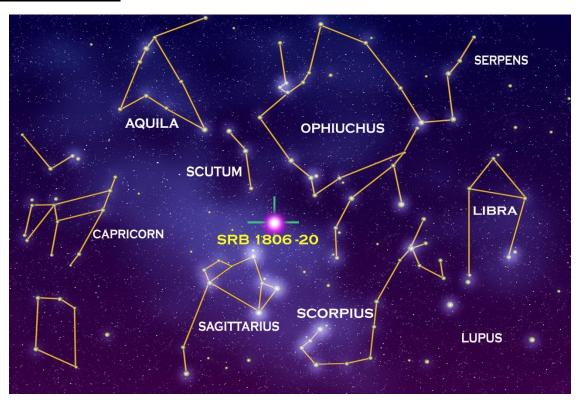
# Title: Constellations

# This question is graded for 1%

### **Problem Statement:**



Abby the Astronaut wants to create new constellations. Given a star map with n different stars, he wants to find the number of different **configurations** he can make to the star map.

He can make a **constellation** from the star map by grouping up x different stars together, where a <= x <= b. He needs to fill the star map with different constellations until no more constellations are possible to be made for it to count as a valid **configuration**. Every star can only be part of at most 1 constellation.

Note that the order where he fills up constellations matters, ie: [1] [2] is different from [2] [1], but [1, 2] is the same as [2, 1].

### Input:

In a single line, integers n, a, b.  $(max(1, n/10) \le a \le b \le n \le 50)$   $(b - a \le 5)$ 

#### Output:

In a single line, the total number of configurations he can make to a star map with n stars, constellations of size a to b, modulo  $10^9 + 7$ .

### Example:

<u>Sample Input 1:</u> 3 \* stars(2,1,3) + 3\*stars(1,1,3) + 1\*stars(0,1,3)

3 1 3

Sample Output 1:

13

Sample Input 2:

7 6 7

Sample Output 2:

8

# **Explanation:**

For Sample Input 1, he can make these 13 configurations:

Config 1: [1, 2, 3]

Config 2: [1, 2] [3]

Config 3: [1, 3] [2]

Config 4: [2, 3] [1]

Config 5: [1] [2, 3]

Config 6: [2] [1, 3]

Config 7: [3] [1, 2]

Config 8: [1] [2] [3] Config 9: [1] [3] [2]

Config 10: [2] [1] [3]

Config 11: [2] [3] [1]

····-9 --- [-3 [-3 [-3

Config 12: [3] [1] [2]

Config 13: [3] [2] [1]

For Sample Input 2, there are 7 possible configurations with 1 constellation of 6 stars and 1 star unpicked, and 1 configuration with 1 constellation of 7 stars only.

#### Appendix: Modulo Distributive Rules:

$$(a + b) \% c = ((a \% c) + (b \% c)) \% c$$

$$(a-b)\%c = ((a\%c)-(b\%c))\%c$$

Image source: https://www.nasa.gov/sites/default/files/thumbnails/image/constellation\_.jpg