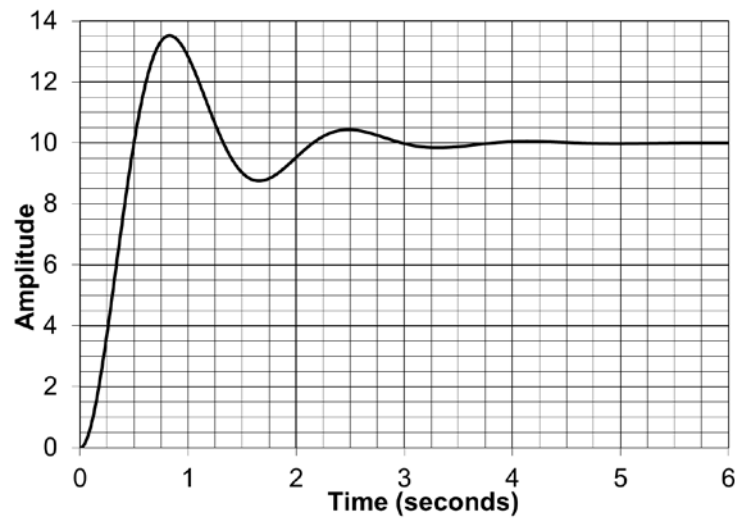
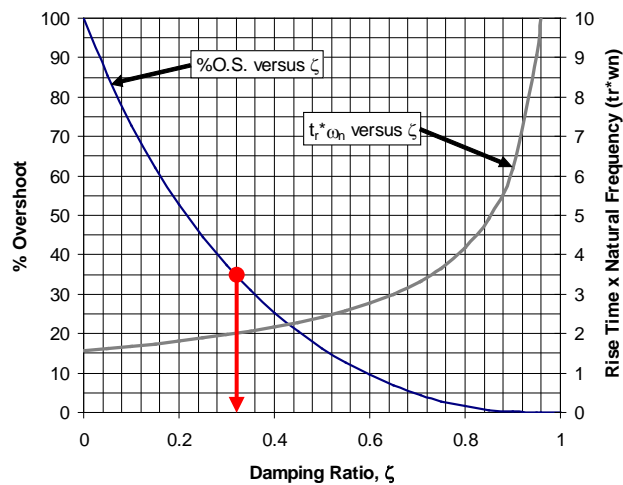


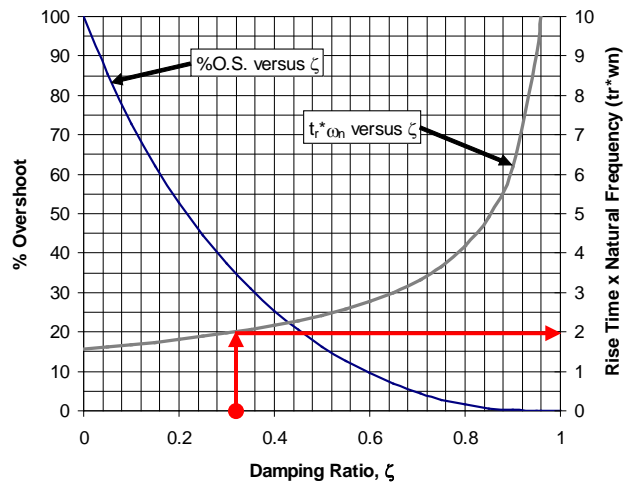
Below is a 2nd order step response. Find ζ and ω_n



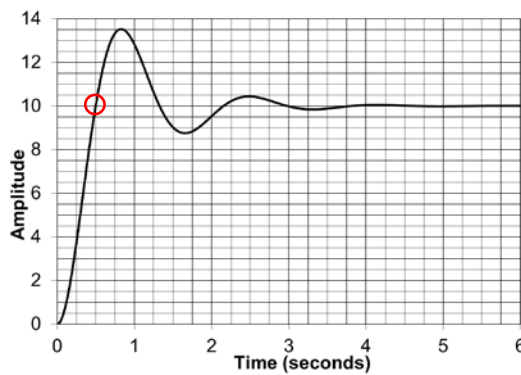
1. Find the plot from slide 105 (textbook pg 81)
2. Using the provided 2nd order response, calculate % overshoot
 - a. $\%OS = \frac{\text{peak value} - \text{SS value}}{\text{SS value} - \text{initial value}} = \frac{13.5 - 10}{10 - 0} = 0.35 \rightarrow 35\%OS$
3. Mark the location of 35 %OS on the ‘%O.S. versus ζ ’ trace and then draw a vertical line down to find the value of ζ that corresponds to 35 %OS
 - a. This results in $\zeta = 0.32$



4. Staying at the same value of ζ , draw a vertical line up until you intersect with the ' $t_r \cdot \omega_n$ versus ζ ' trace and then draw a horizontal line to the right to find the value of $t_r \cdot \omega_n$
- a. This results in $t_r \cdot \omega_n = 2$



5. The rise time (t_r) is the time it takes to 1st cross the steady state value
- a. SS value = 10, $t_r = 0.5 \text{ sec}$



6. Since $t_r \cdot \omega_n = 2$ and $t_r = 0.5 \text{ sec}$, then $\omega_n = 4 \text{ rad/s}$
7. The final answer is $\zeta = 0.32$ and $\omega_n = 4 \text{ rad/s}$