

Study Guide Test 2

In order to do well on the next test, you should be able to do the following:

1. Be able to derive the terms K_m , V_m for different inhibition enzymatic kinetics (ie. competitive inhibition, uncompetitive inhibition, non-competitive inhibition) and understand how concentrations of inhibitor $[I]$ affect K_m and V_m using the Lineweaver-Burke plot.
2. Explain in your own words that the terms *space-time* and *space-velocity*.
3. Be able to apply the mass balance for any reactant (or product) in reactor.
4. Be able to derive performance equations for ideal batch and steady-flow reactors and their integrated expressions for various types of reactions (ie. enzymatic reactions, zero order, 1st order, 2nd order).
5. Be able to solve for the sizes, flow rates, and production rates (qC_0X) of mixed and plug flow reactors, and compare the performance of MFR and PFR for a given duty.
6. Be able to derive performance equations for single reactors in series (PFR, MFR) or combinations in terms of C_n and overall conversion, X , i.e. $X = f(\tau, k)$.

Practice problem:

3 MFR in series

All same volume, $V = 10\text{ L}$

$\tau = 1 \frac{1}{2}\text{ hr}$, $C_0 = 10\text{ mol/L}$, $k = 0.04 \frac{1}{\text{hr}}$

What is overall conversion?

What are intermediate concentrations?

1st order rxn

$$C_1 = \frac{C_0}{1 + k\tau} \quad k\tau = (0.04) \left(\frac{10}{1.5} \right) = 0.4$$

$$\text{So, } C_1 = \frac{C_0}{1 + k\tau} = \frac{10}{1.4} = \underline{\underline{7.1429\text{ mol/L}}}$$

$$C_2 = \frac{C_1}{1 + k\tau} = \frac{7.1429}{1.4} = \underline{\underline{5.102\text{ mol/L}}}$$

etc.

$$C_8 = \frac{C_0}{(1 + k\tau)^n} = \frac{C_0}{(1 + 0.4)^8} = 0.6776 \frac{\text{mol}}{\text{L}}$$

$$X = \frac{C_0 - C_8}{C_0} = \underline{\underline{0.9322}}$$

If conversion X is given, can we calculate τ and reactor size?

Multiple reactor systems

Plug flow

$$\tau = \frac{V}{q} = \int \frac{dC}{r}$$



$$\tau_1 = \frac{V_1}{q} = \int_{C_0}^{C_1} \frac{dC}{r}$$

$$\tau_2 = \frac{V_2}{q} = \int_{C_1}^{C_2} \frac{dC}{r}$$

$$\tau_3 = \frac{V_3}{q} = \int_{C_2}^{C_3} \frac{dC}{r}$$

$$\tau_{\text{total}} = \sum \tau_i = \frac{1}{q} \sum V_i = \int_{C_0}^{C_1} \frac{dC}{r} + \int_{C_1}^{C_2} \frac{dC}{r} + \int_{C_2}^{C_3} \frac{dC}{r}$$

$$= \int_{C_0}^{C_3} \frac{dC}{r}$$

For n reactors in series

$$\tau_{\text{total}} = \frac{1}{q} \sum_{i=1}^n V_i = \int_{C_0}^{C_n} \frac{dC}{r} = -C_0 \int_0^{X_n} \frac{dx}{r}$$

\therefore Series of pfrcs is simply additive.

What is the overall conversion for 1st order reactions i.e. $X = f(\tau_1, \tau_2, \tau_3, k)$?