Tug of War Problem with
Answer Set Programming – clingo
An Encoding

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Road map of this presentation:

1. About the ASP (clingo) – previous presentation (done)
2. Requisites – previous presentation (done)
3. Tug of War (well knowed problem from competitive programming sites and contests)
4. A modelling in ASP
5. A solution in clingo
6. Using Python's code inside of ASP
7. Conclusions

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Attention: some background in logic and declarative language is recommended!

Tug of War Problem

Figura: Practical application of this problem

Tug of War

From: https://www.geeksforgeeks.org/tug-of-war/
and/or https://www.codechef.com/problems/CO319TSH

Given a set of n integers, divide the set in two subsets of $n/2$ sizes
each such that the difference of the sum of two subsets is as
minimum as possible. If n is even, then sizes of two subsets must
be strictly $n/2$ and if n is odd, then size of one subset must be
$(n-1)/2$ and size of other subset must be $(n+1)/2$.

Examples

- ▶ Example 1: let given set be {3, 4, 5, -3, 100, 1, 89, 54, 23, 20}, the size of set is 10. Output for this set should be {4, 100, 1, 23, 20} and {3, 5, -3, 89, 54}. Both output subsets are of size 5 and sum of elements in both subsets is same (148 and 148).

- ▶ Let us consider another example where n is odd. Let given set be {23, 45, -34, 12, 0, 98, -99, 4, 189, -1, 4}. The output subsets should be {45, -34, 12, 98, -1} and {23, 0, -99, 4, 189, 4}. The sums of elements in two subsets are 120 and 121 respectively.

- ▶ This problem is beauty: *easy to understand, hard to solve it*!

Comments

- ▶ Again: all the combinations must be found!
- ▶ Input: a set of numbers, in our implementation an array, aiming a possible repetitions of these numbers.
- ▶ Output: two sets with the same size/cardinality, or with difference of one number for set A or B.
- ▶ Complexity: NP-Complete (all the combinations must be examined) – Set partition problem is NP complete – https://www.geeksforgeeks.org/set-partition-is-np-complete/
- ▶ Optimization: NP-Hard, due the minimum value of the absolute difference between the sum of two sets.

Some comments and motivation:

- ▶ I solved it in Minizinc!
- ▶ Some approaches for this problem can be taken: Simulated Annealing, Ant Colony, Depth-First Search, ..., meta-heuristics in general presents a good efficiency
- ▶ Dynamic Programming is the most suitable for contest programming
- ▶ The full code discussed here is found in: https://github.com/claudiosa/CCS/tree/master/asp_ Answer_Set_Programming/tug_of_war.lp
- ▶ We are commenting the modelling in parts of its code

Modelling:

- The input value of this problem

Modelling:

- ▶ The input value of this problem
- ▶ A help from Python here, it is discussed at the end this modelling

```
$ cat inp_2_tug_of_war.txt
#const n=11.
weights(1,23).  weights(2,45).  weights(3,-34). weights(4,12).
weights(5,0).   weights(6,98).  weights(7,-99). weights(8,4).
weights(9,189). weights(10,-1). weights(11,4).
```

- ▶ Reminding our second case – example:
  {23, 45, -34, 12, 0, 98, -99, 4, 189, -1, 4}
- ▶ Already converted in ground terms

Creating the possible sets as solutions:

```
% creating sets 01 and 02
 { set_01(I,W) }  :-  weights(I,W).
 { set_02(I,W) }  :-  weights(I,W).

%%% a CONSTRAINT here: these sets are disjunctives
:- set_01(I,_), I = 1..n, set_02(J,_), J = 1..n, I == J.
%% any set has the same element referenced by an index
```

The *n* value was defined previously!
Here is the trick of this modelling – think about it!

Counting and summing the elements of each set:

```
%% counting elements of sets 01 and 02 by index
n_1(N) :- N = #count{I: set_01(I,W) }.
n_2(N) :- N = #count{I: set_02(I,W) }.
size(N) :- N = #count{I: weights(I,W)}.

%% summing all elements of sets 01 and 02
sum_set_01(X) :- X = #sum{W,I : I= 1..n, set_01(I,W)}.
sum_set_02(X) :- X = #sum{W,I : I= 1..n, set_02(I,W)}.
```

About the size of each set:

Reminding:

```
n_1(X): X is the cardinality of set_1
n_2(Y): Y is the cardinality of set_2
size(N): N is the cardinality of original set
...
so
..
% constraint 2 ... set 1 and 2 .. are almost the same size
:- n_1(X), n_2(Y) , X - Y > 1 .  % not allowed  IF |X|  > |Y|
:- n_1(X), n_2(Y) , Y - X > 1.   % not allowed  IF |Y|  > |X|
% constraint 1 ... sum of size sets are the same
:- n_1(X), n_2(Y) , size(N) , (X+Y) != N.
```

Preparing for the optimization:

```
%% the abs works fine
diff(Z) :- sum_set_01(X), sum_set_02(Y),  Z = |Y - X|.
%% #abs(Y-X).

%% if "a perfect" balance  -- no differences of weight
answer('y_YES') :- diff(0).
answer('n_NO') :- diff(Z), Z != 0.

%% A minimizations on this difference
#minimize{ Z : diff(Z) }.
```

The outputs:

```
#show n_1/1.
#show n_2/1.
%#show size/1.

%% sets obtained
#show set_01/2.
#show set_02/2.
%% sum of each side
#show sum_set_01/1.
#show sum_set_02/1.
#show diff/1.
#show answer/1.
```

An output:

```
$ clingo tug_of_war.lp inp_2_tug_of_war.txt
qclingo version 5.3.0
Reading from tug_of_war.lp ...
Solving...
Answer: 1
set_02(4,12) set_02(5,0) set_02(3,-34) set_02(7,-99)
set_02(10,-1)
set_01(1,23) set_01(2,45) set_01(6,98) set_01(8,4)
set_01(9,189) set_01(11,4)
sum_set_02(-122) sum_set_01(363) diff(485)
answer('n_NO') n_2(5) n_1(6)
Optimization: 485
Answer: 2
.......................................
```

Many lines omitted!

An output:

Finally in the answer 12:

```
...
Answer: 12
set_02(2,45) set_02(4,12) set_02(6,98) set_02(3,-34)
set_02(10,-1)
set_01(1,23) set_01(5,0) set_01(8,4) set_01(9,189)
set_01(11,4) set_01(7,-99)
sum_set_02(120) sum_set_01(121) diff(1)
answer('n_NO') n_2(5) n_1(6)
Optimization: 1
OPTIMUM FOUND

Models      : 12
  Optimum   : yes
Optimization : 1
Calls       : 1
Time        : 1.181s (Solving: 0.58s 1st Model: 0.03s Unsat: 0.
CPU Time    : 1.181s
```

Using Python's code inside of ASP

- ▶ A big help from Adam Smith (Postasco mailing list)
- ▶ How to deal with input and output values in ASP?

Using Python's code inside of ASP

- A big help from Adam Smith (Postasco mailing list)
- How to deal with input and output values in ASP?
- Some snippets of code in Python!
- The code discussed here:
  `convert_input_value_in_terms_Python.lp`

An example:

```python
#script (python)
def my_size(*terms):
    i=0
    for term in enumerate(terms):
        i+=1
    return i
#end.

#script (python)
def multiset( *terms ):
  result = []
  for i , term in enumerate(terms):
    """ List of Pairs """
    result.append( (i+1, term) )
  return result
#end.
...
```

Using Python's functions embedded in ASP:

```
...
weights(I,W) :- (I,W) = @multiset( 23, 45, -34, 12, 0  ).
size(S) :- S = @my_size(1,2,3,4,9999999999).
.....................................................

$ clingo convert_input_value_in_terms_Python.lp
...
Answer: 1
size(5) weights(1,23) weights(2,45) weights(3,-34)
weights(4,12) weights(5,0)
SATISFIABLE
Models       : 1
...
```

Conclusions:

▶ ASP is strongly declarative (roots from the logic to attack the problems representation)

▶ Generate and test methodology

▶ ASP's workflow, modeling, grounding, solving (and optimizing)

▶ Here, we solved *the tug of war problem*. Easy to understand, but is is a combinatorial problem.

▶ Allows you to embbed a Python coding in order to minimize the difficulties (☺) of input and output data

▶ An encoding in ASP is excellent exercise to keep your mind very active!

▶ Finally, a huge gratitude for the **potassco-users list**, always reactive for my silly doubts, where I had been learning much.

Contact and comments (are must welcome ☺):

- https://claudiocesar.wordpress.com/
- This presentation and the code discussed:
  https://github.com/claudiosa/CCS/tree/master/asp_Answer_Set_Programming
- There is a directory to Youtube!
- The full code discussed here is found in:
  https://github.com/claudiosa/CCS/tree/master/asp_Answer_Set_Programming/tug_of_war.lp
- ✉: ccs1664@gmail.com
- This material has a partial support from WhatsTV Inc.
  https://en.whatstv.com.br/, here our gratitude!
- *Thank you so much*!