Business 4720 - Class 12

Supervised Machine Learning using R

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This Class

What You Will Learn:

- ► Linear Regression Models in R
 - Linear regression
 - Lasso and Ridge regression
- Classification Models in R
 - ► Logistic Regression
 - ► K-NN



Based On

Gareth James, Daniel Witten, Trevor Hastie and Robert Tibshirani: *An Introduction to Statistical Learning with Applications in R.* 2nd edition, corrected printing, June 2023. (ISLR2)

https://www.statlearning.com

Chapters 2, 3, 4, 5

Trevor Hastie, Robert Tibshirani, and Jerome Friedman: *The Elements of Statistical Learning*. 2nd edition, 12th corrected printing, 2017. (ESL)

https://hastie.su.domains/ElemStatLearn/

Chapters 2, 3, 4, 7

Kevin P. Murphy: *Probabilistic Machine Learning – An Introduction*. MIT Press 2022.

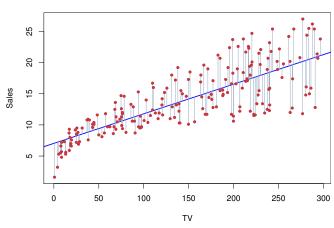
https://probml.github.io/pml-book/book1.html

Chapters 4, 6, 9, 10, 11

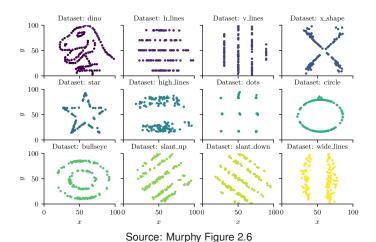


Linear Regression

$$Y = \beta_0 + \beta_1 X + \epsilon$$



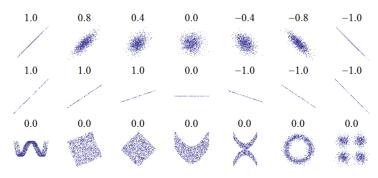
Ensure a Linear Model is Sensible



The "Datasaurus Dozen": All datasets have the same correlation between the two variables!



Ensure a Linear Model is Sensible



Source: Murphy Figure 3.1

Datasets with the same correlation (as indicated above each dataset) between two variables do not need to have the same regression slope!

Estimating Linear Regression [cont'd]

Estimate $\hat{\beta}_0$ and $\hat{\beta}_1$ to minimize the mean squared error (MSE) or residual sum of square (RSS)

$$RSS = \sum_{i} (y_i - \hat{\beta}_0 - \hat{\beta}_1 x_i)^2$$
 $MSE = \frac{1}{n}RSS$

Analytically derivable least squares estimates are

$$\hat{\beta}_1 = \frac{\sum_i (x_i - \bar{x})(y_i - \bar{y})}{\sum_i (x_i - \bar{x})^2}$$

$$\hat{\beta}_0 = \bar{y} - \hat{\beta}_1 \bar{x}$$

where \bar{x} and \bar{y} are the sample means

► MSE ("L2 loss") is susceptible to outlier influence, the MAE ("L1 loss") is more robust

Evaluating Linear Regression Models [cont'd]

- Estimates have standard errors that indicate uncertainty of the estimates
- A *t-test* can be used to determine if a parameter is statistically significant from a value V (typically V=0) using the test statistic

$$t = \frac{\hat{\beta}_1 - V}{SE(\hat{\beta}_1)}$$

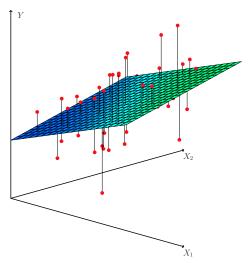
- ► The *p-value* is the probability that the parameter is non-zero, assuming the estimated model is true
- ightharpoonup The R^2 value is the proportion of explained variance

$$R^2 = \frac{TSS - RSS}{TSS} = 1 - \frac{RSS}{TSS}$$

where $TSS = \sum_i (y_i - \bar{y})^2$ is the total sum of squares



Generalization to Multiple Predictors



$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \cdots + \beta_p X_p + \epsilon$$

 R^2 represents the correlation of Y and \hat{Y}

Source: ISLR2 Figure 3.4



Regression with Qualitative Predictors

Qualitative predictors (factors with multiple, exclusive levels) can be used in linear regression models using dummy variables:

$$x_{i1} = egin{cases} 1 & ext{level "a"} \ 0 & ext{else} \end{cases}$$
 $x_{i2} = egin{cases} 1 & ext{level "b"} \ 0 & ext{else} \end{cases}$
 $x_{i3} = egin{cases} 1 & ext{level "c"} \ 0 & ext{else} \end{cases}$

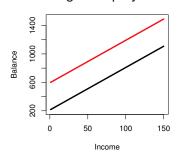
- Note: $x_{i1} = x_{i2} = x_{i3} = 0$ represents level d!
- "Contrasts" determine how factor levels are coded using dummy variables

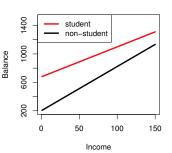
Inputs, Predictors, and Polynomials

Example:

$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_1^2 + \beta_3 X_2 + \beta_4 X_1 X_2 + \epsilon$$

- ▶ Still linear in β_i
- ightharpoonup Two inputs X_1 and X_2
- ▶ Four predictors or features: X_1 , X_1^2 , X_2 , X_1X_2
- ▶ Main effects β_1 and β_3 , interaction effect β_4 , and a degree-2 polynomial

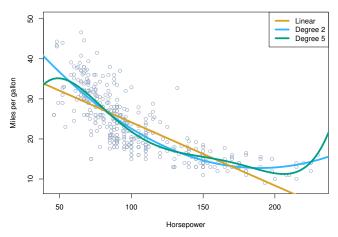




Source: ISLR2 Figure 3.7



Multiple Regression with Polynomial Expansion



Source: ISLR2 Figure 3.8



Multiple Linear Regression in R

The 'Boston' data set contains housing values in Boston in variable medv (median value). Examine the data:

```
# Functions and data from the textbook # 'Modern
# Applied Statistics with S'
library (MASS)
# Data sets from the textbook 'Introduction to
# Statistical Learning with Applications in R'
library(ISLR2)
# Get a description of the data
?Boston
# Get a summary and first few rows
summary (Boston)
head (Boston)
# Bivariate scatterplots
plot (Boston)
```

Fit a simple model, examine the results, and make predictions:

```
# Fit a model with intercept only
fitted.model <- lm(medv ~ 1, data=Boston)
summary(fitted.model)
# Fit a model with predictor 1stat
fitted.model <- lm(medv ~ lstat, data=Boston)
summarv(fitted.model)
# Plot the data and the regression line
plot (medv ~ lstat, data=Boston)
abline (fitted.model, lwd=3, col='red')
# Plot the residuals against predicted values
plot(predict(fitted.model), residuals(fitted.model))
# Predict three new observations of lstat
predict(fitted.model, data.frame(lstat=c(5, 10, 15)),
   interval='confidence')
```

Build more complex models:



Add polynomial terms:

```
# Add a polynomial term; use the I(.) function
# for any data transformations, such as log(),
# or exp() or sqrt() as well as polynomials
fitted.model <- lm(medv ~ lstat + I(lstat^2),
    data=Boston)
summary(fitted.model)

# Add all polynomial terms up to degree 5
fitted.model <- lm(medv ~ poly(lstat, 5), data=Boston)
# Note the coefficients for the polynomials
# in the summary
summary(fitted.model)</pre>
```



Categorical predictors ("factors") using dummy variables:

```
?Carseats
```

Identify factor/categorical variables and their levels:

```
is.factor(Carseats$ShelveLoc)
levels(Carseats$ShelveLoc)
levels(Carseats$Urban)
levels(Carseats$US)
```

Contrasts show the dummy variables created (columns) and the values they take for different factor levels (row):

```
contrasts(Carseats$ShelveLoc)
contrasts(Carseats$US)
```

Fit the model:

```
summary(lm(Sales ~ . , data=Carseats))
```

Hands-On Exercises

(Source: ISLR2 Chapter 3)

Use the Auto data set from the ISLR2 library with mpg as the target.

- 1 Perform a linear regression with horsepower as predictor
- 2 Is there a relationship between the predictor and target? What form and how strong?
- 3 What is the predicted mpg value for a horsepower of 98?
- 4 Plot the response and predictor. Use the abline() function to add the regression line
- 5 Produce a scatterplot of all variables
- Perform a linear regression of all main effects (except for the variable name), then remove non-significant predictors
- 7 Use the ∗ and : symbols to add interaction effects. Retain only significant ones
- Add transformations of the predictors (using the I(.) functions such as $\log(X)$, \sqrt{X} , X^2 .

Hands-On Exercises

(Source: ISLR2 Chapter 3)

Use the Carseats data set from the ISLR2 library with Sales as the target.

- 1 Perform a linear regression with Price, Urban and US as predictors
- Interpret the coefficients. Tip: Some variables are categorical
- 3 Remove non-significant predictors
- 4 How well do the two models fit the data?
- Determine the 95% confidence intervals for the coefficients of each model.
- 6 (How) does the importance of predictors change?



Cross-Validation in R – Holdout Sample

Validation set approach:

```
# Set the seed for the pseudo-random
# number generator (RNG)
set.seed(1)
# Randomly use half the Auto data as training sample
train.idx <- sample(nrow(Auto), nrow(Auto)/2)</pre>
train.data <- Auto[train.idx,]
test.data <- Auto[-train.idx,]
# Fit model to (train model on) a subset
fitted.model <- lm(mpg ~ horsepower, data=train.data)
# Calculate the validation data MSE.
mean((test.data$mpq-predict(fitted.model,test.data))^2)
# Calculate the training MSE, first from residuals,
# then by explicitly predicting the training data
mean (summary (fitted.model) $residuals^2)
mean((train.data$mpq-predict(fitted.model,train.data))^2)
```

Cross-Validation in R – Leave One Out CV

- ► The glm() function fits Generalized Linear Models using maximum-likelihood estimation, not RSS minimization. They yield identical solutions for "ordinary" linear models but MLE is more flexible and can be used on a wide range of models.
- The use of glm() is identical to that of lm() for "ordinary" linear models; the boot package provides cross-validation for glm models
- ▶ **Tip:** LOOCV is K-Fold CV with K = N

```
library(boot)

# Fit a model with glm and show its summary
glm.fit <- glm(mpg ~ horsepower, data=Auto)
summary(glm.fit)

# LOOCV is k-fold CV where k equals N, num of obs
cv.err <- cv.glm(Auto, glm.fit, K=nrow(Auto))
cv.err$delta[1]</pre>
```

Cross-Validation in R – K-Fold CV

K-Fold Cross-Validation using the glm function

```
cv.err <- cv.glm(Auto, glm.fit, K=10)
cv.err$delta[1]</pre>
```

Example: Use cross-validation to compare different models:

```
set.seed(17)
cv.err <- rep(0, 5)
for(i in 1:10) {
   glm.fit <- glm(mpg ~ poly(horsepower,i), data=Auto)
   cv.err[i] <- cv.glm(Auto, glm.fit, K=10)$delta[1]
}
cv.err</pre>
```



Hands-On Exercises – Cross-Validation

Consider the Boston housing data set Boston.

- 1 Fit a regression model using medv as target, and age, lstat, and ptratio as predictors
- Using the validation set approach, compute the test error of this model. Perform the following steps
 - 2.1 Split the data set using 75% for training and 25% for testing
 - 2.2 Fit the model to training data
 - 2.3 Predict the target for the testing data
 - 2.4 Compute the test error
- Repeat the previous step 3 times, using different splits. How do the results change?
- 4 Average the test error of the four splits.
- 5 Include dis as predictor. Does it reduce the test error?
- Calculate the test error estimate using LOOCV. Compare your result to that of step 4.
- Calculate the test error estimate using 4-fold cross-validation. Compare the estimate to that of step

Shrinkage Methods

Goals

- Avoid overfitting
- Reduce variance
- "Shrink" regression coefficients towards zero
- Penalize coefficients that are "too high"
- Type of "regularization"

Ridge Regression

a.k.a Tikhonov Regularization

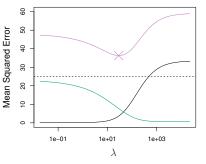
Minimize
$$RSS + \lambda \sum_{i=1}^{p} \beta_j^2 = RSS + \lambda ||\beta||_2^2$$

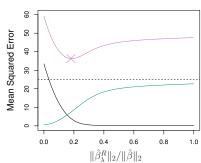
- ▶ L2 regularizer (it penalizes the L2 norm of β)
- ightharpoonup Parameter λ controls the amount of shrinkage
- Larger λ reduce variance but increase bias
- Not scale invariant: Standardize predictors



Ridge Regression

a.k.a Tikhonov Regularization





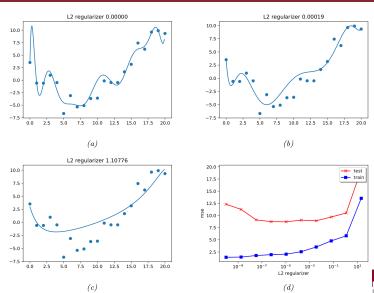
Source: ISLR2 Figure 6.5

- ▶ Bias
- Variance
- ► MSE



Ridge Regression Example

Fitting a Degree 14 Polynomial

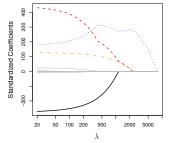


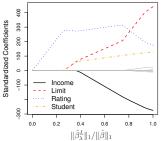
Lasso regression

"Least Absolute Shrinkage and Selection Operator"

$$\label{eq:minimize} \text{Minimize} \quad \textit{RSS} + \lambda \sum_{j=1}^p |\beta_j| = \textit{RSS} + \lambda ||\beta||_1$$

- ▶ L1 regularizer (it penalizes the L1 norm of β)
- ▶ Lasso may exclude variables by forcing their β_i to 0
- Parsimonious, more interpretable models than ridge regression





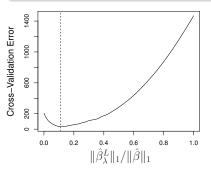
Source: ISLR2 Figure 6.6

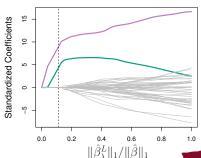


Selecting the Tuning Parameter

Grid Search

- ▶ Define a "grid" of tuning parameters (e.g. λ) to search
- Cross-validate models for each point in the grid (each value of λ)
- Fit the final model to the optimal cross-validated error





Source: ISLR2 Figure 6.13

Elastic Net

The Elastic Net penalty is a mix of L1-norm $||\beta||_1$ and L2-norm $||\beta||_2^2$ penalties, defined by α :

$$\lambda \left(\alpha ||\beta||_1 + (1-\alpha)||\beta||_2^2 \right)$$

- $ightharpoonup \alpha = 0$: Ridge regression
- $ightharpoonup \alpha = 1$: Lasso

The <code>glmnet()</code> function in the <code>glmnet</code> library uses the Elastic Net regularization method.



Ridge Regression in R

Use the Hitters data set to model Salary as outcome and other variables as predictors.

```
library(ISLR2)
library(glmnet)

# Remove missing values
Hitters <- na.omit(ISLR2::Hitters)</pre>
```

The glmnet () function requires separate x and y values, instead of a formula. To create dummy variables for categorical variables, use the model.matrix function:

```
# Create dummy variables for categorical variables
# Remove intercept from model
x <- model.matrix(Salary ~ ., Hitters)[, -1]
y <- Hitters$Salary</pre>
```



Ridge Regression in R [cont'd]

Set up a sequence of λ to try and fit the model for each λ :

```
# Set up the sequence of lambda values to try
grid <- 10^seq(from=10, to=-2, length=100)
print(grid)
ridge.model <- glmnet(x, y, alpha=0, lambda=grid)</pre>
```

Examine some results:

```
# Select the 50th lambda value
ridge.model$lambda[50]
coef(ridge.model)[, 50]
L2.norm = sqrt(sum(coef(ridge.model)[-1, 50]^2))

# Select the 60th lambda value
ridge.model$lambda[60]
coef(ridge.model)[, 60]
L2.norm = sqrt(sum(coef(ridge.model)[-1, 60]^2))
```

Ridge Regression in R [cont'd]

Identify the optimal λ using cross-validation. First, create holdout test data set:

```
# Randomly split the Hitters data
train.idx <- sample(nrow(Hitters), nrow(Hitters)/2)
x.train <- x[train.idx,]
x.test <- x[-train.idx,]
y.train <- y[train.idx]
y.test <- y[-train.idx]</pre>
```

Use the training set for cross-validation:

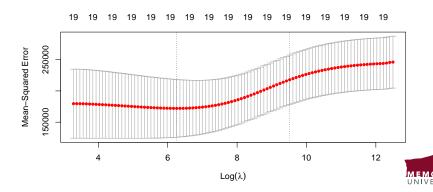
```
# 5-fold cross-valiation, use MSE as metric
cv.out <- cv.glmnet(x.train, y.train, alpha=0,
    nfolds=5, type.measure='mse')</pre>
```



Ridge Regression in R [cont'd]

Show the optimal lambda, the MSE measure, the SE of MSE and the number of non-zero coefficients. Also shown the largest lambda within one SE of the optimal lambda.

```
print(cv.out)
plot(cv.out)
lambda.opt <- cv.out$lambda.min</pre>
```



Ridge Regression in R – Prediction

Fit test data:

```
ridge.test <- glmnet(x.test, y.test, alpha=0)</pre>
```

Compare regression coefficients between ridge using optimal λ and unpenalized least squares:

```
# Show the coefficients at optimal lambda
predict(ridge.test, type='coefficients', s=lambda.opt)
# Compare to unpenalized least-squares fit
coef(lm.fit(x.test, y.test))
```



Ridge Regression in R – Prediction

Predict values for the test data set:

Calculate test MSE to compare to the CV optimal MSE above:

```
mean((predictions - y.test)^2)
```

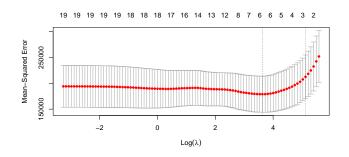
Recall, the CV cross-validated error on the training set is an estimate/approximation of the real test error.



The Lasso in R

Identify the optimal λ using cross-validation:

Note the number of non-zero coefficients in the result:





The Lasso in R – Prediction

Fit test data:

```
lasso.test <- glmnet(x.test, y.test, alpha=1)</pre>
```

Compare regression coefficients between Lasso using optimal λ and unpenalized least squares:

```
# Show the coefficients at optimal lambda, note the
# many zero coefficients
predict(lasso.test, type='coefficients', s=lambda.opt)
# Compare to unpenalized least-squares fit
coef(lm.fit(x.test, y.test))
```

Predict values for the test data set and compute test MSE



Hands-On Exercises – Shrinkage Methods

Source: ISLR2, Chapter 6

Predict the number of applications received using the other variables in the College dataset

- Split the data set into a training and a test set
- 2 Fit an unpenalized linear model on the training set. Report the test error.
- 3 Fit a ridge regression model on the training set, with λ chosen by cross-validation. Report the test error.
- 4 Fit a lasso model on the training set, with λ chosen by cross-validation. Report the test error.
- 5 Compare and conrast the results



Hands-On Exercises – Shrinkage Methods

Source: ISLR2, Chapter 6

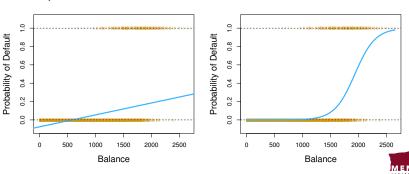
Predict the per-capita crime rate in the Boston data set using the other variables.

- Split the data set into a training and a test set
- 2 Fit an unpenalized linear model on the training set. Report the test error.
- 3 Fit a ridge regression model on the training set, with λ chosen by cross-validation. Report the test error.
- 4 Fit a lasso model on the training set, with λ chosen by cross-validation. Report the test error.
- 5 Compare and conrast the results



Classification

- Qualitative (categorical) outcome
- Estimate/predict probabilities of class membership
- ▶ Problem: Linear combinations of predictors are not limited to [0, 1]
- Solution: "Link" function that transforms the weighted sum of predictors

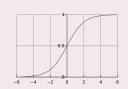


Source: ISLR2 Figure 4.2

Logistic Regression

Logistic / Sigmoid Function

$$\sigma(x) = \frac{1}{1 + e^{-x}} = \frac{e^x}{1 + e^x}$$
$$= 1 - \sigma(-x)$$



Binary Case (Binomial Logistic Regression)

$$\begin{split} \rho(X) &= \sigma(\beta_0 + \beta_1 X) = \frac{e^{\beta_0 + \beta_1 X}}{1 + e^{\beta_0 + \beta_1 X}} \\ &\Rightarrow \quad \frac{\rho(X)}{1 - \rho(X)} = e^{\beta_0 + \beta_1 X} \quad \text{"Odds"} \\ &\Rightarrow \quad \log\left(\frac{\rho(X)}{1 - \rho(X)}\right) = \beta_0 + \beta_1 X \quad \text{"Log-Odds", "Logits"} \end{split}$$

Logistic Regression [cont'd]

Predictions

Given estimates $\hat{\beta}_0$ and $\hat{\beta}_1$, use the link function to predict probabilities:

$$\hat{p}(X) = \frac{e^{\hat{\beta}_0 + \hat{\beta}_1 X}}{1 + e^{\hat{\beta}_0 + \hat{\beta}_1 X}}$$



Logistic Regression [cont'd]

- ▶ Multiple *p* predictors: **Multiple Linear Regression**
- ► Multiple *K* classes: **Multinomial Logistic Regression**
- ▶ Multiple *n* labels: **Multi-label Classification**



Multinomial Logistic Regression

$$\log\left(\frac{\Pr(Y=k|X=x)}{\Pr(Y=K|X=x)}\right) = \beta_{k0} + \beta_{k1}x_1 + \dots + \beta_{kp}x_p, k < K$$

Exponentiating and rearranging:

$$\Pr(Y = k | X = X) = \Pr(Y = K | X = X) e^{\beta_{k0} + \beta_{k1} X_1 + \dots + \beta_{kp} X_p}, k < K$$

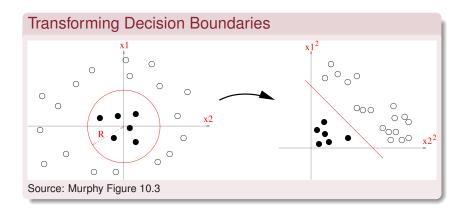
Because probabilities must sum to 1:

$$Pr(Y = K|X = x) = 1 - \sum_{l=1}^{K-1} Pr(Y = l|X = x)$$

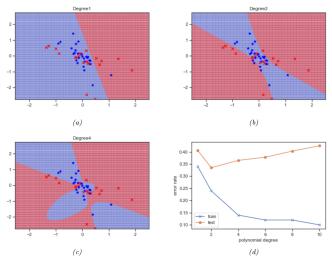
$$= 1 - \sum_{l=1}^{K-1} Pr(Y = K|X = x) e^{\beta_{k0} + \beta_{k1} x_1 + \dots + \beta_{kp} x_p}$$

$$\Rightarrow Pr(Y = K|X = x) = \frac{1}{1 + \sum_{l=1}^{K-1} e^{\beta_{k0} + \beta_{k1} x_1 + \dots + \beta_{kp} x_p}}$$

Logistic Regression with Polynomial Expansion



Logistic Regression with Polynomial Expansion [cont'd]







Logistic Regression in R

Use the stock market data set Smarket to predict the binary outcome Direction (the direction of market changes, up or down) using prior returns as predictors:

```
library(ISLR2)
?Smarket
```

Contrasts show how factor levels are encoded using dummy variables:

```
contrasts(Smarket$Direction)
```

Note the family argument for the glm function:

Logistic Regression in R – Prediction

Predict logits for training set:

```
logreg.logits <-
    predict(logreg.fitted, newdata = Smarket)</pre>
```

Predict probabilities for training set:

Predict categorical outcomes:

```
# Predict 'up' or 'down' based on probabilities
# and a fixed threshold
pred.direction <- rep('Down', nrow(Smarket))
pred.direction[logreg.probabilities > .5] <- 'Up'</pre>
```

Logistic Regression in R – Prediction

```
# Compute confusion matrix
logreg.cm <- table(pred.direction, Smarket$Direction)
print(logreg.cm)

# Compute accuracy
mean(pred.direction == Smarket$Direction)</pre>
```

Logistic Regression in R – Holdout Set

Split data to train and test set. Because this is time-dependent data, split by time to avoid mixing past and future data:

```
train.data <- Smarket[Smarket$Year < 2005,]
test.data <- Smarket[!(Smarket$Year < 2005),]</pre>
```

Fit using training set:

```
logreg.fitted <-
   glm(Direction~Lag1+Lag2+Lag3+Lag4+Lag5+Volume,
   data=train.data, family=binomial(link='logit'))</pre>
```

Predict probabilities for test data and classify:

```
logreg.probabilities <- predict(logreg.fitted,
    newdata = test.data, type='response')
pred.direction <- rep('Down', nrow(test.data))
pred.direction[logreg.probabilities > .5] <- 'Up'</pre>
```

Logistic Regression in R – Holdout Set

Compute confusion matrix and accuracy for test data:

```
logreg.cm <- table(pred.direction, test.data$Direction)
print(logreg.cm)
mean(pred.direction == test.data$Direction)</pre>
```



Logistic Regression in R – Evaluation

Using the ROCR library for classifier evaluation:

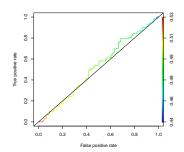
```
library (ROCR)
# A prediction object collects predicted
# probabilities and true labels
pred.obj <- prediction(logreg.probabilities,</pre>
                        test.data$Direction)
# Get some classifier performance metrics
# ROCR varies the threshold.
plot (performance (pred.obj, 'acc'))
plot (performance (pred.obj, 'prec'))
plot (performance (pred.obj, 'rec'))
plot (performance (pred.obj, 'f'))
performance(pred.obj, 'auc')@y.values[[1]]
```

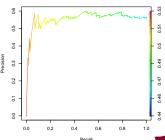


Logistic Regression in R – Evaluation

continued ...

```
# ROC - True positive rate versus false positive rate
plot (performance (pred.obj, 'tpr', 'fpr'), colorize=T)
abline (0, 1)
# Precision/Recall plot
plot (performance (pred.obj, 'prec', 'rec'), colorize=T)
```





Naive Bayes Classifier

Bayes Theorem:

$$\Pr(Y = c | X) = \frac{p(X|Y = c) p(Y = c)}{p(X)}$$

$$= \frac{p(X|Y = c) p(Y = c)}{\sum_{l=1}^{K} p(X|Y = l) p(Y = l)}$$

Naive Bayes Assumption: Within each class c, the D predictors are independent:

$$p(X|Y = c) = p(x_1|Y = c) \times p(x_2|Y = c) \times \cdots \times p(x_D|Y = c)$$
$$= \prod_{i=1}^{D} p(x_d|Y = c)$$

Posterior probability:

$$p(Y = c|X) = \frac{\left(\prod_{d=1}^{D} p(x_d|Y = c)\right) p(Y = c)}{\left(\sum_{l=1}^{K} \prod_{d=1}^{D} p(x_d|Y = l)\right) p(Y = l)}$$



Naive Bayes Classifier in R

Naive Bayes using the naiveBayes function in the e1071 library:

```
library(e1071)

# Fit using same syntax as glm
nb.fitted <-
    naiveBayes(Direction~Lag1+Lag2, data=train.data)

# Output contains prior and conditional
# probabilities (and their SD)
nb.fitted
```

Predict class membership and compute confusion matrix:

```
nb.predictions <- predict(nb.fitted, test.data)
nb.cm <- table(nb.predictions, test.data$Direction)
print(nb.cm)</pre>
```

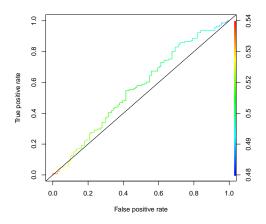


Naive Bayes Classifier in R – Evaluation

Evaluate the classifier:

Assess ROC and AUC:

Naive Bayes Classifier in R – Evaluation





KNN Classification in R

Using the knn function from the class library:

```
library(class)
```

Use only two predictors:

```
train.x <- cbind(train.data$Lag1, train.data$Lag2)
test.x <- cbind(test.data$Lag1, test.data$Lag2)
train.y <- train.data$Direction
test.y <- test.data$Direction</pre>
```

Make predictions from training set for test set, given true classes of training set (k = 3 and return probabilities):

```
knn.pred <- knn(train.x, test.x, train.y, k=3, prob=T)
```



KNN Classification in R

Evaluate the classifier against test data:

```
# Confusion matrix
table(knn.pred, test.y)
# Accuracy
mean(knn.pred == test.y)
```

Save class probabilities of the majority class:

```
knn.probs <- attributes(knn.pred)$prob
```

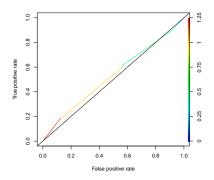
Compute class probabilities of the minority class:

```
knn.class.probs <- knn.probs
knn.class.probs[knn.pred=='Down'] <-
1-knn.probs[knn.pred=='Down']
```



KNN Classification in R [cont'd]

Use ROCR functions to evaluate classifier:





Hands-On Exercises

Source: ISLR2, Chapter 4

Use the Weekly data set in the ISLR2 package.

- Use the full data set to perform a logisttic regression with Direction as target. Which predictors are statistically significant?
- 2 Compute the confusion matrix and accuracy.
- 3 Use the 1990 to 2008 data for a training set and the 2009/2010 for a test set. Fit a logistic regression model with Lag2 as the only predictor.
- 4 Repeat (3) using Naive Bayes
- Repeat (3) using KNN with K = 1
- 6 Which model provides the best results on this data?



Hands-On Exercises

Source: ISLR2, Chapter 4

Use the Auto data set in the ISLR2 package.

- 1 Create a binary variable, mpg01 that contains a 1 if mpg is above its median, 0 otherwise. *Tip*: Use the median() function. Add the new variable to the data frame.
- Split the data set into training and test set
- Perform a logistic regression on the training data to predict mpg01 from the other features. What is the test error of this model?
- 4 Repeat (3) using Naive Bayes
- Repeat (3) using KNN with different values of *K*. What value of *K* performs best?



Hands-On Exercises

Source: ISLR2, Chapter 4

Using the Boston data set in the ISLR2 library, fit classification models to predict whether a given census tract has a crime rate above or below the median.

- 1 Create a new binary variable crime 01 that is 1 is crime is above its median, and 0 otherwise. Combine this variable with the data frame. *Tip*: Use the median() function for this.
- Split your data set into a training and test data set
- Fit logistic regression, Naive Bayes, and KNN (with different K)
- Describe your findings in terms of prediction error, precision, recall, F1 and AUC

