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## Index of Notation

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### General symbols

$\mathbb{C}$	field of complex numbers
$\mathbb{F}_q$	finite field with $q$ elements
$\text{Id}_M$	identity map on the set $M$
$\text{Im}(f)$	image of the map $f$
$\ker(\varphi)$	kernel of the morphism $\varphi$
$\mathbb{N}$	the natural numbers without 0
$\mathbb{N}_0$	the natural numbers with 0
$\mathcal{O}$	discrete valuation ring
$\mathbb{P}$	the prime numbers in $\mathbb{Z}$
$\mathbb{Q}$	field of rational numbers
$\mathbb{Q}_p$	field of $p$ -adic numbers
$\mathbb{R}$	field of real numbers
$\mathbb{Z}$	ring of integer numbers
$\mathbb{Z}_{\geq a}, \mathbb{Z}_{> a}, \mathbb{Z}_{\leq a}, \mathbb{Z}_{< a}$	$\{m \in \mathbb{Z} \mid m \geq a \text{ (resp. } m > a, m \geq a, m < a)\}$
$\mathbb{Z}_p$	ring of $p$ -adic integers
$ X $	cardinality of the set $X$
$\delta_{ij}$	Kronecker's delta
$\cup$	union
$\sqcup$	disjoint union
$\cap$	intersection
$\sum$	summation symbol
$\prod, \times$	cartesian/direct product
$\rtimes$	semi-direct product
$\oplus$	direct sum
$\otimes$	tensor product
$\emptyset$	empty set
$\forall$	for all
$\exists$	there exists
$\cong$	isomorphism
$a \mid b, a \nmid b$	$a$ divides $b$ , $a$ does not divide $b$
$(a, b)$	gcd of $a$ and $b$
$(F, \mathcal{O}, k)$	$p$ -modular system
$f _S$	restriction of the map $f$ to the subset $S$
$\hookrightarrow$	injective map
$\twoheadrightarrow$	surjective map

## Group theory

$\text{Aut}(G)$	automorphism group of the group $G$
$\mathfrak{A}_n$	alternating group on $n$ letters
$C_m$	cyclic group of order $m$ in multiplicative notation
$C_G(x)$	centraliser of the element $x$ in $G$
$C_G(H)$	centraliser of the subgroup $H$ in $G$
$D_{2n}$	dihedral group of order $2n$
$\delta : G \rightarrow G \times G$	diagonal map
$\text{End}(A)$	endomorphism ring of the abelian group $A$
$G/N$	quotient group $G$ modulo $N$
$\text{GL}_n(K)$	general linear group over $K$
$HgL$	$(H, L)$ -double coset
$[H \backslash G / L]$	set of $(H, L)$ -double coset representatives
$H \leqslant G, H < G$	$H$ is a subgroup of $G$ , resp. a proper subgroup
$N \trianglelefteq G$	$N$ is a normal subgroup of $G$
$N_G(H)$	normaliser of $H$ in $G$
$N \rtimes_\theta H$	semi-direct product of $N$ in $H$ w.r.t. $\theta$
$\mathfrak{S}_n$	symmetric group on $n$ letters
$\text{SL}_n(K)$	special linear group over $K$
$\mathbb{Z}/m\mathbb{Z}$	cyclic group of order $m$ in additive notation
${}^x g$	conjugate of $g$ by $x$ , i.e. $gxg^{-1}$
$\langle g \rangle \subseteq G$	subgroup of $G$ generated by $g$
$ G : H $	index of the subgroup $H$ in $G$
$[G/H]$	set of left coset representatives of $H$
$\bar{x} \in G/N$	class of $x \in G$ in the quotient group $G/N$
$\{1\}, 1$	trivial group

## Module theory

$\text{Hom}_R(M, N)$	$R$ -homomorphisms from $M$ to $N$
$\text{End}_R(M)$	$R$ -endomorphism ring of the $R$ -module $M$
$\text{hd}(M)$	head of the module $M$
$KG$	group algebra of the group $G$ over the commutative ring $K$
$\varepsilon : KG \longrightarrow K$	augmentation map
$I(KG)$	augmentation ideal
$\text{Irr}(R)$	set of representatives of the isomorphism classes of simple $R$ -modules
$J(R)$	Jacobson radical of the ring $R$
$M \mid N$	$M$ is a direct summand of $N$
$M \otimes_R N$	tensor product of $M$ and $N$ balanced over $R$
$M^G$	$G$ -fixed points of the module $M$
$M_G$	$G$ -cofixed points of the module $M$
$M \downarrow_H^G, \text{Res}_H^G(M)$	restriction of $M$ from $G$ to $H$
$M \uparrow_H^G, \text{Ind}_H^G(M)$	induction of $M$ from $H$ to $G$
$\text{Inf}_{G/N}^G(M)$	inflation of $M$ from $G/N$ to $G$
$R^\times$	units of the ring $R$
$R^\circ$	regular left $R$ -module on the ring $R$
$\text{rad}(M)$	radical of the module $M$
$\text{soc}(M)$	socle of the module $M$

$\langle X \rangle_R$	$R$ -module generated by the set $X$
$V^F$	extension of scalars $F \otimes_{\mathcal{O}} V$
$Z(R)$	centre of the ring $R$

### Character and block theory

$b^G$	Brauer correspondent of $b$
$C$	Cartan matrix of $G$
$\text{Cl}_F(G), \text{Cl}_F(G_{p'})$	the class functions on $G$ or $G_{p'}$
$\text{Dec}_p(G)$	decomposition matrix
$G_{p'}$	$p$ -regular elements of $G$
$\text{Irr}_F(G)$	ordinary irreducible $F$ -characters of $G$
$\text{IBr}_p(G)$	irreducible $p$ -Brauer characters of $G$
$\chi_{\text{reg}}$	regular character
$\rho_{\text{reg}}$	regular representation
$\Phi_\varphi$	projective indecomposable character associated to $\varphi \in \text{IBr}(G)$

### Category theory

$\text{Ob } \mathcal{C}$	objects of the category $\mathcal{C}$
$\text{Hom}_{\mathcal{C}}(A, B)$	morphisms from $A$ to $B$
$\text{Set}$	the category of sets
$\text{Vec}_k$	the category of vector spaces over the field $k$
$\text{Top}$	the category of topological spaces
$\text{Grp}$	the category of groups
$\text{Ab}$	the category of abelian groups
$\text{Rng}$	the category of rings
${}_R\text{Mod}$	the category of left $R$ -modules
$\text{Mod}_R$	the category of left $R$ -modules
${}_R\text{Mod}_S$	the category of $(R, S)$ -bimodules