metrics

Binary vectors, as their name suggest, do not have metrics based in arithmetics a-la floating point vectors. Similarity metrics for binary vectors instead rely on either set mathematics, bit manipulation, or a combination of both (it's okay, I also hate discrete math). Here are the formulas for two commonly used binary vector similarity metrics:

1.
$$d_J(\mathbf{a}, \mathbf{b}) = 1 - \frac{\mathbf{a} \cdot \mathbf{b}}{|a|^2 + |b|^2 - \mathbf{a} \cdot \mathbf{b}}$$

2.
$$d_J(\mathbf{a}, \mathbf{b}) = \sum_{i=1}^{N} \mathbf{a}_i \oplus \mathbf{b}_i$$

The first equation is called Tanimoto/Jaccard distance, and is essentially a measure of the amount of overlap between two binary vectors. The second equation is Hamming distance, and is a count of the number of vector elements in a and b which differ from each other.

You can most likely safely ignore these similarity metrics, since the majority of applications use cosine similarity over floating point embeddings.

Wrapping up

In this tutorial, we took a look at vector similarity search, along with some common vector search algorithms and distance metrics. Here are some key takeaways:

- Embedding vectors are powerful representations, both in terms of distance between the vectors and in terms of vector arithmetic. By applying a liberal quantity of vector algebra to embeddings, we can perform scalable semantic analysis using just basic mathematical operators.
- There are a wide variety of approximate nearest neighbor search algorithms and/or index types to choose from. The most commonly one used today is HNSW, but a different indexing algorithm may work better for your particular application, depending on the total number of embeddings you have in addition to the length of each individual vector.
- The two primary distance metrics used today are L2/Euclidean distance and cosine distance. These two metrics, when used on normalized embeddings, are functionally equivalent.

Thanks for joining us for this tutorial! We covered a fairly math-heavy topic. In future tutorials, we'll be doing some deeper dives into the most commonly used ANNS algorithms - HNSW and ScaNN.

See you in the next tutorial.