```
{-# OPTIONS --guardedness #-}
open import Codata.Musical.Notation
open import Data.Nat using (; suc; zero)
open import Relation.Binary.Core using (Rel)
open import Relation.Binary.Bundles using (Setoid)
open import Relation. Binary. Definitions using (Reflexive; Symmetric; Transitive)
open import Relation.Binary.PropositionalEquality using (__; subst; subst) renaming (sym to eqSym; trans to
import Level using (zero)
open import Data. Maybe using (Maybe; nothing; just)
open import Data. Maybe. Properties
open import Data. Bool using (Bool; true; false)
open import Data.Product
open import Data.Sum
open import Function.Base using (case_of_)
open import Relation. Nullary using (contradiction)
open import nakata. Traces hiding (module Trace)
open import nakata.Language
module latex. Trace1 where
data Trace: Set where
  \mathsf{tnil}: \mathsf{State} \to \mathsf{Trace}
  \mathsf{tcons}: \mathsf{State} \to \ \mathsf{Trace} \to \mathsf{Trace}
data __ : Rel Trace Level.zero where
  \mathsf{tnil}: \ \{st\} 	o (\mathsf{tnil}\ st) \ (\mathsf{tnil}\ st)
  tcons: \{st\ tr\ tr\}
    \rightarrow ( tr tr)
    \rightarrow (tcons st \ tr) (tcons st \ tr)
mutual
  data exec : Stmt \rightarrow State \rightarrow Trace \rightarrow Set where
    execWhileLoop:
       \{c : \mathsf{Expr}\}\ \{b : \mathsf{Stmt}\}
       \{st : \mathsf{State}\}\ (tr\ tr : \mathsf{Trace})
```

```
\begin{array}{l} \rightarrow \text{ (isTrue } (c\ st)) \ \text{ true} \\ \rightarrow \text{ execseq } b \text{ (tcons } st \text{ (tnil } st)) \ tr \\ \rightarrow \text{ execseq (Swhile } c\ b) \ tr \ tr \\ \rightarrow \text{ exec (Swhile } c\ b) \ st \ tr \\ \\ \\ \textbf{data execseq : Stmt} \rightarrow \textbf{Trace} \rightarrow \textbf{Trace} \rightarrow \textbf{Set where} \\ \text{ execseqNil : } \{st: \textbf{State}\} \ \{s: \textbf{Stmt}\} \ \{tr: \textbf{Trace}\} \\ \rightarrow \text{ exec } s \ st \ tr \\ \rightarrow \text{ execseq } s \text{ (tnil } st) \ tr \\ \\ \\ \textbf{execseqCons : } \{s: \textbf{Stmt}\} \\ \text{ (}st: \textbf{State}) \ (tr \ tr: \textbf{Trace}) \\ \rightarrow \text{ (execseq } s \ (tr) \ (tr)) \\ \rightarrow \text{ execseq } s \text{ (tcons } st \ tr) \text{ (tcons } st \ tr) \\ \end{array}
```