

ESM232- HW7

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Rabbits & Hawks, Assignment 7:

A small city with a large urban park has decided to introduce a rare species of rabbits into this park - Rabbits are cute and the kids love them, and giving a rare species a new home sounds like a good idea. The urban park manager is concerned about how this rabbit population might grow over the next few decades. Rabbits have no natural predators in the region where the park is situated. The manager would like to know, approximately, how many rabbits there will be 20 years from now if the rabbits are introduced as planned. The manager reviewed the literature and found the following estimates for survival and fertility rates for the rare rabbit population, for 4 different age classes. The estimates for these rates are shown below:

Fertility (rabbit/female)

- Young (age 0-1): 0
- Sub-Adults (age 1-2): 2
- Adult (age 2-3): 6
- Aged (age 3-4): 1

Survivability (male and female)

- Young (age 0-1): 0.8
- Sub-Adults (age 1-2): 0.85
- Adult (age 2-3): 0.65
- Aged (age 3-4): 0.1

Part 1

Using a matrix population model approach answer the following questions for the manager:

Assume that we start with 10 adult rabbits. (group 3)

What is the total rabbit population after 20 years?

How many young rabbits (first age class) are there in the population at that time?

```
fert = c(0/2,2/2,6/2,1/2) #divide fertility (just for females) by 2
surv=c(0.8,0.85, 0.65, 0.1) #survivability

source("R/evolve_pop.R")
evolve_pop
```

```

## function (fertility, survivability, initialpop, nstep)
## {
##   nclasses = length(fertility)
##   if ((nclasses != length(survivability))) {
##     return(sprintf("fertility %d doesnâ\200\231t match survivability %d",
##       nclasses, length(survivability)))
##   }
##   if ((nclasses != length(initialpop))) {
##     return(sprintf("population initialization %d doesnâ\200\231t match fertility %d ",
##       length(initialpop), length(fertility)))
##   }
##   leslie_matrix = matrix(nrow = nclasses, ncol = nclasses)
##   leslie_matrix[, ] = 0
##   leslie_matrix[1, ] = fertility
##   for (i in 1:(nclasses - 1)) {
##     leslie_matrix[i + 1, i] = survivability[i]
##   }
##   leslie_matrix[nclasses, nclasses] = survivability[nclasses]
##   pop_structure = matrix(nrow = nclasses, ncol = nstep)
##   total_pop = rep(0, times = nstep)
##   pop_structure[, 1] = initialpop
##   total_pop[1] = sum(initialpop)
##   for (i in 2:nstep) {
##     pop_structure[, i] = leslie_matrix %*% pop_structure[,
##       i - 1]
##     total_pop[i] = sum(pop_structure[, i])
##   }
##   return(list(popbyage = pop_structure, poptot = total_pop))
## }

```

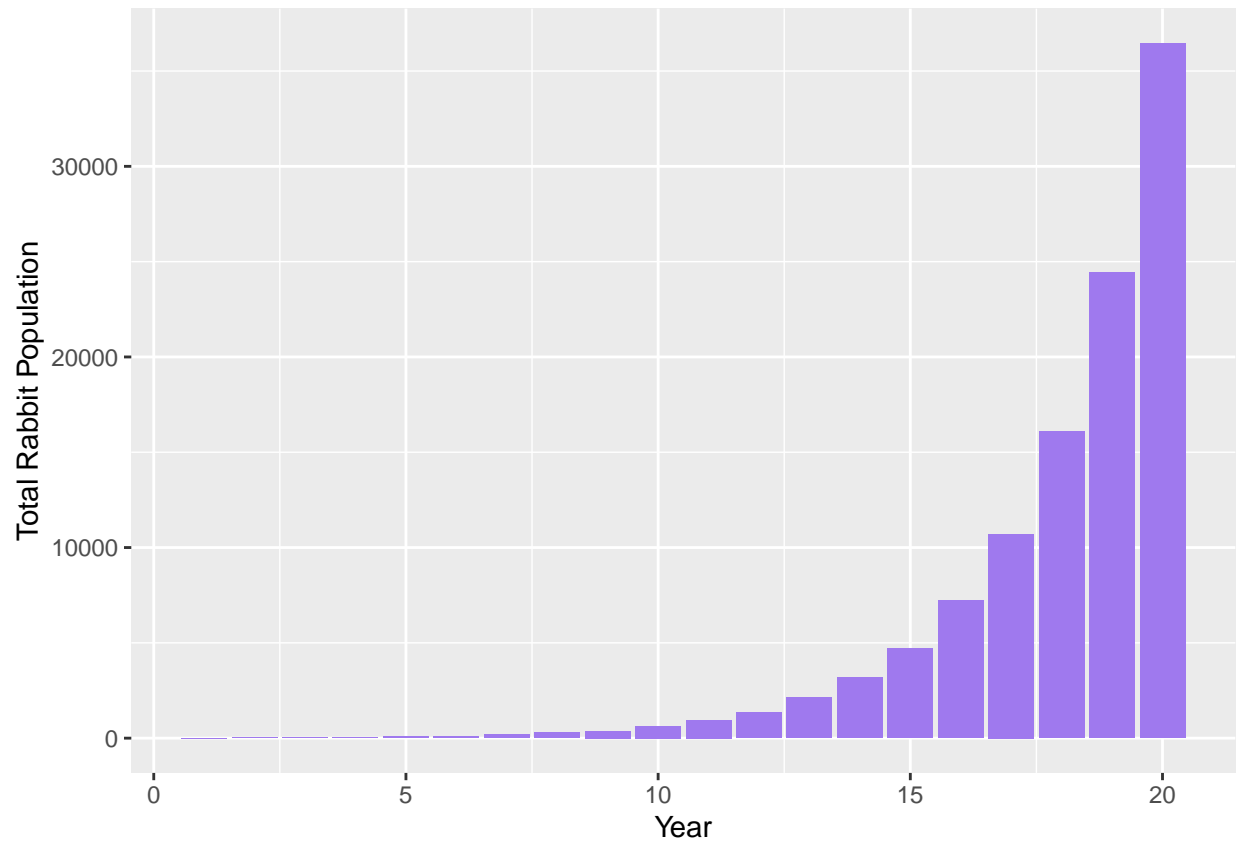
```

ini = c(0,0,10,0) #start with 10 adult rabbits
nyr=20 #number of years to run
rabbit_pop=evolve_pop(fert, surv, ini, nyr) #run evolve_pop.R

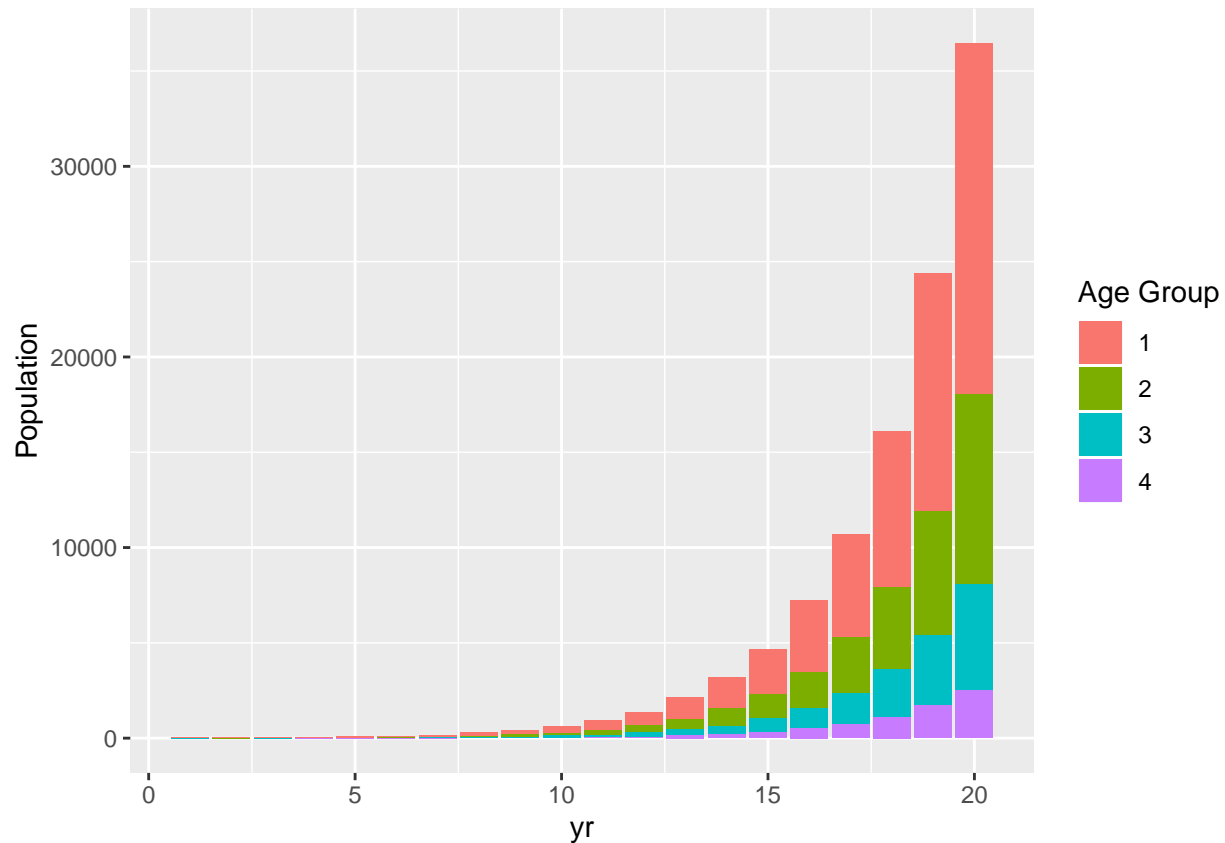
# note: from the code from class, the rabbit_pop at t=1 was giving 0 instead of 10,
#so I had to account for this in lines 57 and 62 when creating the dataframes

yr = seq(from=1, to=nyr) #sequence of years
rabbit_tot = cbind.data.frame(yr=yr, poptot=(rabbit_pop$poptot))
ggplot(rabbit_tot, aes(yr, poptot))+
  geom_col(fill="mediumpurple2")+
  labs(y="Total Rabbit Population", x="Year")

```



```
# plot information about ages
rabbit_ages = cbind.data.frame(yr=yr, t(rabbit_pop$popbyage))
rabbit_ages1 = rabbit_ages %>%
  gather(key="agecat", value="pop",-yr)
ggplot(rabbit_ages1, aes(yr, pop, fill=agecat))+
  geom_col()+
  labs(y="Population", fill="Age Group")
```



```
#What is the total rabbit population after 20 years?
rabbit_tot$poptot[20]
```

```
## [1] 36452.35
```

```
#How many young rabbits (first age class) are there in the population at that time?
rabbit_ages$1[20]
```

```
## [1] 18371.88
```

Part 2

The park manager is also thinking of ways to keep the population under control - by encouraging nesting of hawks that eat the rabbits.

Hawks generally only eat younger rabbits- thus they reduce the survivability of the young and sub-adults age classes (the first two classes). The estimates are that survivability reduced to between 0.65 and 0.75 for Ages 0-1 and between 0.75 and 0.8 for Ages 1-2. You can assume that distributions are uniform

Perform a sensitivity analysis on the survivability of Young Age and Sub-Adults age class parameters. Use Sobol to generate variation in the survivability parameters. Then for each parameter set, compute total rabbit population after 20 years. Similar to what we did in the agestructure.Rmd in class.

Plot how total rabbit population after 20 years varies with a) survivability of Young Age and b) Young Adult. Also generate a box plot of the variation in total rabbit population. How does this compare with

total rabbit population after 20 years in your original population model (without the hawk related change to survivability)?

```
# survivability of rabbit age classes 1 and 2
p12=0.8
p23=0.85
p34=0.65
p4d=0.1

# fertility
f1=0
f2=1
f3=3
f4=0.5

#number of samples for Sobol parameters
nsample=200

# create our samples for Sobol
sobol_1 = cbind.data.frame(p12=runif(min=0.65, max=0.75, n=nsample),
                           p23 = runif(min=0.75, max=0.8, n=nsample))

sobol_2 = cbind.data.frame(p12=runif(min=0.65, max=0.75, n=nsample),
                           p23 = runif(min=0.75, max=0.8, n=nsample))

# put all survivabilities and fertilities together (is this right)?
allp1 = cbind.data.frame(sobol_1,p34=rep(p34,times=nsample),
                         p4d= rep(p4d,times=nsample), f1=rep(f1,times=nsample),
                         f2= rep(f2,times=nsample),f3=rep(f3,times=nsample),
                         f4= rep(f4,times=nsample))

allp2 = cbind.data.frame(sobol_2,p34=rep(p34,times=nsample),
                         p4d= rep(p4d,times=nsample), f1=rep(f1,times=nsample),
                         f2= rep(f2,times=nsample),f3=rep(f3,times=nsample),
                         f4= rep(f4,times=nsample))

# get Sobol samples
sens_micro=soboljansen(model = NULL, allp1, allp2, nboot = 100)

head(sens_micro$X)
```

```
##      p12      p23  p34 p4d f1 f2 f3  f4
## 1 0.6711828 0.7856477 0.65 0.1  0  1  3 0.5
## 2 0.6943585 0.7883562 0.65 0.1  0  1  3 0.5
## 3 0.6854147 0.7806714 0.65 0.1  0  1  3 0.5
## 4 0.6956049 0.7984675 0.65 0.1  0  1  3 0.5
## 5 0.7458798 0.7590182 0.65 0.1  0  1  3 0.5
## 6 0.6592712 0.7707005 0.65 0.1  0  1  3 0.5
```

```

nsim=nrow(sens_micro$X)

# run model and save what we care about: final population after 20 years
# this is already output by evolve_pop so we don't need a compute_metric function

ini = c(0,0,10,0)
nyears = 20

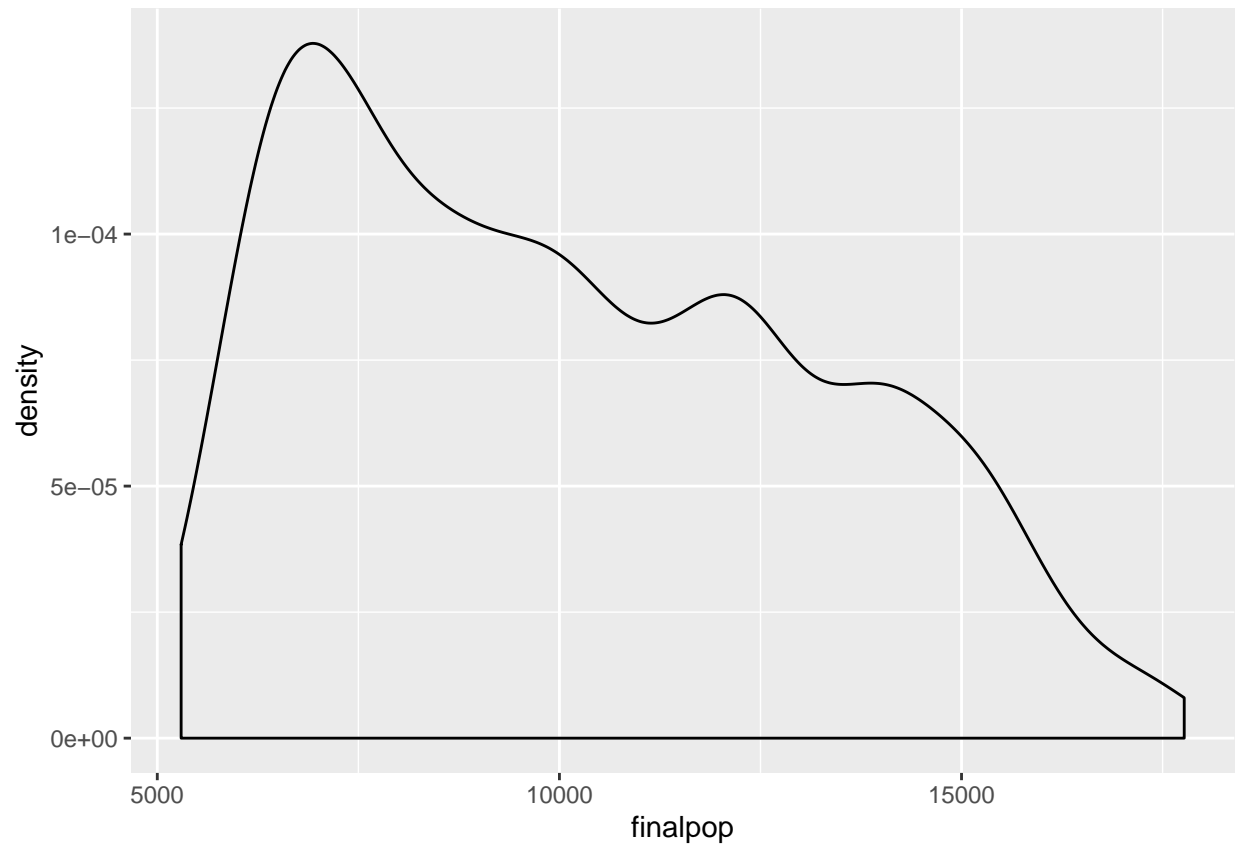
# as before combine our application of the the dynamics model - for each
# parameter set, with code to extract our metric of interest (final population)
p_wrapper = function(p12, p23, p34, p4d, f1,f2,f3, f4, use_func, initialpop, nstep ) {
  fertility=c(f1,f2,f3, f4)
  survivability= c(p12,p23,p34, p4d)
  res = use_func(survivability = survivability, fertility = fertility,
                initialpop=initialpop,
                nstep=nstep)
  # now return the final population total
  return(finalpop=res$poptot[nstep])
}

res = as.data.frame(sens_micro$X) %>% pmap_dbl(p_wrapper, initialpop=ini,
                                              nstep=nyears, use_func=evolve_pop)

# use pmap to specify rows of our sensitivity analysis parameter object
res = as.data.frame(sens_micro$X) %>%
  pmap_dbl(p_wrapper, initialpop=ini, nstep=nyears, use_func=evolve_pop)

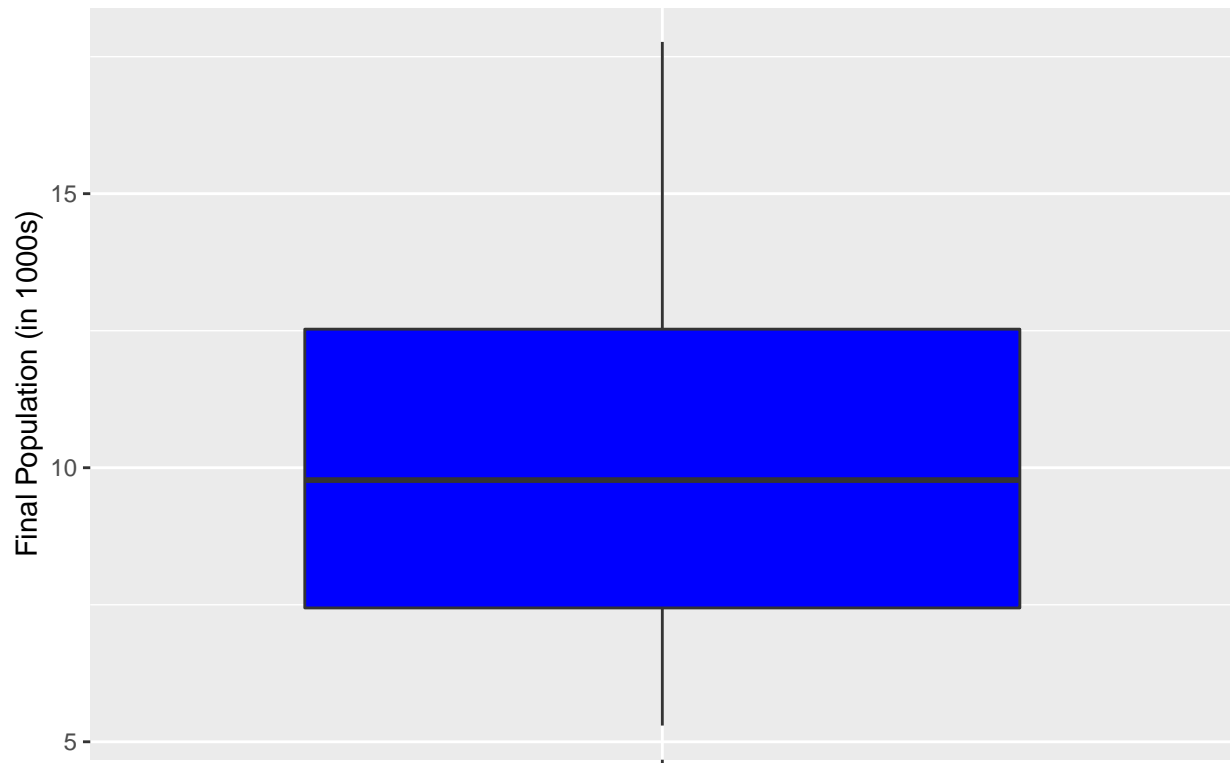
# plot results
ggplot(data.frame(finalpop=res), aes(x=finalpop))+
  geom_density()

```



```
# or a boxplot
ggplot(data.frame(finalpop=res), aes(x="", y=finalpop/1000) )+
  geom_boxplot(fill="blue")+
  theme(axis.title.x = element_blank())+
  labs(y="Final Population (in 1000s)")+
  labs(title = "Rabbit Population After 20 Years, With Hawks Introduced")
```

Rabbit Population After 20 Years, With Hawks Introduced



```
# give results to sensitivity structure
```

```
sens_micro=tell(sens_micro, res)
```

```
# results
```

```
sens_micro$S[1:2,]
```

```
##          original          bias std. error min. c.i. max. c.i.
## p12  0.93599330 -0.001099614 0.008602403  0.9201157 0.9570432
## p23 -0.01803952 -0.010206391 0.077679321 -0.1757174 0.1414926
```

```
sens_micro$T[1:2,]
```

```
##          original          bias std. error min. c.i. max. c.i.
## p12  1.00302129 0.007901879 0.076702079 0.83285205 1.15751049
## p23  0.06498773 0.001721431 0.008406981 0.04401255 0.07927491
```

```
# graph sensitive parameter
```

```
tmp = cbind.data.frame(sens_micro$X, pop20=sens_micro$y)
```

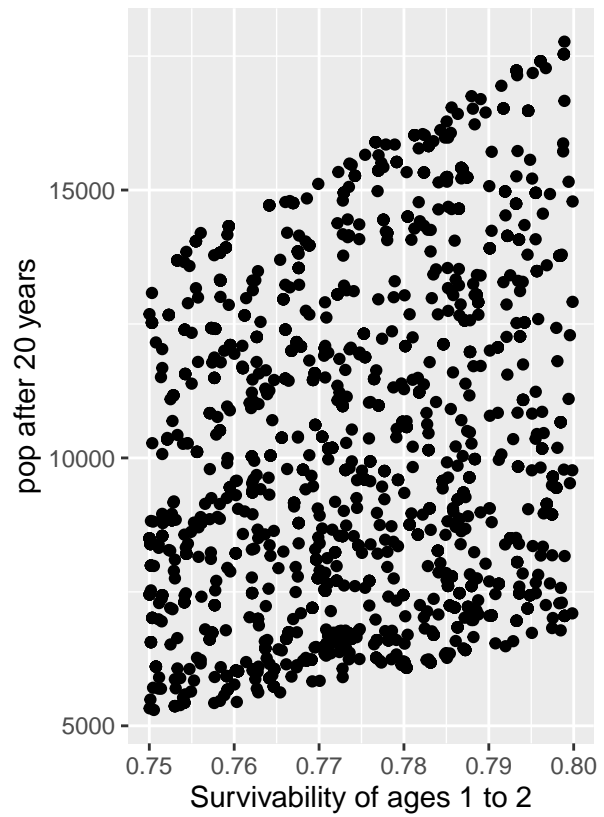
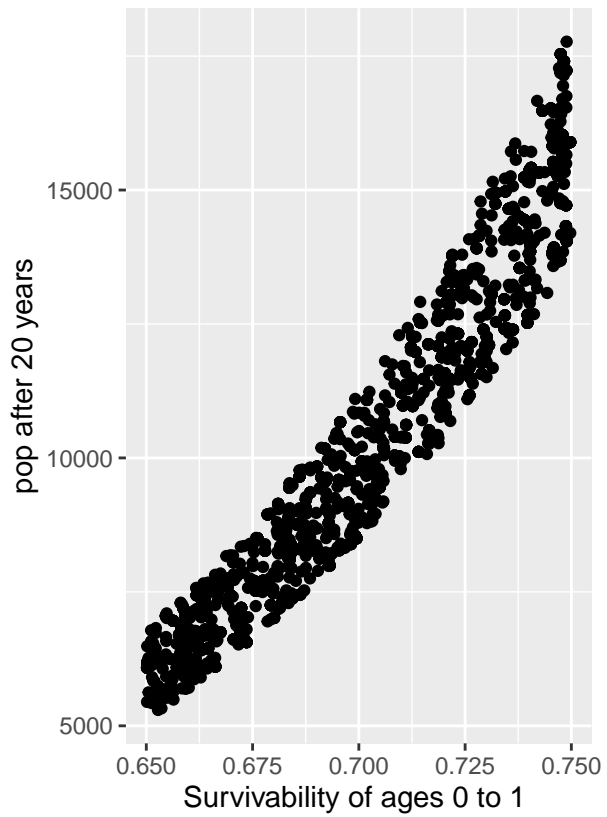
```
# graph for young (age 0-1)
```

```
p1 <- ggplot(tmp, aes(p12, pop20))+
  geom_point()+
  labs(x="Survivability of ages 0 to 1 ",y="pop after 20 years")
```

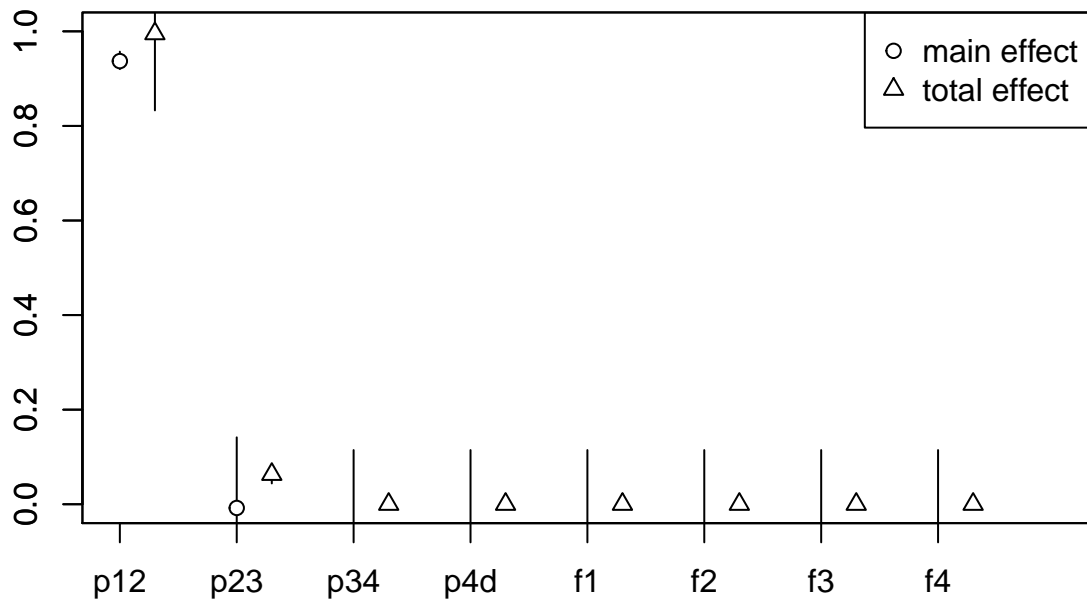


```
# graph for sub-adults (age 1-2)
p2 <- ggplot(tmp, aes(p23, pop20))+
  geom_point()+
  labs(x="Survivability of ages 1 to 2",y="pop after 20 years")

p3 <- p1 +p2
p3
```



```
plot(sens_micro)
```



The total rabbit population in the original population model without the hawk is 36452, but with the hawks ranges from 5325 to 17718, with a mean of 10362. The mean without the hawk is about 3.5 times lower with the hawk.