

ABE 201

Biological Thermodynamics 1

Module 14

Psychrometrics

Overview

- Psychrometric charts illustrate graphically the relationship between thermodynamic properties of air-water vapor mixtures.
- Much like steam tables, compressibility charts, and the Antoine equation, these charts can be used to solve mass/energy balances where water/air are involved.

Psychrometry

- The measurement (μέτρον) of cold (ψυχρόν) gas-vapor mixtures.
- Most commonly, the gas is air and the vapor is water.
- In practice, psychrometry relates measurable properties of air/water mixtures to thermodynamic state properties

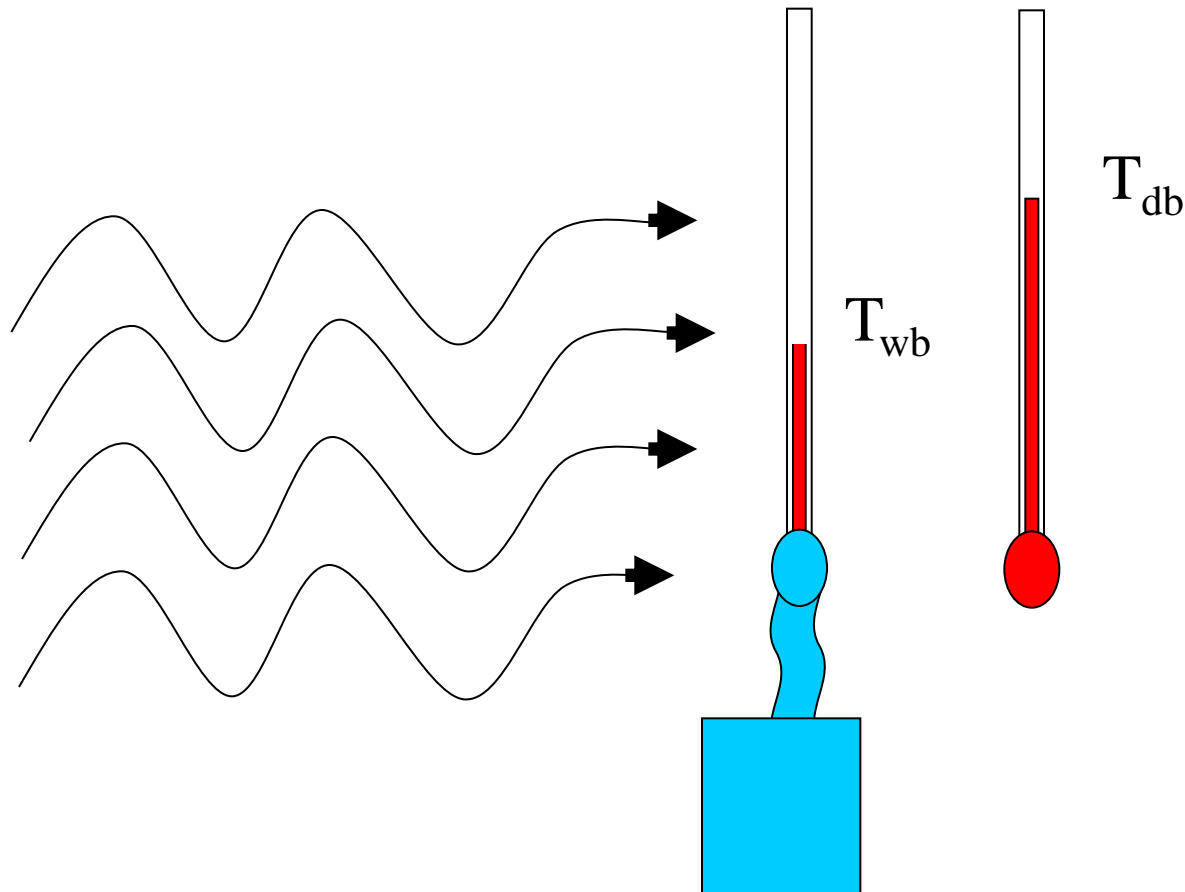
Psychrometric Measurements

- Dry-Bulb Temperature, T or T_{db} = air temperature as measured by thermometer (or equivalent)
- Wet-Bulb Temperature, T_{wb} = temperature of air after undergoing evaporative cooling
- Dew Point, T_{dp} = temperature at which humid air becomes saturated (constant pressure)

State Properties

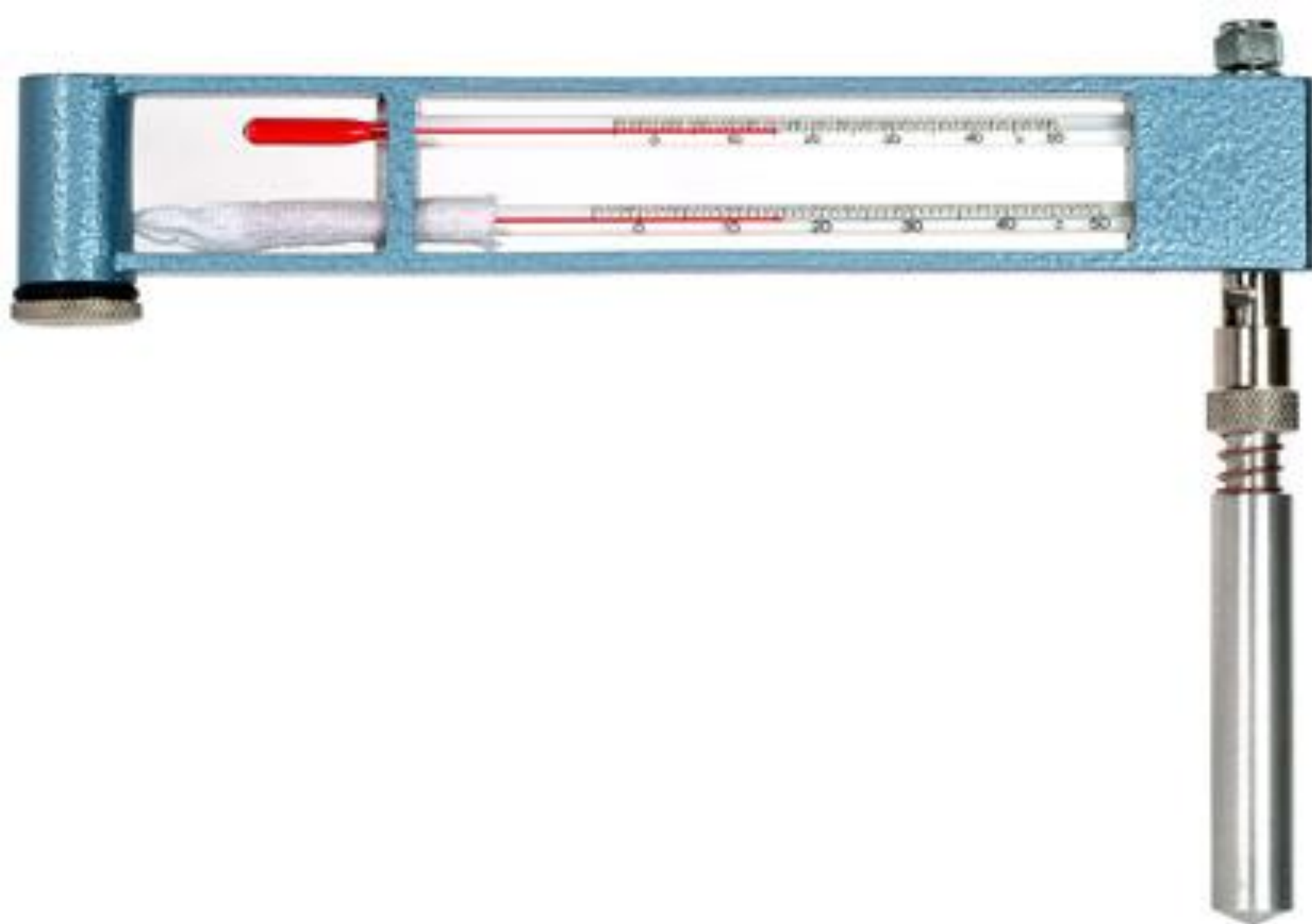
- Specific Volume, \hat{V} = the specific volume of DA (minus volume of water vapor)
- Specific Enthalpy, \hat{H} = the enthalpy of the dry air
- Absolute Humidity, h_a = the ratio of water vapor to dry air (DA), aka moisture content
- Relative Humidity, $h_r = 100\% * p_{H_2O} / p^*_{H_2O}$

Wet-Bulb Temperature, T_{wb}



Wet-Bulb Temperature, T_{wb}

- Evaporation of the water from the wick cools the thermometer bulb
- Wet-bulb temperature is a function of:
 - Dry-bulb temperature
 - Moisture content of air
- If the air is saturated (100% rel. hum.), no water evaporates and $T_{wb} = T_{db}$







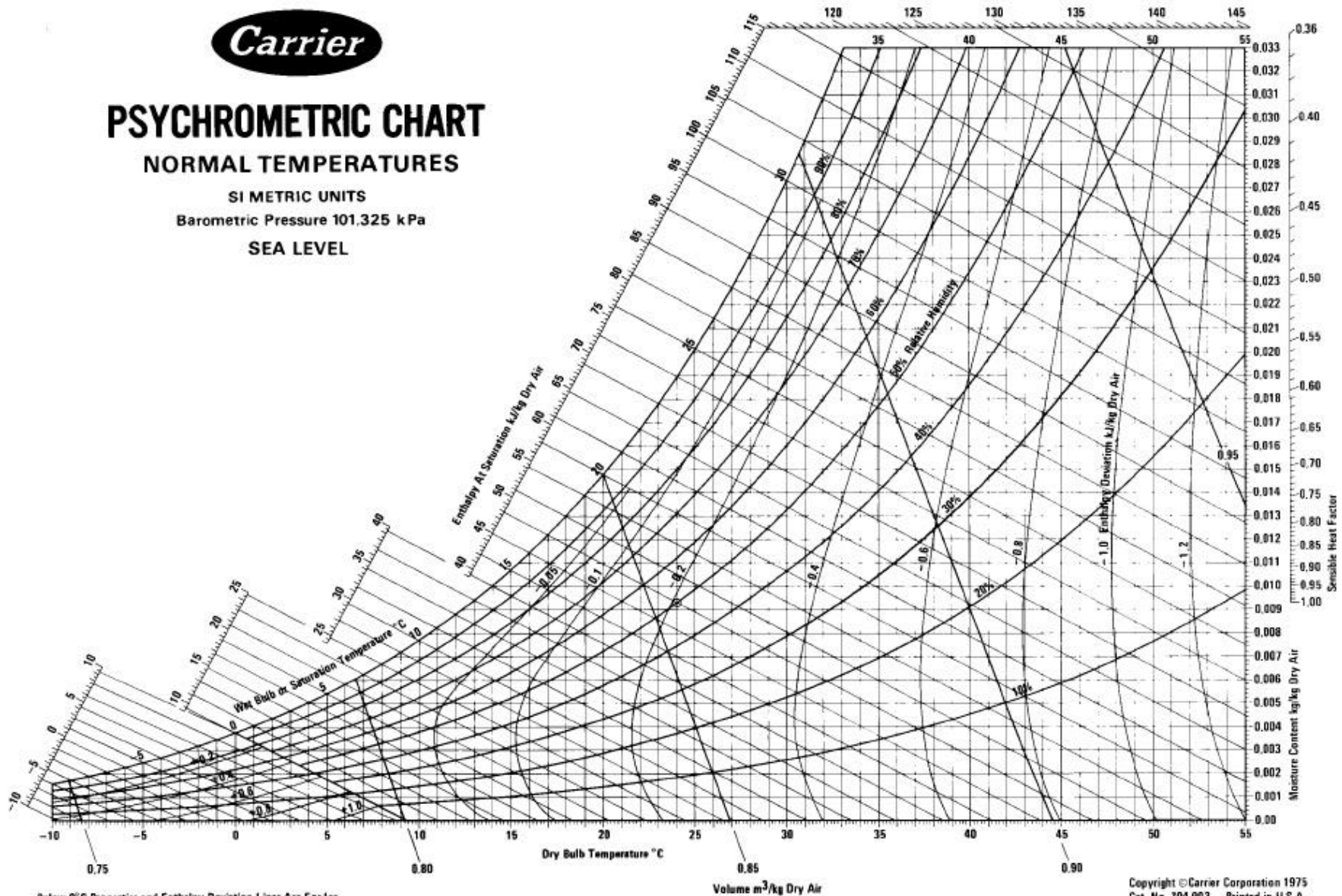
PSYCHROMETRIC CHART

NORMAL TEMPERATURES

SI METRIC UNITS

Barometric Pressure 101.325 kPa

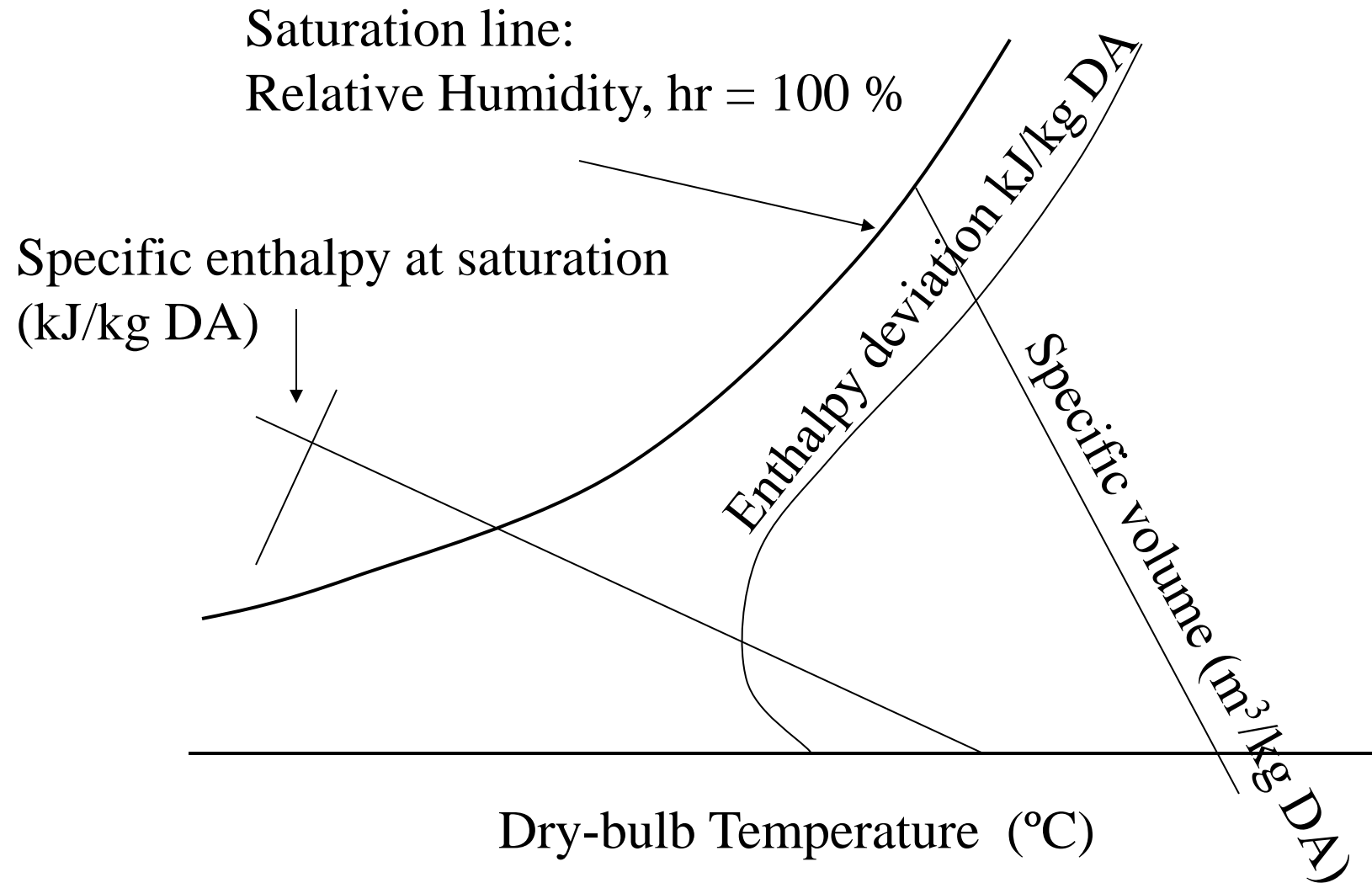
SEA LEVEL



Below 0°C Properties and Enthalpy Deviation Lines Are For Ice

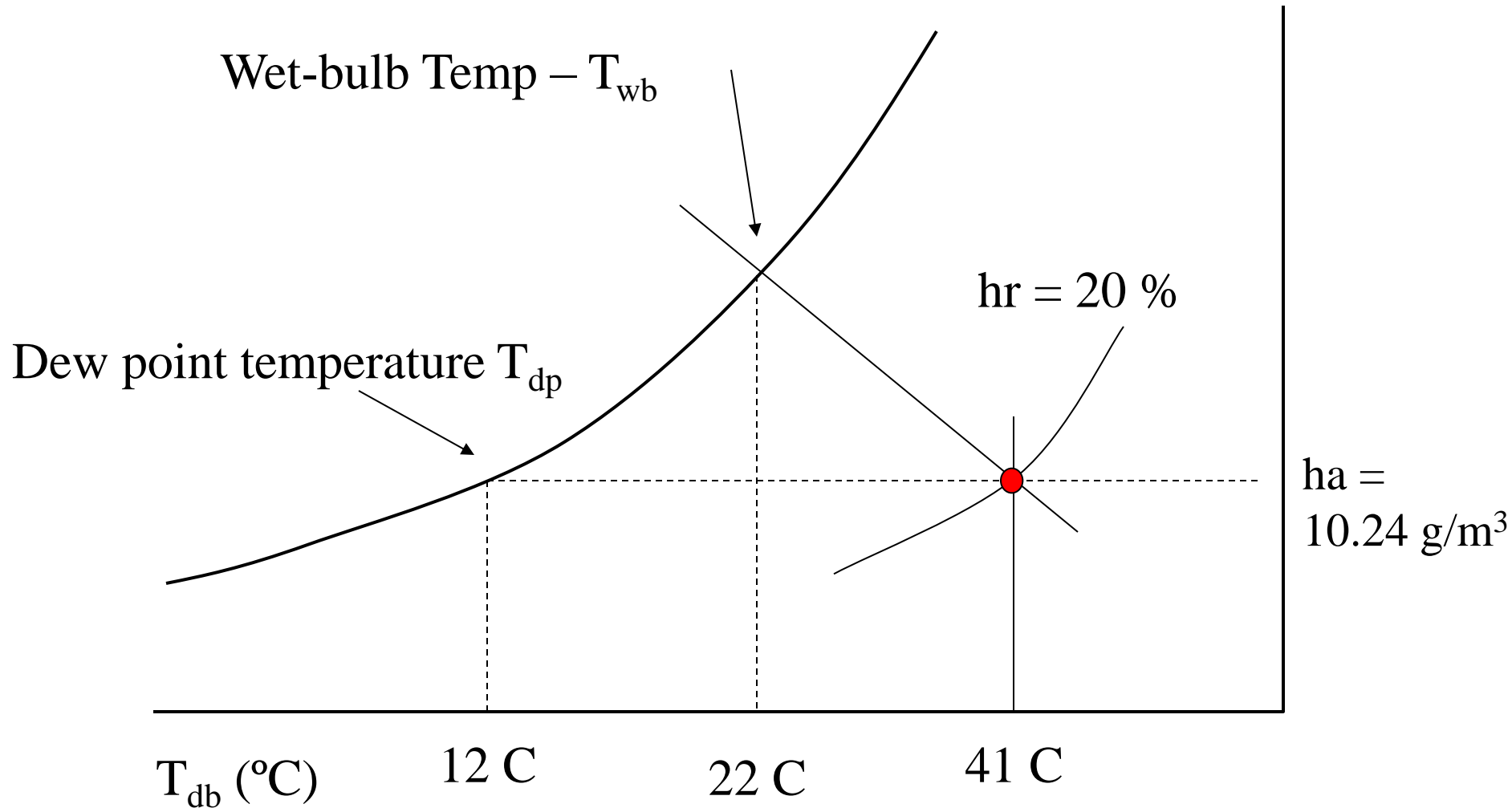
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Basic Components of the chart



Absolute humidity: h_a (mass $H_2O(v)$ /mass Dry Air)

More information on the chart!



Using the Psychrometric Chart

- $T_{db} = 36\text{ C}$ and $h_a = 0.015\text{ kg/kg DA}$
- Convert $h_a = 0.015\text{ kg/kg DA}$ into mass fraction.
- What is the Relative Humidity?
- What is the volume of 1 kg Dry air?
- What is the specific enthalpy ?
- What is the wet-bulb temperature?
- What is the dew point?



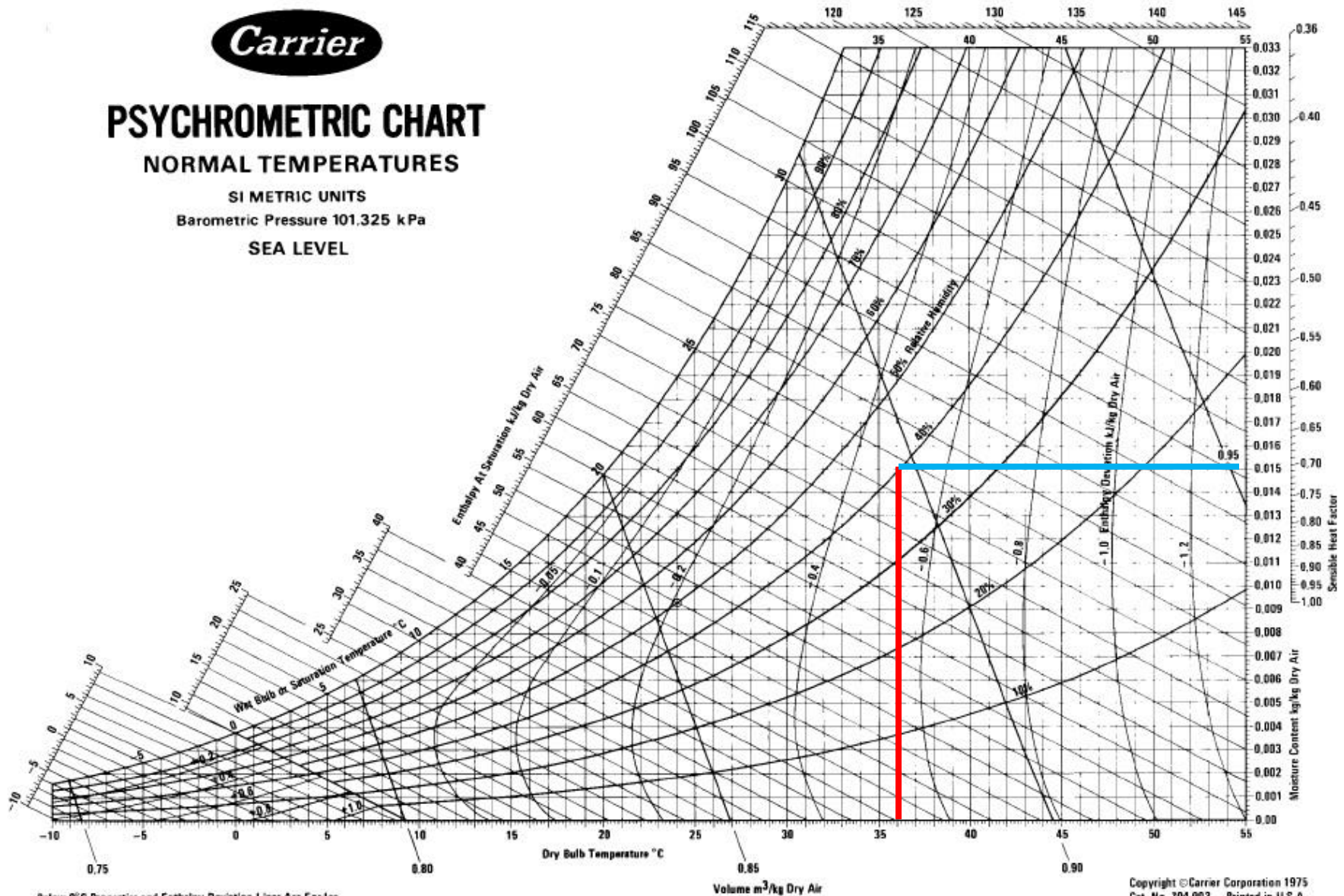
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1 kg of DA has 0.015 kg of water.

$$X_{\text{water}} = 0.015 / (1 + 0.015) = .0148$$

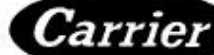
$$RH = 40 \%$$

$$V_h = 0.895 \text{ m}^3/\text{kg}$$

$$H_{\text{hat}} = (76 - 0.5) \text{ kJ/kg dry air}$$

$$T(\text{wb}) = 24.6 \text{ C}$$

$$T(\text{dp}) = 20.3 \text{ C}$$



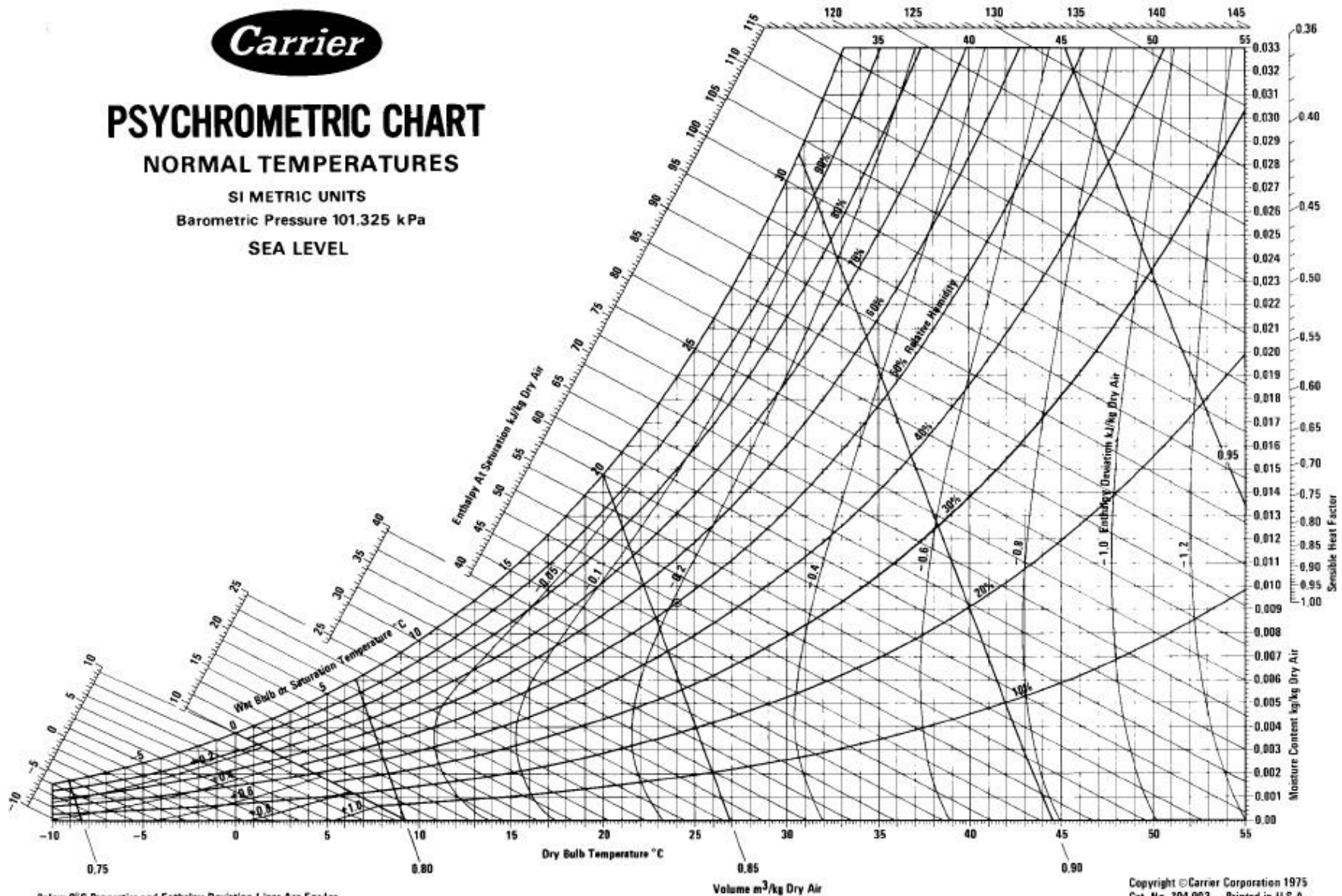
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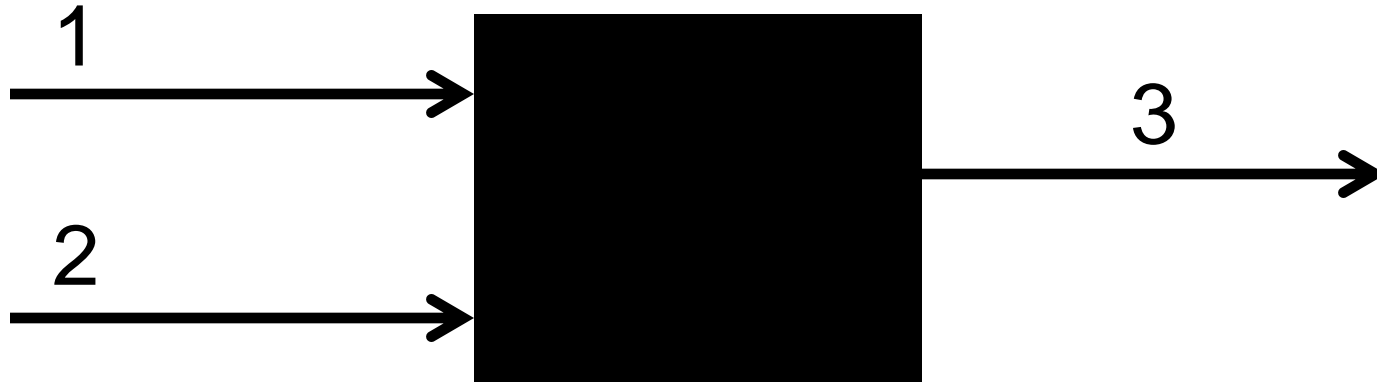


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Mixing Air Streams

2 kg DA/min of air from an AC (22C, 54% RH) is mixed with 3 kg DA/min of warm air (41C, 40% RH), what are the psychrometric properties of the mixed air?



Stream 1

$m_1 = 2 \text{ kg DA/min}$

$T(\text{db}) = 22 \text{ C}$

$\text{RH} = 54\%$

$h_a = 8.92 \text{ g/kg}$

$H = 44.72 \text{ kJ/kg DA}$

$T(\text{wb}) = 16 \text{ C}$

$T(\text{dp}) = 12.3 \text{ C}$

Stream 2

$m_2 = 3 \text{ kg DA/min}$

$T(\text{db}) = 41 \text{ C}$

$\text{RH} = 40\%$

$h_a = 19.81 \text{ g/kg}$

$H = 92.18 \text{ kJ/kg DA}$

$T(\text{wb}) = 28.6 \text{ C}$

$T(\text{dp}) = 24.7 \text{ C}$

Mass Balance around Dry Air

$$m_1 + m_2 = m_3$$

$$2 + 3 = 5$$

Mass Balance around Water

$$m_1 * ha_1 + m_2 * ha_2 = m_3 * ha_3$$

$$ha_1 = 8.92 \text{ g/kg}, ha_2 = 19.81$$

$$ha_3 = 15.45 \text{ g w/kg DA}$$

Energy Balance

$$H_1 * m_1 + H_2 * m_2 = H_3 * m_3$$

$$H_1 = 44.72 \text{ kJ/kg DA},$$

$$H_2 = 92.18 \text{ kJ/kg DA}$$

$$H_3 = 73.20 \text{ kJ/kg}$$

$$ha = 15.45 \text{ g/kg}$$

$$H = 73.2 \text{ kJ/kg}$$

$$T(\text{db}) = 33.5 \text{ C}$$

$$T(\text{wb}) = 24.3$$

$$T(\text{dp}) = 20.7$$

$$\text{RH} = 47\%$$

$$V = 0.8903 \text{ m}^3/\text{kg}$$



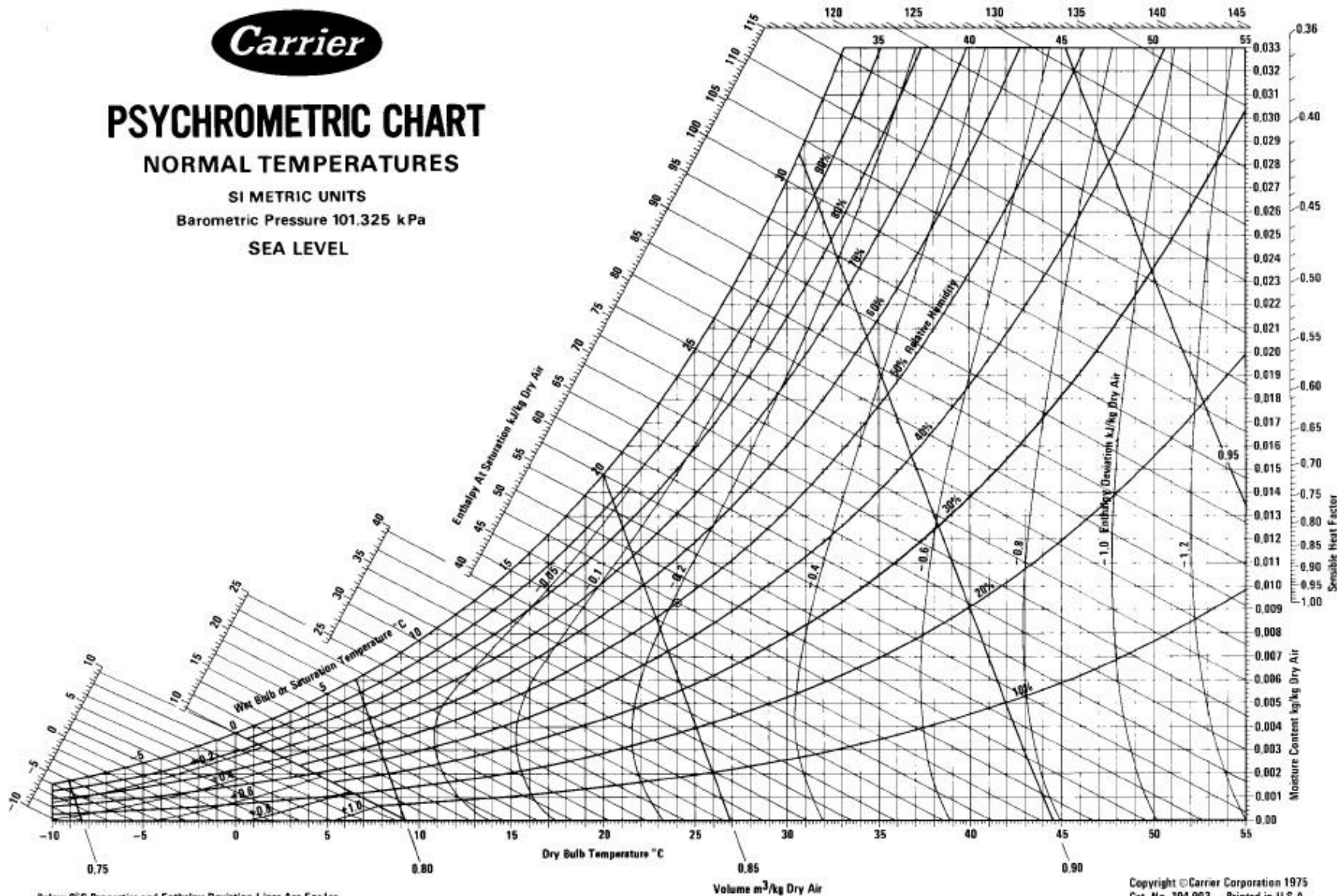
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Drying Processes

- Drying converts water in the material from liquid to vapor.
- If no heat is added, the process remains at a constant enthalpy
 - The air temperature will drop
 - Sensible heat is traded for latent heat
- This process follows a constant enthalpy line on the psychrometric chart

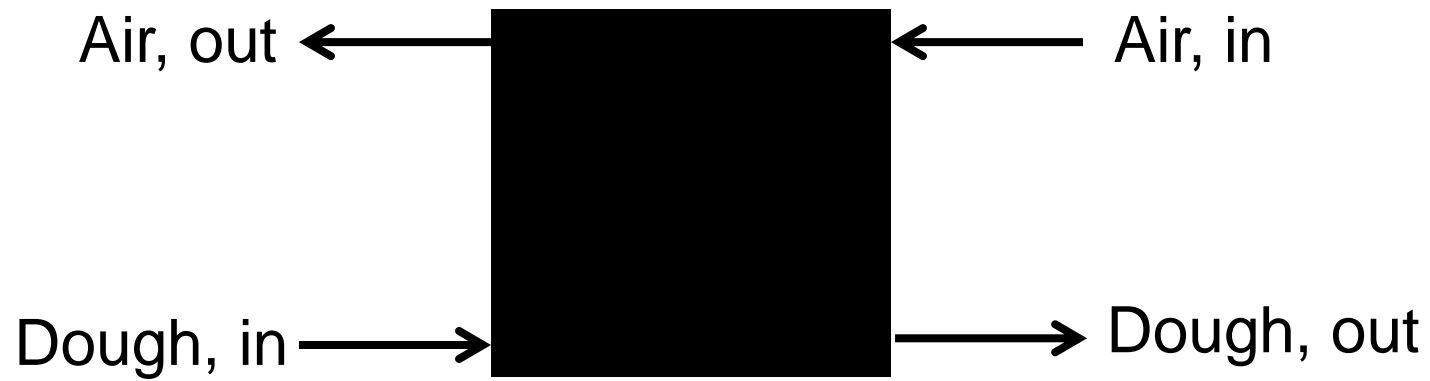
Drying Problem

A counter-current of 200 kg/min of dry air at 49.5 C and 20% RH is used to dry 5 kg/min of dough starting at 20C and 80% MC(wb) to 70% MC(wb). Assume that the dough has a constant

$$C_p = 1.90 \text{ kJ/kg-K}$$

and the dry air is constant enthalpy.

At steady-state, what is the temperature and relative humidity of the exit air and the temperature of the dough?



Find 49.5 C and 20% RH on chart:

$h = 0.015 \text{ kg/kg}$, $H = 89 \text{ kJ/kg}$

Mass Balances

Air

$$m_{DA,in} = m_{DA,out} = 200 \text{ kg / min}$$

Water

$$h_{a,in} m_{DA,in} + x_{w,in} m_{dough,in} = h_{a,out} m_{DA,out} + x_{w,out} m_{dough,out}$$

$$(0.015)(200) + (0.8)(5) = h_{a,out} (200) + (0.7)(3.33)$$

$$h_{a,out} = 0.023$$

Dough solids

$$x_{s,in} m_{dough,in} = x_{s,out} m_{dough,out}$$

$$(1 - 0.8)(5) = (1 - 0.7) m_{dough,out}$$

$$m_{dough,out} = 3.33 \text{ kg / min}$$

1st Law Energy Balance

$$\Delta H = 0$$

$$H_{a,in} m_{DA,in} + C_p m_{dough,in} (20 - 0) = H_{a,out} m_{DA,out} + C_p m_{dough,out} (X - 0)$$

$$(89)(200) + (1.90)(5)(20 - 0) = 89(200) + (1.90)(3.33)(X - 0)$$

$$h = 0.023 \text{ kg/kg}, H = 89 \text{ kJ/kg}$$

$$T(\text{db}) = 30 \text{ }^{\circ}\text{C}$$

$$T(\text{wb}) = 28 \text{ }^{\circ}\text{C}$$

$$T(\text{dp}) = 27 \text{ }^{\circ}\text{C}$$

$$\text{RH} = 84\%$$

$$T(\text{dough}) = 30 \text{ }^{\circ}\text{C}$$

Mixing Air Streams

Cool, wet air ($T_{db} = 10\text{ C}$, $RH = 80\%$) is mixed with warm, dry air ($T_{db} = 50\text{ C}$, $RH = 10\%$). If the cool air is mixed with the warm air in a 3:1 ratio (cool:warm), what is the temperature and relative humidity of the final mixture?

$T(\text{db}) = 10\text{ C}, \text{ RH} = 80\%,$

$H = 25\text{ kJ/kg}, h = 0.006\text{ kg/kg}$

$T(\text{db}) = 50\text{ C}, \text{ RH} = 10\%,$

$H = 71.5\text{ kJ/kg}, h = 0.0078\text{ kg/kg}$

Air Balance

$$1 + 3 = 4$$

Moisture out, $h_a = [3*(0.006) + 1*(0.0078)] / [4\text{ kg}] = 0.00645\text{ kg/kg}$

Enthalpy out, $H = [3*(25) + 1*(71.5)]/[4\text{ kg}] = 36.625\text{ kJ/kg}$

These two points intersect: $T(\text{db}) = 20\text{ C}; \text{ RH} = 44\%$

$T(\text{wb}) = 13.1, T(\text{dp}) = 7.5$