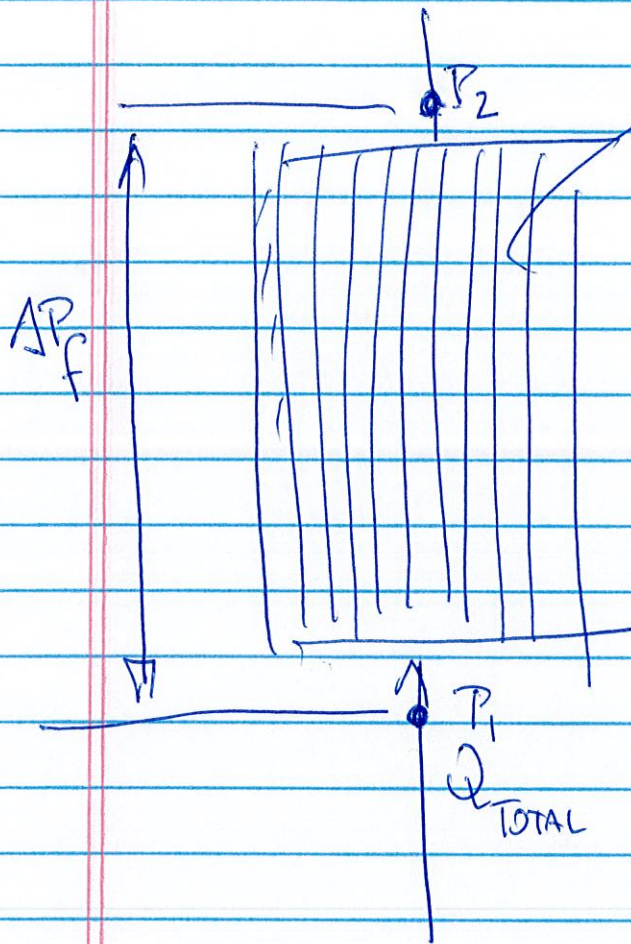


OFFICE HOURS 11/13/2017

(0)



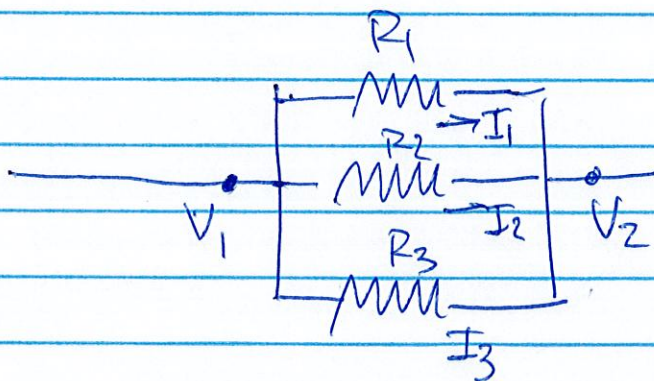
$$\Delta P_f = P_1 - P_2$$

$$\Delta P_f = \frac{2LK}{R} \left(\frac{3n+1}{4n} \right) \left(\frac{4Q}{\pi R^3} \right)^n$$

Because the pressure is calculated for 1 tube

$$Q = \frac{Q_{TOTAL}}{N_T}$$

Electrical problem



$$V_1 - V_2 = R_1 \times I_1$$

$$V_1 - V_2 = R_2 \times I_2$$

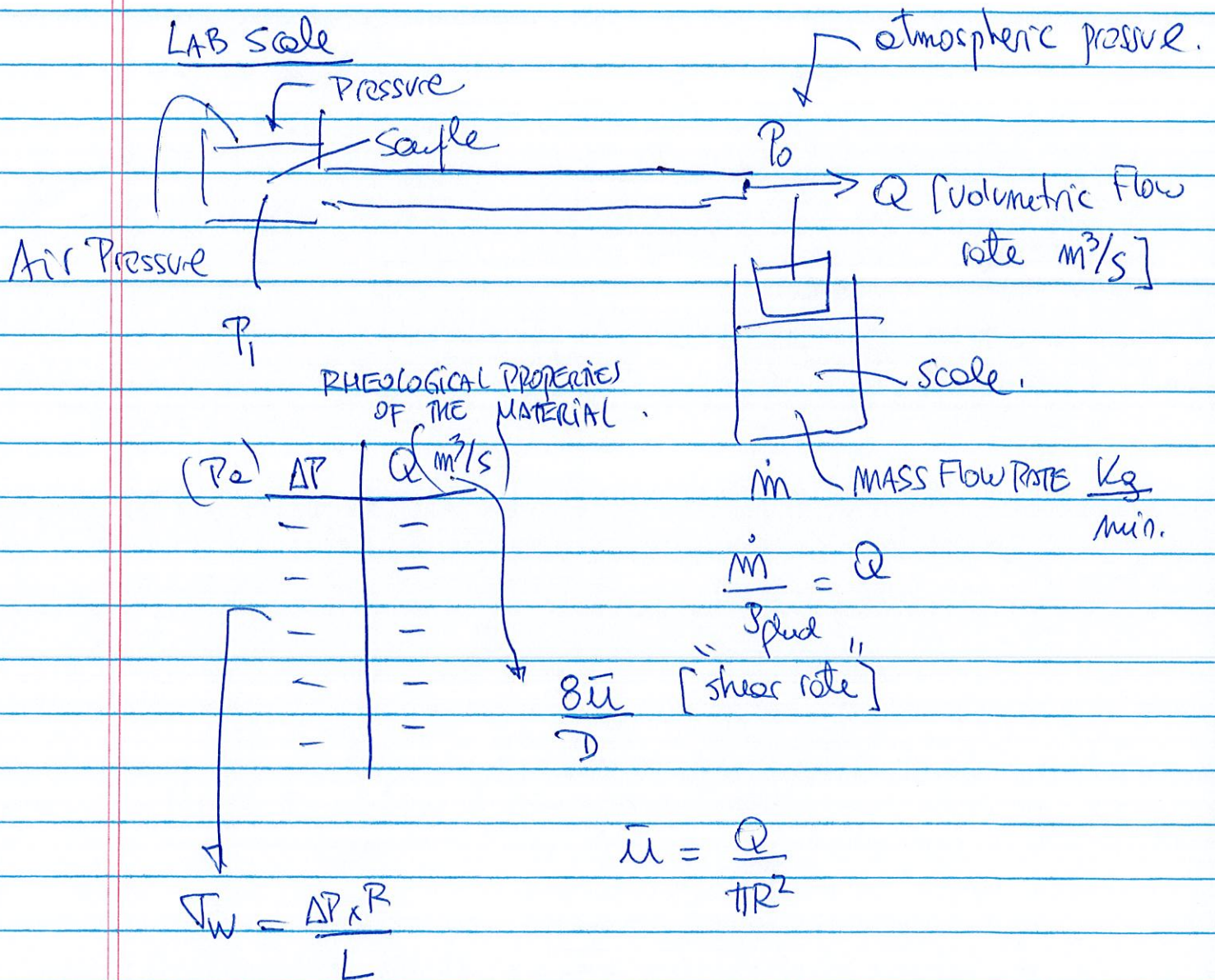
$$V_1 - V_2 = R_3 \times I_3$$

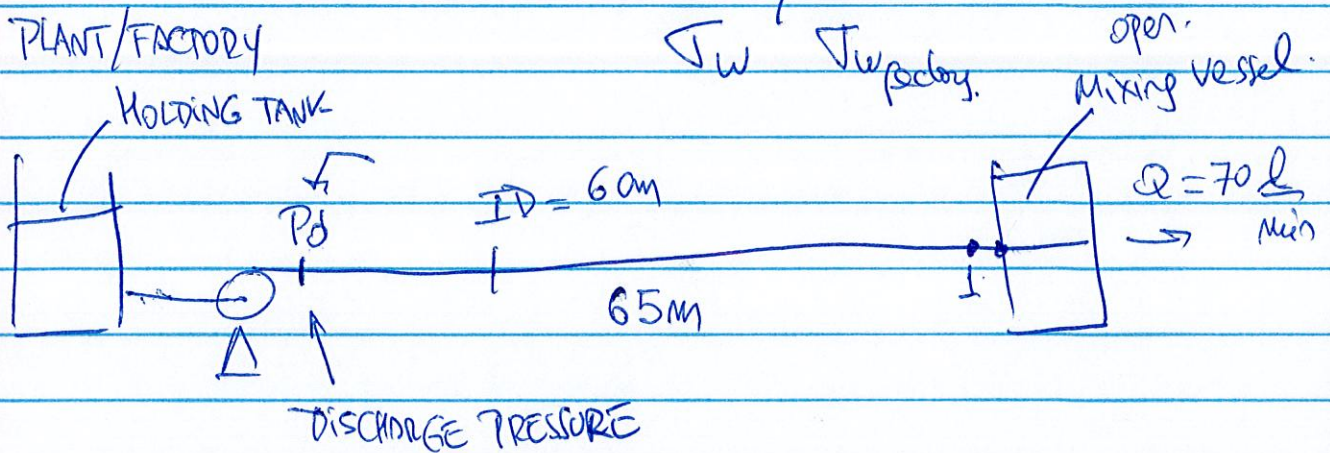
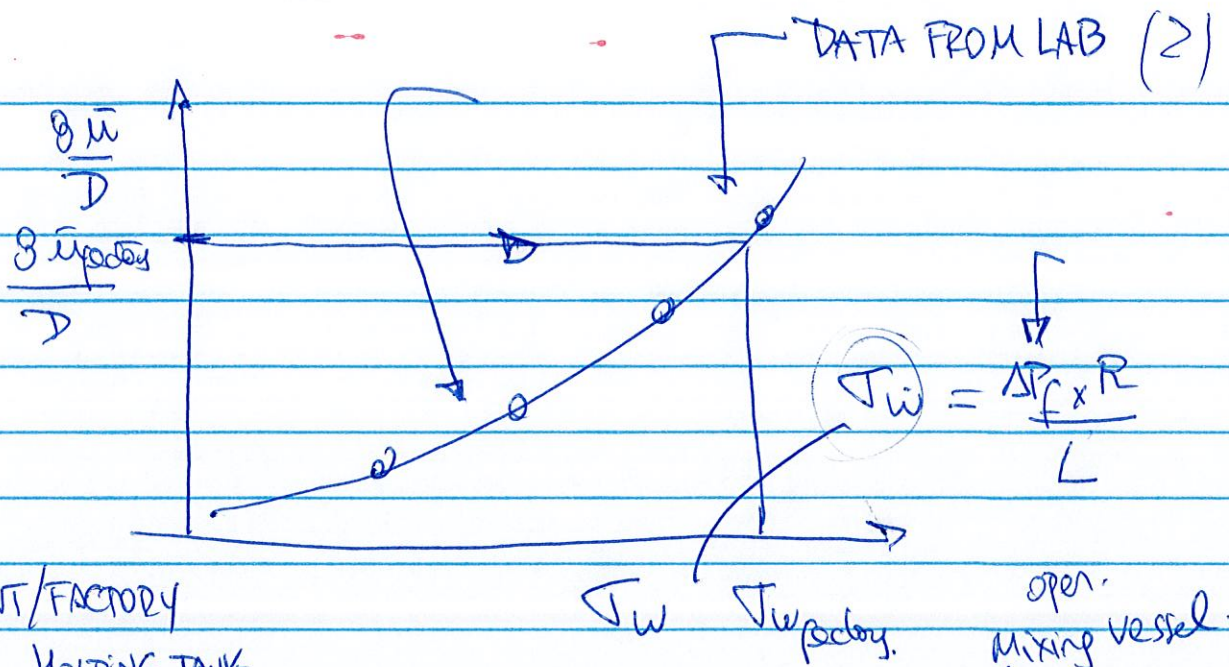
Question 2

(1)

Scale-up Process

LAB Scale





MECHANICAL ENERGY BALANCE BETWEEN "d" [discharge of the pump] and location "1"

equal if diameter of pipe is one

$$\Delta P_{pump} = (P_1 - P_d) + \rho g (h_1 - h_d) + \rho \frac{\bar{u}_d^2 - \bar{u}_1^2}{2\alpha}$$

$P_{atm} = 0 \leftarrow \text{gauge pressure}$

$$+ \Delta P_{f d \rightarrow 1}$$

$$0 = P_1 - P_d + 0 + 0 + \Delta P_{f d \rightarrow 1} \quad (1)$$

$h_1 = h_d$

THERE IS NO PUMP BETWEEN "d" and "1"

From Eq. (1)

(3)

$$P_d = \Delta P_{f d \rightarrow 1}$$

Factory

$$Q = 70 \frac{\text{l}}{\text{factory min.}} = 70 \frac{\text{l}}{\text{min}} \times \frac{1 \text{ min}}{60 \text{ sec.}} \times \frac{1 \text{ m}^3}{1000 \text{ l}} = \frac{70}{60,000} \frac{\text{m}^3}{\text{s}}$$

$$\bar{u}_{\text{factory}} = \frac{Q_{\text{factory}}}{\pi R_{\text{factory}}^2} \quad \begin{matrix} \nearrow 70 \\ 60,000 \end{matrix}$$

\uparrow ? $R = \frac{0.06 \text{ m}}{2}$

$\frac{8 \bar{u}_{\text{factory}}}{D_{\text{factory}}}$

From Plot

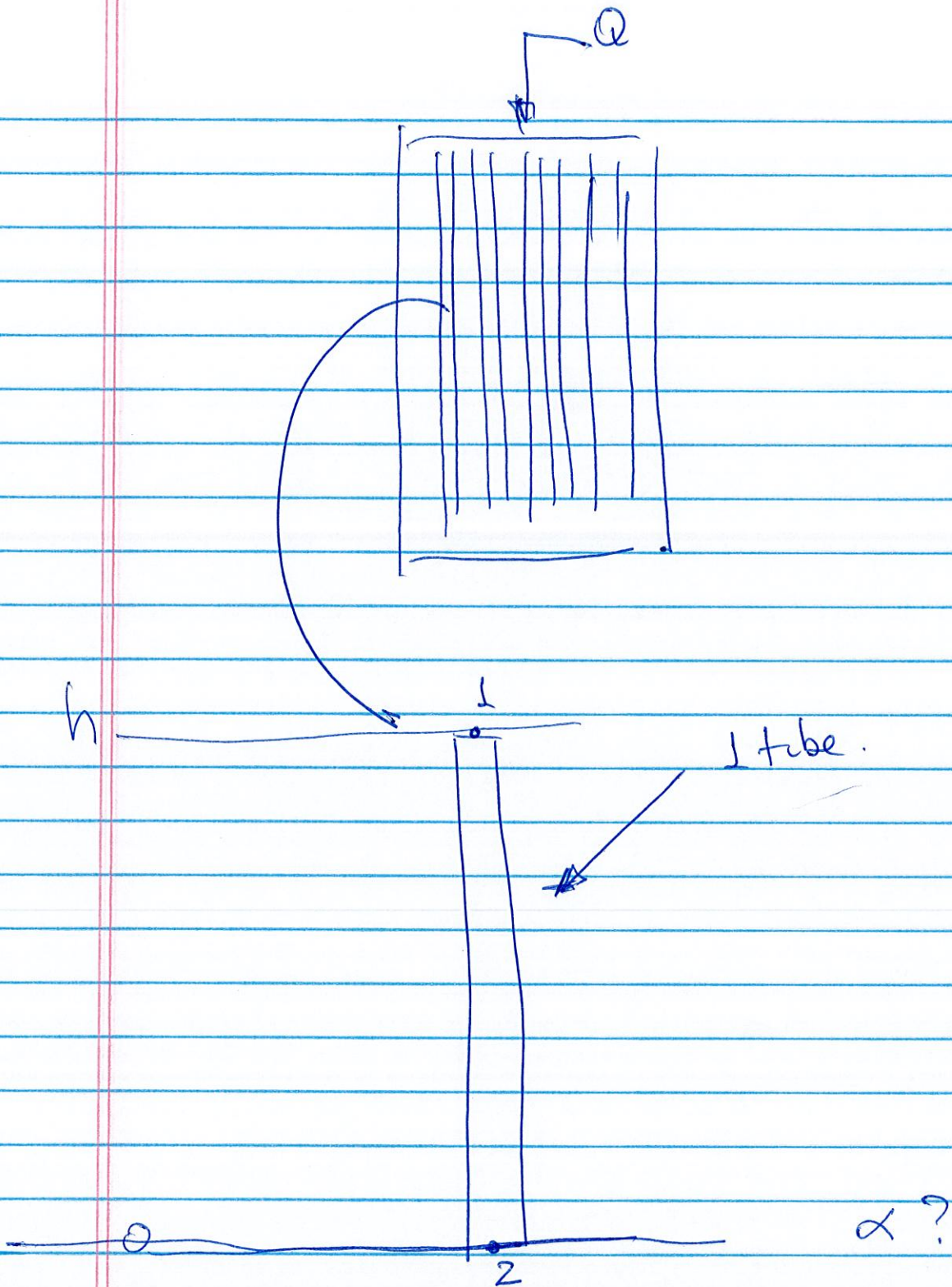
$\Delta P_{f, \text{factory}} \quad \nabla w_{\text{factory}}$

✓ From factory conditions.

$$\Delta P_{f d \rightarrow 1} = \frac{\nabla w \times L}{R} \quad \begin{matrix} \leftarrow 65 \text{ m} \\ \uparrow 0.03 \text{ m} \end{matrix}$$

$$P_d = \Delta P_{f d \rightarrow 1}$$

(4)



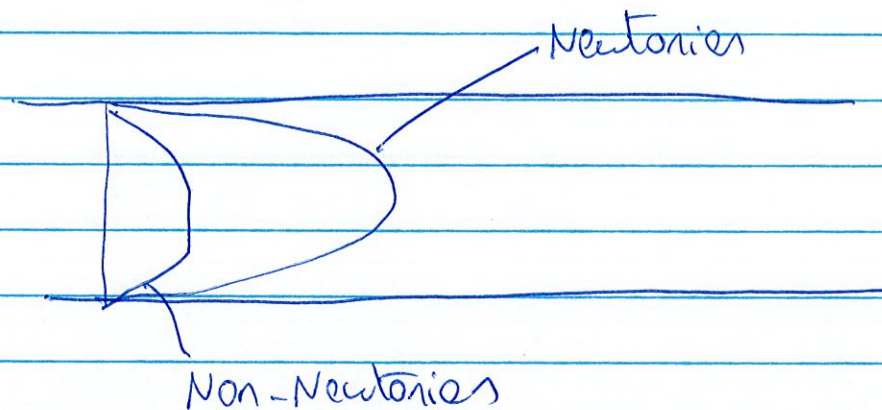
ENERGY BALANCE BETWEEN 1 & 2

$$\Delta P_{\text{pump}} = (\cancel{P_2 - P_1}) + \rho g (h_2 - h_1) + \frac{\rho}{2\alpha} (\cancel{u_2^2 - u_1^2}) + \Delta P_{f1 \rightarrow 2}$$

\uparrow \uparrow
 0 $0 + h$

Why we are using α ?

(5)



$$\text{Kinetic Energy Change} = \frac{1}{2} \rho (\bar{u}_2^2 - \bar{u}_1^2)$$

Correction for Rheology - [check notes for Equations for different fluids]

if needed it will be provided in the exam

$\Delta P_{f1 \rightarrow 2} = \rho g h$

$\frac{2 \mu K (3n+1)}{R} \left[\frac{4Q}{\pi R^3} \right]^n = \rho g h$

$\rightarrow Q$

P_1

P_2

ASIDE how we determine the value of h (6)

h

$$\rho g (h_2 - h_1)$$

$$\rho g (0 - h) = -\rho g h$$

$\uparrow (+)$

$h_2 = 0$

$$\rho g (h_2 - h_1) = -\rho g h$$

$\downarrow (-)$

$\uparrow (+)$

h_1

$$h_1 = 0$$

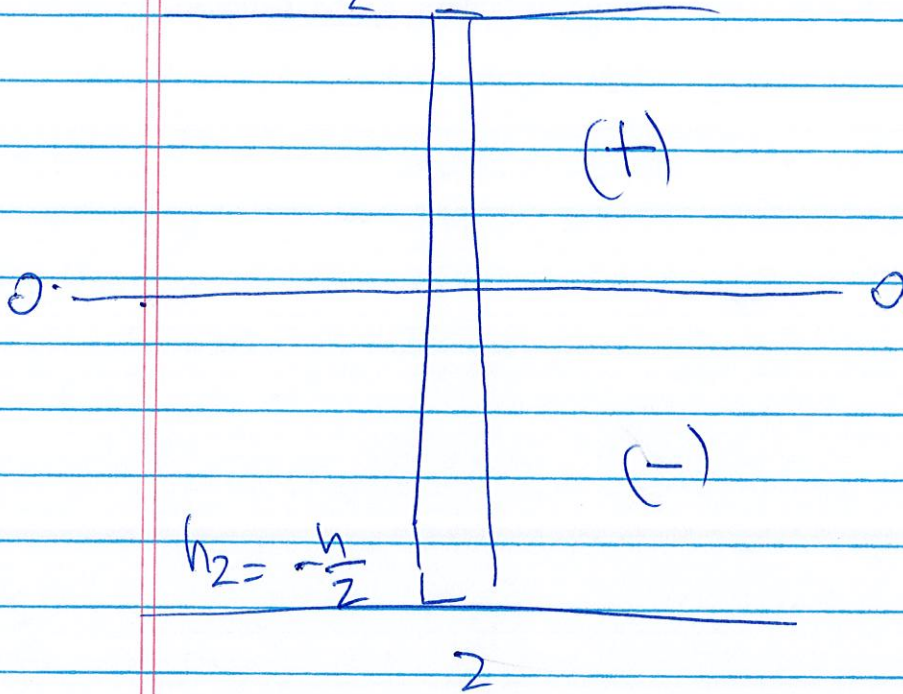
$$h_2 = -h$$

$\downarrow (-)$

h_2

$$h_1 = \frac{h}{2}$$

(7)



$$\rho g (h_2 - h_1) =$$

$$= \rho g \left(-\frac{h}{2} - \frac{h}{2} \right) =$$

$$= -\rho g h$$

$$\Delta P_{\text{pump}} = \underbrace{(P_2 - P_1)}_{\text{}} + \underbrace{\rho g (h_2 - h_1)}_{\text{}} + \frac{\rho}{2\alpha} (\vec{u}_2^2 - \vec{u}_1^2) + \underbrace{\Delta P_{1 \rightarrow 2}}_{\text{}}$$