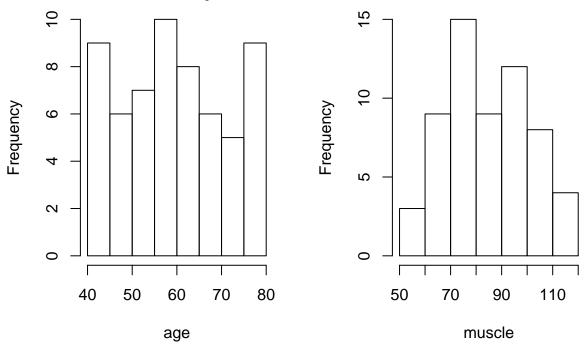
Stats 206 Homework 2

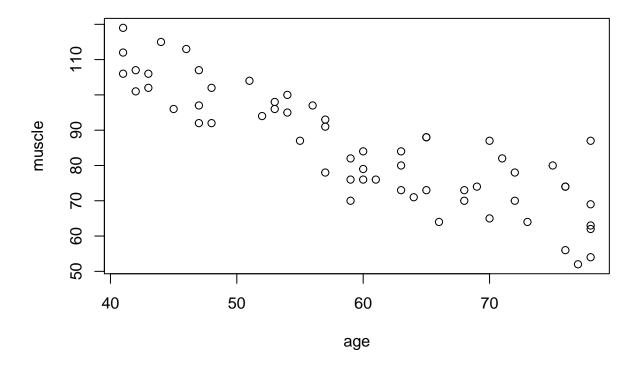
Clark Fitzgerald October 16, 2014

1a

The histograms of muscle and age are unsurprising. The ranges are as expected. Age appears to be roughly uniform and muscle has a bell shape.



The relation between age and muscle appears to be linear, and it looks like muscle mass decreases with age.



1b

After fitting the linear model we extract regression coefficients with their standard errors, the mean squared error (MSE), and its degrees of freedom.

Regression coefficients:

```
## (Intercept) age
## 156.346564 -1.189996
```

Standard errors for regression coefficients:

```
## (Intercept) age
## 5.51226249 0.09019725
```

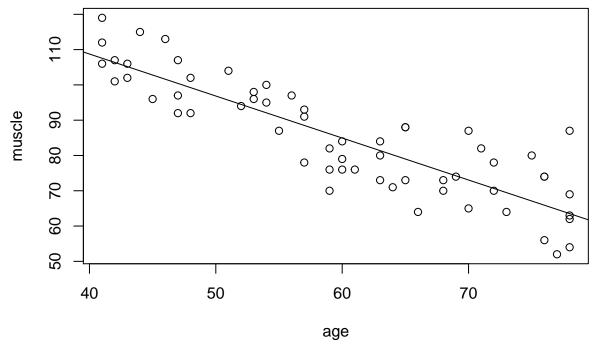
The MSE and its degrees of freedom are:

```
## [1] 66.80082 58.00000
```

1c

The fitted regression line is:

```
## [1] "muscle = 156.35 + -1.19 * age"
```



 It

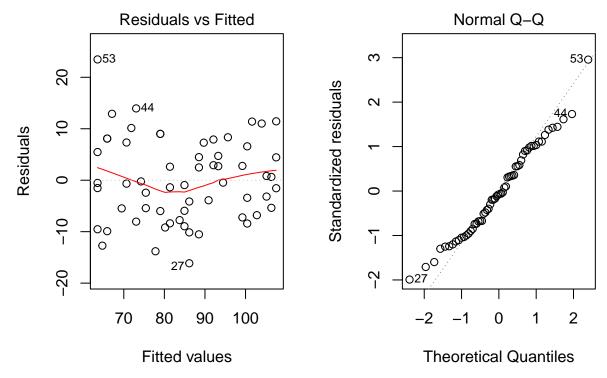
looks like the linear regression is a good fit.

1d

The fitted values for the 6th and 16th cases are:

The residuals for the 6th and 16th cases are:

1e



Using linear algebra notation, the simple linear regression model with Normal errors assumes - $y = X\beta + \epsilon$ The response is a linear function of the predictors. - ϵ Normal $(0, \sigma^2 I_n)$ The error terms are normally distributed and uncorrelated.

TODO - interpret plot

1f

A 99 percent confidence interval for the estimated regression intercept is:

We are 99 percent confident that the true parameter lies within this interval.

1g

We test at level 0.01 to see if there is a negative linear association between muscle mass and age. H_0 is $\beta_1 \geq 0$ and H_1 is the left sided alternative hypothesis $\beta_1 < 0$.

The test statistic is $T^* = \frac{\hat{(}\beta_1) - 0}{se(\hat{(}\beta_1))} \ t(n-2).$

The decision rule is to reject H_0 if $T^* < t(0.99, n-2)$.

[1] "If -13.193 is less than -2.392 we reject HO"

We reject the null hypothesis and conclude that there is a significant negative linear association between amount of muscle mass and age.

1h

A 95% prediction interval for the muscle mass for women of age 60 is:

```
## fit lwr upr
## 1 84.94683 68.45067 101.443
```

The fit is the expected value. We expect 95% of new observations to fall between the lower and upper bounds.

1i

The limits of a the 95% simultaneous confidence bands for the regression line at $x_h = 60$ are:

```
## [1] 105.65106 64.24261
```

1j

The ANOVA table for this data is:

We use an F test at level 0.01 to see if there is a linear association between muscle mass and age. H_0 is $\beta_1 = 0$ and H_1 is the two sided alternative hypothesis $\beta_1 \neq 0$.

```
The test statistic is F^* = \frac{\hat{\beta}_1 - 0}{se(\hat{\beta}_1)} t(n-2).
```

The decision rule is to reject H_0 if $F^* > F(0.99; 1, n-2)$.

```
## [1] "If 0.967 is less than 24.189 we reject HO"
```

We reject the null hypothesis and conclude that there is a significant linear association between amount of muscle mass and age.

1k

The proportion of total variation in muscle mass explained by age is \mathbb{R}^2 as viewed in the summary of the model:

```
##
## Call:
## lm(formula = muscle ~ age, data = women)
##
## Residuals:
```

```
1Q
                     Median
                                   3Q
## -16.1368 -6.1968 -0.5969
                               6.7607 23.4731
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 156.3466
                           5.5123
                                   28.36
                                            <2e-16 ***
               -1.1900
                           0.0902 -13.19
                                           <2e-16 ***
## age
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 8.173 on 58 degrees of freedom
## Multiple R-squared: 0.7501, Adjusted R-squared: 0.7458
## F-statistic: 174.1 on 1 and 58 DF, p-value: < 2.2e-16
```

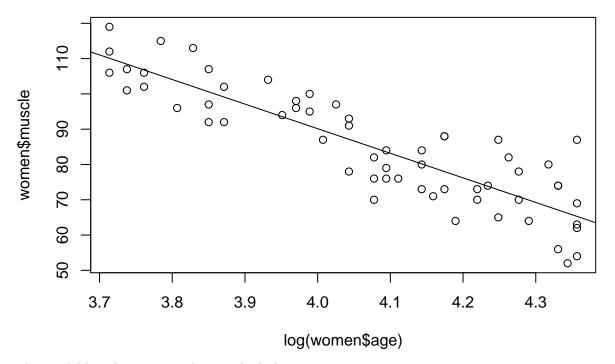
The correlation between muscle mass and age is:

```
## [1] -0.866064
```

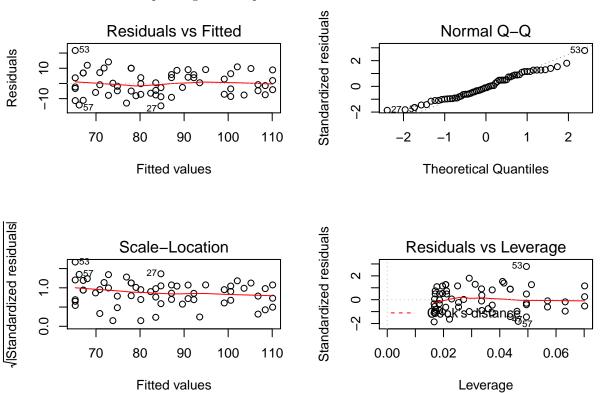
11

We fit the model using the log of age.

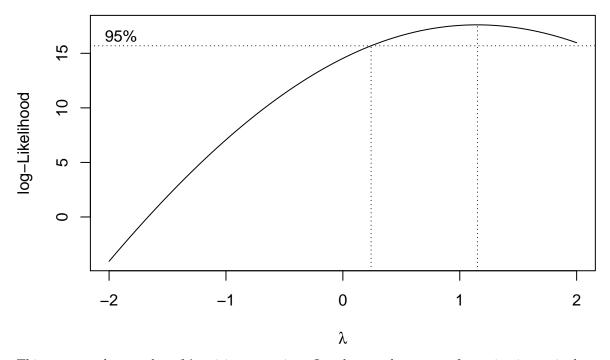
```
##
## Call:
## lm(formula = muscle ~ log(age), data = women)
##
## Residuals:
                 1Q
                      Median
       Min
                                   3Q
                                           Max
## -14.7382 -6.5901 -0.8211
                               6.5403 21.7113
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 368.816
                           20.894
                                    17.65
                                            <2e-16 ***
                            5.122 -13.60
                                            <2e-16 ***
## log(age)
               -69.669
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.987 on 58 degrees of freedom
## Multiple R-squared: 0.7613, Adjusted R-squared: 0.7572
## F-statistic: 185 on 1 and 58 DF, p-value: < 2.2e-16
```



This model has the corresponding residual plots:



 ${f 1}$ We plot the Box-Cox power transformation.



This suggests that a value of $\lambda=1$ is appropriate. In other words, no transformation is required.