
Solve-MOND-MM

Release e

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Nov 05, 2020

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FOLDER STRUCTURE

Here is the folder structure of the code:

```
.
├── bin
├── gravity
│   ├── commons_multigrid
│   ├── mond_mass
│   └── newton
│       └── fft_solver
├── grid
├── libs
├── pm
├── tests
└── time_evolution
```

Details:

- `bin` contains the Makefile
- `gravity` contains the gravity solvers.
- `gravity/commons_multigrid` support routines for multigrid solvers which do not depend on the model.
- `gravity/mond_mass` contains the multigrid solver for the model we are dealing with (MOND with mass terms).
- `gravity/newton` contains an FFT based solver for Poisson's equation (needed for standard simulations).
- `grid` all routines related to the grid including allocation routines and initialization of the FFTW variables.
- `libs` miscellaneous including cosmology, utility files for allocating 3D arrays and routines for reading parameter files.
- `pm` (particle mesh). Everything related to the particles at their connection to the grid. Here we allocate memory for particles and transfer information from the particles through the grid (for calculating density in the grid) and viceversa (for calculating force in the particles).
- `tests` has routines for testing. Here you can find the routines for the spherical test.
- `time_evolution` contains the main time loop.

DATA STRUCTURE

We have the following structures defined in the code:

- **params**: defined in `solve.h`. It contains input parameters and some physical constants (including expansion factor).
- **parts**: defined in `pm/init_parts.h`. It contains particles' positions and velocities, which are allocated in `pm/init_parts.c`
- **grids**: defined in `grid/init_grid.h`. It contains all the fields and space for doing FFTs. Everything is allocated in `grid/init_grid.h`. Note that there are additional grids allocated by the multigrid solver.
- **grids_gravity_mm**: defined in `gravity/mond_mass/solve_multigrid_mm.h`. It contains everything related to the MOND-MM multigrid solver (including the coarse grids, which are allocated in `gravity/mond_mass/solve_multigrid_mm.c`).

Detailed definitions follow:

type params

Structure with input parameters and fields

double **H0**

double **a**

Expansion factor.

double **box**

Mpc/h and then converted to Mpc in `init_physics`.

double **cte_poisson**

char [1000] **file_in_parts**

char [1000] **file_out**

int **gravity**

0 -> Newton 1 -> MOND with mass term.

int **grid**

Grid size (the code is not tested with this number being different than the number of particles).

int **grid_p**

Grid of particles (cubic root of total number of particles).

double **hsmall**

double **mm_KB**

MOND constant.

double **mm_M**

MOND mass in h/Mpc and converted to 1/Mpc.

```
double mm_a0
    MOND a0 in km/sec^2 and converted to Mpc/Gyr^2.

int n_outputs

int nparts
    Total number of particles.

int nsteps
    Number of time steps.

int nthreads
    Number of threads. (interesting only if OPENMP).

double omega1

double omegam

int static_test

double [1000] t_of_a

int verbose

int verbose_mm

int verbose_mm_coarse

double z_end

double z_init

type particles

    double *pos_1
    double *pos_2
    double *pos_3
    double *vel_1
    double *vel_2
    double *vel_3

type grids

    double ***chi_bar_mm
    fftw_complex *data
    double ***delta
    double ***force_1
    double ***force_2
    double ***force_3
    double ***force_chi_bar_mm_1
    double ***force_chi_bar_mm_2
    double ***force_chi_bar_mm_3
    double ***force_phi_bar_mm_1
```



```

double ***force_phi_bar_mm_2
double ***force_phi_bar_mm_3
fftw_plan p_backward
fftw_plan p_forward
double ***phi
double ***phi_bar_mm
double ***source

```

type grids_gravity_mm

Main data structure of the multigrid solver.

Comments:

- Note that here we have a copy of the main parameters of the code. That is to avoid having to accessing too many structures in some of the loops in the solver.

```

double KB
    MOND parameter KB

double a2M2
    MOND parameter  $M^2$  (multiplied by  $a^2$ ).

double aa0
    MOND parameter  $a_0$ 

double ***chi[20]
    Solution for the MOND equation ( ).

double cte_poisson_over_a

double fourh[20]
    This one is optimization

int g
    Grid in which we are working. 0 = finest (so what people call V cycle, is actually a Lambda).

double h[20]
    Spacing of each grid.

int n[20]
    Size of each grid.

int num_grids
    Number of grids according to the finest.

struct params *par
    Pointer to the parameter structure of the main code (see solve.h for details).

struct params

double ***phi[20]
    Solution for the Newtonian potential .

double ***res_chi[20]
    Residual of the equation for chi.

double ***res_phi[20]
    Residual of the equation for phi.

```

```
double ***rho[20]
    Density (or overdensity) (see how it is used in gs routine)).

double ***[20] source_chi

double ***source_phi[20]
    Source of the equation for coarse grids in the FAS algorithm

double ***[20] temp2_chi
double ***[20] temp2_phi
double ***[20] temp_chi
double ***[20] temp_phi

double ***trunc_chi[20]
    truncation error in all cells all grids.

double ***trunc_phi[20]
    truncation error in all cells all grids.

int verbose
int verbose_coarse
```

3.1 gravity

3.1.1 mond_mass

`cycles_mm.c`

Here is the V cycle of multigrid iterations.

Since our first grid is number zero, we go to coarse grids by going up, so the cycle is inverted.

Converge criteria:

- See box in page 157 of Trottenberg, Oosterlee, Schuller, “Multigrid” for details.
- The convergence criteria are based on the mean value of the residual
- What we mean by “mean value” is defined in `grid/get_mean_max_two_fields`.
- **We have three criteria:**
 - Absolute value of the residual (which has units, so it is not good).
 - Ratio of residual of latest step and first step. This is the one implemented in Ramses. It depends on how good or bad the initial guess is, so it makes no sense.
 - Comparison with truncation error.

```
int cycle_v_mm (struct grids_gravity_mm *gg, double a)
void cycle_v_mm_recursive (struct grids_gravity_mm *gg, double a)
void do_one_v_cycle (struct grids_gravity_mm *gg, double a)
void verbose_fine (struct grids_gravity_mm *gg, double a, int write_pot)
```

`differential_operators_mm.c`

Definition of the differential operator for both equations (Poisson like and MOND like).

```
void L_mm (double ***phi, double ***chi, double aa0, double a2M2, double h, double fourh, int i, int j, int k,
           int ip1, int im1, int jp1, int jm1, int kp1, int km1, double *operator_phi, double *operator_chi)
    Evaluates differential operators on a node

void evaluate_differential_operator_mm (struct grids_gravity_mm *gg, int grid, double
                                       ***phi, double ***chi, double ***operator_phi, double ***operator_chi)
    Evaluates differential operators on the grid given by the second argument. Note that the grid does not have to
```

necessarily be the grid `gg->g`. we do not store the result in the corresponding variables in `gg` (instead we store it in the arguments `res_phi`, `res_chi`). This is in case you want to store it somewhere else.

double **mu** (double *x*)

go_up_and_down_mm.c

Two routines for going to coarse (up) and fine (down) grids.

void **go_down_mm** (**struct** *grids_gravity_mm* **gg*, double *a*)
Moves everything to the next finer grid

Comments:

- `gg->g` is the coarse.
- `gg->g-1` fine

void **go_up_mm** (**struct** *params* **par*, **struct** *grids_gravity_mm* **gg*, double *a*)

Moves everything to the next coarser grid.

- Calculates source in coarse grid.
- Transfer density and solution.

See box in Trottenberg, pag 157.

The source is calculated with: $S = \text{operator}(R(\phi), R(\rho), R(S)) - R(\text{residual}(\phi, \rho, S))$

For first term:

- Restrict three fields (including the source in this level, which is zero in the fine grid).
- Evaluate operator.

For the second term:

- Calculate the residual in the level where we are.
- Restrict that residual.

gs_residual_truncation_error_mm.c

Routines for doing one Gauss-Seidel sweep, calculating residual and truncation error (all in one grid).

Note: This is basically the core of the solver where the equations are included. See also `differential_operators_mm.c`.

void **gs_mm** (**struct** *grids_gravity_mm* **gg*)

void **gs_node_mm** (double *rho*, double *source_phi*, double *source_chi*, double ****phi*, double ****chi*, double *cte_poisson_over_a*, double *aa0*, double *a2M2*, double *h*, double *fourh*, int *i*, int *j*, int *k*, int *ip1*, int *im1*, int *jp1*, int *jm1*, int *kp1*, int *km1*)

This routine does Gauss-Seidel (GS) iteration in one node.

Comments:

- There are a lot of arguments to prevent the routine from accessing the pointer to `grids_gravity_mm` and make it more efficient.
- Whatever you put here is crucial for the performance of the code. In particular, “if” statements can kill the performance.

void **residual_mm**(**struct** *grids_gravity_mm* *gg, int *grid*, double ****res_phi*, double ****res_chi*)

Calculates residual on the grid “grid”. Comments:

- Note that the grid does not have to necessarily be the grid gg->g.
- We do not store the result by default in the corresponding variables in gg (instead we store it in the arguments *res_phi*, *res_chi*). This is in case you want to store it somewhere else.

sx_first_mm

sy_first_mm

sz_first_mm

void **trunc_err_mm**(**struct** *grids_gravity_mm* *gg, int *grid*, double ****trunc_phi*, double ****trunc_chi*)

Estimates truncation error (i.e. error associated to the discretization of the differential equation).

Comments:

- Note that the grid does not have to necessarily be the grid gg->g.
- The estimator is: $\tau = P[D(R(\phi)) - R(D(\phi))]$

initial_guess_mm.c

Initial guess for multigrid solver.

Comments:

- Use this if you do not have a better solution (such as the solution in previous time step).
- This must be called before you call the multigrid solver.
- For the MOND case, zero is not good enough (that’s why we put a random number).
- A better initial guesses can be obtained by what we have in *solve_spherical_mond*.

void **initial_guess_mm**(**struct** *params* *par, double ****chi_bar*, double ****phi_bar*)

solve_multigrid_mm.c

Multigrid solver for the non-linear Bekenstein-Milgrom MM equation in a 3D uniform grid given a source. See Brent 1977, Trottenberg 2000 or Wesseling 1992.

Comments:

- User should give an initial condition in phi for the iterations (zero is wrong).
- Grids start from zero, meaning that the V cycle looks more like an inverted V (i.e. when we go up, we go to coarse grids).

void **allocate_grids_mm**(**struct** *grids_gravity_mm* *gg, double ****dens*, double ****phi*, double ****chi*)

Allocate additional coarse grids for the multigrid solver. For the fine grid, we do not make a copy, but just keep a pointer to the variables in the main structure par.

void **deallocate_grids_mm**(**struct** *grids_gravity_mm* *gg, double ****dens*, double ****phi*, double ****chi*)

Clean up the coarse grids.

Comments:

- We do not clean up the fine grid because we only have a pointer to the main variables in the main code (in the structure *grid*).

- We could call this after obtaining a solution. Which means that we have to allocate everything again in the following time step. I am not sure if that is the best thing to do, but in any case, the overhead is negligible compare with everything else.

```
int solve_multigrid_mm(struct params *par, double ***dens, double ***phi, double ***chi, double  
                      box, double grid, double a)  
Main routine of the multigrid solver for MOND-MM potentials
```

solve_multigrid_mm.h

GO_UP_FIRST

default=1. If 0 then solver does not go up in the first multigrid level (i.e. one grid scheme).

GO_UP_SECOND

MAX_GRIDS

Number of pointers to grids (not necessarily allocated). (i.e. not important unless you want to have more than 20 levels).

MAX_ITERATION

Maximun number of complete V cycles before accepting that the solver will not converge.

MINUS

For evaluating the MOND operator.

NGS

Number of Gauss-Seidel iterations per level.

PLUS

For evaluating the MOND operator.

X

For evaluating the MOND operator.

Y

For evaluating the MOND operator.

Z

For evaluating the MOND operator.

struct grids_gravity_mm

Main data structure of the multigrid solver.

Comments:

- Note that here we have a copy of the main parameters of the code. That is to avoid having to accessing too many structures in some of the loops in the solver.

double **KB**

MOND parameter KB

double **a2M2**

MOND parameter M^2 (multiplied by a^2).

double **aa0**

MOND parameter a_0

double *****chi**[20]

Solution for the MOND equation ().

double **cte_poisson_over_a**

```

double fourh[20]
    This one is optimization

int g
    Grid in which we are working. 0 = finest (so what people call V cycle, is actually a Lambda).

double h[20]
    Spacing of each grid.

int n[20]
    Size of each grid.

int num_grids
    Number of grids according to the finest.

struct params *par
    Pointer to the parameter structure of the main code (see solve.h for details).

struct params
double ***phi[20]
    Solution for the Newtonian potential .

double ***res_chi[20]
    Residual of the equation for chi.

double ***res_phi[20]
    Residual of the equation for phi.

double ***rho[20]
    Density (or overdensity) (see how it is used in gs routine)).

double ***[20] source_chi
double ***source_phi[20]
    Source of the equation for coarse grids in the FAS algorithm

double ***[20] temp2_chi
double ***[20] temp2_phi
double ***[20] temp_chi
double ***[20] temp_phi
double ***trunc_chi[20]
    truncation error in all cells all grids.
double ***trunc_phi[20]
    truncation error in all cells all grids.

int verbose
int verbose_coarse

extern int solve_multigrid_mm(struct params *par, double ***dens, double ***chi, double
    ***phi, double box, double grid, double a)

```

`solve_spherical_mond.c`

Routines for solving for the spherical mond potential given by the standard poisson's equation. The calculation of the source and everything is made here. - See appendix in Llinares' thesis 2010.

`pow2(x)`

`pow3(x)`

`pow4(x)`

`pow5(x)`

`pow6(x)`

`int solve_spherical_mond(double ***phi, double a, fftw_complex *data, fftw_plan p_forward,`
`fftw_plan p_backward, double power_a0)`

This routine comes from the thesis. It has to be merged into the new code. It is not included in the Makefile.

The routine solves an equation for the spherical mond potential which can be obtained by calculating the derivative of the integral (yes, that's what I wrote) of the MOND equation. The method is:

- get newtonian forces.
- get spherical mond forces.
- take divergence.
- solve poisson's equation with that source.

Parameters

- `phi = newtonian potential.` (-) -
- `a = expansion factor.` (-) -

Returns

- `phi` = spherical mondian potential.

Comments:

- No units (they come with whatever you put as input).
- THIS ROUTINE REWITES PHI.

3.1.2 newton

`fft_solver`

`solve_poisson_fftw.c`

Solve Poisson's equation in a 3D uniform grid given a source.

Comments:

- No 4 pi G involved (it should come with the source if there is any).
- You can get the 4 pi G for standard gravity by calling `calc_newt_source`.
- No units (again, they should come with the density).

`void anti_transforms(double ***gr, double ***gi, double box, int grid, fftw_complex *data, fftw_plan`
`p_forward)`

index (i, j, k)

int **solve_poisson_fftw** (**struct** *params* **par*, **struct** *grids* **grid*, **struct** *units* **unit*)

void **transforms** (double ****gr*, double ****gi*, double *box*, int *grid*, fftw_complex **data*, fftw_plan *p_backward*)

calc_newt_source.c

Calculates the source of standard Poisson's equation. Comments:

- This routine can probably be simplified, but having this separate from the solver allow us to used the FFT solver for many things (for instance, for calculating initial conditions for the MOND equation.

void **calc_newt_source** (**struct** *params* **par*, **struct** *grids* **grid*, **struct** *units* **unit*, double *a*)

3.1.3 prolonge.c

Prologation routines which interpolate a field from a coarse grid back to a fine grid.

Comments:

- See Trottenberg, Oosterlee, Schuller, "Multigrid" for details.
- These routines are needed by the multigrid solver to move between grids.
- There are several routines that use different interpolation order. Higher order is not necessarily better.
- The only public routine is `prolonge`. The other routines are accessed through it. Uncomment the call you want to use.

pow2 (x)

void **prolonge** (double ****old*, double ****new*, int *n_old*, double *h_old*)

void **prolonge_first_order** (double ****old*, double ****new*, int *n_old*, int *n_new*, double *h_old*, double *h_new*)

void **prolonge_second_order** (double ****old*, double ****new*, int *n_old*, int *n_new*, double *h_old*, double *h_new*)

void **prolonge_trilinear** (double ****old*, double ****new*, int *n_old*, int *n_new*, double *h_old*, double *h_new*)

3.1.4 restrict.c

Restriction routines which interpolate a field from a fina grid to a coarse grid (with half the number of points per dimension).

Comments:

- See Trottenberg, Oosterlee, Schuller, "Multigrid" for details.
- These routines are needed by the multigrid solver to move between grids.
- There are several routines that use different interpolation order. Higher order is not necessarily better.
- The only public routine is `restrict_grid`. The other routines are accessed through it. Uncomment the call you want to use.

void **restrict_grid** (double ****old*, double ****new*, long *n_old*)

void **restrict_grid_cospatial** (double ****old*, double ****new*, long *n_old*)

```
void restrict_grid_original (double ***old, double ***new, long n_old)
```

3.1.5 get_forces.c

Calculates force in the grid by deriving a potential.

```
void forces (struct params *par, double ***phi, double ***dphi_dx, double ***dphi_dy, double  
            ***dphi_dz)  
    Derives a potential.
```

Parameters

- **par** = pointer to params structure (-) -
- **phi** = pointer to the potential. (-) -
- **dphi_dx...** = derivatives. (-) -

```
pow2 (x)
```

3.1.6 get_gravity.c

Calculates forces on the grid from scratch (including calculation of the density and potential).

Comments:

- The result is returned in the corresponding variable in the grid structure.
- The density and potential will also end up in the corresponding variables in the structure grid.

```
void get_gravity (struct params *par, struct grids *grid, struct particles *part, struct units  
                 *unit, double t)
```

3.1.7 get_lap.c

```
void calc_lap (struct params *par, double ***phi, double ***lap_phi)
```

3.2 grid

3.2.1 add_two_fields.c

```
void add_two_fields (double ***field1, double ***field2, int n, double ***result)
```

3.2.2 clean_up_grid.c

```
void clean_up_grid (struct params *par, struct grids *grid)
```

3.2.3 get_mean_max_two_fields.c

```
void get_mean_max_two_fields (double ***field1, double ***field2, int n, double *mean, double *maximum)
new_max (x, y)
```

3.2.4 init_fftw.c

```
void init_fftw (struct params *par, struct grids *grid)
```

3.2.5 init_grid.c

```
void init_grid (struct params *par, struct grids *grid)
```

3.2.6 init_grid.h

```
struct grids
```

```
double ***chi_bar_mm
fftw_complex *data
double ***delta
double ***force_1
double ***force_2
double ***force_3
double ***force_chi_bar_mm_1
double ***force_chi_bar_mm_2
double ***force_chi_bar_mm_3
double ***force_phi_bar_mm_1
double ***force_phi_bar_mm_2
double ***force_phi_bar_mm_3
fftw_plan p_backward
fftw_plan p_forward
double ***phi
double ***phi_bar_mm
double ***source
```

```
extern void init_grid (struct params *par, struct grids *grid)
```

3.2.7 write_phi.c

```
void write_phi (struct params *par, struct grids *grid)
```

3.3 libs

3.3.1 allocator.c

```
void alloc_char_2 (char ***a, int d1, int d2)
void alloc_char_3 (char ****a, int d1, int d2, int d3)
void alloc_char_4 (char *****a, int d1, int d2, int d3, int d4)
void alloc_double_2 (double ***a, int d1, int d2)
void alloc_double_3 (double ****a, int d1, int d2, int d3)
void alloc_double_4 (double *****a, int d1, int d2, int d3, int d4)
void alloc_double_5 (double *****, int d1, int d2, int d3, int d4, int d5)
void alloc_float_2 (float ***a, int d1, int d2)
void alloc_float_3 (float ****a, int d1, int d2, int d3)
void alloc_float_4 (float *****a, int d1, int d2, int d3, int d4)
void alloc_int_2 (int ***a, int d1, int d2)
void alloc_int_3 (int ****a, int d1, int d2, int d3)
void alloc_int_4 (int *****a, int d1, int d2, int d3, int d4)
void alloc_long_2 (long ***a, int d1, int d2)
void alloc_long_3 (long ****a, int d1, int d2, int d3)
void alloc_long_4 (long *****a, int d1, int d2, int d3, int d4)
```

3.3.2 a_of_time.c

```
int a_dot_supercom_for_rk (double t, const double y[], double f[], void *params)
double a_of_supercom_time (struct params *par, struct units *unit, double tau)
int jac_a_dot_supercom_for_rk (double t, const double y[], double *dfdy, double dfdt[], void
                               *params)

pow2 (x)
pow3 (x)
pow4 (x)

void test_a_of_time (struct params *par, struct units *unit)
double time_of_a_supercom (struct params *par, struct units *unit, double a_init)
```

3.3.3 cosmology.c

```
double A (struct params *par, struct units *unit, double a)
double F (struct params *par, struct units *unit, double a)
double a_dot (struct params *par, struct units *unit, double a)
double a_of_t (struct params *par, double t)
double hubble (struct params *par, struct units *unit, double a)
double hubble2 (struct params *par, struct units *unit, double a)
double hubble_dot (struct params *par, struct units *unit, double a)
double integrand_time (double a, void *parameters)
double integrate_time_of_a (struct params *par, double a)
struct params_int

    struct params *par
void tabulate_t_of_a (struct params *par)
```

3.3.4 ran3.c

```
FAC
MBIG
MSEED
MZ
float ran3 (long *idum)
```

3.3.5 read_params.c

```
/// file read_params.c
void check_keyword (char keywords[50][1000], void *values[50], char type[50][10], int *found, char *key,
                    char *val)
void delete_spaces (char *str)
void init_keywords (struct params *par, char keywords[50][1000], void *values[50], char type[50][10],
                    int *found)
void read_params (struct params *par)
```

3.3.6 releaser.c

```
void free_char_2 (char **a)
void free_char_3 (char ***a)
void free_char_4 (char ****a)
void free_double_2 (double **a)
void free_double_3 (double ***a)
void free_double_4 (double ****a)
void free_float_2 (float **a)
void free_float_3 (float ***a)
void free_float_4 (float ****a)
void free_int_2 (int **a)
void free_int_3 (int ***a)
void free_int_4 (int ****a)
void free_long_2 (long **a)
void free_long_3 (long ***a)
void free_long_4 (long ****a)
```

3.3.7 utils.c

```
void change_system (double vec[3][3], double *x, double *y, double *z)
double dist (double x, double y, double z)
double euclides (double x, double y, double z)
double euclides2 (double x, double y, double z)
FILE *fopen_check (char *file, char *type)
void index_1d_to_3d (double q, int *i, int *j, int *k, int n)
double modulus (double x, double y)
void sort_3_values (double *a)
```

3.4 pm

3.4.1 calc_delta_cic.c

Calculates overdensity on the grid from the particle's positions using cloud in cell (CIC) smoothing. Comments:

- Details in the CIC scheme can be found in Hockney R. W., Eastwood J. W., 1988, Computer simulation using particles.

```
void calc_delta_cic (struct params *par, struct units *unit, double *pos_1, double *pos_2, double
                    *pos_3, double ***delta)
```

Calculates overdensity on the grid from the particle's positions using cloud in cell (CIC) smoothing..

Note: This is a note for testign Sphinx.

Parameters

- **par** – par structure.
- **unit** – units structure.
- **pos_1** – X component of position vector.
- **pos_2** – X component of position vector.
- **pos_3** – X component of position vector.
- **delta** – to return overdensity.

Returns Overdensity in the parameter delta, which should be allocated.

3.4.2 init_parts.c

Here we allocate memory for the particles and read initial conditions.

```
void init_parts (struct params *par, struct particles *part, struct units *unit)
```

3.4.3 init_parts.h

```
extern void init_parts (struct params *par, struct particles *part, struct units *unit)
```

```
struct particles
```

```
    double *pos_1
```

```
    double *pos_2
```

```
    double *pos_3
```

```
    double *vel_1
```

```
    double *vel_2
```

```
    double *vel_3
```

3.4.4 input_particles.c

Here we read initial conditions for particles. Comments:

- Units in the input file are expected to be Mpc/h for the positions and km/sec for the velocities.
- Units are converted later to Mpc and Mpc/Gyr.

```
void read_particles (struct params *par, struct units *unit, double *pos_1, double *pos_2, double
                    *pos_3, double *vel_1, double *vel_2, double *vel_3, char *file_name)
```

3.4.5 interp_force_cic.c

Interpolates a force vector from the grid to the particles usign CIC scheme. Comments:

- Details in the CIC scheme can be found in Hockney R. W., Eastwood J. W., 1988, Computer simulation using particles.

```
void interp_force_cic (struct params *par, struct grids *grid, struct particles *part, double  
                      ***force_1, double ***force_2, double ***force_3, double move_part)
```

3.4.6 write_particles.c

```
void write_particles (struct params *par, struct units *unit, double *pos_1, double *pos_2, dou-  
                    ble *pos_3, double *vel_1, double *vel_2, double *vel_3, int num)
```

3.5 tests

3.5.1 static_test.c

This is a static test. If the corresponding flag is on in the parameter file, then the code will read initial conditions, calculate all the relevant fields, write them in a file and stops execution. Comments:

- There is a comparison between solutions obtained here and analytic solutions in the directory tests.

```
void static_test (struct params *par, struct grids *grid, struct particles *part, struct units  
                 *unit)
```

3.6 time_evolution

3.6.1 time_evolution_standard_variable.c

Here is the main time loop.

```
void leap_frog_variable (struct params *par, struct grids *grid, struct particles *part,  
                        struct units *unit)
```

3.7 init_physics.c

```
void init_physics (struct params *par, struct units *unit)
```

Initializes a lot of physical constants including the factor in front of the density in the Poisson's equation (which somehow contains the effective gravitational constant). So if you want to change G , this is probably the place to do it. Although, keep in mind that additional changes are made later on to include the dependence with expansion factor.

Parameters

- **par** – parameter structure.
- **unit** – units structure.

Returns Changes are included in the two structures that you input.

3.8 init_physics.h

```
extern void init_physics (struct params *par, struct units *unit)
```

3.9 solve.c

Here is the main function.

Units:

input:

- [x] = Mpc/h
- [v] = km sec⁻¹

internal:

- [x] = Mpc
- [v] = Mpc/Gyr
- [source] = 1/Gyr²
- [phi] = Mpc²/Gyr² (it takes units from distances)

Comments:

- The program can NOT restart.

```
int main (int argc, char *argv[])
```

Main routine. It initializes everything (physics, fine grid and particles) and gives control to the routine that does the time evolution.

3.10 solve.h

struct params

Structure with input parameters and fields

double **H0**

double **a**

Expansion factor.

double **box**

Mpc/h and then converted to Mpc in init_physics.

double **cte_poisson**

char [1000] **file_in_parts**

char [1000] **file_out**

int **gravity**

0 -> Newton 1 -> MOND with mass term.

int **grid**

Grid size (the code is not tested with this number being different than the number of particles).

int **grid_p**

Grid of particles (cubic root of total number of particles).

```
double hsmall1
double mm_KB
    MOND constant.
double mm_M
    MOND mass in h/Mpc and converted to 1/Mpc.
double mm_a0
    MOND a0 in km/sec^2 and converted to Mpc/Gyr^2.
int n_outputs
int nparts
    Total number of particles.
int nsteps
    Number of time steps.
int nthreads
    Number of threads. (interesting only if OPENMP).
double omega1
double omegam
int static_test
double [1000] t_of_a
int verbose
int verbose_mm
int verbose_mm_coarse
double z_end
double z_init

pow2 (x)
pow3 (x)
pow4 (x)
pow5 (x)
pow6 (x)
pow7 (x)

struct units

    double H0
    double clight
    double cm2mpc
    double cte_poisson
    double gyr2sec
    double kg2msun
    double km2mpc
```

```
double m2mpc  
double mpc2km  
double mpc2km_over_gyr2sec  
double mpc2m  
double pi  
double sec2gyr  
double twopi
```


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