

Is water viscoelastic?

$$t_R \times \omega \ll 1 \quad \text{LIQUID BEHAVIOR}$$

$$t_R \times \omega \gg 1 \quad \text{SOLID BEHAVIOR}$$

$$t_R \approx 10^{-12} \text{ seconds.}$$

$$10^{-12} \times \omega \gg 1 \quad \text{SOLID BEHAVIOR}$$

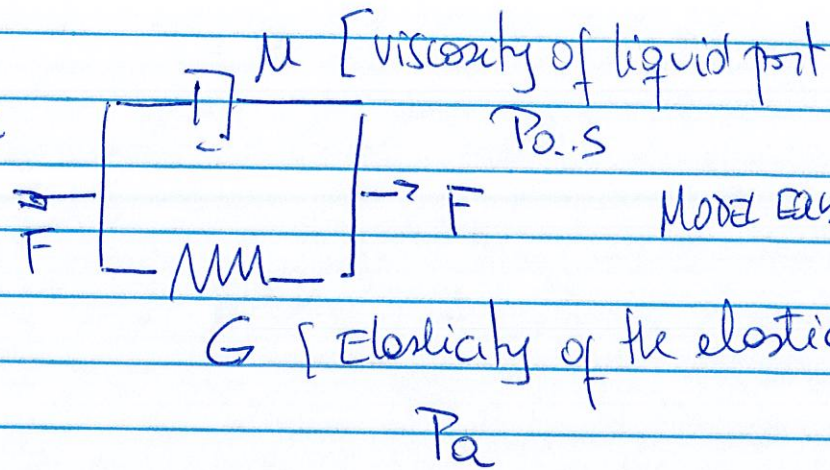
$$\omega \geq 10^{12} \text{ Hz [Kertz]}$$

Maximum you can achieve for mechanical characterizations of materials 10^6 Hz

↑
ULTRASOUND

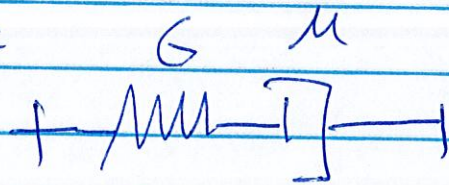
MODELS

Viscoelastic
Kelvin
Voigt
Model.



MODEL EQUATION ?

Viscoelastic
material
Maxwell
Model.



MODEL EQUATION ?

PURE ELASTIC

HOOKE
MODEL

stress

RHEOLOGY

$$\sigma = G \gamma$$

strain.



SIMPLE MODEL

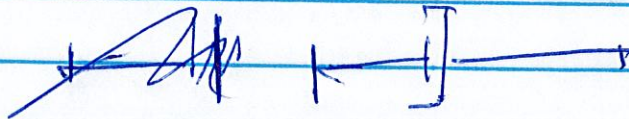
$$F = kL$$

Constant
of rubber
band.

Force

length
of rubber
band

PURE VISCOUS MATERIAL (LIQUID)



$$F = \mu \frac{dL}{dt}$$

$$\sigma = \mu \frac{d\gamma}{dt} = \mu \dot{\gamma}$$

Newton Equation

~~QUESTION~~

PURE ELASTIC MATERIAL

(3)

Simple

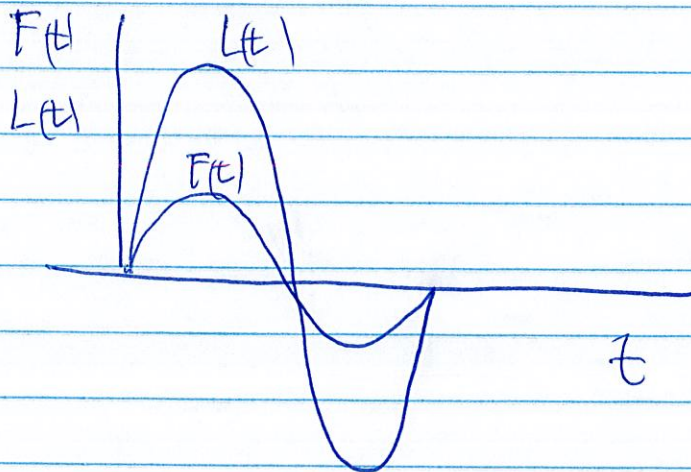
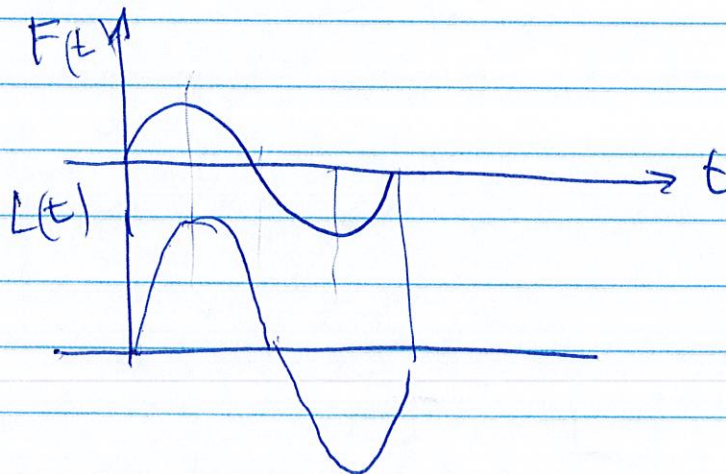
$$F(t) = K L(t)$$



RHEOLOGY

$$\sigma(t) = G \gamma(t)$$

$$L(t) = L_0 \sin \omega t$$



PURE LIQUID MATERIAL

(4)

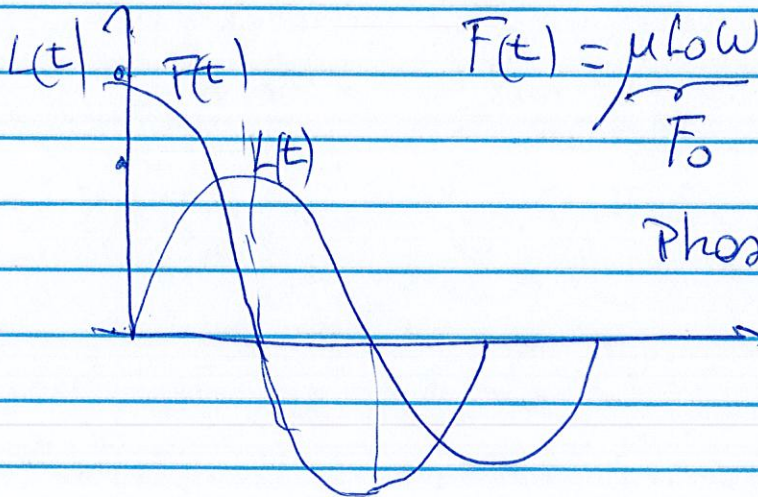
Simple

$$F(t) = \mu \frac{dL(t)}{dt}$$

Rheology

$$\sigma(t) = \mu \frac{d\gamma(t)}{dt}$$

$$L(t) = L_0 \sin \omega t$$



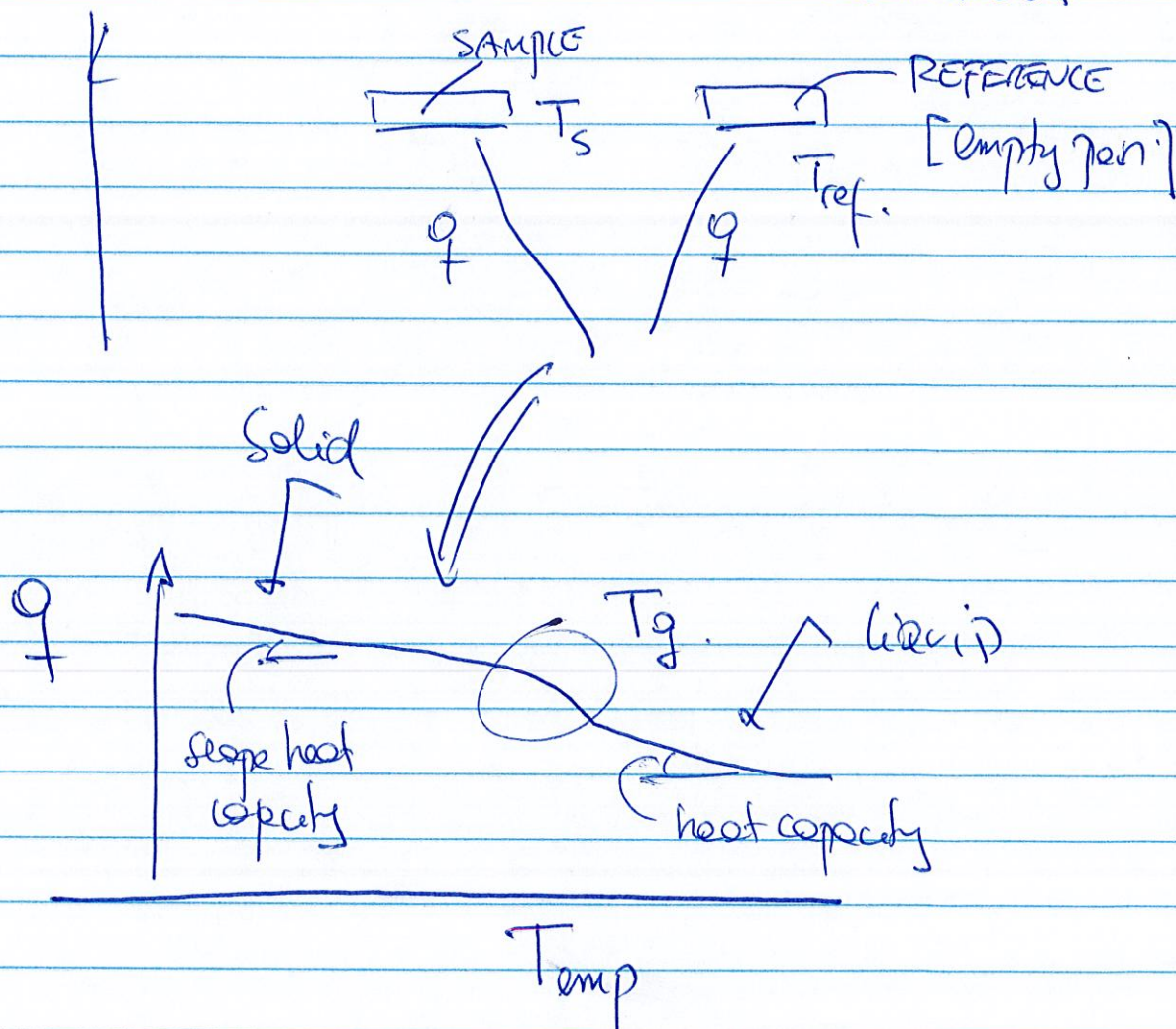
$$F(t) = \underbrace{\mu L_0 \omega}_{F_0} \cos \omega t$$

$$\text{Phase} = \frac{\pi}{2} \text{ or } 90^\circ$$

GLASS TRANSITION TEMPERATURE T_g

(5)

T_g can be measured by DSC [Differential Scanning Calorimeters]



$$\Delta C_p = C_{p, \text{solid}} - C_{p, \text{liquid}} \approx 5\%$$

Difficult to detect for complex systems.

T_g using DMA technique

(Dynamic Mechanical Analysis)

