

ABE 30800 - Spring 2018

Examples Problems External and Internal Convection

Problem 1

The African elephant has developed the pinna or external ear that functions as a radiator-convector (see page 60 in the textbook for more discussion). The pinna can be modeled as a flat plate with air flowing over it.

- (1) Find and plot the convective heat loss from the pinna as the surface temperature of the pinna ranges from 21°C to 36°C. Since, the temperature of the ears varied it could be hard to estimate the properties of the film you can use the air temperature that is at 20°C. Remember that an elephant has two ears!!, and heat is lost equally from both sides of the ear. The air velocity is 2m/s, the surface of one ear is 0.84m², and the average length of one side of the ear is 1m. Use table of properties of air.
- (2) If the rate of metabolic heat production for a 2000 kg elephant is 1650 W, what is the maximum percentage of the metabolic heat that can be lost by convection through the pinna?

Problem 2

A glass-door fire screen panel is used to reduce heat loss from the room through the chimney. The panel has a height of 0.7m and a width of 1m and reaches a uniform temperature of 250°C. If the temperature of the room is maintained at 20°C and the air in, the room is considered still:

- (a) Under what type of convection is heat transferred to the room? Explain the principles behind the type of convection you selected.
- (b) Estimate the heat transferred to the room, please state all your assumptions.

Problem 3

Hot tub designers have found that for a typical hot tub system, water loss by evaporation is about 0.001 kg/s if the operating conditions are the ones illustrated in the schematic figure given below. Evaporation of water can be calculated as:

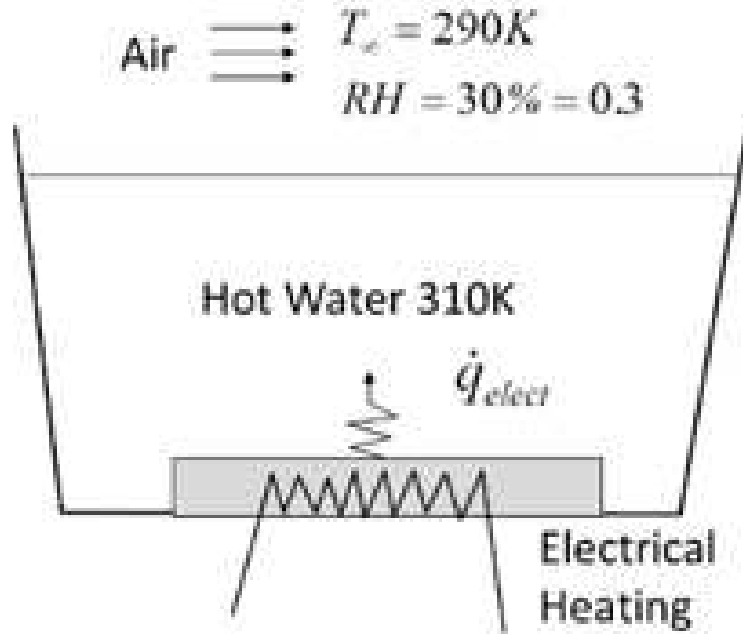
$$q_{w, \text{evap}} = h_m A (\rho_{w, \text{sat}} - \rho_{w, \text{air}})$$

\bar{h}_m (in m/s) is the mass convection coefficient, which is related to the heat transfer coefficient by the following equation:

$$\frac{\bar{h}}{\bar{h}_m} = \rho c \left(\frac{\alpha}{D_{w, \text{air}}} \right)^{2/3}$$

$D_{w, \text{air}}$ is the diffusion coefficient of water vapor in air and equals to 26x10⁻⁶ m²/s. The other properties can be found or calculated in the Appendix of the textbook tables. Write all your assumptions in solving this problem.

- (a) Estimate the power required to keep the temperature of the hot tube at 310K
- (b) Give and briefly explain the mechanism under which the temperature of the water pool gets cool. Compare the energy used in each of these mechanisms.



Problem 4

An inventor is proposing a system to cool down a house without using an air conditioner system. The system is simple, air is routed from the house through a plastic pipe ($k=0.15 \text{ W/m.K}$). The internal and external diameters of the pipe are $D_i=0.15\text{m}$ and $D_o=0.17\text{m}$ respectively, and the pipe is submerged in a body of water. The water temperature is near constant at 17°C , and the external convection coefficient is $h_o=1,500 \text{ W/m}^2.\text{K}$.

- (a) If air from the home enters the pipe at a temperature of $T_{a,in} = 30^\circ\text{C}$ with a volumetric flow rate of $\dot{V} = 0.025 \text{ m}^3/\text{s}$, what pipe length L (only consider the length shown in the figure, i.e. ignore the bends and vertical sections) is needed to provide a temperature outlet temperature $T_{a,out} = 21^\circ\text{C}$?
- (b) Estimate and compare the different heat resistances in the system (**consider a cylindrical geometry**). Write clearly all your assumptions

