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THE AWARDS
2020

UNIVERSITY
OF THE YEAR

System-wide probabilistic energy forecasting

Energy Forecasting Innovation Conference

24 May 2022

WORLD
CHANGING
GLASGOW

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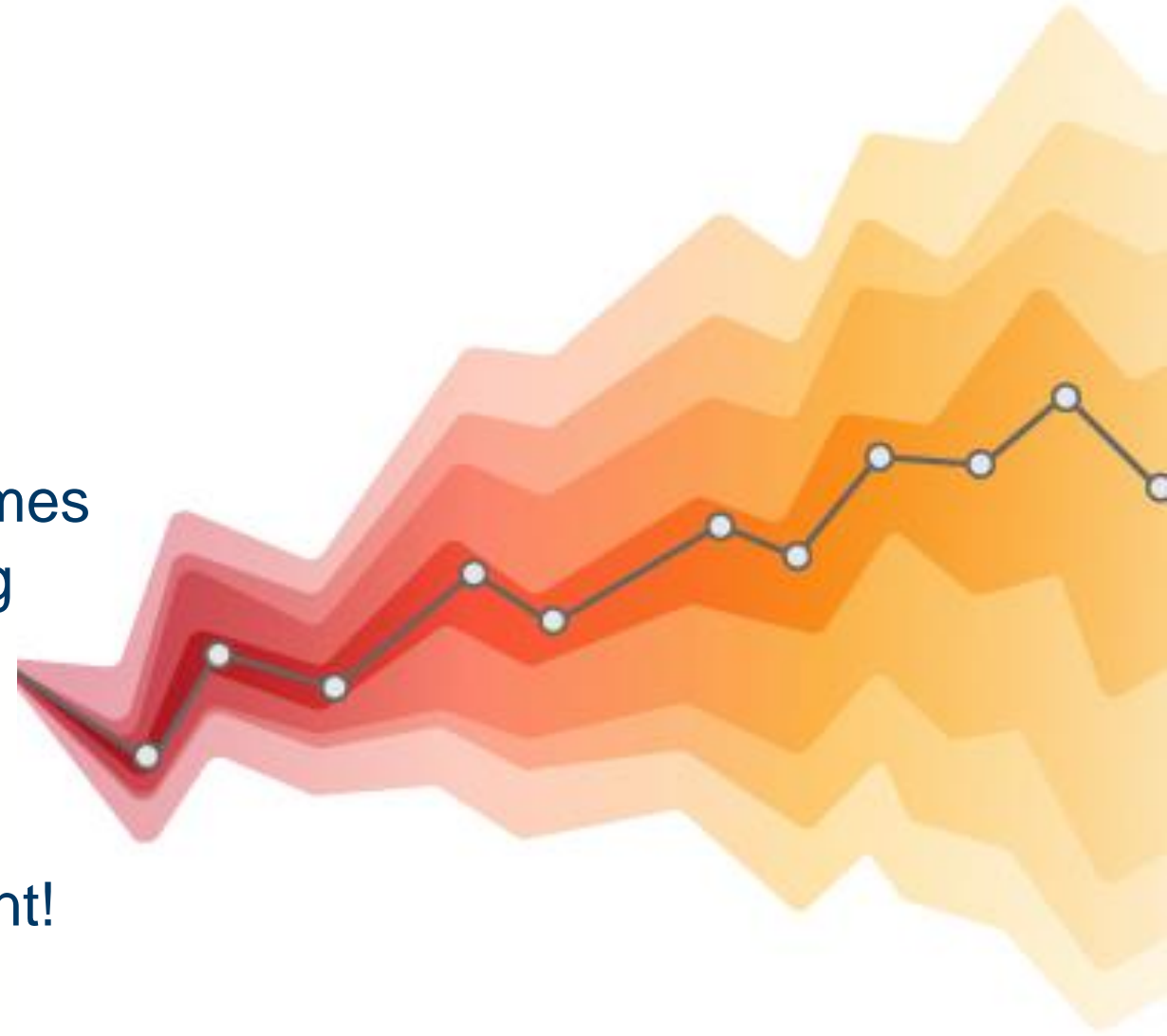
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Contents

- Project overview
- Research outcomes
 - Net-demand forecasting and extremes
 - Large-scale wind power forecasting
 - Time-varying covariance
- Visions of energy forecasting
 - Probabilistic forecasting
 - Opportunities: data-rich environment!
- Summary





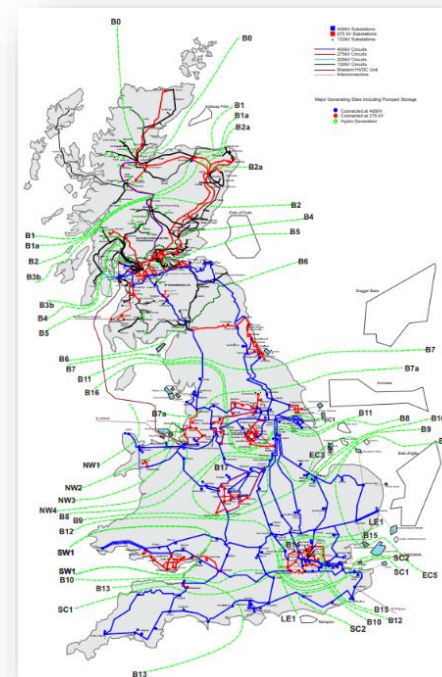
System-wide probabilistic energy forecasting

Motivation

- Energy systems operated under significant and growing uncertainty
- Necessitate that uncertainty is minimised and accurately described to achieve:
 - Efficiency/“*optimisation*”
 - Satisfy risk appetite
- Forecast uncertainty is complex but structured
 - Spatio-temporal
 - Weather and non-weather dynamics

Aim:

- Develop (some of) the statistical methods required to underpin this capability
- Establish potential value for key decision-making problems with partners



Decisions

- Energy Balancing
- Reserve
- Constraints
- Trading

**All are multi-variate,
spatio-temporal
problems!**

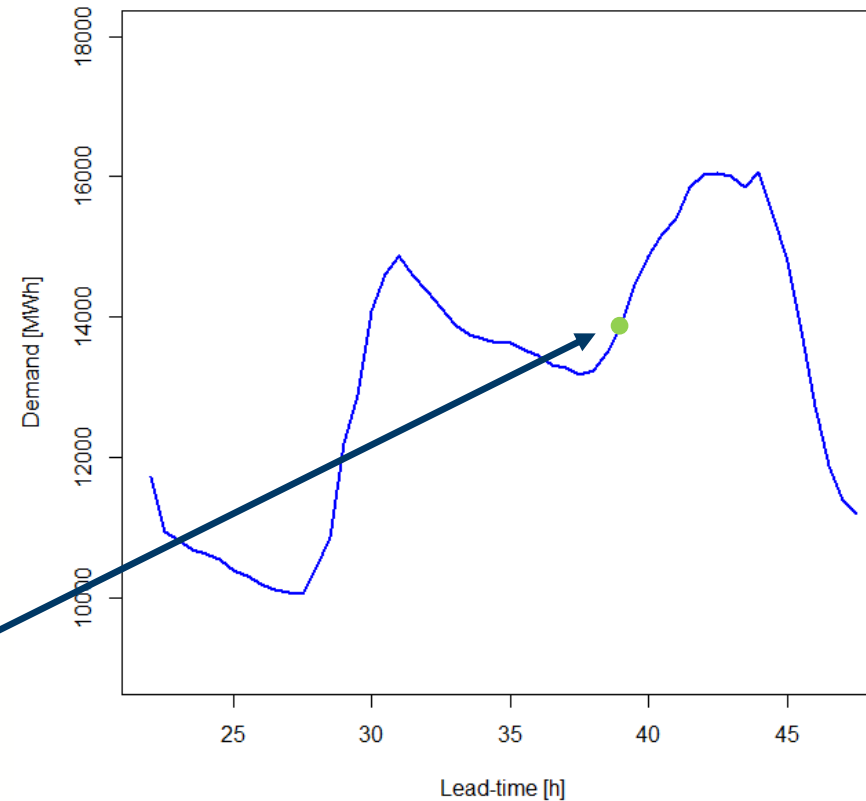




Deterministic forecast

Consider this day-ahead
forecast of load on the
GB transmission system:

Forecast at each time
point is a **single number**



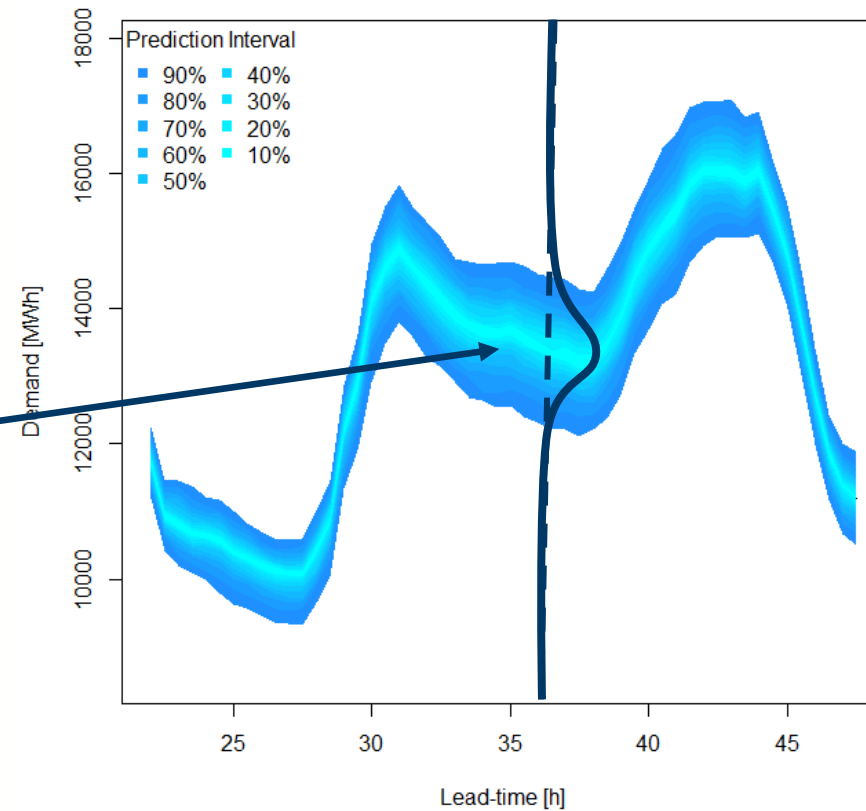
Suitable for decision making if:

1. Cost of over/under predicting is symmetric
2. User is *risk neutral*



Probabilistic forecast

Forecast at each time point is a **probability distribution**



Can make decision based on:

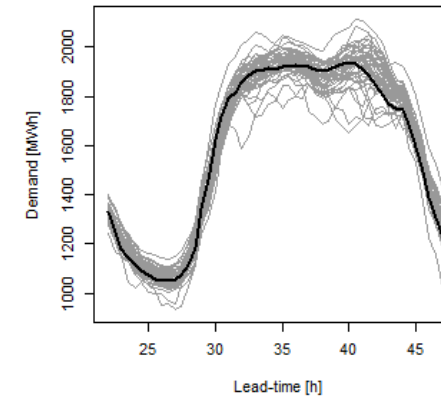
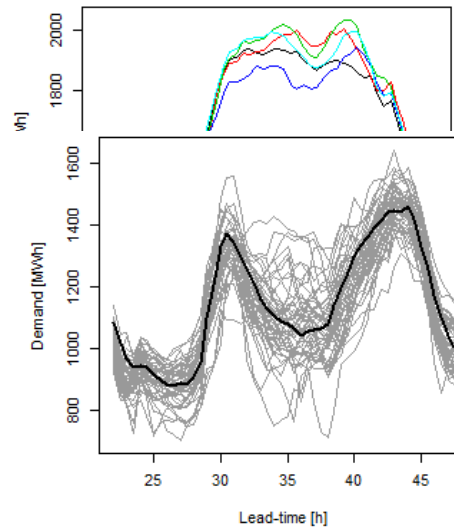
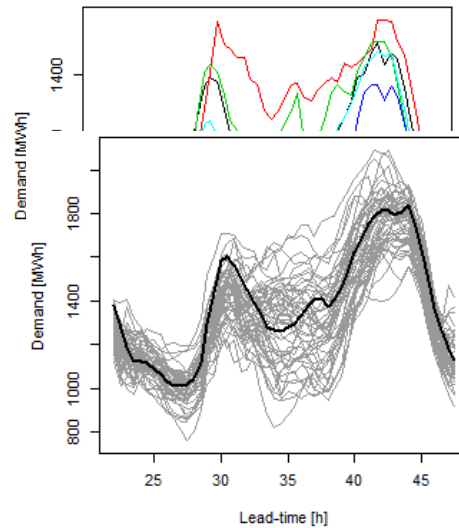
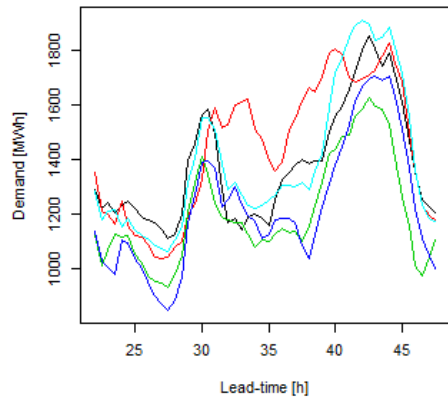
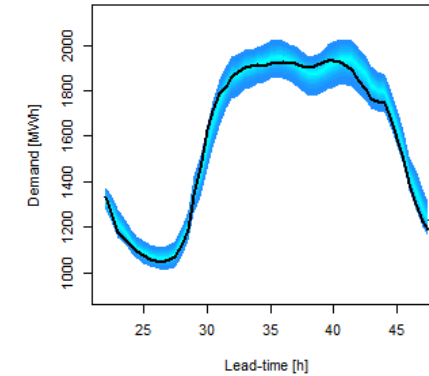
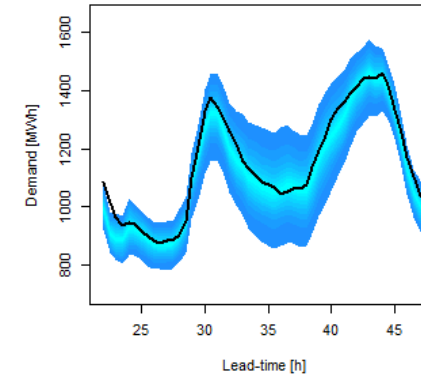
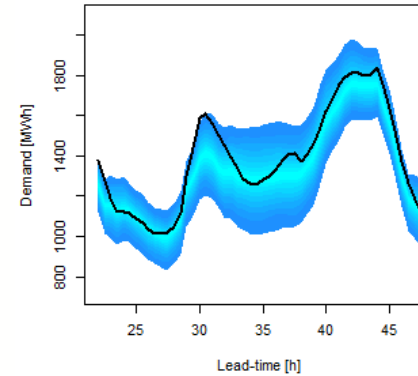
1. **Asymmetric costs** of over/under predicting
2. **Risk indices/metrics**



Probabilistic Forecasting

Probabilistic Forecast, a forecast that includes uncertainty quantification:

- Prediction intervals and quantiles
- Density forecasts
- Trajectories or scenarios





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Probabilistic forecasting of regional net-load with conditional extremes

Work with Matteo Fasiolo

IEEE Trans. Smart Grid

<https://doi.org/10.1109/TSG.2021.3107159>

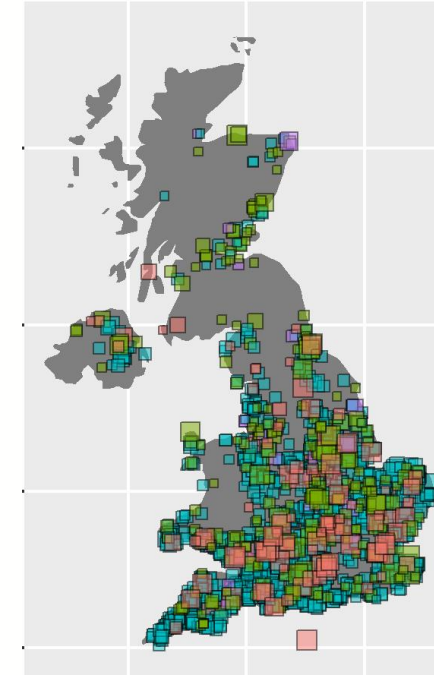


Visitor in Data Science 2019

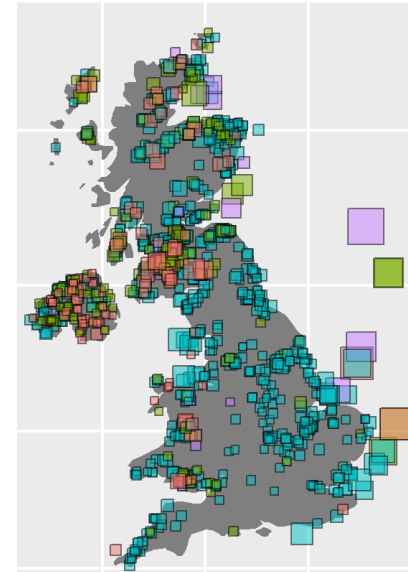


Motivation

1. Regions can differ greatly in type and capacity of embedded generation
 - Do we need different input data and methods/models?
2. Regional behaviour important to manage power flow on the grid
 - Spatial dependency must be retained for probabilistic power flow forecasting
3. Reserve is scheduled by region based on import/export capacity
 - Volume of reserve based on forecast uncertainty and TSO's risk appetite



As of March 2021:
1501 Solar Farms (+domestic PV) ↑
1037 Wind Farms →

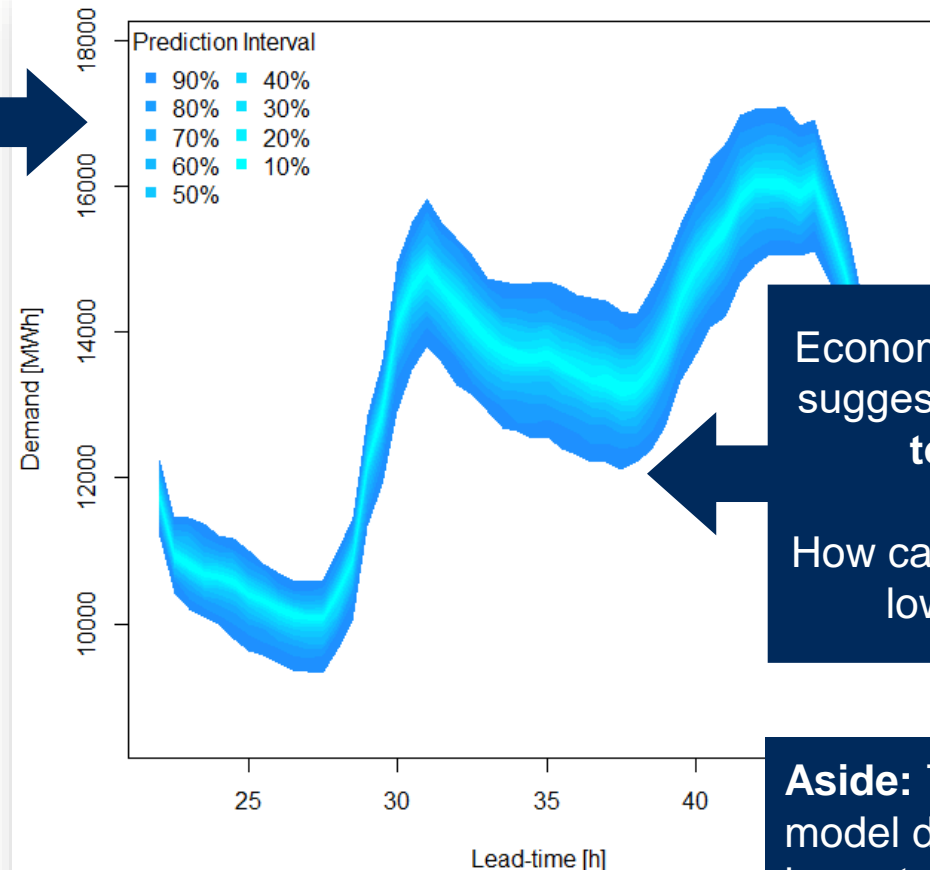


Net-load is increasingly
complex!



Motivation

Probabilistic
forecasts quantifies
*forecast
uncertainty*



Economics and current practice
suggest we're interest in **0.25%
to 0.01%** quantiles!

How can we forecast these very
low probability levels?

Aside: This is also important if we want to
model dependency later this can be negatively
impacted if tails are poorly modelled...

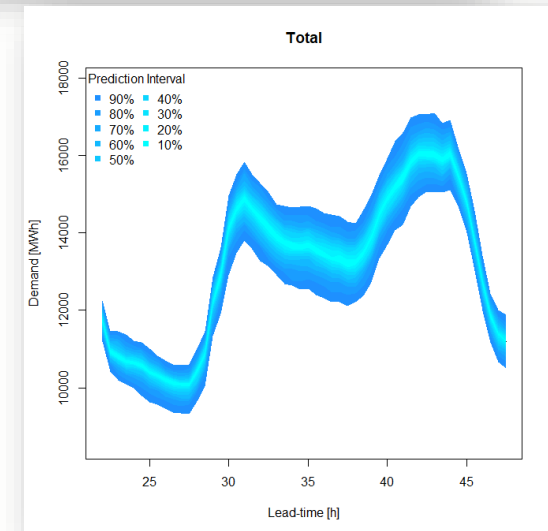
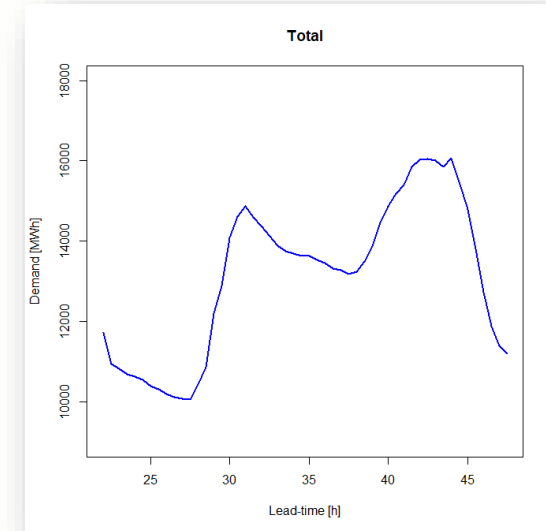


Density Forecasting Overview

Summary:

1. Generalised Additive Model point-forecast
 - a) Date/time features
 - b) Weather forecast features: temperature, wind speed and solar radiation. Summary statistics by regions
 - c) Interactions...
2. Linear Quantile Regression on residuals
 - a) Second-order polynomial on point forecast
 - b) Linear in date/time and weather features
 - c) Quantiles from 0.05%-99.95%
3. Generalised Pareto tails
 - a) From 2.5%/97.5% or 5%/95% quantiles

Steps 1 & 2 based on: Pierre Gaillard, Yannig Goude, Raphaël Nedellec, Additive models and robust aggregation for GEFCom2014 probabilistic electric load and electricity price forecasting, IJF 32(3), 2016, [10.1016/j.ijforecast.2015.12.001](https://doi.org/10.1016/j.ijforecast.2015.12.001)



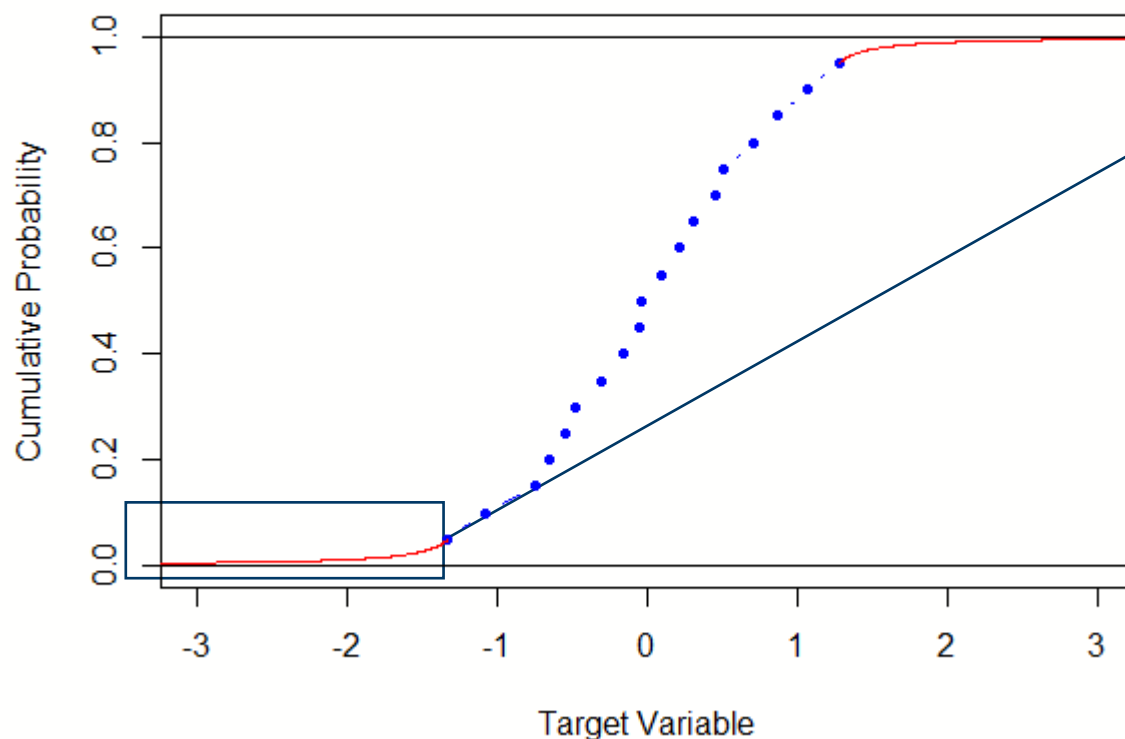


Density Forecasting

Generalised Pareto Tails

Tail Distribution
Static
Generalised
Pareto

Predictive Distribution



$$F(x; \sigma, \xi) = \begin{cases} 1 - \left(1 + \frac{\xi x}{\sigma}\right)^{-\frac{1}{\xi}} & \text{for } \xi \neq 0 \\ 1 - \exp\left(-\frac{x}{\sigma}\right) & \text{for } \xi = 0 \end{cases}$$

Shape and Scale parameters
estimated using peak-over-
threshold method

Threshold is last reliable
conditional quantile
 x = exceedance of quantile

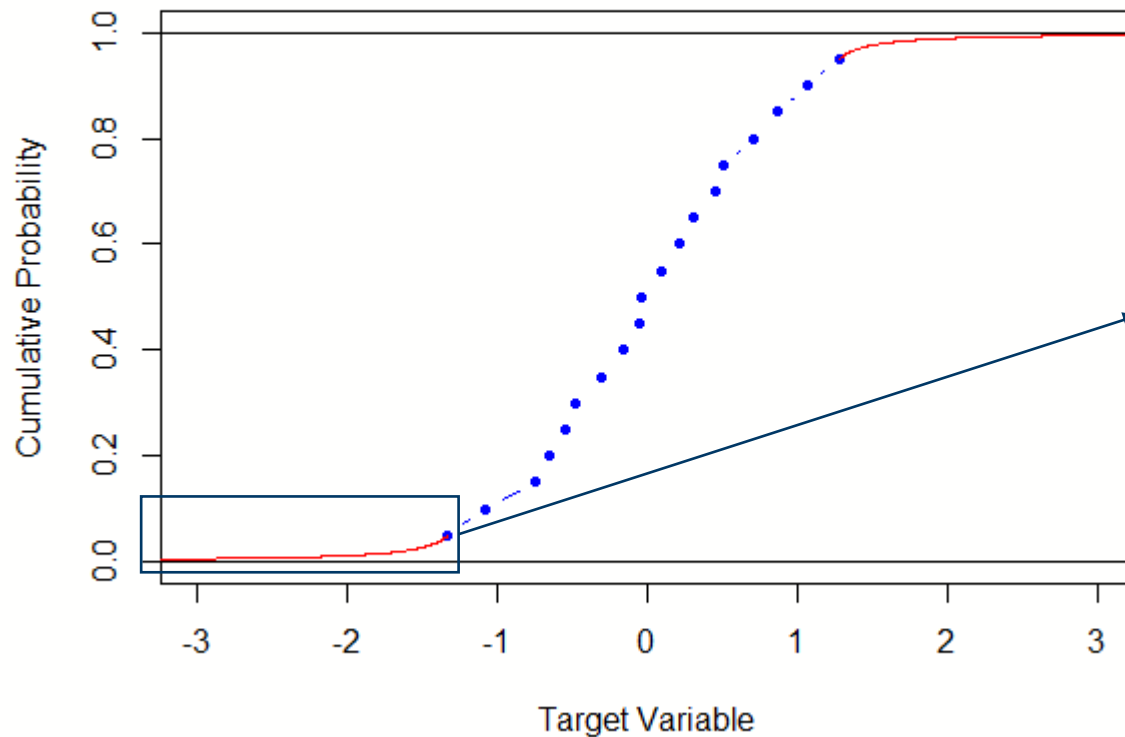


Density Forecasting

GAMLSS Generalised Pareto Tails

Tail Distribution
Conditional
Generalised
Pareto

Predictive Distribution



$$F_{GPD}(\sigma, \xi)$$

Scale:

$$\log(\sigma) = X_1\beta_1 + \sum_j^{J_1} f_{j1}(x_1)$$

Shape:

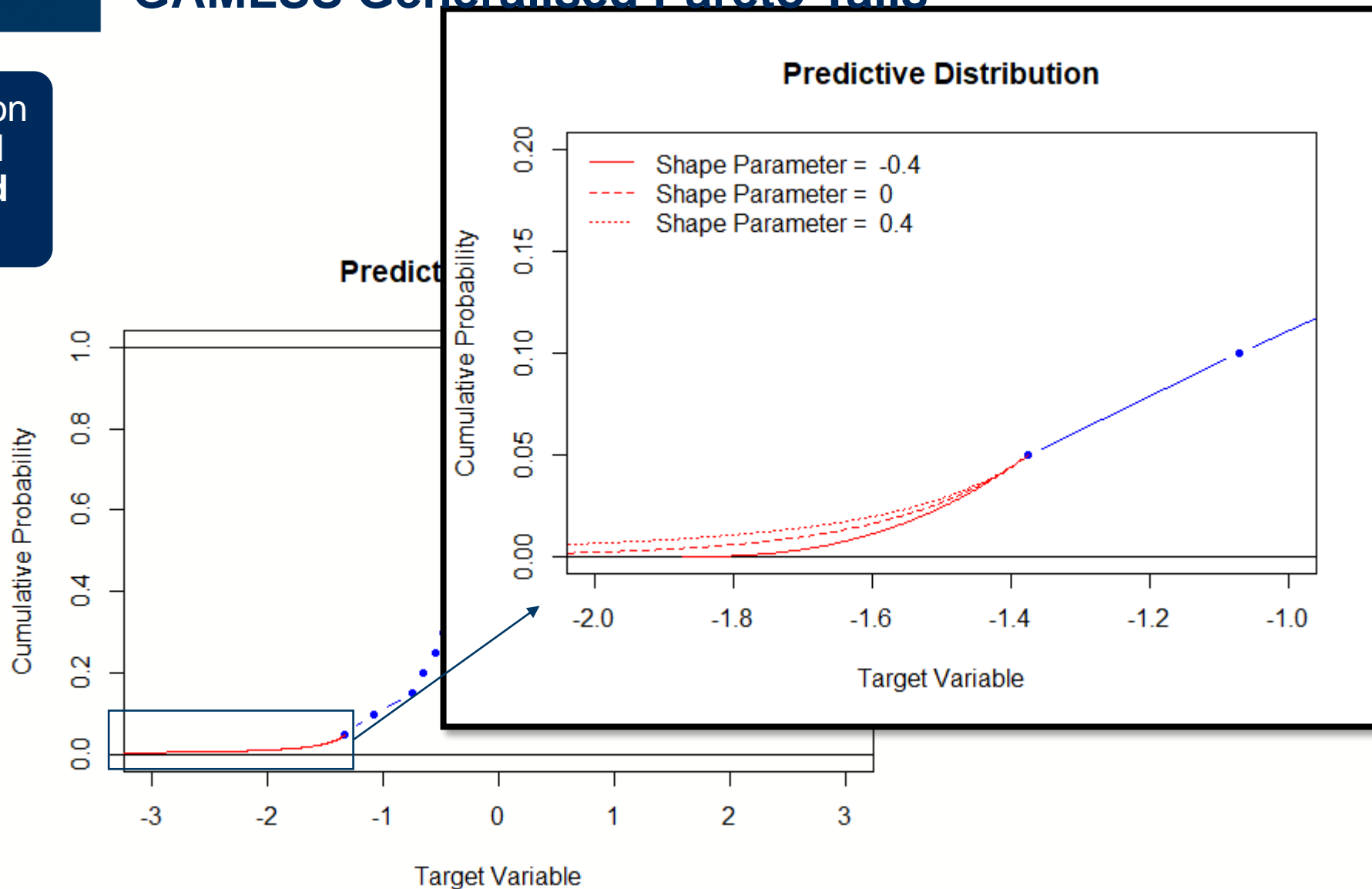
$$\xi = X_2\beta_2 + \sum_j^{J_2} f_{j2}(x_2)$$



Density Forecasting

GAMLSS Generalised Pareto Tails

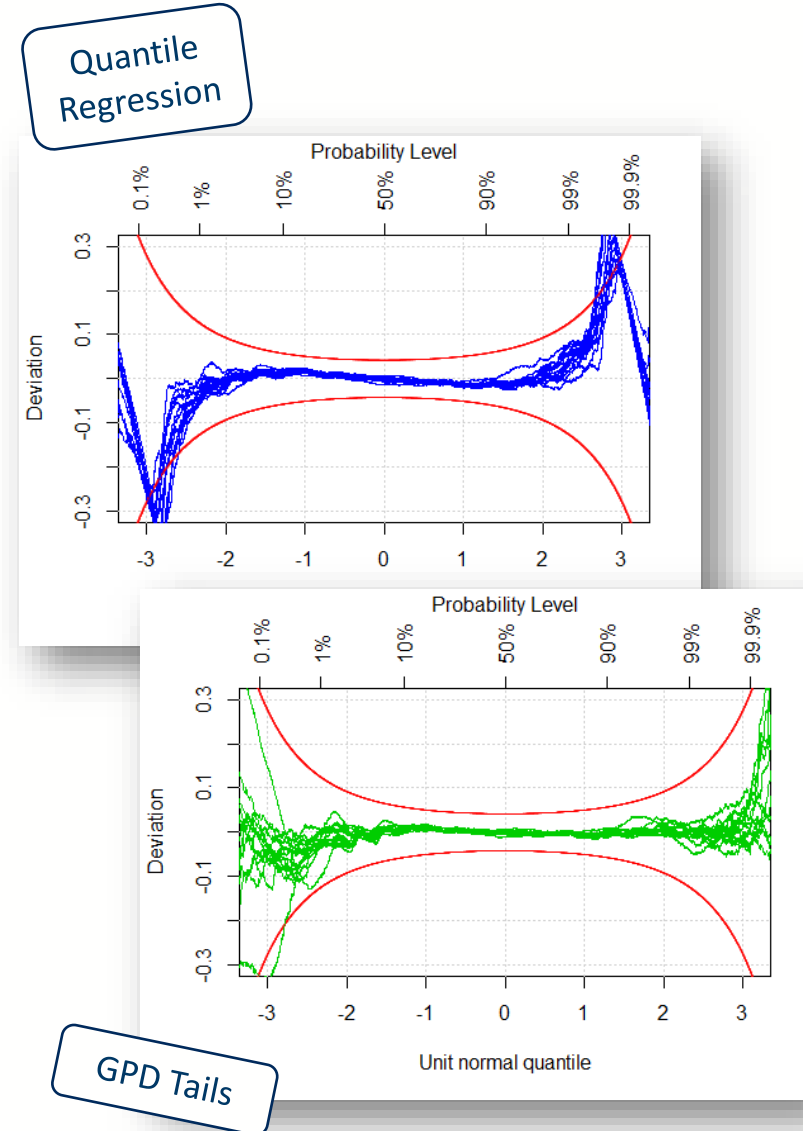
Tail Distribution
Conditional
Generalised
Pareto





Density Forecasting Case Study: Results

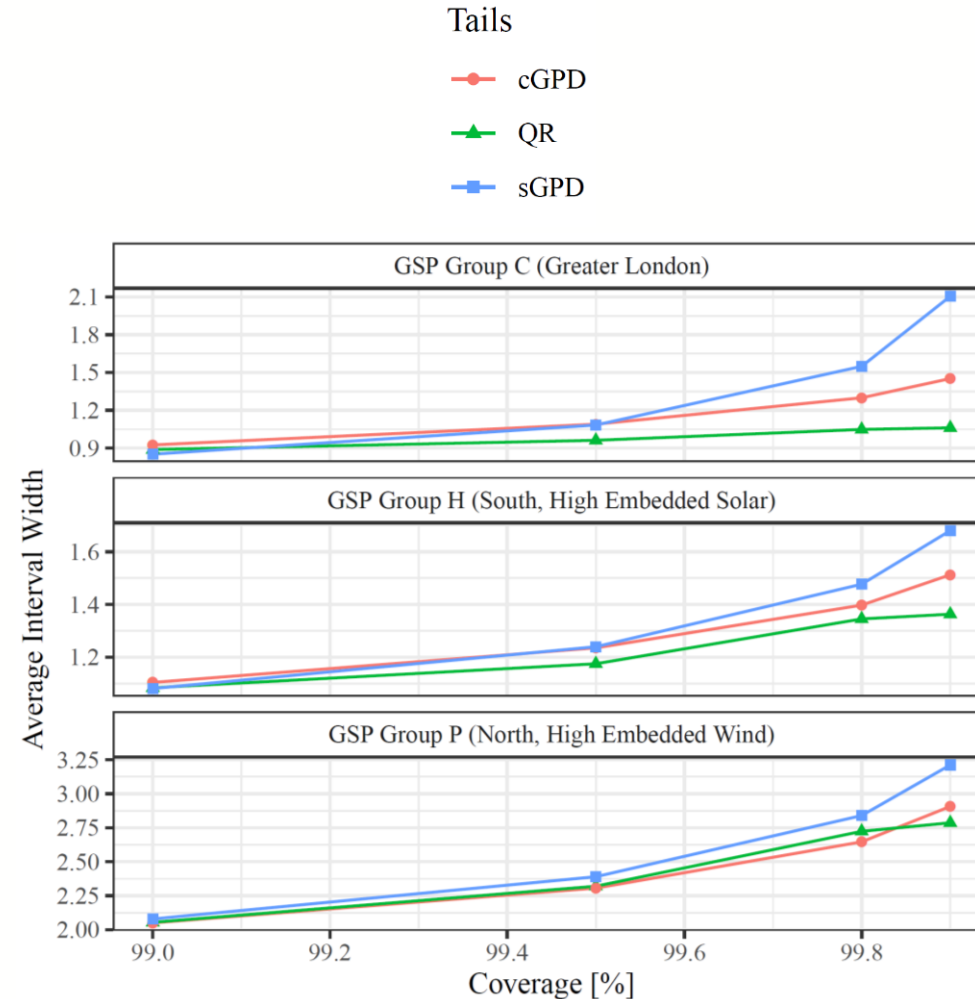
- Tails are challenging to evaluate:
 - not much data
 - poor discrimination by usual metrics
- Worm plot:
 - Shows quantile bias
 - 95% consistency band considering serial correlation
- Quantile regression vs GPD:
 - QR tails uncalibrated, too sharp/over-confident
 - GPD tails calibrated, sharpness can be improved by conditioning on covariates





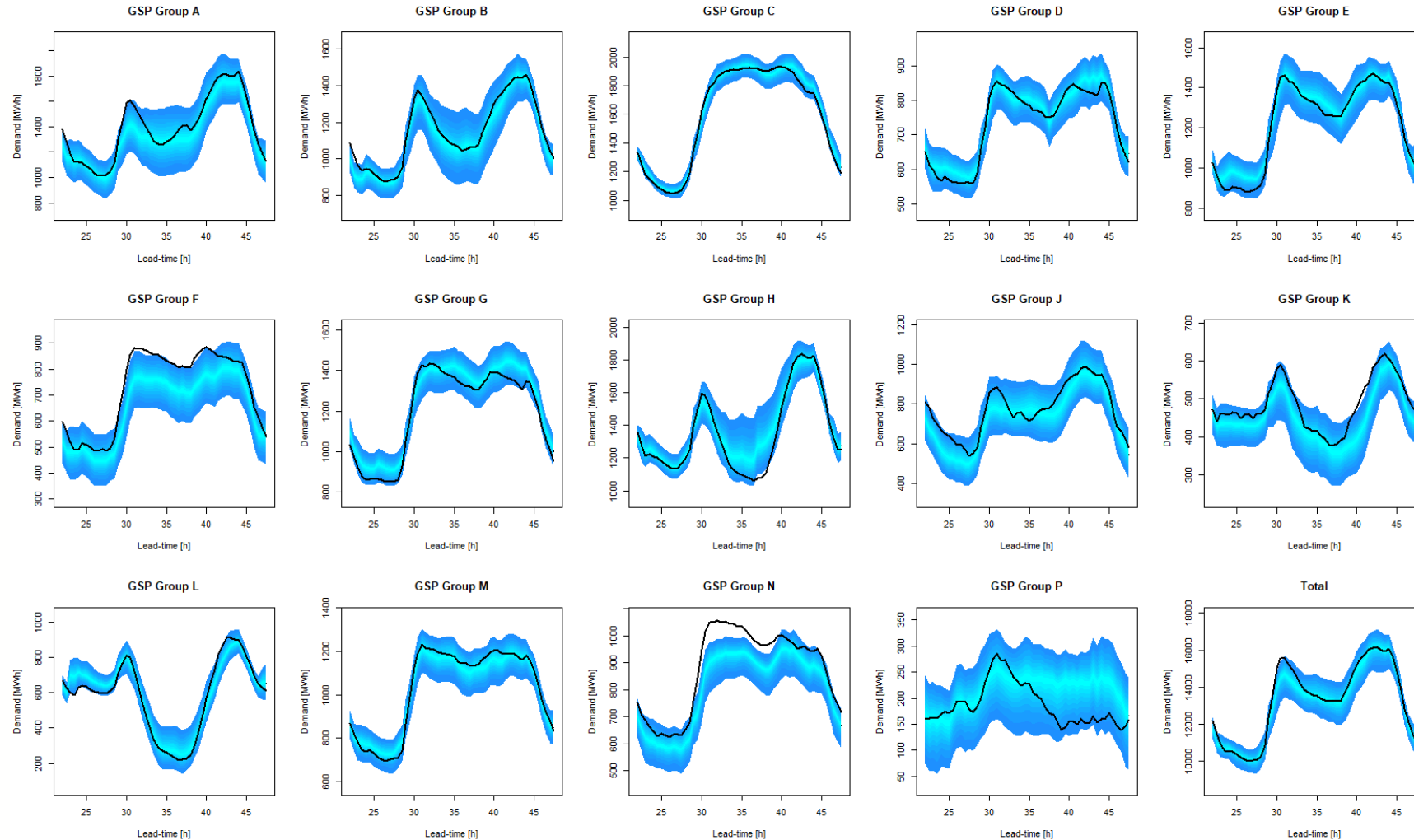
Density Forecasting Case Study: Results

- **Sharpness** = average interval width
- **Quantile Regression** not calibrated → throw out
- **Conditional GPD** much sharper than **Static GPD**
- Sharper intervals → less uncertainty → *better* decisions?





Density Forecasts





Use-case: Reserve setting

- Reserve energy required in case:
 - Power plant fails
 - Market fails to deliver
 - Forecast is “*wrong*”
- How much to buy?
 - Risk appetite/policy
 - Cost-Loss: marginal cost of more reserve vs loss if reserve is insufficient

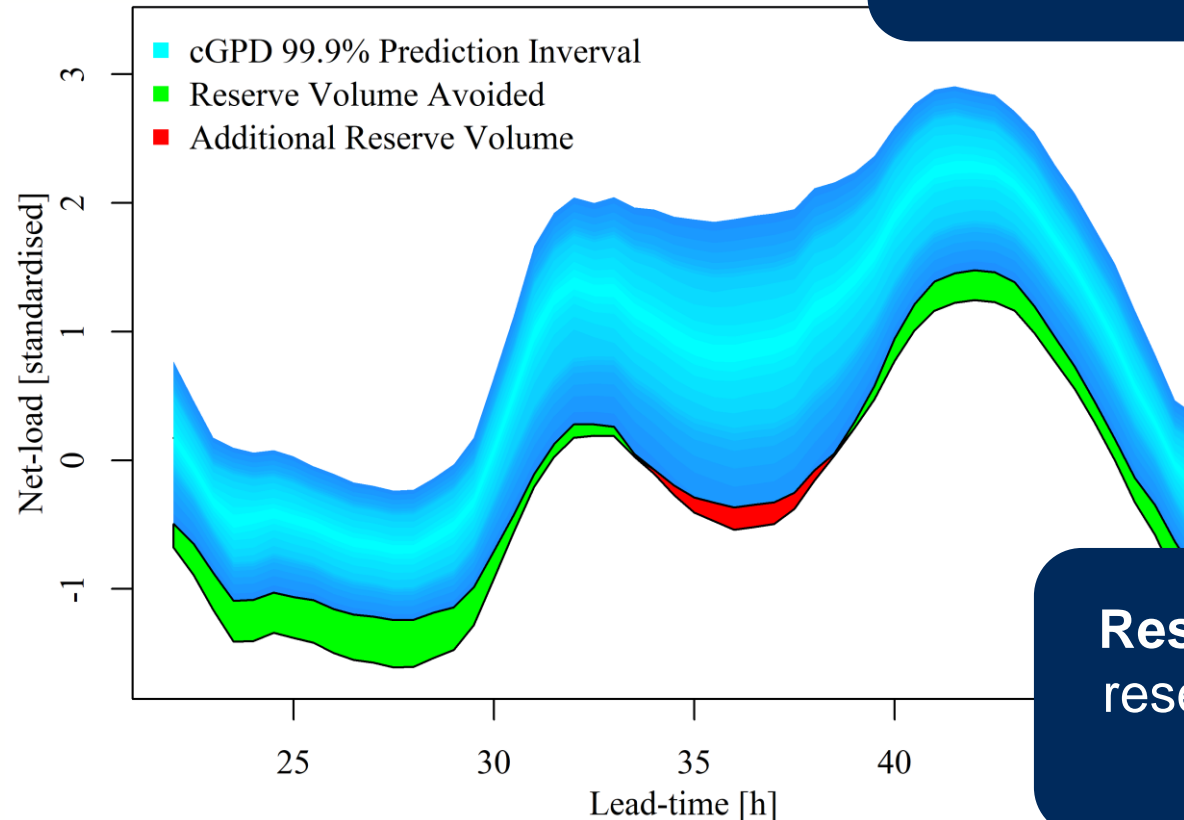
Benchmark: empirical
quantile of historic
deterministic forecast
errors

Here: conditional quantile
of density forecast

$\alpha = 0.25\%$ to 0.01%



Use-case: Reserve setting



Sometimes (~25%) we need **more** reserve than benchmark to satisfy risk appetite

Mostly we can hold **less** reserve than benchmark

Result: overall reduction in reserve holding, preferable risk profile



Probabilistic Forecasting of Regional Net-load with Conditional Extremes

Summary:

1. Wind and solar weather features are essential to capture embedded generation in net-load forecasting, including in tails (*not shown today*)
2. Generalised Pareto Distribution tails provide reliable extreme quantiles where quantile regression fails
3. Forecasting extreme quantiles reveals opportunities to reduce risk and save consumers £££!



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High-dimensional wind power forecasting

Work with Ciaran Gilbert

C. Gilbert, “Topics in high-dimensional energy forecasting”, PhD Thesis, University of Strathclyde, 2021, online: <https://stax.strath.ac.uk/concern/theses/9306sz801>



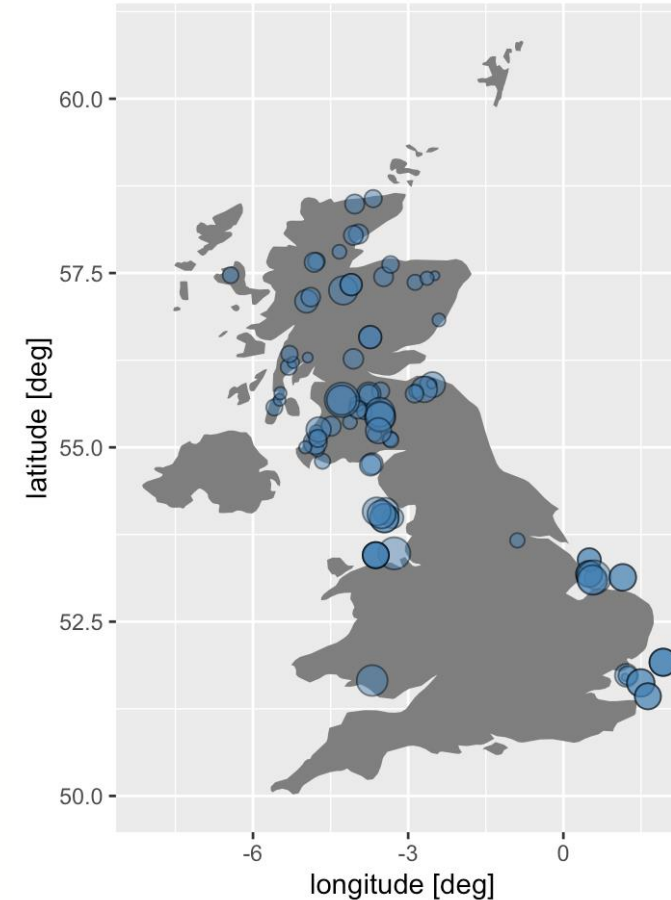
CG PhD Studentship
EPSRC



Spatio-temporal dependency

Motivation

- Spatial dependency:
 - Portfolio effects
 - Power flow & constraints
- Temporal dependency:
 - Trading block products
 - Ramps
 - Storage and plant run times





Spatio-temporal dependency

Case study

- 92 Wind Balancing Mechanism Units
- Density forecasting: 92 units \times 27 quantiles \times 5 cv-folds = 12,420 models to fit!
- Implemented using *ProbCast* on AWS

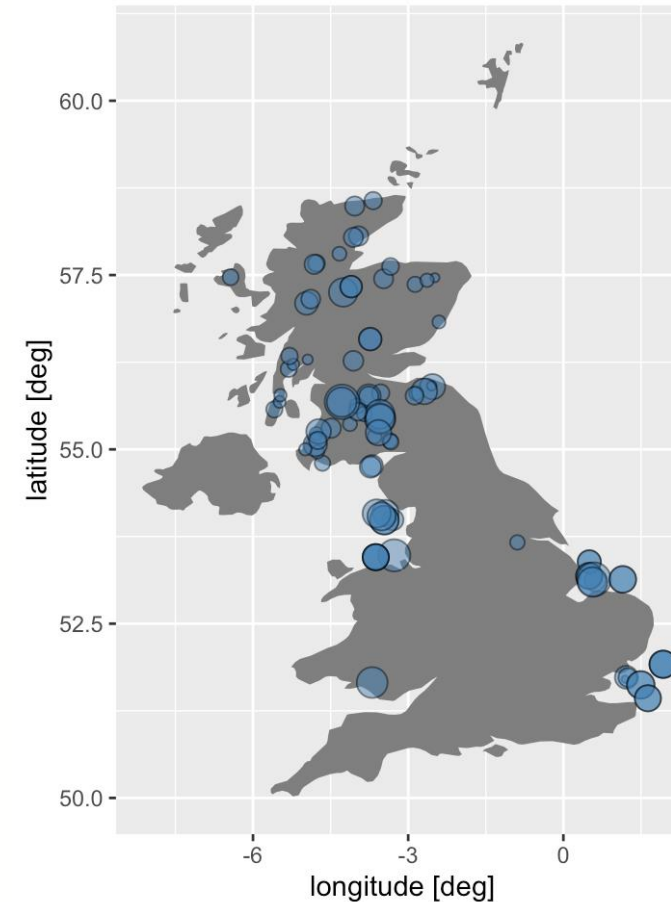
Density
Forecast:
GBT



Tail
Distribution:
Exponential



Dependency
Structure:
**Gaussian
Copula**

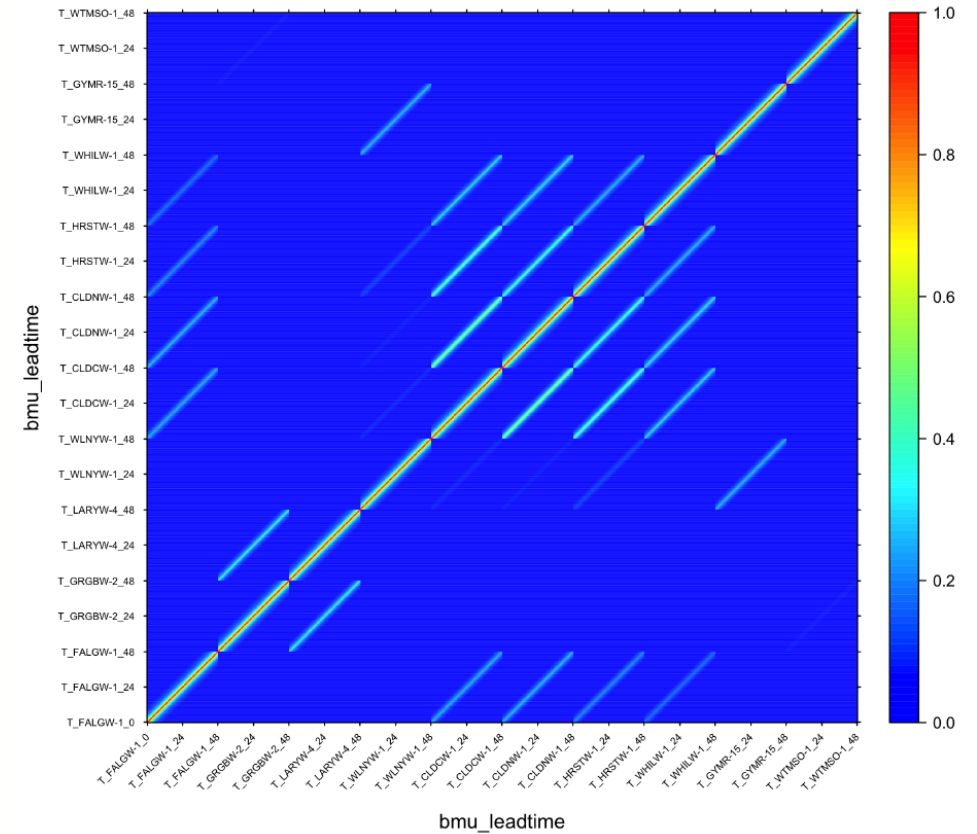




Spatio-temporal dependency

Dependency
Structure:
**Gaussian
Copula**

- Very large covariance matrix!
Parametrisation necessary
 - Cauchy for temporal
 - Exponential for spatial
 - Interaction (non-separable)
- Probably dynamic!
 - Regime-switching?
 - Dependence on covariate?



$$\Sigma_{(k,t),(k',t')} = \frac{1-\nu}{1+a|\delta t|^{2\tau_t}} \left[\exp \left(-\frac{|\delta k|}{\tau_k(1+a|\delta t|^{2\tau_t})^{\beta/2}} \right) + \frac{\nu}{1-\nu} \mathbf{1}(|\delta k|=0) \right]$$



Dynamic spatio-temporal dependency

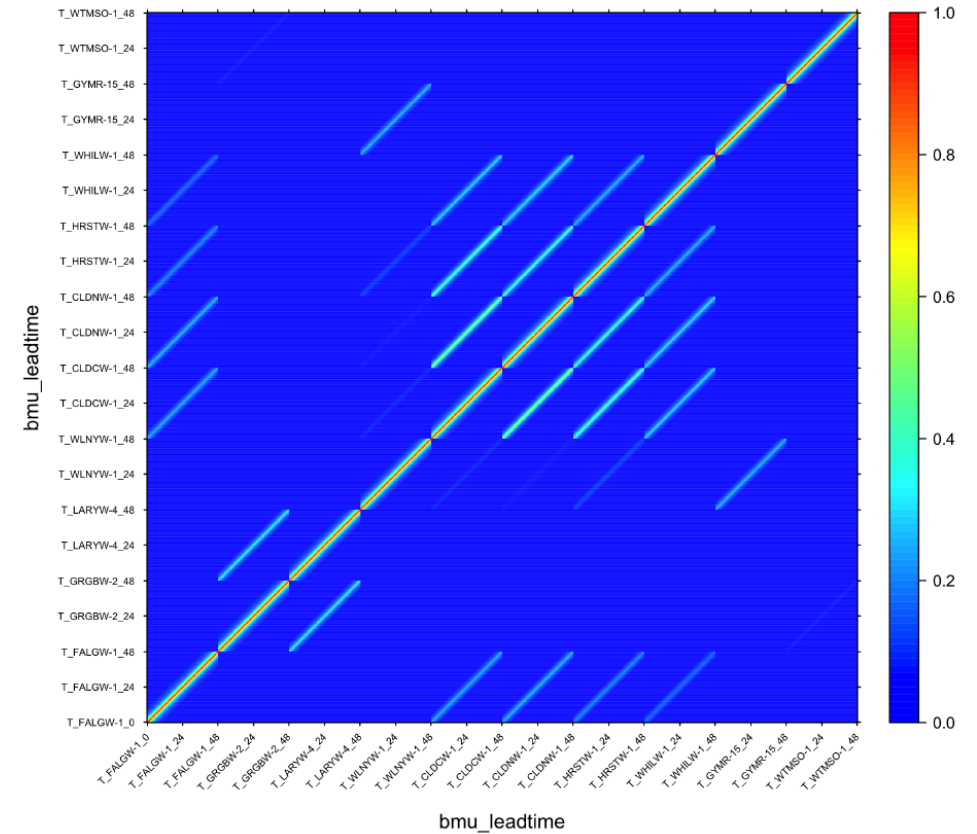
Dependency
Structure:
Gaussian
Copula

Regime-switching:

- Estimating separate parameters based on weather regime
- Signs of benefit, but inconclusive

Parameters as functions of covariates:

- Enables more flexible structures
- Explicit time-dependency rather than adaptive updates
- First results to be presented in June. Pre-print of accepted article now online



$$\Sigma_{(k,t),(k',t')} = \frac{1-\nu}{1+a|\delta t|^{2\tau_t}} \left[\exp \left(-\frac{|\delta k|}{\tau_k(1+a|\delta t|^{2\tau_t})^{\beta/2}} \right) + \frac{\nu}{1-\nu} \mathbf{1}(|\delta k| = 0) \right]$$



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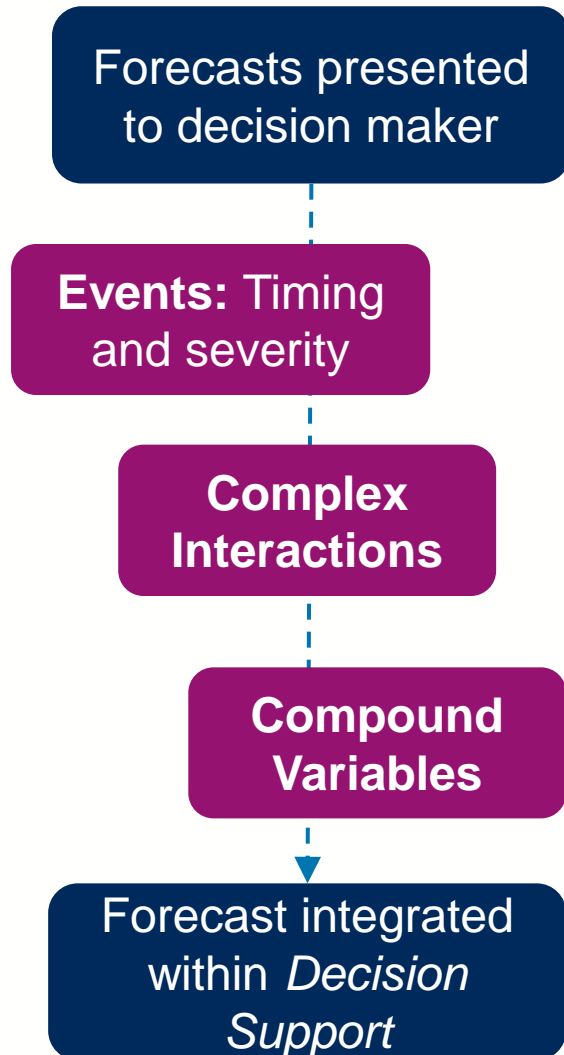
A vision for energy forecasting

Ambitions beyond “better forecasts”





What do we want to predict anyway?



- **Energy:** Blocks of energy for trading and generator scheduling, risk/reserve requirements
- **Power:** ramps for balancing; instantaneous power for ancillary services, reactive power
- **Interdependency with markets:** risk management, algorithmic trading, embedded flexibility
- **Network flows/constraints:** probability of constraint, regional balancing, TSO/DSO flow



Opportunities: data-rich environment!

Need and opportunities for energy forecasting:

- Critical capability for weather-dependent (weather-led?) energy systems, supporting:
 - Reliability
 - Cost minimisation
 - De-carbonisation!!!
- Massive increase in data coverage and availability:
 - Load monitoring and digitization (controllability and automation)
 - Energy networks: metering and asset health monitoring, small flexible (virtual) power plants
 - Weather data availability and forecast performance

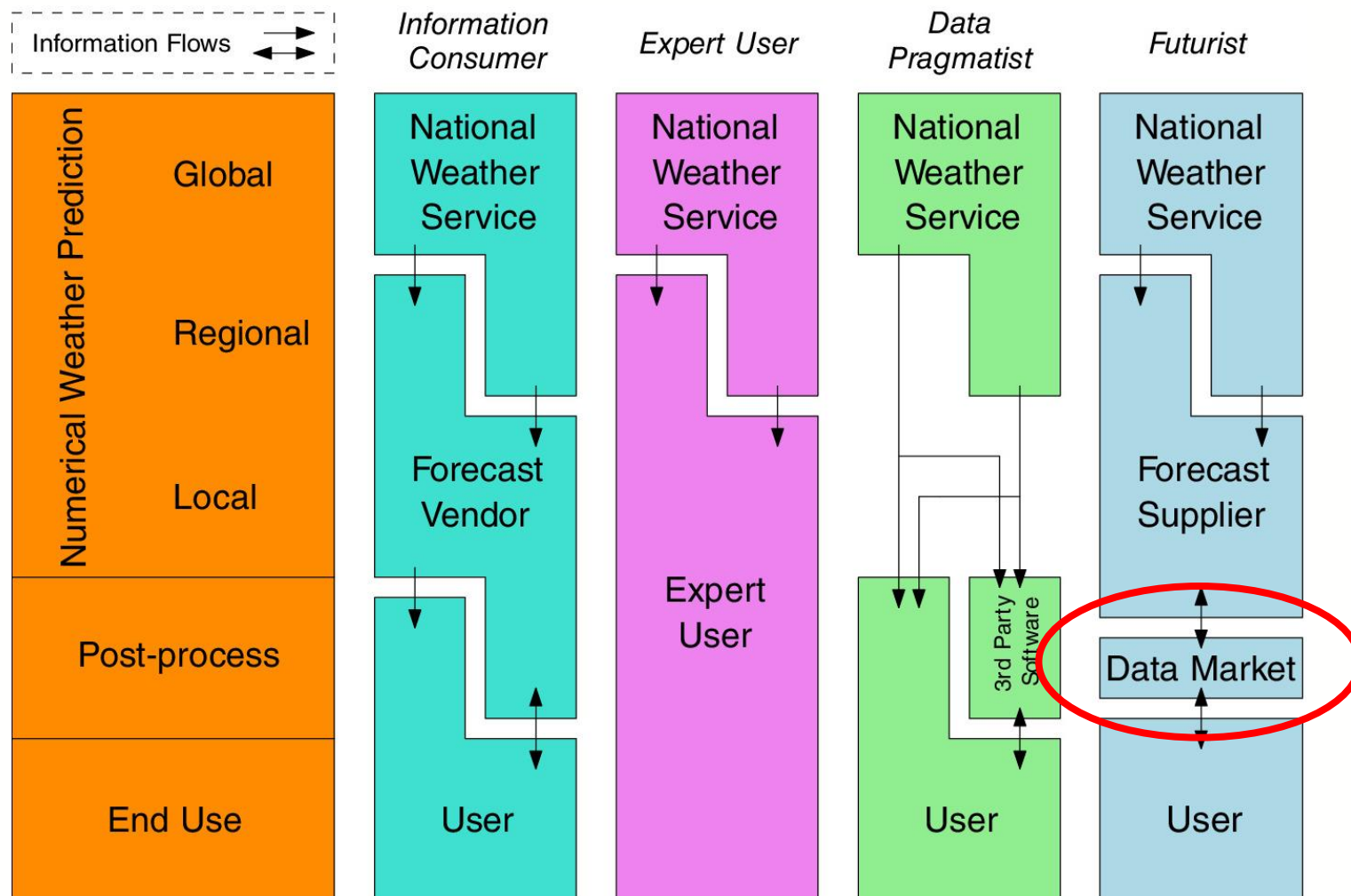
Challenges:

- Data 1: coverage and quality never going to be (even close to) perfect!
- Harmonising physical constraints with non-physical systems (digital, markets)
- Data 2: sharing, privacy, (apparent lack of) commercial incentives
- Converting complex forecast information into decisions
- Coherent exchange of forecasts and other data (e.g. TSO-DSO interface)

Fundamental
challenges, not simply
an IT problem!



The future of energy forecasting?



What do we need from this information exchange?

- “Full” probabilistic forecasts?
- Partial forecasts?
- Covariates?
- Coherence with other data

Decision-centric views:

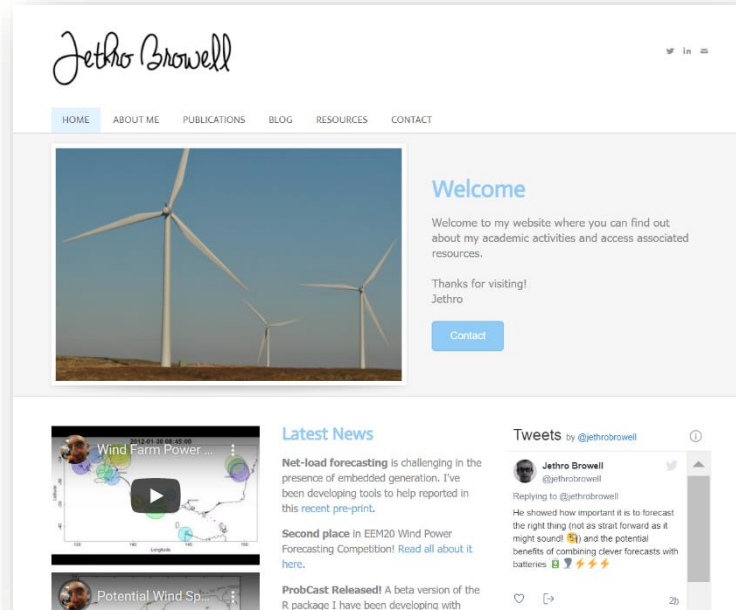
1. Retain “full” information, collapse to only what is required for use:
 - Coherence across all data and forecasts...
 - BUT we lack a parsimonious mathematical framework.
2. Avoid explicit forecasting completely using reinforcement learning...



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Thanks!

Papers, code etc. linked from www.jethrobrowell.com



Methodologies available in ProbCast – *User feedback welcome!!*

<https://github.com/jbrowell/ProbCast>

```
R>>> devtools::install_github("jbrowell/ProbCast")
```





References

Today:

- J. Browell and M. Fasiolo, "Probabilistic Forecasting of regional net-load with conditional extremes and gridded NWP", IEEE Transactions on Smart Grid, vol. 12, no. 6, pp. 5011-5019, Nov 2021, <https://doi.org/10.1109/TSG.2021.3107159>
- C. Gilbert, "Topics in high-dimensional energy forecasting", PhD Thesis, University of Strathclyde, 2021, online: <https://stax.strath.ac.uk/concern/theses/9306sz801>
- J. Browell, C. Gilbert and M. Fasiolo, "Covariance Structures for High-dimensional Energy Forecasting", Electric Power Systems Research (Special Issue for PSCC 2022), 2022, (preprint at www.jethrobrowell.com)
- C. Sweeney, R.J. Bessa, J. Browell and P. Pinson, "The Future of Forecasting for Renewable Energy," WIREs Energy and Environment, vol. 9, no. 2, 2020, <https://doi.org/10.1002/wene.365>

Other outputs from *System-wide probabilistic energy forecasting*:

- J. Browell and C. Gilbert, "Predicting electricity imbalance prices and volumes: capability and opportunity", Energies, 15(10), 3645, 2022, <https://doi.org/10.3390/en15103645>
- M. Farrokhabadi, J. Browell, Y. Wang, S. Makonin, W. Su, and H. Zareipour, "Day-Ahead Electricity Demand Forecasting Competition: Post-COVID Paradigm", IEEE Open Access Journal of Power and Energy, 2022, <https://doi.org/10.1109/OAJPE.2022.3161101>
- R.M. Graham, J. Browell, D. Bertram and C.J. White, "The application of sub-seasonal to seasonal (S2S) predictions for hydropower forecasting", Meteorological Applications, 29(1), e2047, 2022, <https://doi.org/10.1002/MET.2047>
- E. Heylen, J. Browell and F. Teng, "Probabilistic day-ahead inertia forecasting", IEEE Transactions on Power Systems, <https://doi.org/10.1109/TPWRS.2021.3134811>
- R. Telford, B. Stephen, J Browell and S. Haben, "Dirichlet Sampled Capacity and Loss Estimation for LV Distribution Networks with Partial Observability", IEEE Transaction on Power Delivery, vol. 36, no. 5, pp. 2676-2686, Oct. 2021, <http://www.doi.org/10.1109/TPWRD.2020.3025125>

Q&A

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