



$$x(t) = \begin{cases} -1 & -\pi < t < 0 \\ 1 & 0 \leq t \leq \pi \end{cases} \quad T = 2\pi$$

$$X_k = \frac{1}{2\pi} \int_{-\pi}^{\pi} x(t) e^{-j \frac{k}{2\pi} t} dt$$

$$X_k = \frac{1}{2\pi} \int_{-\pi}^0 -e^{-jkt} dt + \frac{1}{2\pi} \int_0^{\pi} e^{-jkt} dt$$

$$X_k = \frac{1}{2\pi jk} \left[e^{-jkt} \right]_{-\pi}^0 - \frac{1}{2\pi jk} \left[e^{-jkt} \right]_0^{\pi}$$

$$X_k = \frac{1 - e^{jk\pi} - e^{-jk\pi} + 1}{2\pi jk} = \frac{1 - (-1)^k}{\pi jk}$$

$$X_k = \begin{cases} 0 & k \text{ pair} \\ \frac{2}{\pi jk} & k \text{ impair} \end{cases}$$

$$X_{-k} = -\frac{2}{\pi jk}$$

$$a_k = x_k + x_{-k} = 0$$

$$x_0 = 0$$

$$b_k = j(x_k - x_{-k}) = \frac{4}{\pi k}$$

$$x(t) = \frac{4}{\pi} \left(\frac{\sin t}{1} + \frac{\sin 3t}{3} + \frac{\sin 5t}{5} + \dots + \frac{\sin(2p+1)t}{2p+1} + \dots \right)$$