Statistics Exercises

Data Analytics (Nov 2020)

Clara Carbó Canals

Week 1: Building Blocks for Problem Solving - Practice quiz on Sets (3 questions)

Practice quiz on Sets
Cuestionario Práctico • 15 min

¡Felicitaciones! ¡Aprobaste!
PARA APROBAR 75 % o más

Continúa aprendiendo

CALIFICACIÓN
100 %

Practice quiz on Sets

PUNTOS TOTALES DE 3

1. Let $A = \{1, 3, 5\}$. Is the following statement: $3 \in A$. True or false?

   - (•) True
   - ( ) False

   Correcto
   The symbol $\in$ stands for "is an element of" and it is true that 3 is an element of A. The other two elements of A are 1 and 5.

2. Let $E = \{-1, -2, -3\}$. Compute the cardinality $|E|$ of E:

   - ( ) -3
   - ( ) 0
   - ( ) E
   - (•) 3

   Correcto
   Recall that the cardinality of a set is the number of elements in it. Since E has three elements (which are -1, -2, -3), the cardinality of E is $|E| = 3$.

3. Let $A = \{1, 3, 5\}$ and $B = \{3, 5, 10, 11, 14\}$.

   Which of the following sets is equal to the intersection $A \cap B$?

   - (•) $\{3, 5\}$
   - ( ) $\{3, 5, 10\}$
   - ( ) $\{3\}$
   - ( ) $\{1, 3, 5\}$

   Correcto
   The intersection of two sets consists precisely of the elements they share in common. The elements 3 and 5 are in both A and B.

Week 1: The infinite World of Real Numbers - Practice quiz on the Number Line, including Inequalities (8 questions)

Practice quiz on the Number Line, including Inequalities

Cuestionario Práctico • 25 min

¡Felicitaciones! ¡Aprobaste!

PARA APROBAR 75 % o más

Continúa aprendiendo

CALIFICACIÓN 100 %

Practice quiz on the Number Line, including Inequalities

PUNTOS TOTALES DE 8

1. Which of the following real numbers is ***not*** an integer?

- ○ 0
- ○ -3
- ○ 7
- ◉ 4.3

✓ **Correcto**

4.3 is a decimal that is between two consecutive integers (4 and 5).

2. Which of the following is the absolute value $|-7|$ of the number -7?

- ○ -7
- ○ 1
- ◉ 7
- ○ 0

✓ **Correcto**

The absolute value of a number x is the distance along the number line from x to 0. In this case, -7 is 7 units away from 0, and so $|-7| = 7$.

3. Suppose I tell you that x and y are two real numbers which make the statement $x < y$ true. Which pair of numbers ***cannot*** be values for x and y?

- ○ $x = -17.3$ and $y = -17.1$
- ○ $x = 1$ and $y = 7.3$
- ◉ $x = 5$ and $y = 3.3$
- ○ $x = -1$ and $y = 0$

✓ **Correcto**

The statement $x < y$ means that x is to the left of y on the real number line. Since 5 is to the right of 3.3, these cannot be values for x and y.

4. Suppose I tell you that w is a real number which makes both of the following statements true: $w > 1$ and $w < 1.2$. Which of the following numbers could be w?

- ○ $w = 0$
- ◉ $w = 1.05$
- ○ $w = 1.2$
- ○ $w = 11$

✓ **Correcto**

$1.05 > 1$ is true since 1.05 is to the right of 1 on the real number line, and $1.05 < 1.2$ is also true, since 1.05 is to the left of 1.2 on the real number line.

5. Suppose that x and y are two real numbers which satisfy $x+3=4y+1$. **Which of the following statements are false?**

- $x=4y-2$
- (selected) $x=4y$
- $x+2=4y$
- $2x+6=8y+2$

✓ **Correcto**

The equation $x=4y$ cannot be derived from the given equation.

6. Which of the following real numbers is in the open interval $(2,3)$?

- 1
- (selected) 2.1
- 3
- 2

✓ **Correcto**

Recall that the open interval $(2,3)$ consists of all real numbers x which satisfy $2<x<3$. Since $2.1>2$ and $2.1<3$, the number 2.1 is in this open interval.

7. Which of the following real numbers are in the open ray $(3.1,\infty)$?

- 0
- 3.1
- (selected) 4.75
- -5

✓ **Correcto**

Recall that $(3.1,\infty)=\{x\in\mathbb{R}|\ x>3.1\}$. Since $4.75>3.1$ is true, $4.75\in(3.1,\infty)$.

8. Which of the following values for x solves the equation $-3x+2=-4$

- $x=-2$
- All values of x such that $x\leq 2$
- $x=\frac{2}{3}$
- (selected) $x=2$

✓ **Correcto**

First we subtract 2 from both sides of the given equation, to obtain $-3x=-6$. Finally, to isolate x we divide both sides of the equation by -3 to obtain $x=2$.

Week 1: That Jagged S Symbol - Practice quiz on Simplification Rules and Sigma Notation (6 questions)

Practice quiz on Simplification Rules and Sigma Notation

Cuestionario Práctico • 20 min

✓ **¡Felicitaciones! ¡Aprobaste!**

PARA APROBAR 75 % o más

Continúa aprendiendo

CALIFICACIÓN 100 %

Practice quiz on Simplification Rules and Sigma Notation

PUNTOS TOTALES DE 6

1. Which of the numbers below is equal to the following summation: $\Sigma_{i=1}^{3} i^2$?

- 30
- 14
- 1
- 9

✓ **Correcto**

We compute $\Sigma_{i=1}^{3} i^2 = 1^2 + 2^3 + 3^2 = 14$

2. Suppose that $A = \Sigma_{k=1}^{100} k^4$ and $B = \Sigma_{j=1}^{100} j^4$

Which of the following statements is true?

- $B > A$
- $A > B$
- There is not enough information to do the problem
- $A = B$

✓ **Correcto**

A = B. Both summations evaluate to the same number, since k and j are just dummy indices.

3. Which of the numbers below is equal to the summation $\Sigma_{i=1}^{10} 7$?

- 70
- 7
- 55
- 0

✓ **Correcto**

According to one of our Sigma notation simplification rules, this summation is just equal to 10 copies of the number 7 all added together, and so we get $10 \times 7 = 70$.

4. Suppose that $X = \Sigma_{i=1}^{5} i^3$ and $Y = \Sigma_{i=1}^{5} i^4$.

Which of the following expressions is equal to the summation $\Sigma_{i=1}^{5} (2i^3 + 5i^4)$?

- $2X + 5Y$
- 3375
- 7
- $X + Y$

✓ **Correcto**

To get here, you apply two of our Sigma notation simplification rules $\Sigma_{i=1}^{5} 2i^3 + 5i^4 = 2\left(\Sigma_{i=1}^{5} i^3\right) + 5\left(\Sigma_{i=1}^{5} i^4\right) = 2X + 5Y$.

5. Which of the following numbers is the mean μ_Z of the set $Z = \{-2, 4, 7\}$?

- 4
- 9
- 3 (selected)
- $\frac{13}{3}$

Correcto

To get the mean of a set of numbers, you need to perform two steps: first add them all up (in this case getting $-2 + 4 + 7 = 9$), and then divide by the number of elements in the set (in this case that number is 3).

So you should obtain $\mu_Z = \frac{9}{3} = 3$, which you did!

6. Suppose the set X has five numbers in it: $X = \{x_1, x_2, x_3, x_4, x_5\}$. Which of the following expression represents the mean of the set X?

- $\frac{1}{5}[\sum_{i=1}^{5} x_i]$ (selected)
- $\sum_{i=1}^{5} x_i$
- $\frac{1}{N}[\sum_{i=1}^{N} x_i]$
- $\frac{1}{5}[\sum_{i=1}^{5} (x_i - \mu_X)^2]$

Correcto

To obtain the mean of a set of numbers, you first add them all up (which is expressed here by the sigma operation inside the square brackets) and then you divide by the number of numbers in the set (which is expressed here by the $\frac{1}{5}$ outside the square brackets).

WEEK 1: That Jagged S Symbol - Graded quiz on Sets, Number Line, Inequalities, Simplification, and Sigma Notation (13 questions)

Graded quiz on Sets, Number Line, Inequalities, Simplification, and Sigma Notation

Graded Quiz • 35 min

Congratulations! You passed!

TO PASS 75% or higher

Keep Learning

GRADE 100%

Graded quiz on Sets, Number Line, Inequalities, Simplification, and Sigma Notation

CALIFICACIÓN DEL ÚLTIMO ENVÍO

100%

1. Let $B = \{3, 5, 10, 11, 14\}$. Is the following statement true or false: $3 \notin B$ — 1 / 1 puntos

- (•) False
- ( ) True

Correcto

The symbol $\notin$ stands for "is not an element of." Since 3 is in an element of the set B, the given statement is not true.

2. Let $A = \{1, 3, 5\}$ and $B = \{3, 5, 10, 11, 14\}$. Which of the following sets is equal to the union $A \cup B$? — 1 / 1 point

- ( ) $\{1, 10, 18\}$
- ( ) $\{3, 5, 10, 11, 14\}$
- (•) $\{1, 3, 5, 10, 11, 14\}$
- ( ) $\{1, 3, 5, 3, 5, 10, 11, 14\}$

Correct

The union of two sets consists precisely of the elements that are in at least one of the two sets. That is precisely what is listed here.

3. How many real numbers are there between the integers 1 and 4? — 1 / 1 point

- ( ) None
- ( ) 2
- (•) Infinitely many
- ( ) 4

Correct

There are in fact infinitely many real numbers between any pair of distinct integers, or indeed any pair of distinct real numbers!

4. Suppose I tell you that x and y are two real numbers which make the statement $x \geq y$ true. Which pair of numbers ***cannot*** be values for x and y? — 1 / 1 point

- ( ) $x = 2$ and $y = 1$
- ( ) $x = 10$ and $y = 10$
- (•) $x = -1$ and $y = 0$
- ( ) $x = 5$ and $y = 3.3$

Correct

Recall that the statement $x \geq y$ means that x is either equal to y or x is to the right of y on the real number line. Since -1 is actually to the left of 0, these cannot be values for x and y.

5. Suppose that z and w are two positive numbers with $z < w$. Which of the following inequalities is false? — 1 / 1 point

- ( ) $z + 3 < w + 3$
- ( ) $-z > -w$
- ( ) $w - 7 > z - 7$
- (•) $-5z < -5w$

Correct

If we start with $z < w$ and multiply both sides by -5, we need to flip the less-than sign, which would give $-5z > -5w$. For an example, try $z = 1$ and $y = 2$ and see what happens!

6. Find the set of all x which solve the inequality $-2x + 5 \leq 7$ 1 / 1 point

- $x = -1$
- $x \geq -6$
- $x \leq -1$
- $x \geq -1$

Correct

Subtracting 5 from both sides of the given inequality gives $-2x \leq 2$. Then we divide both sides by -2, remembering to flip the inequality sign, and we obtain this answer

7. Which of the following real numbers is not in the closed interval $[2, 3]$ 1 / 1 point

- 1
- 2.1
- 2
- 3

Correct

Recall that the closed interval $[2, 3]$ consists of all real numbers x which satisfy $2 \leq x \leq 3$. Since $2 \leq 1$ is false, $1 \notin [2, 3]$

8. Which of the following intervals represents the set of all solutions to: 1 / 1 point

$-5 \leq x + 2 < 10$?

- $(7, 8)$
- $[-7, 8)$
- $[-5, 10)$
- $[-7, 8]$

Correct

Subtracting 2 from all sides of the inequalities gives $-7 \leq x < 8$, and the set of all real numbers x which make that true is exactly the half-open interval $[-7, 8)$.

9. Which of the numbers below is equal to the following summation: $\Sigma_{k=2}^{5} 2k$? 1 / 1 point

- 28
- 4
- 14
- 10

Correct

We compute $\Sigma_{k=2}^{5} 2k = 4 + 6 + 8 + 10 = 28$.

10. Suppose we already know that $\Sigma_{k=1}^{20} k = 210$. Which of the numbers below is equal to $\Sigma_{k=1}^{20} 2k$?

1 / 1 point

- 40
- 420
- 2
- 210

Correct

By applying one of our Sigma notation simplification rules, we can rewrite the summation in question as $2\left(\Sigma_{k=1}^{20} k\right) = 2 \times 210 = 420$.

11. Which of the numbers below is equal to the summation $\Sigma_{i=2}^{10} 7$?

1 / 1 point

- 48
- 63
- 7
- 70

Correct

According to one of our Sigma notation simplification rules, this summation is just equal to 9 copies of the number 7 all added together, and so we get $9 \cdot 7 = 63$.

12. Which of the following numbers is the variance of the set $Z = \{-2, 4, 7\}$?

1 / 1 point

- $\sqrt{14}$
- 14
- 69
- 42

Correct

To get the variance of a set of numbers, you need to perform four steps:

First compute the mean (which is 3)

Then calculate all the squared differences between the numbers in the set and this mean (here you get $25, 1, 16$)

13. Which of the following sets does *not* have zero variance? (hint: don't do any calculation here, just think!)

1 / 1 point

- $\{1, 1, 1, 1\}$
- $\{0, 0, 0, 0, 0, 0, 0\}$
- $\{2, 5, 9, 13\}$
- $\{5, 5, 5, 5, 5, 5, 5, 5, 5, 5, 5, 5, 5, 5\}$

Correct

Intuitively, the numbers in this set are spread out.

WEEK 2 – Descartes Was Really Smart - Practice quiz on the Cartesian Plane (5 questions)

Practice quiz on the Cartesian Plane

Practice Quiz • 15 min

Congratulations! You passed!

TO PASS 75% or higher

Keep Learning

GRADE 100%

Practice quiz on the Cartesian Plane

TOTAL POINTS 5

1. Which of the following points in the Cartesian Plane is on the y-axis? 1 / 1 point

- $(1, 1)$
- $(5, 0)$
- $(0, -5)$ ✓
- $(-5, 0)$

Correct

The y-axis is defined to be all points in the Cartesian plane with zero as x-coordinate. The point $(0, -5)$ meets that requirement.

2. Find the distance between the points $A = (2, 2)$ and $C = (3, 3)$: 1 / 1 point

- 1
- 2
- $\sqrt{2}$ ✓
- 0

Correct

Recall that the distance between points (a, b) and (c, d) is $\sqrt{(c-a)^2 + (d-b)^2}$.

In this case $(a, b) = (2, 2)$ and $(c, d) = (3, 3)$, so the distance is $\sqrt{(3-2)^2 + (3-2)^2} = \sqrt{2}$.

3. Find the point-slope form of the equation of the line that goes between $A = (1, 1)$ and $B = (5, 3)$: 1 / 1 point

- $y - 1 = \frac{1}{2}(x - 1)$ ✓
- $y = \frac{1}{2}x$
- $y - 3 = \frac{1}{2}(x - 1)$
- $y - 1 = \frac{1}{2}(x - 5)$

Correct

The point-slope form for the equation of a line with slope m that goes through the point (x_0, y_0) is $y - y_0 = m(x - x_0)$

In this case, the slope $m = \frac{3-1}{5-1} = \frac{1}{2}$

We can choose either A or B for the point on the line, but in neither case do we get this chosen answer.

4. Which of the following points is on the line with equation: 1 / 1 point

$y - 1 = 2(x - 2)$?

- $(2, 3)$
- $(0, 0)$
- $(2, 1)$ ✓
- $(3, 2)$

Correct

If we plug in 1 for y and 2 for x in the equation of the line, we make a true statement, $0 = 0$, so this point lies on the line.

5. Suppose that a line ℓ has slope 2 and goes through the point $(-1, 0)$. What is the y-intercept of ℓ? 1 / 1 point

- 1
- -1
- 0
- 2 ✓

Correct

Recall that the y-intercept of ℓ is the y-coordinate of where ℓ hits the y-axis.

Since $(-1, 0) \in \ell$, the point on ℓ with $x = 0$ is obtained by running one unit from $(-1, 0)$ while rising two units.

This gives $y = 2$ as the y-intercept.

WEEK 2 – Input-Output Machines - Practice quiz on Types of Functions (6 questions)

¡Felicitaciones! ¡Aprobaste!

PARA APROBAR 75 % o más

Continúa aprendiendo

CALIFICACIÓN 100 %

Practice quiz on Types of Functions

PUNTOS TOTALES DE 6

1. Suppose that $A = \{1, 2, 10\}$ and $B = \{4, 8, 40\}$. Which of the following formulae do ***not*** define a function $f : A \to B$? — 1 / 1 puntos

- (●) $f(1) = 5$, $f(2) = 8$, and $f(10) = 40$.
- ( ) $f(1) = 4$, $f(2) = 40$, and $f(10) = 8$.
- ( ) $f(1) = 4$, $f(2) = 4$, and $f(10) = 4$.
- ( ) $f(a) = 4a$, for each $a \in A$

✓ Correcto

A function $f : A \to B$ is a rule which assigns an element $f(a) \in B$ to each $a \in A$. In this case, unfortunately, $f(1) = 5 \notin B$.

2. Suppose that A contains every person in the VBS study (see the second video in the course if you're confused here!). Suppose that $Y = \{+, -\}$ and $Z = \{H, S\}$ — 1 / 1 puntos

Suppose that $T : A \to Y$ is the function which gives $T(a) = +$ if person a tests positive and $T(a) = -$ if they test negative.

Suppose that $D : A \to Z$ is the function which gives $D(a) = H$ does not actually have VBS and $D(a) = S$ if the person actually has VBS.

Which of the following must be true of person a if we have a false positive?

- ( ) $T(a) = -$ and $D(a) = S$
- (●) $T(a) = +$ and $D(a) = H$
- ( ) $T(a) = +$ and $D(a) = S$
- ( ) $T(a) = -$ and $D(a) = H$

✓ Correcto

Recall that a false positive is a positive test result (so $T(a) = +$) which is misleading because the person actually does not have the disease ($D(a) = H$)

3. Consider the function $g : \mathbb{R} \to \mathbb{R}$ defined by $g(x) = x^2 - 1$. Which of the following points are *not* on the graph of g? — 1 / 1 puntos

- ( ) $(0, -1)$
- ( ) $(-1, 0)$
- ( ) $(1, 0)$
- (●) $(2, -1)$

✓ Correcto

Recall that the graph of g consists of all points (x, y) such that $y = g(x)$. Here $g(2) = 3 \neq -1$, so the point $(2, -1)$ is \emph{not} on the graph of g.

4. Let the point $A = (2, 4)$. Which of the following graphs does *not* contain the point A? — 1 / 1 puntos

- ( ) The graph of $s(x) = x^2$
- ( ) The graph of $f(x) = 2x$
- ( ) The graph of $g(x) = x + 2$
- (●) The graph of $h(x) = x - 1$

✓ Correcto

The graph of h consists of all points (x, y) such that $y = h(x)$. Here $h(2) = 1 \neq 4$, so the point $(2, 4)$ is *not* on the graph of h.

5. Suppose that $h(x) = -3x + 4$. Which of the following statements is true? — 1 / 1 puntos

- ( ) h is neither a strictly increasing function nor a strictly decreasing function.
- (●) h is a strictly decreasing function
- ( ) All statements are correct
- ( ) h is a strictly increasing function

✓ Correcto

A function h is called strictly decreasing if whenever $a < b$, then $h(a) > h(b)$

Since the graph of h is a line with negative slope, this is in fact true!

6. Suppose that $f : \mathbb{R} \to \mathbb{R}$ is a strictly increasing function, with $f(3) = 15$ — 1 / 1 puntos

Which of the following is a possible value for $f(3.7)$?

- (●) 17
- ( ) 14.7
- ( ) -3
- ( ) 3

✓ Correcto

A function f is called strictly increasing if whenever $a < b$, then $f(a) < f(b)$.

Since $f(3) = 15$ is given and $3 < 3.7$, it must be that $15 < f(3.7)$, and this answer satisfies that.

WEEK 2 – Input-Output Machines - Graded quiz on Cartesian Plane and Types of Function (13 questions)

¡Felicitaciones! ¡Aprobaste!

PARA APROBAR 75 % o más

Continúa aprendiendo

CALIFICACIÓN
76,92 %

Graded quiz on Cartesian Plane and Types of Function

CALIFICACIÓN DEL ÚLTIMO ENVÍO
76.92%

1. Which of the following points in the Cartesian Plane have positive x-coordinate and negative y-coordinate? 1 / 1 puntos

- (●) $(7, -1)$
- ( ) $(5, 7)$
- ( ) $(-4, 5)$
- ( ) $(0, 0)$

Correcto
The x-coordinate, 7, is positive, and the y-coordinate, -1, is negative.

2. Which of the following points is in the first quadrant of the Cartesian Plane? 0 / 1 puntos

- (●) $(-5, 1)$
- ( ) $(5, -1)$
- ( ) $(7, 11)$
- ( ) $(-4, -7)$

Incorrecto
The first quadrant is defined to be all points in the Cartesian plane whose coordinates are both positive. The first coordinate here is negative.

3. Let A, B, C, D be points in the Cartesian Plane, and let the set $S = \{B, C, D\}$ 1 / 1 puntos

Suppose that the distances from A to B, C, D are $5.3, 2.1$, and 11.75, respectively.

Which of the following points is the nearest neighbor to the point A in the set S?

- (●) C
- ( ) A
- ( ) B
- ( ) D

Correcto
The distance from A to C is 2.1 and that is smaller than the distance from A to any other element of S.

4. Find the distance between the points $A = (2, 2)$ and $B = (-1, -2)$. 1 / 1 puntos

- (●) 5
- ( ) -25
- ( ) 1
- ( ) 25

Correcto
Recall that the distance between points (a, b) and (c, d) is $\sqrt{(c-a)^2 + (d-b)^2}$

In this case we have:

$$\sqrt{(-1-2)^2 + (-2-2)^2} = \sqrt{(-3)^2 + (-4)^2} = \sqrt{25} = 5$$

5. Find the slope of the line segment between the points $A = (0, 1)$ and $B = (1, 0)$. 1 / 1 puntos

- (●) -1
- ( ) 1
- ( ) $\sqrt{2}$
- ( ) 0

✓ **Correcto**

The slope of this line segment is $\frac{0-1}{1-0} = -1$

6. Find the point-slope form of the equation of the line with slope -2 that goes through the point $(5, 4)$. 0 / 1 puntos

- ( ) $(5, 4)$
- (●) $y - 4 = 2(x - 5)$
- ( ) $y - 5 = -2(x - 4)$
- ( ) $y - 4 = -2(x - 5)$

! **Incorrecto**

Remember that the point-slope form for the equation of a line with slope m that goes through the point (x_0, y_0) is $y - y_0 = m(x - x_0)$

In this case, the slope $m = -2$ is given. But this equation uses $m = 2$ instead.

7. Which of the following equations is for a line with the same slope as $y = -3x + 2$? 0 / 1 puntos

- ( ) $y = 8x - 3$
- ( ) $y = -3x - 8$
- ( ) $y = 5x$
- ( ) $y = 5x + 2$

! **Incorrecto**

No seleccionaste una respuesta.

8. Which of the following equations is for a line with the same y-intercept as $y = -3x + 2$? 1 / 1 puntos

- ( ) $y = 8x - 3$
- ( ) $y = -3x - 8$
- ( ) $y = 5x$
- (●) $y = 5x + 2$

✓ **Correcto**

The the slope-intercept formula for a line is $y = mx + b$, where m is the slope and b is the y-coordinate of the point where the line hits the y-axis. This line has a y-intercept of 2 which is the same as the given line.

9. How many lines contain both the point $A = (1, 1)$ and the point $B = (2, 2)$? 1 / 1 puntos

- ( ) None
- (●) 1
- ( ) infinitely many
- ( ) 2

✓ **Correcto**

The line with equation $y = x$ is the one and only line that meets the stated requirements.

10. Suppose that we have two sets, $A = \{a, b\}$ and $Z = \{x, y\}$. How many different functions $F : A \to Z$ are possible? 1 / 1 puntos

- ○ 1
- ○ There are infinitely many
- ◉ 4
- ○ There are none

✓ **Correcto**
A function $F : A \to Z$ is a rule which assigns an element $F(a) \in Z$ to each element $a \in A$.

11. How many graphs contain both the point $A = (0, 0)$ and the point $B = (1, 1)$ 1 / 1 puntos

- ○ 2
- ○ 1
- ◉ Infinitely many
- ○ None

✓ **Correcto**
The graphs of $f(x) = x, g(x) = x^2, h(x) = x^3, s(x) = x^4, \ldots$ all contain both A and B

12. Suppose that $g : \mathbb{R} \to \mathbb{R}$ is a continuous function whose graph intersects the x-axis more than once. Which of the following statements is true? 1 / 1 puntos

- ◉ g is neither strictly increasing nor strictly decreasing.
- ○ g is strictly decreasing.
- ○ All of the above.
- ○ g is strictly increasing.

✓ **Correcto**
The function g fails the horizontal line test, so it can neither be strictly increasing nor strictly decreasing.

13. Find the slope of the line segment between the points $A = (1, 1)$ and $B = (5, 3)$. 1 / 1 puntos

- ○ $\sqrt{20}$
- ○ 2
- ○ 4
- ◉ $\frac{1}{2}$

✓ **Correcto**
The slope of this line segment is $\frac{3-1}{5-1} = \frac{1}{2}$, where $3 - 1$ is the rise and $5 - 1$ is the run.

WEEK 3 – This is about that derivative stuff - Practice quiz on Tangent Lines to Functions

¡Felicitaciones! ¡Aprobaste!

PARA APROBAR 75 % o más

Continúa aprendiendo

CALIFICACIÓN
100 %

Practice quiz onTangent Lines to Functions

PUNTOS TOTALES DE 2

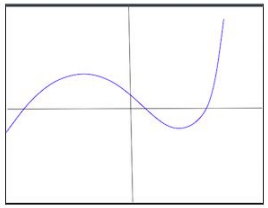
1. Suppose that $f : \mathbb{R} \to \mathbb{R}$ is a function. Which of the following expressions corresponds to $f'(2)$, the slope of the tangent line to the graph of $f(x)$ at $x = 2$? 1 / 1 puntos

- $f'(2) = \lim_{h \to 0} \frac{f(a+h)-f(a)}{h}$
- $f'(2) = \lim_{h \to 0} \frac{f(2+h)-f(2)}{h}$
- $f'(2) = 2$
- $f'(2) = mx + b$

Correcto

This expression can be obtained from the first screen of our video by plugging in 2 for a.

2. Suppose that $h : \mathbb{R} \to \mathbb{R}$ is a function whose graph is shown as the blue curve in the figure. For how many values of a is $h'(a) = 0$? 1 / 1 puntos



- 3
- Never
- Always
- 2

Correcto

$h'(a)$ gives the slope of the tangent line to the graph of h at the point $x = a$.

WEEK 3 – Fast Growth, Slow Growth - Practice quiz on Exponents and Logarithms (12 questions)

✓ **¡Felicitaciones! ¡Aprobaste!**

PARA APROBAR 75 % o más

Continúa aprendiendo

CALIFICACIÓN 100 %

Practice quiz on Exponents and Logarithms

TOTAL POINTS 12

1. Re write the number $784 = 2 \times 2 \times 2 \times 2 \times 7 \times 7$ using exponents. 1 / 1 point

- $(16^4)(49^2)$
- $(2 \times 7)^6$
- ◉ $(2^4)(7^2)$
- $(2^6)(7^6)$

✓ Correct

For this type of problem, count the number of times each relevant factor appears in the product. That number is the exponent for that factor.

2. What is $(x^2 - 5)^0$? 1 / 1 point

- ◉ 1
- $(x^2) - 5$
- -4
- (x^2)

✓ Correct

Any real number (except zero) raised to the"zeroith" power $= 1$.

3. Simplify $((x-5)^2)^{-3}$ 1 / 1 point

- ◉ $(x-5)^{-6}$
- $(x-5)^{-5}$
- $(x-5)$
- $(x-5)^{-1}$

✓ Correct

By Rule 2, "Power to a Power," multiply the exponents and get:

$(x-5)^{(2\times -3)} = (x-5)^{-6}$

By the definition of negative exponents, this is equal to $\frac{1}{(x-5)^6}$

4. Simplify $(\frac{8^2}{8^7})^2$ 1 / 1 point

- 8^{-5}
- ◉ 8^{-10}
- 8^{-1}
- 8^{-4}

✓ Correct

We can first simplify what is inside the parenthesis to 8^{-5} using the Division and Negative Powers Rule.

Then apply division and negative powers-- the result is the same. $\frac{8^4}{8^{14}} = 8^{-10}$

5. $\log 35 = \log 7 + \log x$ 1 / 1 point

Solve for x

- (•) 5
- ( ) 7
- ( ) 28
- ( ) 4

✓ Correct

$\log(x) = \log 35 - \log 7$

$\log(x) = \log\left(\frac{35}{7}\right)$

By the Quotient Rule $\log x = \log 5$

6. $\log_3(x^2 + 5x + 7) = 0$ 1 / 1 point

Solve for x

- (•) $x = -2$ or $x = -3$
- ( ) $x = 2$
- ( ) $x = 3$
- ( ) $x = 2$ or $x = 3$

✓ Correct

We use the property that $b^{\log_b a} = a$

Use both sides as exponent for 2.

$2^{\log_2 x^2+5x+7} = 2^0$

$x^2 + 5x + 7 = 1$

$x^2 + 5x + 6 = 0$

$(x + 3)(x + 2) = 0$

$x = -3$ OR

$x = -2$

7. Simplify $\log_2 72 - \log_2 9$ 1 / 1 point

- ( ) $\log_2 63$
- (•) 3
- ( ) $\log_2 4$
- ( ) 4

✓ Correct

By the quotient rule, this is $\log_2 \frac{72}{9} = \log_2 2^3 = 3$

8. Simplify $\log_3 9 - \log_3 3 + \log_3 5$ 1 / 1 point

- ( ) 8
- (•) $\log_3 15$
- ( ) $\log_3 8$
- ( ) 15

✓ Correct

By the Quotient and Product Rules, this is $\log_3 \frac{9 \times 5}{3} = \log_3 15$

9. Simplify $\log_2(3^8 \times 5^7)$ 1 / 1 point

- (•) $(8 \times \log_2 3) + (7 \times \log_2 5)$
- ( ) $(5 \times \log_2 3) + (8 \times \log_2 5)$
- ( ) $15 \times \log_2 56$
- ( ) $56 \times \log_2 15$

✓ Correct

We first apply the Product Rule to convert to the sum: $\log_2(3^8) + \log_2(5^7)$. Then apply the power and root rule.

10. If $\log_{10} y = 100$, what is $\log_2 y =$? 1 / 1 point

- ( ) 20
- (•) 332.19
- ( ) 500
- ( ) 301.03

✓ Correct

Use the change of base formula, $\log_a b = \frac{\log_x b}{\log_x a}$

Where the "old" base is x and the "new" base is a.

So $\frac{100}{\log_{10}(2)} = \frac{100}{0.30103} = 332.19$

11. A tree is growing taller at a continuous rate. In the past 12 years it has grown from 3 meters to 15 meters. What is its rate of growth per year? 1 / 1 point

- ( ) 12.41%
- (•) 13.41%
- ( ) 10.41%
- ( ) 11.41%

✓ Correct

$\frac{\ln \frac{15}{3}}{12} = 0.1341$

12. Bacteria can reproduce exponentially if not constrained. Assume a colony grows at a continually compounded rate of 400% per day. How many days before a colony with initial mass of 6.25×10^{-10} grams weights 1000 Kilograms? 1 / 1 point

- ( ) 875 days
- ( ) 87.5 days
- ( ) 0.875 days
- (•) 8.75 days

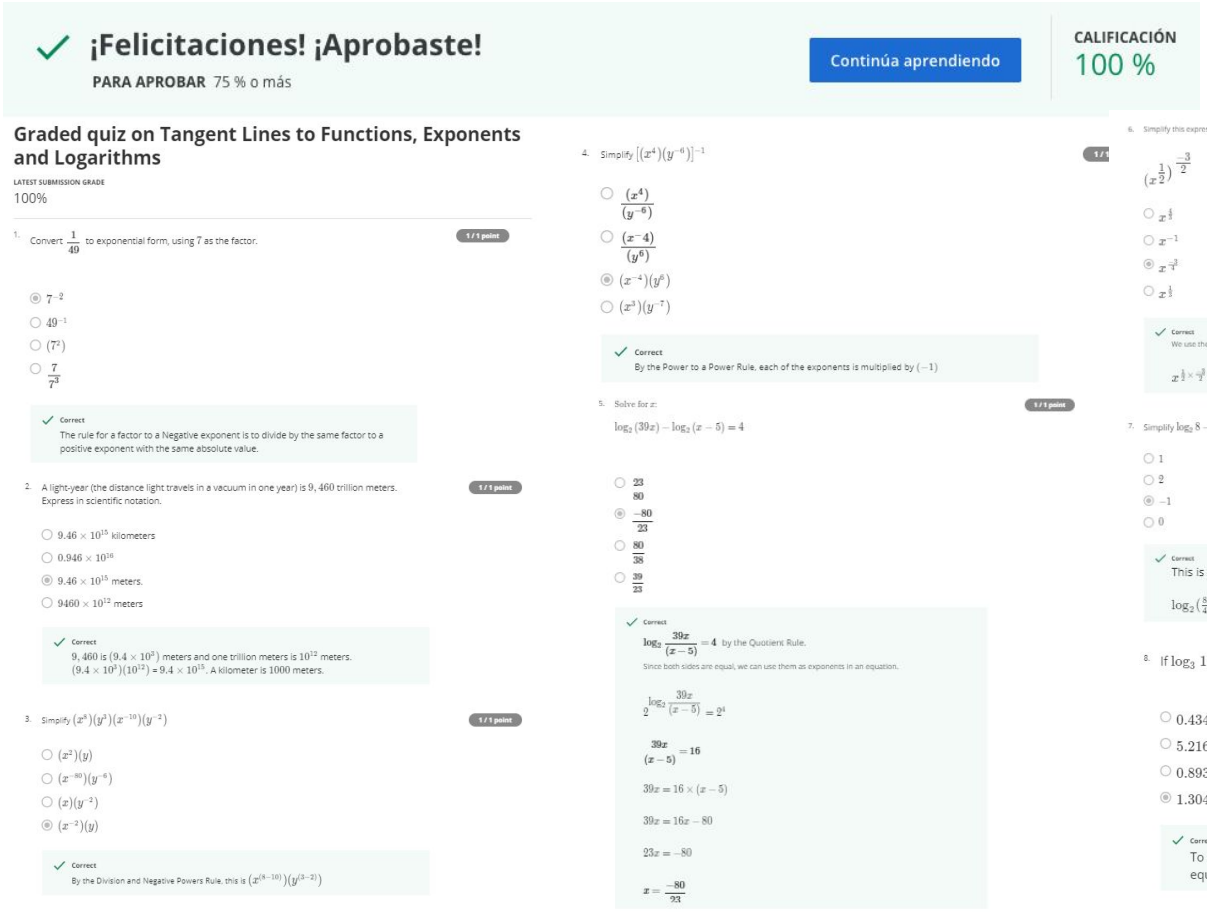
✓ Correct

$6.25 \times 10^{-10} \times e^{4t} = 10^6$

$4t = \ln\left(\frac{10^6}{(6.25 \times 10^{-10})}\right) = 35.00878$

$t = \ln \frac{10^6}{6.25 \times 10^{-10}} = 8.752195$

WEEK 3 – Fast Growth, Slow Growth - Graded quiz on Tangent Lines to Functions, Exponents and Logarithms (13 questions)



¡Felicitaciones! ¡Aprobaste!

PARA APROBAR 75 % o más

Continúa aprendiendo

CALIFICACIÓN 100 %

Graded quiz on Tangent Lines to Functions, Exponents and Logarithms

LATEST SUBMISSION GRADE

100%

1. Convert $\frac{1}{49}$ to exponential form, using 7 as the factor. 1 / 1 point

- ◉ 7^{-2}
- ○ 49^{-1}
- ○ (7^2)
- ○ $\frac{7}{7^3}$

Correct

The rule for a factor to a Negative exponent is to divide by the same factor to a positive exponent with the same absolute value.

2. A light-year (the distance light travels in a vacuum in one year) is $9,460$ trillion meters. Express in scientific notation. 1 / 1 point

- ○ 9.46×10^{15} kilometers
- ○ 0.946×10^{16}
- ◉ 9.46×10^{15} meters.
- ○ 9460×10^{12} meters

Correct

$9,460$ is (9.4×10^3) meters and one trillion meters is 10^{12} meters.
$(9.4 \times 10^3)(10^{12}) = 9.4 \times 10^{15}$. A kilometer is 1000 meters.

3. Simplify $(x^8)(y^3)(x^{-10})(y^{-2})$ 1 / 1 point

- ○ $(x^2)(y)$
- ○ $(x^{-80})(y^{-6})$
- ○ $(x)(y^{-2})$
- ◉ $(x^{-2})(y)$

Correct

By the Division and Negative Powers Rule, this is $(x^{(8-10)})(y^{(3-2)})$

4. Simplify $[(x^4)(y^{-6})]^{-1}$ 1 / 1

- ○ $\frac{(x^4)}{(y^{-6})}$
- ○ $\frac{(x^{-4})}{(y^6)}$
- ◉ $(x^{-4})(y^6)$
- ○ $(x^3)(y^{-7})$

Correct

By the Power to a Power Rule, each of the exponents is multiplied by (-1)

5. Solve for x: 1 / 1 point

$\log_2(39x) - \log_2(x-5) = 4$

- ○ $\frac{23}{80}$
- ◉ $\frac{-80}{23}$
- ○ $\frac{80}{38}$
- ○ $\frac{39}{23}$

Correct

$\log_2 \frac{39x}{(x-5)} = 4$ by the Quotient Rule.

Since both sides are equal, we can use them as exponents in an equation.

$2^{\log_2 \frac{39x}{(x-5)}} = 2^4$

$\frac{39x}{(x-5)} = 16$

$39x = 16 \times (x-5)$

$39x = 16x - 80$

$23x = -80$

$x = \frac{-80}{23}$

6. Simplify this expression: 1 / 1 point

$(x^{\frac{1}{2}})^{\frac{-3}{2}}$

- ○ $x^{\frac{4}{1}}$
- ○ x^{-1}
- ◉ $x^{\frac{-3}{4}}$
- ○ $x^{\frac{1}{4}}$

Correct

We use the Power to a Power Rule -- multiply exponents:

$x^{\frac{1}{2} \times \frac{-3}{2}} = x^{\frac{-3}{4}}$

7. Simplify $\log_2 8 - \log_2 4 - (\log_2 4.5 + \log_2 2)$ 1 / 1 point

- ○ 1
- ○ 2
- ◉ -1
- ○ 0

Correct

This is equivalent to:

$\log_2(\frac{8}{4}) - \log_2(4.5 \times 2) = 1 - 2 = -1$

8. If $\log_3 19 = 2.680$, what is $\log_9 19$? 1 / 1 point

- ○ 0.4347
- ○ 5.216
- ○ 0.8934
- ◉ 1.304

Correct

To convert from $\log_3$ to $\log_9$, divide by $\log_3 9$. Which is equal to 2, so the answer is 1.34

9. If $\log_{10} b = 1.8$ and $log_a b = 2.5752$, what is a? 1 / 1 point

- 6
- (•) 5
- 4
- 3

✓ Correct

To solve for a in the formula;

$$\log_a b = \frac{\log_x b}{\log_x a}$$

$\log_a b = 2.5752$ and $\log_{10} b = 1.8$

Therefore, $\log_{10} a$ must equal to $\frac{1.8}{2.5752} = 0.69897$

Treating both sides of equation $\log_{10} a = 0.69897$ as exponents of 10 gives $a = 10^{0.69897} = 5$

10. An investment of $1,600$ is worth $7,400$ after 8.5 years. What is the continuously compounded rate of return of this investment? 1 / 1 point

- (•) 18.02%
- 17.01%
- 19.01%
- 20.01

✓ Correct

$$\frac{\ln \frac{7400}{1600}}{8.5} = 0.18017$$

11. A pearl grows in an oyster at a continuously compounded rate of .24 per year. If a 25-year old pearl weighs 1 gram, what did it weigh when it began to form? 1 / 1 point

- 0.02478
- 0.2478
- (•) 0.002478
- 0.0002478

✓ Correct

$e^{(0.24 \times 25)} = \frac{1}{x}$

$x = \frac{1}{(e^{0.24 \times 25})}$

$x = \frac{1}{403.4288}$

$x = 0.002478$

12. $\log_2 z = 6.754$. What is $\log_{10}(z)$? 1 / 1 point

- 1.3508
- 0.49185
- 0.82956
- (•) 2.03316

✓ Correct

$\frac{\log_2 z}{\log_2 10} =$

$(\log_{10} z) \times (\log_2 10) = 3.321928$

Therefore, $\log_{10} z = \frac{6.754}{3.321928} = 2.03316$

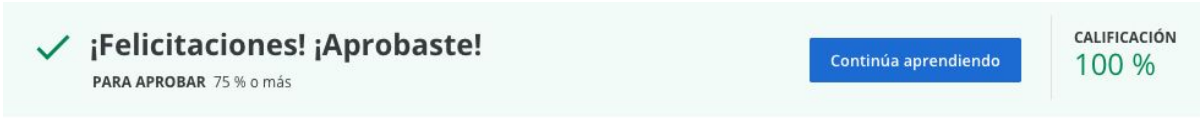
13. Suppose that $g : \mathbb{R} \to \mathbb{R}$ is a function, and that $g(1) = 10$. Suppose that $g'(a)$ is negative for every single value of a.Which of the following could possibly be $g(1.5)$? 1 / 1 point

- (•) $g(1.5) = 9.7$
- $g(1.5) = 11$
- $g(1.5) = 103.4$
- $g(1.5) = 10.1$

✓ Correct

Since the slope of the tangent line to the graph of g is negative everywhere on the graph, we know that g is *decreasing* function! And therefore we must have $g(1.5) < g(1)$. That is the case here, so this value is at least possible.

WEEK 4 – Basic Probability Definitions - Practice quiz on Probability Concepts (9 questions)



Practice quiz on Probability Concepts

TOTAL POINTS 9

1. If $x =$ "It is raining," what is $\sim (\sim x)$? — 1 / 1 point

- "It is raining"
- "It is not raining"
- "It is always raining"
- "It is never raining"

Correct
The second negation cancels out the first one.

Similarly $\sim (\sim (\sim x)) = \sim x$

2. If the statement "I am 25 years old" is assigned probability 0, what probability is assigned to the statement "I am not 25 years old"? — 1 / 1 point

- -1
- 0
- Unknown
- 1

Correct
It is always the case that $p(x) + p(\sim x) = 1$.

3. If I assign to the statement x = "it will rain today" a probability of $p(x) = 0.35$, what probability must I assign to the statement "it will not rain today?" — 1 / 1 point

- 0
- .35
- .5
- .65

Correct
$p(x) + p(\sim x) = 1$

4. Is the following collection of statements a probability distribution? — 1 / 1 point

1. I own a Toyota pickup truck
2. I do not own a Toyota pickup truck
3. I own a non-Toyota pickup truck
4. I do not own a non-Toyota pickup truck

- Yes
- No

Correct
The statements are not *exclusive*:1 and 4 could both be true, 2 and 3 could both be true, 2 and 4 could both be true, and even (1) and (3) could both be true (if I owned more than one pickup truck).

5. I don't know what it means to be "ingenuous." What probability would I assign to the statement, "I am ingenuous OR I am not ingenuous"? 1 / 1 point

- (●) 1
- ( ) -1
- ( ) .5
- ( ) 0

✓ Correct
It is always the case, regardless of the content of the statement x, that $p(x$ or $\sim x) = 1$

6. A friend of mine circumscribes a circle inside a square, so that the diameter of the circle and the edge of the square are the same length. He asks me to close my eyes and pick a point at random inside the square. He says the probability that my point will also be inside the circle is $\frac{\pi}{4}$ 1 / 1 point

Is this correct?

- (●) Yes
- ( ) No

✓ Correct

7. The probability of drawing a straight flush (including a Royal Flush) in a five-card poker hand is 0.0000153908 1 / 1 point

What is the probability of **not** drawing a straight flush?

- ( ) .9967253809
- ( ) .9996582672
- (●) .9999846092
- ( ) .9999745688

✓ Correct
$p(\sim x) = 1 - p(x)$

8. What is the probability that a fair, six-sided die will come up with a prime number? (Recall that prime numbers are positive integers other than 1 that are divisible only by themselves and 1) 1 / 1 point

- ( ) $\frac{2}{3}$
- ( ) $\frac{1}{3}$
- ( ) $\frac{1}{6}$
- (●) $\frac{1}{2}$

✓ Correct
The faces with 2, 3 and 5 satisfy the condition – which makes 3 relevant outcomes out of the "universe" of 6 outcomes = $\frac{3}{6} = \frac{1}{2}$

9. The joint probability p (the die will come up 5, the next card will be a heart) Is equal to the joint probability: 1 / 1 point

- ( ) p (the next card will **not** come up 5, the next card will be a heart)
- ( ) p (the die will **not** come up 5, the next card will **not** be a heart)
- (●) p (the next card will be a heart, the die will come up 5)
- ( ) p (the next card will be a heart, the die will **not** come up 5)

✓ Correct

WEEK 4 – Problem Solving Methods - Practice quiz on Problem Solving (9 questions)

¡Felicitaciones! ¡Aprobaste!

PARA APROBAR 75 % o más

Continúa aprendiendo

CALIFICACIÓN
100 %

Practice quiz on Problem Solving

TOTAL POINTS 9

1. I am given the following 3 joint probabilities:

   p(I am leaving work early, there is a football game that I want to watch this afternoon) = .1

   p(I am leaving work early, there is not a football game that I want to watch this afternoon) = .05

   p(I am not leaving work early, there is not a football game that I want to watch this afternoon) = .65

   What is the probability that there is a football game that I want to watch this afternoon?

   - (•) .3
   - ( ) .1
   - ( ) .2
   - ( ) .35

   ✓ Correct
   Getting the answer is a two-step process. First, recall that the sum of probabilities for a probability distribution must sum to 1. So the "missing" joint distribution

   p(I am not leaving work early, there is a football game I want to watch this afternoon) must be $1-(0.1+0.05+0.65)=0.2$

   By the sum rule, the marginal probability p(there is a football game that I want to watch this afternoon) = the sum of the joint probabilities

   P(I am leaving work early, there is a football game that I want to watch this afternoon) + P(I am not leaving work early, there is a football game I want to watch this afternoon) = $.1+.2=.3$

2. The Joint probability of my summiting Mt. Baker in the next two years AND publishing a best-selling book in the next two years is $.05$. If the probability of my publishing a best-selling book in the next two years is 10%, and the probability of my summiting Mt. Baker in the next two years is 30%, are these two events dependent or independent?

   - (•) Dependent
   - ( ) Independent

   ✓ Correct
   We know this because the joint distribution of 5% does not equal the product distribution of $(0.1)\times(0.3)=3\%$. If I summit Mt. Baker, I am more likely to publish a best-selling book, and vice versa.

3. The Joint probability of my summiting Mt. Baker in the next two years AND my publishing a best-selling book in the next two years is .05. 1 / 1 point

   If the probability of my publishing a best-selling book in the next two years is 10%, and the probability of my summiting Mt. Baker in the next two years is 30%, what is the probability that (sadly) in the next two years I will neither summit Mt. Baker nor publish a best-selling book?

   - (•) .65
   - ( ) .9
   - ( ) .95
   - ( ) .25

   ✓ Correct
   Set A = I will summit Mt. Baker in the next two years

   Set B = I will publish a best-selling book in the next two years.

   Since $p(A)=0.3$ and $p(A,B)=0.05$, by the SUM RULE we know that $p(A,\sim B)=(0.3-0.05)=0.25$

   Since $p(B)=0.1, p(\sim B)=0.9$

   Since $p(\sim B)=0.9$ and $p(A,\sim B)=0.25$ and again by the SUM RULE, $p(\sim A,\sim B)=0.9-0.25=.65$

4. I have two coins. One is fair, and has a probability of coming up heads of .5. The second is bent, and has a probability of coming up heads of $.75$. If I toss each coin once, what is the probability that *at least* one of the coins will come up heads?

   - (•) .875
   - ( ) .375
   - ( ) .625
   - ( ) 1.0

   ✓ Correct
   We apply the rule p(A or B or both)

   = 1 - (p(~A)p(~B))

   = 1 - ((1- .5)(1-.75))

   = 1 - .125

   =.875

5. What is $\frac{11!}{9!}$?

   - ( ) $110,000$
   - (•) 110
   - ( ) $4,435,200$
   - ( ) $554,400$

   ✓ Correct
   $\frac{11!}{9!}=11\times10=110$

6. What is the probability that, in six throws of a die, there will be exactly one each of "1" "2" "3" "4" "5" and "6"?

   - ( ) .00187220
   - ( ) .01176210
   - ( ) .01432110
   - (•) .01543210

   ✓ Correct
   There are $6!=720$ permutations where each face occurs exactly once.

   There are $6\times6\times6\times6\times6\times6=46656$ total permutations of 6 throws.

The probability is therefore $\frac{720}{46656} = 0.01543210$

7. On 1 day in 1000, there is a fire and the fire alarm rings. 1 / 1 point

On 1 day in 100, there is no fire and the fire alarm rings (false alarm)

On 1 day in $10,000$, there is a fire and the fire alarm does not ring (defective alarm).

On $9,889$ days out of $10,000$, there is no fire and the fire alarm does not ring.

If the fire alarm rings, what is the (conditional) probability that there is a fire?

Written p(there is a fire | fire alarm rings)

- 1.12%
- 90.9%
- 1.1%
- 9.09%

✓ Correct

10 days out of every $10,000$ there is fire and the fire alarm rings.

100 days out of every $10,000$ there is no fire and the fire alarm rings.

110 days out of every $10,000$ the fire alarm rings

The probability that there is a fire, given that the fire alarm rings, is $\frac{10}{110} = 9.09\%$

8. On 1 day in 1000, there is a fire and the fire alarm rings. 1 / 1 point

On 1 day in 100, there is no fire and the fire alarm rings (false alarm)

On 1 day in $10,000$, there is a fire and the fire alarm does not ring (defective alarm).

On $9,889$ days out of $10,000$, there is no fire and the fire alarm does not ring.

If the fire alarm does not ring, what is the (conditional) probability that there is a fire?

p(there is a fire | fire alarm does not ring)

- .01000%
- 0.01011%
- .10011%
- 1.0001%

✓ Correct

On $(1 + 9,889) = 9,890$ days out of every $10,000$ the fire alarm does not ring.

On 1 of those $10,000$ days there is a fire.

$\frac{1}{9890} = 0.01011\%$

9. A group of 45 civil servants at the State Department are newly qualified to serve as Ambassadors to foreign governments. There are 22 countries that currently need Ambassadors. How many distinct groups of 22 people can the President promote to fill these jobs? 1 / 1 point

- 8.2334 \times (10^12)
- =2.429*(10^-13)
- =1.06*(10^35)
- $$4.1167 \times (10^12)

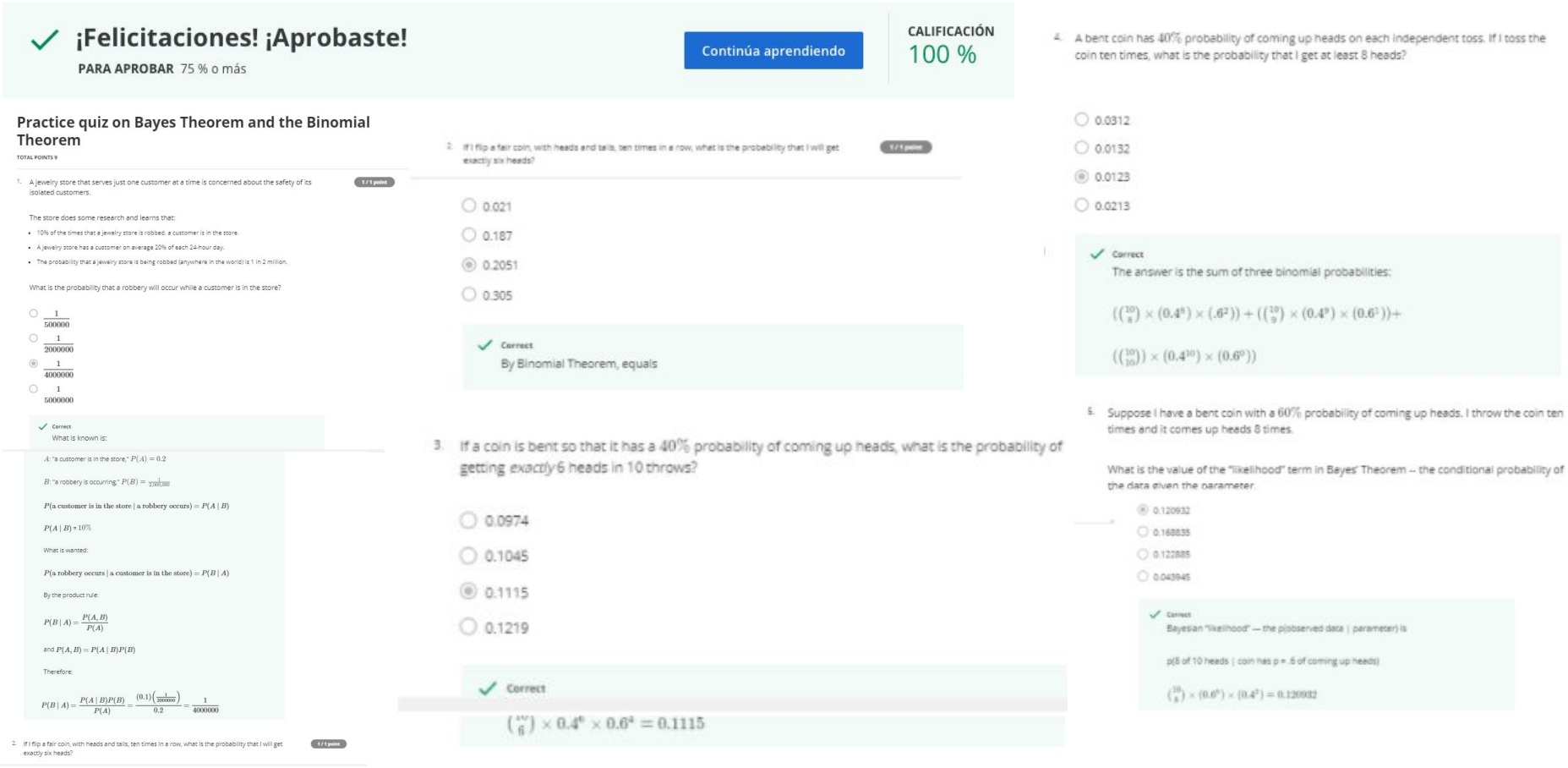
✓ Correct

$(\frac{45}{22})$

$= 45!/(23!)(22!)$

$= \frac{45!}{23! \times 22!}$

WEEK 4 – Applying Bayes Theorem and the Binomial Theorem - Practice quiz on Bayes Theorem and the Binomial Theorem (9 questions)



¡Felicitaciones! ¡Aprobaste!

PARA APROBAR 75 % o más

Continúa aprendiendo

CALIFICACIÓN 100 %

Practice quiz on Bayes Theorem and the Binomial Theorem

TOTAL POINTS 9

1. A jewelry store that serves just one customer at a time is concerned about the safety of its isolated customers. 1 / 1 point

The store does some research and learns that:

- 10% of the times that a jewelry store is robbed, a customer is in the store.
- A jewelry store has a customer on average 20% of each 24-hour day.
- The probability that a jewelry store is being robbed (anywhere in the world) is 1 in 2 million.

What is the probability that a robbery will occur while a customer is in the store?

- $\frac{1}{500000}$
- $\frac{1}{2000000}$
- ◉ $\frac{1}{4000000}$
- $\frac{1}{5000000}$

Correct

What is known is:

A: "a customer is in the store," $P(A) = 0.2$

B: "a robbery is occurring," $P(B) = \frac{1}{2000000}$

$P(\text{a customer is in the store} \mid \text{a robbery occurs}) = P(A \mid B)$

$P(A \mid B) = 10\%$

What is wanted:

$P(\text{a robbery occurs} \mid \text{a customer is in the store}) = P(B \mid A)$

By the product rule:

$$P(B \mid A) = \frac{P(A, B)}{P(A)}$$

and $P(A, B) = P(A \mid B)P(B)$

Therefore:

$$P(B \mid A) = \frac{P(A \mid B)P(B)}{P(A)} = \frac{(0.1)\left(\frac{1}{2000000}\right)}{0.2} = \frac{1}{4000000}$$

2. If I flip a fair coin, with heads and tails, ten times in a row, what is the probability that I will get exactly six heads? 1 / 1 point

- 0.021
- 0.187
- ◉ 0.2051
- 0.305

Correct

By Binomial Theorem, equals

$$\binom{10}{6} \times 0.4^6 \times 0.6^4 = 0.1115$$

3. If a coin is bent so that it has a 40% probability of coming up heads, what is the probability of getting *exactly* 6 heads in 10 throws?

- 0.0974
- 0.1045
- ◉ 0.1115
- 0.1219

Correct

4. A bent coin has 40% probability of coming up heads on each independent toss. If I toss the coin ten times, what is the probability that I get at least 8 heads?

- 0.0312
- 0.0132
- ◉ 0.0123
- 0.0213

Correct

The answer is the sum of three binomial probabilities:

$$\left(\binom{10}{8} \times (0.4^8) \times (.6^2)\right) + \left(\binom{10}{9} \times (0.4^9) \times (0.6^1)\right) +$$

$$\left(\binom{10}{10}\right) \times (0.4^{10}) \times (0.6^0))$$

5. Suppose I have a bent coin with a 60% probability of coming up heads. I throw the coin ten times and it comes up heads 8 times.

What is the value of the "likelihood" term in Bayes' Theorem -- the conditional probability of the data given the parameter.

- ◉ 0.120932
- 0.168835
- 0.122885
- 0.043945

Correct

Bayesian "likelihood" — the p(observed data | parameter) is

p(8 of 10 heads | coin has p = .6 of coming up heads)

$$\binom{10}{8} \times (0.6^8) \times (0.4^2) = 0.120932$$

6. We have the following information about a new medical test for diagnosing cancer.

Before any data are observed, we know that 5% of the population to be tested actually have Cancer.

Of those tested who do have cancer, 90% of them get an accurate test result of "Positive" for cancer. The other 10% get a false test result of "Negative" for Cancer.

Of the people who do not have cancer, 90% of them get an accurate test result of "Negative" for cancer. The other 10% get a false test result of "Positive" for cancer.

What is the conditional probability that I have Cancer, if I get a "Positive" test result for Cancer?

**Formulas in the feedback section are very long, and do not fit within the standard viewing window. Therefore, the font is a bit smaller and the word "positive test" has been abbreviated as PT.

- (selected) 32.1% probability that I have cancer
- 9.5%
- 4.5%
- 67.9%

✓ Correct

I still have a more than $\frac{2}{3}$ probability of not having cancer

Posterior probability:

p(I actually have cancer | receive a "positive" Test)

By Bayes Theorem:

$$= \frac{(\text{chance of observing a PT if I have cancer})(\text{prior probability of having cancer})}{(\text{marginal likelihood of the observation of a PT})}$$

$$= \frac{p(\text{receiving positive test} \mid \text{has cancer})p(\text{has cancer (before data is observed)})}{p(\text{positive} \mid \text{has cancer})p(\text{has cancer}) + p(\text{positive} \mid \text{no cancer})p(\text{no cancer})}$$

= (90%)(5%) / ((90%)(5%) + (10%)(95%)

=32.1%

7. We have the following information about a new medical test for diagnosing cancer. 1 / 1 point

Before any data are observed, we know that 8% of the population to be tested actually have Cancer.

Of those tested who do have cancer, 90% of them get an accurate test result of "Positive" for cancer.

The other 10% get a false test result of "Negative" for Cancer.

Of the people who do not have cancer, 95% of them get an accurate test result of "Negative" for cancer.

The other 5% get a false test result of "Positive" for cancer.

What is the conditional probability that I have cancer, if I get a "Negative" test result for Cancer?

- .80%
- 99.1%
- 88.2%
- (selected) 0.9%

✓ Correct

$$p(\text{cancer} \mid \text{negative test}) =$$

$$\frac{p(\text{negative test} \mid \text{Cancer})\,p(\text{Cancer})}{p(\text{negative test} \mid \text{cancer})\,p(\text{cancer}) + p(\text{negative test} \mid \text{no cancer})\,p(\text{no cancer})}$$

$$\frac{(10\%)(8\%)}{(10\%)(8\%)+(95\%)(92\%)}$$

$$\frac{0.8\%}{0.8\%+87.4\%}$$

$$\frac{0.8\%}{88.2\%}$$

$$= 0.9\%$$

8. An urn contains 50 marbles - 40 blue and 10 white. After 50 draws, exactly 40 blue and 10 white are observed. 1 / 1 point

You are not told whether the draw was done "with replacement" or "without replacement."

What is the probability that the draw was done with replacement?

- 87.73%
- (selected) 12.27%
- 13.98%
- 1

✓ Correct

p(40 blue and 10 white | draws without replacement) = 1 [this is the only possible outcome when 50 draws are made without replacement]

p(40 blue and 10 white | draws with replacement)

S = 40

N = 50

P = .8 [for draws with replacement] because 40 blue of 50 total means p(blue) = 40/50 = .8

$$\left(\binom{50}{40}\right)(0.8^{40})(0.2^{10})$$

$$= 13.98\%$$

By Bayes' Theorem:

p(draws with replacement | observed data) =

$$\frac{13.98\%(.5)}{(13.98\%)(.5)+(1)(.5)}$$

$$= \frac{0.1398}{1.1398}$$

$$= 12.27\%$$

9. According to Department of Customs Enforcement Research: 99% of people crossing into the United States are not smugglers. 1 / 1 point

The majority of all Smugglers at the border (65%) appear nervous and sweaty.

Only 8% of innocent people at the border appear nervous and sweaty.

If someone at the border appears nervous and sweaty, what is the probability that they are a Smuggler?

- 7.92%
- 92.42%
- (selected) 7.58%
- 8.57%

✓ Correct

By Bayes' Theorem, the answer is

$$(.65)(.01)$$

WEEK 4 – Applying Bayes Theorem and the Binomial Theorem - Probability (basic and Intermediate) Graded Quiz (12 questions)

¡Felicitaciones! ¡Aprobaste!

PARA APROBAR 75 % o más

Continúa aprendiendo

CALIFICACIÓN
100 %

Probability (basic and Intermediate) Graded Quiz

LATEST SUBMISSION GRADE
100%

1. What additional statement, added to the three below, forms a probability distribution? — 1 / 1 point

(1) I missed only my first class today

(2) I missed only my second class today

(3) I missed both my first and second class today

Correct

2. My friend takes 10 cards at random from a 52-card deck, and places them in a box. Then he puts the other 42 cards in a second, identical box. He hands me one of the two boxes and asks me to draw out the top card. What is the probability that the first card I draw will be the Ace of Spades? — 1 / 1 point

Correct

3. I will go sailing today if it does not rain. Are the following two statements Independent or dependent? — 1 / 1 point

(1) "I will go sailing today"

(2) "It will not rain today"

Correct

4. The probability that I will go sailing today AND the fair six-sided die will come up even on the next roll is .3.

If these events are independent, what is the probability that I will go sailing today?

Correct

5. I have two coins. One is fair, and has a probability of coming up heads of.5.
The second is bent, and has a probability of coming up heads of.75.
If I toss each coin once, what is the probability that at least one of the coins will come up tails?

Correct

6. What is the probability, when drawing 5 cards from a fair 52-card deck, of drawing a "full house" (three of a kind and a pair) in the form AAABB?

Correct

7. If it rains, I do not go sailing. It rains 10% of days; I go sailing 3% of days.

If it does not rain, what is the (conditional) probability that I go sailing?

Written "p(I go sailing | it does not rain)"?

Correct

8. I am at my office AND not working 2% of the time. I am at my office 10% of the time. What is the conditional probability that I am not working, if I am at my office?

1 / 1 point

✓ Correct

9. The factory quality control department discovers that the conditional probability of making a manufacturing mistake in its precision ball bearing production is 4% on Tuesday, 4% on Wednesday, 4% on Thursday, 8% on Monday, and 12% on Friday.

The Company manufactures an equal amount of ball bearings (20%) on each weekday. What is the probability that a defective ball bearing was manufactured on a Friday?

1 / 1 point

✓ Correct

10. An Urn contains two white marbles and one black marble. A marble is drawn from the Urn without replacement and put aside without my seeing it. Then a second marble is drawn, and it is white.

What is the probability that the unknown removed marble is white, and what is the probability that it is black?

1 / 1 point

✓ Correct

11. What is the probability, if I flip a fair coin with heads and tails ten times in a row, that I get at least 8 heads?

1 / 1 point

✓ Correct

12. Suppose I have either a fair coin or a bent coin, and I don't know which. The bent coin has a 60% probability of coming up heads.

I throw the coin ten times and it comes up heads 8 times. What is the probability I have the fair coin vs. the probability I have the bent coin?

Assume at the outset there is an equal $(.5, .5)$ prior probability of either coin.

*Please note that in order to fit the entire formula in the feedback, probability has been abbreviated to "prob."

1 / 1 point

✓ Correct