# ABE 201 Biological Thermodynamics 1

Module 4
Degree of Freedom Analysis
and
Multiple Unit Operations

## Summary

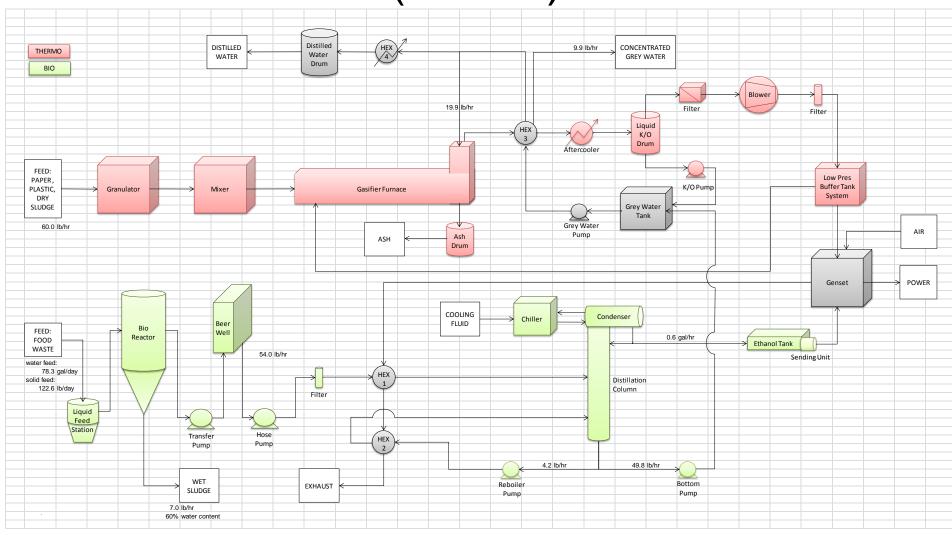
- Defining Systems in Complex Processes
  - Boundaries must be contiguous
  - Boundaries define what's in and what's out!
  - Careful selection of system boundaries can be used to solve complex problems

- Degree of Freedom Analysis
  - Determine if a unique solution is possible for the system as you have defined it.
  - The number of equations must equal or exceed the number of unknown variables

Tactical Garbage to Energy Reactor (TGER)



## Tactical Garbage to Energy Reactor (TGER)

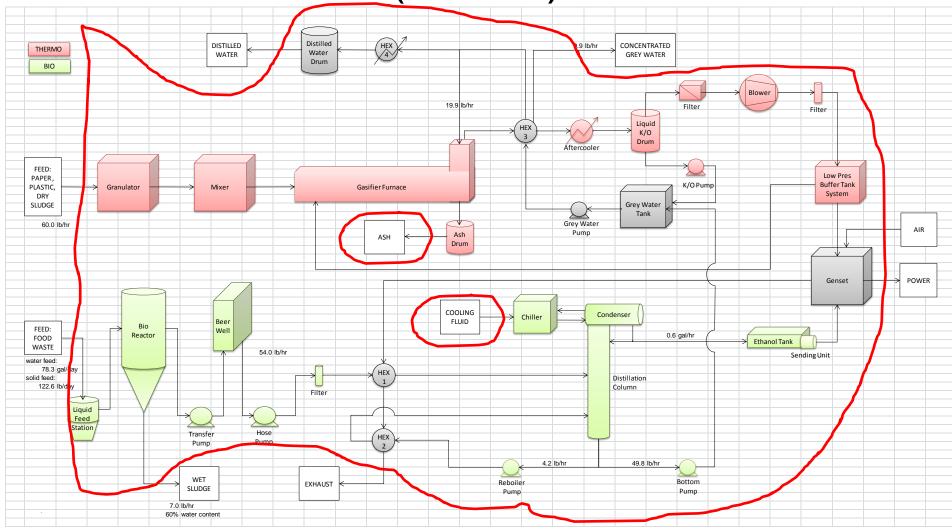


### **TGER**

 How many unit operations are shown in the process flow diagram?

How many systems can be defined?

Tactical Garbage to Energy Reactor (TGER)



## Pharmaceutical Recovery

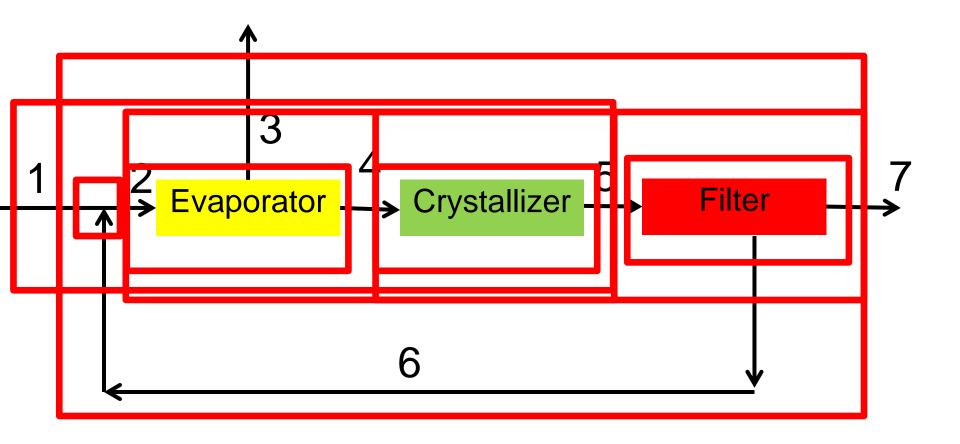
After synthesis, a pharmaceutical is recovered from solvent at steady state. The starting material (feed) is made at 4521 kg/h and contains 3% (w/w) drug and the remainder is solvent. It is mixed with recycled solvent and unrecovered drug before processing.

In the first processing step, 50% of the solvent is removed by evaporation, leaving the drug behind and concentrated in the remaining solvent.

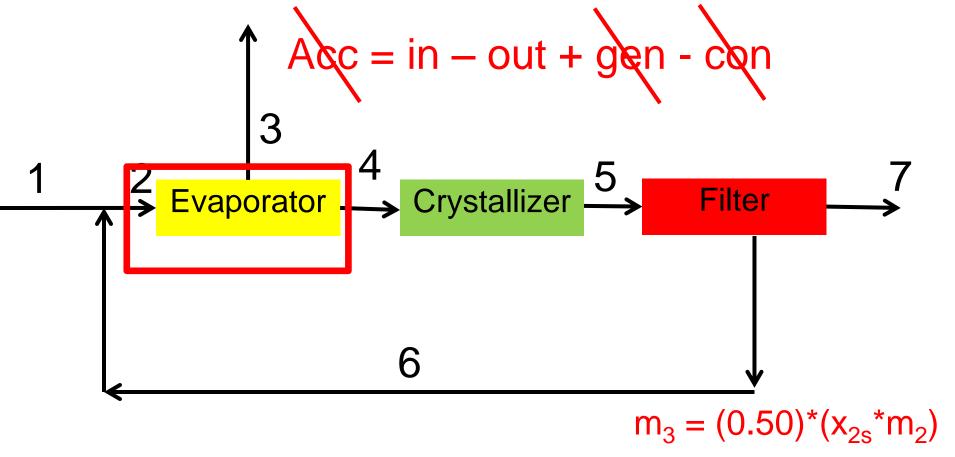
In the second step, the mixture (2573 kg/h) is cooled causing 95% of the drug entering the second step to crystalize and precipitate from solution.

In the third step, the crystalized drug is filtered out. The filter cake is 75% drug and 25% solvent. The remaining solvent with un-crystalized drug is recycled where it is blended with the feed and fed to the evaporator.

What is the mass flow rate of the recycled solvent and drug?

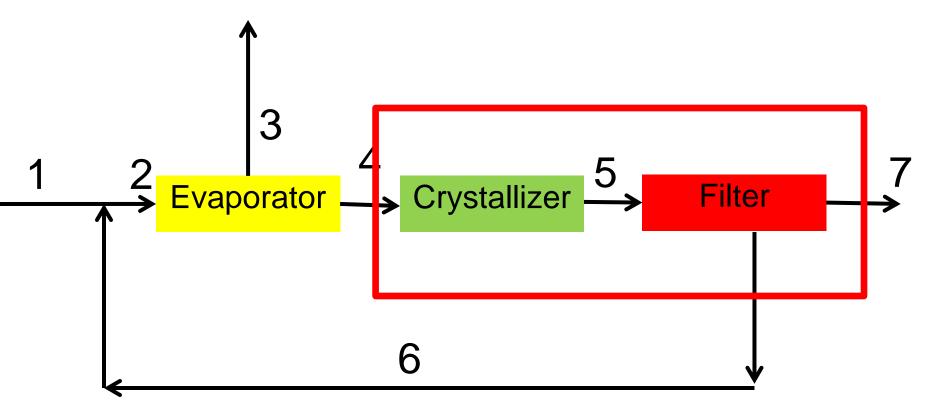


	1	2	3	4	5	6	7
m (kg/h)	4521	$m_2$	$m_3$	2573	m <sub>5</sub>	m <sub>6</sub>	m <sub>7</sub>
x <sub>d</sub>	0.03	X <sub>2d</sub>	0	X <sub>4d</sub>	X <sub>5d</sub>	X <sub>6d</sub>	0.75
X <sub>s</sub>	0.97	X <sub>2s</sub>	1	X <sub>4s</sub>	X <sub>5s</sub>	x <sub>6s</sub>	0.25



	1	2	3	4	5	6	7
m (kg/h)	4521	$m_2$	$m_3$	2573	$m_5$	$m_6$	$\mathfrak{M}_7$
x <sub>d</sub>	0.03	X <sub>2d</sub>	0	X <sub>4d</sub>	X <sub>50</sub>	X <sub>60</sub>	0.75
X <sub>s</sub>	0.97	X <sub>2s</sub>	1	X <sub>4s</sub>	X <sub>5s</sub>	X <sub>6s</sub>	0.25

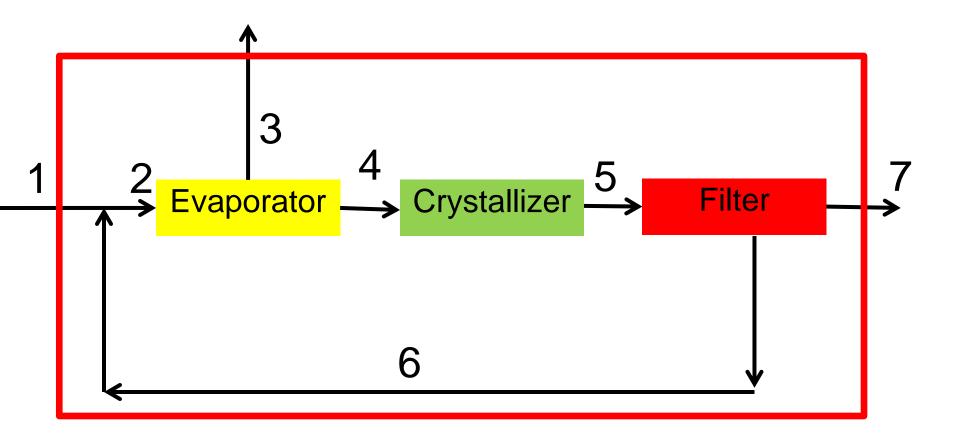
$$DOF = V - B - P - C = 6 - 2 - 0 - 3 = 1$$



$$x_{7d}^*m_7 = (0.95)^*(x_{4d}^*m_4)$$

	1	2	3	4	5	6	7
m (kg/h)	4521	$m_2$	$m_3$	2573	$m_5$	$m_6$	m <sub>7</sub>
x <sub>d</sub>	0.03	X <sub>2d</sub>	0	$x_4d$	<b>X</b> <sub>5a</sub>	X <sub>6d</sub>	0.75
X <sub>s</sub>	0.97	X <sub>2s</sub>	1	X <sub>4s</sub>	X <sub>5s</sub>	X <sub>6s</sub>	0.25

$$DOF = V - B - P - C = 6 - 2 - 0 - 3 = 1$$



	1	2	3	4	5	6	7
m (kg/h)	4521	$m_2$	$m_3$	2573	$m_5$	$m_6$	m <sub>7</sub>
x <sub>d</sub>	0.03	X <sub>2d</sub>	0	X <sub>4d</sub>	X <sub>5d</sub>	X <sub>6d</sub>	0.75
X <sub>s</sub>	0.97	X <sub>2s</sub>	1	X <sub>4s</sub>	X <sub>5s</sub>	X <sub>6s</sub>	0.25

$$DOF = V - B - P - C = 2 - 2 - 0 - 0 = 0$$

$$0 = In - Out$$

#### **Total Mass**

$$0 = (m_1) - (m_3 + m_7)$$

$$0 = 4521 - (m_3 + m_7)$$
  $m_3 = 4340.6$  kg/h

#### **Drug Mass**

$$0 = (x_{1d}*m_1) - (x_{3d}*m_3 + x_{7d}*m_7)$$

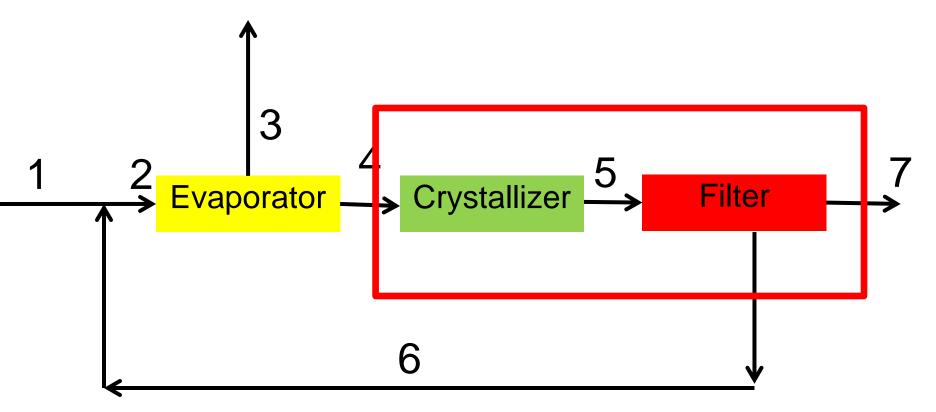
$$0 = (0.03*4521) - (0 + 0.75*m_7)$$

 $m_7 = 180.4 \text{ kg/h}$ 

#### **Solvent Mass**

$$0 = (x_{1s}^* m_1) - (x_{3s}^* m_3 + x_{7s}^* m_7)$$

$$0 = (0.97*4521) - (m_3 + 0.25*m_7)$$



$$x_{7d}^*m_7 = (0.95)^*(x_{4d}^*m_4)$$

	1	2	3	4	5	6	7
m (kg/h)	4521	$m_2$	4340.6	2573	$m_5$	$m_6$	180.4
x <sub>d</sub>	0.03	X <sub>2d</sub>	0	$x_4d$	X <sub>50</sub>	X <sub>6d</sub>	0.75
X <sub>s</sub>	0.97	X <sub>2s</sub>	1	X <sub>4s</sub>	X <sub>5s</sub>	X <sub>6s</sub>	0.25

$$DOF = V - B - P - C = 5 - 2 - 0 - 3 = 0$$

$$0 = In - Out$$

#### **Total Mass**

$$0 = (m_4) - (m_7 + m_6)$$

$$0 = 2573 - (180.4 + m_6)$$

$$m_6 = 2392.6 \text{ kg/h}$$

## Example

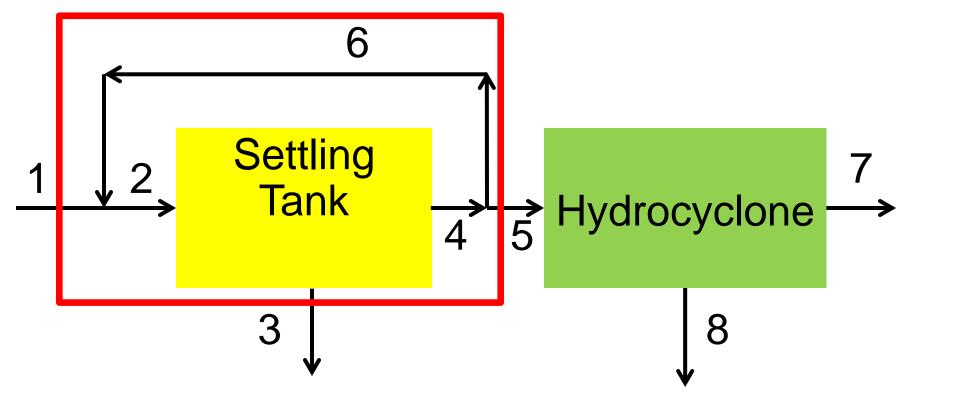
Waste water treatment slurry (50.% solids) is processed at a rate of 100. kg/hr.

The slurry is mixed with a recycle stream and goes into a settling tank where some of the solids settle out to form a sludge (90.% solids) which is removed from the bottom by a conveyor.

The upper layer (40.% solids) is pumped from the far side of the settling tank at 125 kg/hr. A portion is recycled to dilute the incoming waste while the remainder is pumped through a hydrocyclone that produces a heavy cake (98% solids) and a light effluent (1.0% solids). Assume steady-state operation.

## Questions

- What percent of effluent is being recycled?
- What is the flow rate of clarified effluent from the hydrocyclone?
- What is the total flow rate of high solids streams (sludge + heavy cake)?



	1	2	3	4	5	6	7	8
m	100	$m_2$	$m_3$	125	$m_5$	$m_6$	$m_7$	m <sub>8</sub>
X <sub>s</sub>	0.5	X <sub>2s</sub>	0.9	0.4	0.4	0.4	0.01	0.98
X <sub>w</sub>	0.5	X <sub>2w</sub>	0.1	0.6	0.6	0.6	0.99	0.02

$$DOF = V - B - P - C = 2 - 2 - 0 - 0 = 0$$

#### Acc = In - Out + Gen - Con

 $m_3 = 20 \text{ kg/h}$ 

 $m_5 = 80 \text{ kg/h}$ 

#### **Total Mass**

$$0 = (m_1) - (m_3 + m_5)$$

$$0 = 100 - (m_3 + m_5)$$

#### **Solids Mass**

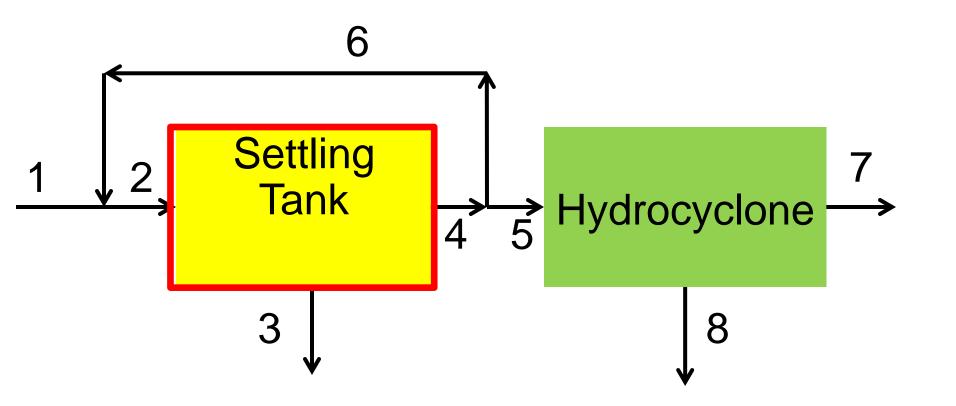
$$0 = (x_{1s}*m_1) - (x_{3s}*m_3 + x_{5s}*m_5)$$

$$0 = (50) - (0.9*m_3 + 0.4*m_5)$$

#### **Water Mass**

$$0 = (x_{1w}^*m_1) - (x_{3w}^*m_3 + x_{5w}^*m_5)$$

$$0 = (50) - (0.1*m_3 + 0.6*m_5)$$



	1	2	3	4	5	6	7	8
m	100	$m_2$	20	125	80	$m_6$	$\mathfrak{m}_7$	m <sub>8</sub>
X <sub>s</sub>	0.5	X <sub>2s</sub>	0.9	0.4	0.4	0.4	0.0	0.98
X <sub>w</sub>	0.5	X <sub>2w</sub>	0.1	0.6	0.6	0.6	0.99	0.02

$$DOF = V - B - P - C = 3 - 2 - 0 - 1 = 0$$

#### Acc = In - Out + Gen - Con

#### **Total Mass**

$$m2 = 145 \text{ kg/h}$$

$$0 = (m_2) - (m_3 + m_4)$$

$$0 = m_2 - (20 + 125)$$

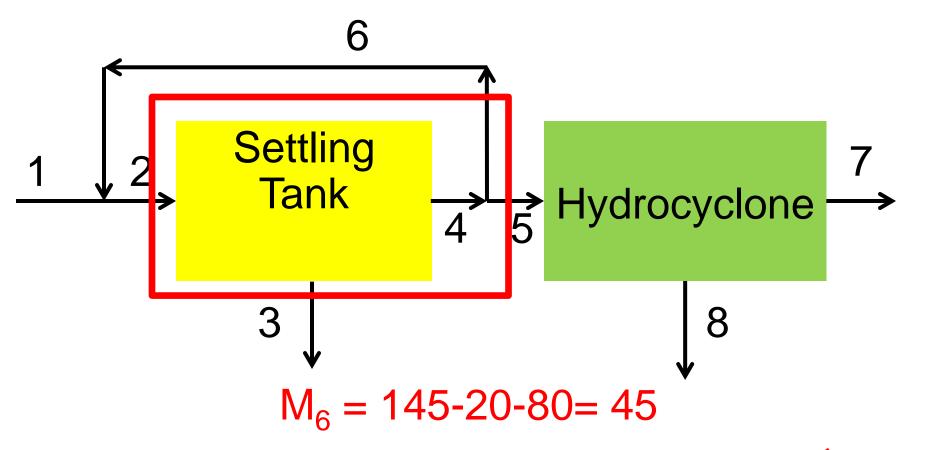
#### **Solids Mass**

$$0 = (x_{2s} * m_2) - (x_{3s} * m_3 + x_{4s} * m_4)$$

$$0 = x_{2s}(145) - (0.9*20 + 0.4*125)$$

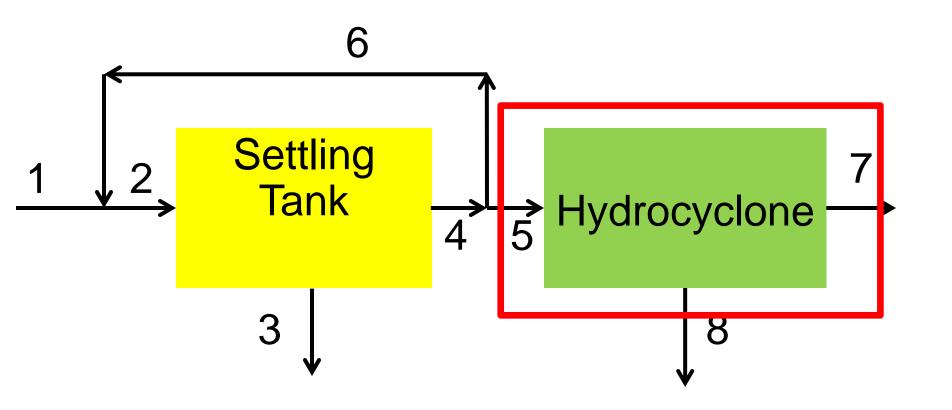
$$x_{2s} = 0.469$$

$$x_{2w} = 1 - x_{2s} = 0.531$$



	1	2	3	4	5	6	7	8
m	100	145	20	125	80	$m_6$	$m_7$	m <sub>8</sub>
X <sub>s</sub>	0.5	0.469	0.9	0.4	0.4	0.4	0.0	0.98
X <sub>w</sub>	0.5	0.531	0.1	0.6	0.6	0.6	0.99	0.02

% recycled =  $M_6 / M_4 = 45/125 = 36\%$ 



	1	2	3	4	5	6	7	8
m	100	145	20	125	80	45	m <sub>7</sub>	m <sub>8</sub>
X <sub>s</sub>	0.5	0.469	0.9	0.4	0.4	0.4	0.01	0.98
X <sub>w</sub>	0.5	0.531	0.1	0.6	0.6	0.6	0.99	0.02

#### Acc = In - Out + Gen - Con

#### **Total Mass**

$$0 = (m_5) - (m_7 + m_8)$$
  $m_7 = 47.8 \text{ kg/h}$   $m_8 = 32.2 \text{ kg/h}$ 

$$0 = 80 - (m_7 + m_8)$$
 Total sludge =

Solids Mass 
$$m_3 + m_8 = 20.0 + 32.2$$

$$0 = (x_{5s}*m_5) - (x_{7s}*m_7 + x_{8s}*m_8) = 52.2$$
kg/h

$$0 = (0.4*80) - (0.01*m7 + 0.98*m8)$$

#### **Water Mass**

$$0 = (x_{1w}^*m_1) - (x_{7w}^*m_7 + x_{8w}^*m_8)$$

$$0 = (0.6*80) - (0.99*m_7 + 0.02*m_8)$$