# Deformable MR Prostate Segmentation via Deep Feature Learning and Sparse Patch Matching



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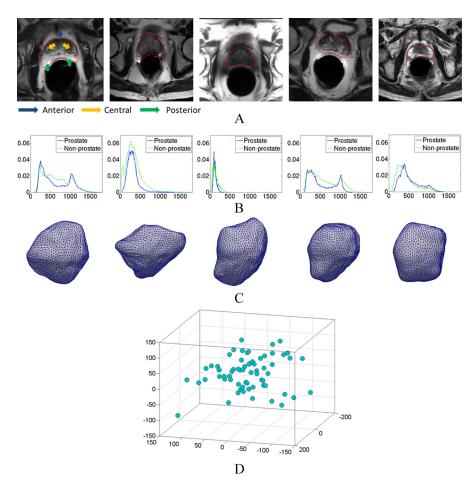
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## 9.1 BACKGROUND

Prostate cancer is the second leading cause of cancer death in American men, behind only lung cancer [1]. As the main imaging modality for clinical inspection of the prostate, Magnetic Resonance (MR) imaging provides better soft tissue contrast than ultrasound imaging in a non-invasive way and has an emerging role in prostate cancer diagnosis and treatment [2,3]. The accurate localization of the prostate is an important step for assisting diagnosis and treatment, such as for guiding biopsy procedure [2] and radiation therapy [3]. However, manual segmentation of the prostate is tedious and time-consuming, and it also suffers from intra- and inter-observer variability. Therefore, developing automatic and reliable segmentation methods for MR prostate is clinically desirable and an important task.

However, accurate prostate localization in MR images is difficult due to the following two main challenges. First, the appearance patterns vary a lot around the prostate boundary across patients. As we can see from Fig. 9.1A, the image contrasts



(A) Typical T2-weighted prostate MR images. Red contours indicate the prostate glands manually delineated by an expert. (B) Intensity distributions of the prostate and background voxels around the prostate boundary of (A). (C) The 3D illustrations of prostate surfaces corresponding to each image in (A). (D) The prostate shape distribution obtained from PCA analysis.

at different prostate regions, i.e., the anterior, central, and posterior regions, change across different subjects and also within each subject. Fig. 9.1B gives the intensity distributions of the prostate and background voxels around the prostate boundary, respectively. As shown in the figure, the intensity distributions vary highly across different patients and often do not follow the Gaussian distribution.

To evaluate the shape difference in our dataset, we adopt the PCA analysis by mapping each high-dimensional shape vector onto a space spanned by the first three

principal components. Note that the shape vector is formed by the concatenation of all vertex coordinates, and then linearly aligned to the mean shape before PCA analysis. Fig. 9.1D shows the distribution of 66 prostate shapes, from which we can see inter-patient shape variation in the shape repository.

## 9.2 PROPOSED METHOD

## 9.2.1 RELATED WORK

Most of recent studies in T2-weighted MR prostate segmentation focus on two types of methods: multi-atlas-based [4–7] and deformable-model-based [8,9] segmentation methods. Multi-atlas-based methods are widely used in medical imaging [10–12]. Most of research focuses on the design of sophisticated atlas-selection or label-fusion methods. For example, Yan et al. [5] proposed a label image constrained atlas selection and label fusion method for prostate MR segmentation. During the atlas selection procedure, label images are used to constrain the manifold projection of intensity images; by doing so, the misleading projection can be potentially avoided due to the use of other anatomical structures. Ou et al. [7] proposed an iterative multi-atlas label fusion method by gradually improving the registration based on the prostate vicinity between the target and atlas images. For deformable-model-based methods, Toth [8] proposed to incorporate different features in the context of AAMs (Active Appearance Models). Besides, with the adoption of a level set, the issue of landmark correspondence can be avoided.

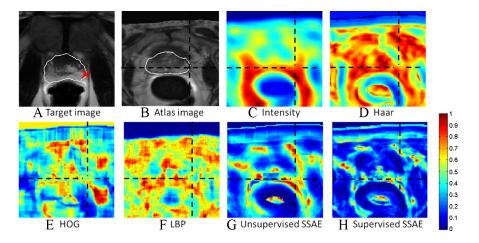
Handcrafted vs. Deep-Learned Features. Both types of above-mentioned methods require careful feature engineering to achieve good performance. The multi-atlas based methods require good features for identifying correspondences between a new testing image and each atlas image [13], while the deformable model relies on discriminative features for separating the target object (e.g., the prostate) from the background [14]. Traditionally, intensity patch is often used as features for the above two methods [15,16]. However, due to the inhomogeneity of MR images, the simple intensity features often fail in the segmentation of MR images with different contrasts and illuminations. To overcome this problem, recent MR prostate segmentation methods started to use features that are specifically designed for vision tasks, such as gradient [17], Haar-like wavelets [18], Histogram of Oriented Gradients (HOG) [19], SIFT [20], Local Binary Patterns (LBP) [21], and variance adaptive SIFT [14]. Compared to simple intensity features, these vision-based features show better invariance to illumination, and they also provide certain invariance to small rotations. In [22], the authors showed that better prostate segmentation could be obtained by using the combination of these features.

One major limitation of the aforementioned handcrafted features is the inability of adapting themselves to the data at hand. This means that the representation power and effectiveness of these features could vary across different kinds of image data. To deal with this limitation, the learning based feature representation methods [23,24] have been developed to extract latent information that can be adapted to the data at

hand. As one important type of feature learning methods, deep learning has recently become a hot topic in machine learning [23], computer vision [25], and many other research fields, including medical image analysis [26]. Compared with handcrafted features, which need expert knowledge for careful design and also lack sufficient generalization power to different domains, deep learning is able to automatically learn effective feature hierarchies from the data. Therefore, it draws an increasing interest in the research communities. For example, Vincent et al. [27] showed that the features learned by deep belief network and the stacked denoising auto-encoder beat the state-of-the-art handcrafted features for the digit classification problem in the MINST dataset. Farabet et al. [28] proposed to use the convolutional neural network to learn useful feature representations, which are more powerful in the application of scene labeling than the engineered features, and their method also achieved the state-of-theart performance. In the field of medical image analysis, Shin et al. [29] applied the stacked auto-encoders to organ identification in MR images, which shows the potential of deep learning methods in analysis of medical images. In summary, compared with handcrafted features, deep learning has the following advantages: (i) Instead of designing effective features for a new task by trial and error, deep learning largely saves researchers' time by automating this process. Also, it is capable of exploiting the complex feature patterns, for which the manual feature engineering is not good. (ii) Unlike the handcrafted features, which are usually shallow in feature representation due to the difficulty of designing the high-level abstract features, deep learning is able to learn the feature hierarchy in a layer-by-layer manner, by first learning the low-level features and then recursively building more comprehensive high-level features based on the previously learned low-level features. (iii) When unsupervised pre-training is combined with supervised fine-tuning, the deep-learned features can be optimized for a certain task, such as segmentation, thus boosting the final performance. Motivated by the above factors, we propose to learn a hierarchical feature representation based on deep feature learning [30,31] from MR prostate images.

Before presenting the proposed deep feature learning, we first demonstrate the limitations of handcrafted features in MR prostate images. In computer vision, the common handcrafted features include Haar features [18], HOG features [20], and Local Binary Patterns [21]. They have been proposed in different applications, with promising results such as in object detection of natural images. However, these features are not suitable for MR prostate images, as they are not invariant to both the inhomogeneity of MR images and the appearance variations of the prostate gland. To illustrate limitations of these handcrafted features, we compare the effectiveness of different features in identifying correspondences in two images, in the context of multi-atlas based segmentation methods.

Fig. 9.2 shows a typical example by computing the similarity maps between one point (shown as a red cross in Fig. 9.2A) in the target image (Fig. 9.2A) and all points in an aligned atlas image (Fig. 9.2B). The white contours in (A) and (B) show the prostate boundaries, and the black dashed cross in Fig. 9.2B indicates correct correspondence of the red-cross target point in the atlas image. The effectiveness of features can be reflected by the similarity map. If features are distinctive for corre-



The similarity maps computed between a reference voxel (red cross) in the target image (A) and all voxels in the atlas image (B) by the four handcrafted feature representations, i.e., intensity (C), Haar (D), HOG (E), and LBP (F), as well as the two deep-learned feature representations, namely the unsupervised SSAE (G) and the supervised SSAE (H). White contours indicate the prostate boundaries, and the black dashed crosses indicate the ground-truth correspondence in (B), which is corresponding to the red cross in (A).

spondence detection, the similarity computed by using these features would be high for correct correspondences while low for incorrect correspondences. Figs. 9.2C–F show the similarity maps computed using different handcrafted features, such as intensity patch features, Haar features, HOG features, and LBP features, respectively. It is clear that none of these features can capture correct correspondence, as the similarity between the corresponding voxels indicated by red crosses is low, compared to that of nearby voxels. This shows that the existing handcrafted features are insufficient in multi-atlas based segmentation for the MR prostate.

Thus, to relieve the limitation of handcrafted features, it is necessary to learn discriminant features adaptive to MR prostate images. To demonstrate the effectiveness of deep learning features, Figs. 9.2G and 9.2H provide the similarity maps computed using the two kinds of deep-learned features obtained by our proposed *unsupervised* and *supervised* stacked sparse auto-encoder (SSAE), respectively. Compared to the similarity maps of handcrafted features, it is clear that the correct correspondence can be better identified with the deep-learned features, especially for the supervised SSAE.

## 9.2.2 LEARNING DEEP FEATURE REPRESENTATION

**Auto-Encoder.** Serving as the fundamental component for SSAE, the basic auto-encoder (AE) trains a feed-forward nonlinear neural network, which contains three

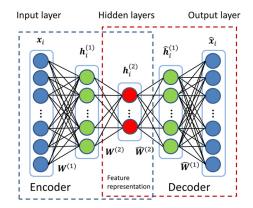


FIGURE 9.3

Construction of a basic AE.

layers, i.e., input layer, hidden layer, and output layer, as illustrated in Fig. 9.3. Each layer is represented by a number of nodes. Blue nodes on the left and right sides of Fig. 9.3 indicate the input and output layers, respectively, and green nodes indicate the hidden layer. Nodes in the two neighboring layers are fully connected, which means that each node in the previous layer can contribute to any node in the next layer. Basically, AE consists of two steps, namely encoding and decoding. In the encoding step, AE encodes the input vector into a concise representation through connections between input and hidden layers. In the decoding step, AE tries to reconstruct the input vector from the encoded feature representation in the hidden layer. The goal of AE is to find a concise representation of the input data, which could be used for the purpose of best reconstruction. Since we are interested in the representation of image patches, in this application the input to AE is an image patch, which is concatenated as a vector. In the training stage, given a set of training patches  $X = \{x_i \in \mathbb{R}^L, i = 1, ..., N\}$ , where N and L are the number and the dimension of training patches, respectively, AE automatically learns the weights of all connections in the network by minimizing the reconstruction error in Eq. (9.1),

$$\underset{\boldsymbol{W},\boldsymbol{b},\hat{\boldsymbol{W}},\hat{\boldsymbol{b}}}{\operatorname{argmin}} \sum_{i=1}^{N} \|\boldsymbol{x}_{i} - (\hat{\boldsymbol{W}}(\sigma(\boldsymbol{W}\boldsymbol{x}_{i} + \boldsymbol{b})) + \hat{\boldsymbol{b}})\|_{2}^{2}$$
(9.1)

where  $W, b, \hat{W}, \hat{b}$  are the parameters in the AE network, and  $\sigma(a) = (1 + \exp(-a))^{-1}$ . Given an input vector  $x_i$ , AE first encodes it into the concise representation  $h_i = \sigma(Wx_i + b)$ , where  $h_i$  is the responses of  $x_i$  at the hidden nodes, and the dimension of h equals to the number of nodes in the hidden layer. In the next step, AE tries to decode the original input from the encoded representation, i.e., with  $\hat{W}h_i + \hat{b}$ . To learn effective features for the input training patches, AE requires the dimension of the hidden layer to be less than that of the input layer. Otherwise, the

minimization of Eq. (9.1) would lead to trivial solutions, e.g., identity transformation. Studies [32] have also shown that the basic AE learns very similar features as PCA.

Once the weights  $\{W, b, \hat{W}, \hat{b}\}$  have been learned through the training patches, in the testing stage the AE could efficiently obtain a concise feature representation for a new image patch  $x_{\text{new}}$  by a forward passing step, i.e.,  $h_{\text{new}} = \sigma(Wx_{\text{new}} + b)$ .

**Sparse Auto-Encoder.** Rather than limiting the dimension of hidden layer (i.e., feature representation), an alternative could be imposing regularization on the hidden layer. Sparse auto-encoder (SAE) falls into this category. Instead of requiring the dimension of hidden layer to be less than that of the input layer, SAE imposes a sparsity regularization on the responses of hidden nodes (i.e., h) to avoid the problem of trivial solutions suffered by the basic AE. Specifically, SAE enforces the average response of each hidden node over the training set to be infinitesimal, i.e.,  $\rho^j = \sum_{i=1}^N h_i^j \approx \rho$ , where  $h_i^j$  is the response of the ith training input at hidden node j, and  $\rho$  is a very small constant. In this way, to balance both the reconstruction power and the sparsity of the hidden layer, only a few useful hidden nodes could have responses for each input, thus forcing the SAE network to learn sparse feature representation of the training data. Mathematically, we can extend Eq. (9.1) to derive the objective function of SAE by adding a sparsity constraint term shown below:

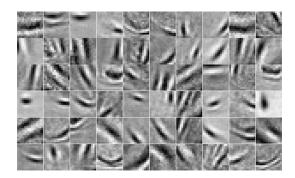
$$\underset{\boldsymbol{W},\boldsymbol{b},\hat{\boldsymbol{W}},\hat{\boldsymbol{b}}}{\operatorname{argmin}} \sum_{i=1}^{N} \|\boldsymbol{x}_{i} - (\hat{\boldsymbol{W}}(\sigma(\boldsymbol{W}\boldsymbol{x}_{i} + \boldsymbol{b})) + \hat{\boldsymbol{b}})\|_{2}^{2} + \delta \sum_{j=1}^{M} KL(\rho \mid \rho^{j})$$

$$KL(\rho \mid \rho^{j}) = \rho \log \frac{\rho}{\rho^{j}} + (1 - \rho) \log \frac{1 - \rho}{1 - \rho^{j}}$$
(9.2)

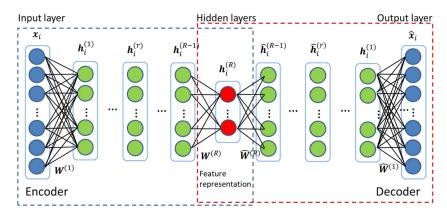
where  $\delta$  is a parameter to balance between reconstruction and sparsity terms, and M is the number of hidden nodes.  $KL(\rho \mid \rho^j)$  is the Kullback–Leibler divergence between two Bernoulli distributions with probability  $\rho$  and  $\rho^j$ . As we can see, the sparsity term is minimized only when  $\rho^j$  is close to  $\rho$  for every hidden node j. Since  $\rho$  is set to be a small constant, minimizing Eq. (9.2) could lead to the sparse responses of hidden nodes, thus the sparsity of learned feature representation.

**Stacked Sparse Auto-Encoder.** By using SAE, we can learn the low-level features (such as Gabor-like features as shown in Fig. 9.4) from the original data (MR image patches). However, low-level features are not good enough due to large appearance variations of the MR prostate. It is necessary to learn abstract high-level features, which could be invariant to the inhomogeneity of MR images. Motivated by the human perception, which constitutes a deep network to describe concepts in a hierarchical way using multiple levels of abstraction, we recursively apply SAE to learn more abstract/high-level features based on the features learned from the low-level. This multi-layer SAE model is referred to as a stacked sparse auto-encoder (SSAE), which stacks multiple SAEs on top of each other for building deep hierarchies.

Fig. 9.5 shows a typical SSAE with R stacked SAEs. Let  $\mathbf{W}^{(r)}$ ,  $\mathbf{b}^{(r)}$ ,  $\mathbf{\hat{W}}^{(r)}$ , and  $\mathbf{\hat{b}}^{(r)}$  denote the connection weights and intercepts between the input layer and



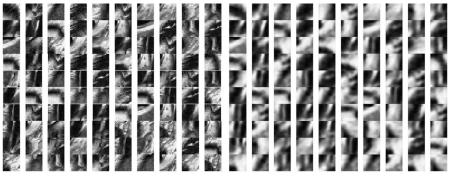
The low-level feature representation learned from the SAE. Here, we reshape each row in  $\mathbf{W}$  into the size of image patch, and visualize only its first slice as an image filter.



#### FIGURE 9.5

Construction of the *unsupervised* SSAE with *R* stacked SAEs.

hidden layer, and the weights and intercepts between the hidden layer and output layer in the rth SAE, respectively. In the encoding part of the SSAE, the input vector  $\mathbf{x}_i$  is first encoded by the first SAE for obtaining the low-level representation  $\mathbf{h}_i^{(1)}$ , i.e.,  $\mathbf{h}_i^{(1)} = \sigma(\mathbf{W}^{(1)}\mathbf{x}_i + \mathbf{b}^{(1)})$ . Then, the low-level representation  $\mathbf{h}_i^{(1)}$  of the first SAE is considered as the input vector to the next SAE, which encodes it into higher level representation  $\mathbf{h}_i^{(2)}$ , i.e.,  $\mathbf{h}_i^{(2)} = \sigma(\mathbf{W}^{(2)}\mathbf{h}_i^{(1)} + \mathbf{b}^{(2)})$ . Generally, the rth level representation  $\mathbf{h}_i^{(r)}$  can be obtained by a recursive encoding procedure  $\mathbf{h}_i^{(r)} = \sigma(\mathbf{W}^{(r)}\mathbf{h}_i^{(r-1)} + \mathbf{b}^{(r)})$  with  $\mathbf{h}_i^{(0)} = \mathbf{x}_i$ . Similarly, the decoding step of SSAE recursively reconstructs the input of each SAE. In this example, SSAE first reconstructs the low-level representation  $\hat{\mathbf{h}}_i^{(r-1)}$  from the high-level representation  $\hat{\mathbf{h}}_i^{(r)}$ , i.e.,  $\hat{\mathbf{h}}_i^{(r-1)} = \hat{\mathbf{W}}^{(r)}\hat{\mathbf{h}}_i^{(r)} + \hat{\mathbf{b}}^{(r)}$  with  $\hat{\mathbf{h}}_i^{(R)} = \mathbf{h}_i^{(R)}$  for  $r = R, \ldots, 2$ . Then, using the



A Original patches

B Reconstructed patches

Typical prostate image patches (A) and their reconstructions (B) by using the unsupervised SSAE with four stacked SAEs.

reconstructed low-level representation  $\hat{h}_i^{(1)}$ , the original input vector could be estimated, i.e.,  $\hat{x}_i = \hat{W}^{(1)}\hat{h}_i^{(1)} + \hat{b}^{(1)}$ .

After stacking multiple SAEs together by feeding the output layer from the low-level SAE as the input layer of a high-level SAE, SSAE is able to extract more useful and general high-level features. In the optimization of SSAE, this deep architecture is first pre-trained in an unsupervised layer-wise manner and then fine-tuned by the back propagation. Since the aforementioned SSAE network is trained based only on the original image patches, without using the supervised label information, it is denoted as the *unsupervised SSAE*. Fig. 9.6 shows some typical prostate image patches and their reconstructions by the unsupervised SSAE with R=4.

However, since the unsupervised SSAE trains the whole network on the unlabeled data, the high-level features learned from unsupervised SSAE are only data-adaptive, that is, not necessarily discriminative to separate prostate and background voxels. To make the learned feature representation discriminative [33,34], the supervised finetuning is often adopted by stacking another classification output layer on the top of the encoding part of the SSAE, as shown in the red dashed box of Fig. 9.7. This top layer is used to predict the label likelihood of the input data  $x_i$  by using the features learned from the most high-level representation  $h_i^{(R)}$ . The number of nodes in the classification output layer equals to the number of labels (i.e., "1" denotes the prostate, and "0" denotes the background). Using the optimized parameters from the pre-training of SSAE as initialization, the entire neural network (Fig. 9.7) can be further fine-tuned by back-propagation to maximize the classification performance. This tuning step is referred to as the supervised fine-tuning, in contrast with the unsupervised fine-tuning mentioned before. Accordingly, the entire deep network is referred to as the supervised SSAE. Fig. 9.8 gives a visual illustration of typical feature representations of the first and second hidden layers learned by a four-layer supervised

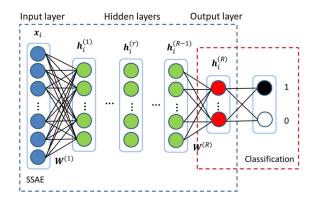


FIGURE 9.7

Construction of the supervised SSAE with a classification layer, which fine-tunes the SSAE with respect to the task of voxel-wise classification between prostate (label = 1) and background (label = 0).

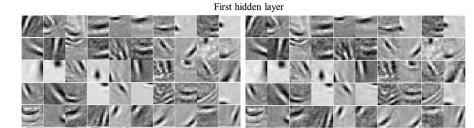
SSAE based on the visualization method in [35]. Here, Figs. 9.8A and 9.8B show the visualization of 60 units obtained from the first and second hidden layers under unsupervised pre-training (with unlabeled image patches) and supervised fine-tuning (with labeled image patches), respectively. It can be seen that higher hidden layer tends to be more affected by the classification layer we introduced.

After learning all the parameters  $\{\boldsymbol{W}^{(r)}, \boldsymbol{\hat{w}}^{(r)}, \boldsymbol{b}^{(r)}, \boldsymbol{\hat{b}}^{(r)}\}$  of SSAE  $(r=1,\ldots,R)$ , where R denotes the number of stacked SAEs, the high-level representations of a new image patch  $\boldsymbol{x}_{\text{new}}$  can be efficiently obtained by a forward pass, i.e.,  $\boldsymbol{h}_{\text{new}}^r = \sigma(\boldsymbol{W}^{(r)}\boldsymbol{h}_{\text{new}}^{(r-1)} + \boldsymbol{b}^{(r)})$  with  $\boldsymbol{h}_{\text{new}}^0 = \boldsymbol{x}_{\text{new}}$  for  $r=1,\ldots,R$ . The final high-level representation  $\boldsymbol{h}_{\text{new}}^R$  will be used as features to guide the sparse patch matching (Section 9.2.3), and propagate labels from atlas images to the target image for estimating the prostate likelihood map.

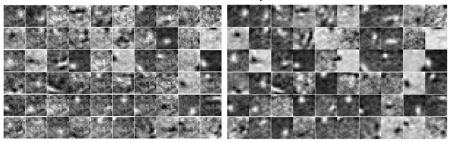
## 9.2.3 SEGMENTATION USING LEARNED FEATURE REPRESENTATION

**Sparse Patch Matching with the Deep-Learned Features.** Before sparse patch matching, all atlas images are registered to the target image. This registration includes two steps. First, linear registration is applied for initial alignment, with the guidance from the landmarks automatically detected around the prostate region [36]. Then, the free-form deformation (FFD) [37] is further adopted to the linearly-aligned images for deformable registration.

After learning the SSAE networks (either in unsupervised or supervised manner), each new image patch in the testing stage can be encoded as a high-level feature vector (i.e., the last hidden layer of the SSAE). These features can be fed into a segmentation framework for labeling voxels as either the prostate or the background. As one of the popular segmentation frameworks, multi-atlas based segmentation demon-



Second hidden layer



A Pre-training result

B Fine-tuning result

Visualization of typical feature representations of the first hidden layer (first row) and second hidden layer (second row) for the unsupervised pre-training (A) and supervised fine-tuning (B), respectively.

strates its effectiveness on dealing with image variations in different applications [38,39]. However, traditionally the multi-atlas based segmentation adopts only the intensity or handcrafted features for measuring the similarity between different local patches, or computing the weights of different patches during label propagation. Since MR prostate images exhibit large structural and appearance variations, we propose to incorporate the deep learning features, instead of the conventional handcrafted features, into the multi-atlas segmentation framework. As the features extracted by the deep learning methods are usually more robust and discriminative, the performance of multi-atlas segmentation can be improved at the same time. Fig. 9.9 gives the general description of our multi-atlas based method, called sparse patch matching. In this method, instead of computing pair-wise intensity similarity as a matching weight, we propose to select only a small number of similar atlas patches by sparse representation, which is more robust to outliers. In the following, we give the detailed description of our sparse patch matching method.

In order to estimate the prostate likelihood map of a target image  $I_s$ , we first align all the atlas images  $\{I_p, p = 1, ..., P\}$  and their label maps  $\{G_p, p = 1, ..., P\}$  onto the target image  $I_s$ . Then, to determine the prostate likelihood of a particular

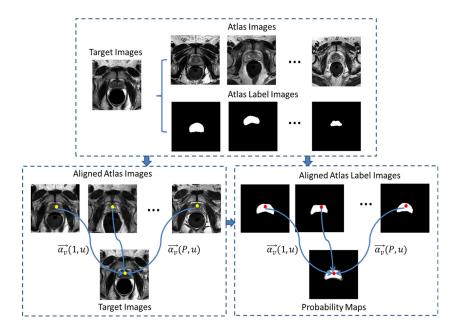


FIGURE 9.9

The schematic description of sparse patch matching.

voxel v in the target image  $I_s$ , we first extract the image patch centered at voxel v from the target image, and then all image patches within a certain searching neighborhood  $\mathbb{N}(v)$  across all the aligned atlas images.

Next, the deep-learned feature representations for those extracted intensity patches are obtained through the encoding procedure of the learned SSAE as introduced in Section 9.2.2. Denote  $f_s(v)$  as the deep-learned features for the target image patch at point v, and denote  $A_v$  as the feature matrix resulted from columnwise combination of deep-learned features of atlas patches, i.e.,  $A_v = [f_p(u) \mid p = 1, \ldots, P; u \in \mathbb{N}(v)]$ . To estimate the prostate likelihood  $Q_s(v)$  for voxel v in the target image  $I_s$ , we linearly combine the label of each voxel  $u \in \mathbb{N}(v)$  from each atlas image  $I_p$  with a weighting vector  $\boldsymbol{\alpha}_v = [\alpha_v(p, u)]_{u=1, \ldots, |\mathbb{N}(v)|; p=1, \ldots, P}$  as follows:

$$Q_s(v) = \frac{\sum_{p=1}^P \sum_{u \in \mathbb{N}(v)} \alpha_v(p, u) \times G_p(u)}{\sum_{p=1}^P \sum_{u \in \mathbb{N}(v)} \alpha_v(p, u)}.$$
 (9.3)

According to Eq. (9.3), it is easy to see that the robustness and accuracy of prostate likelihood estimation depend on how well the weighting vector  $\boldsymbol{\alpha}_v$  is determined. In the literature, different weight estimation methods have been proposed [40,41]. Most multi-atlas based segmentation methods directly compute  $\boldsymbol{\alpha}_v$  as the pair-wise similarity between intensity patches, such as using the Euclidean distance. In our method, we compute the weighting vector  $\boldsymbol{\alpha}_v$  different from the previous methods in respect to

the following two aspects. *First*, instead of using the intensity or handcrafted features, the high-level features are learned from the deep learning architecture. *Second*, with the help of recently proposed sparse representation method [4], we enforce sparsity constraint upon the weighting vector  $\boldsymbol{\alpha}_{v}$ . In this way, we seek for the best representation of the target patch using a limited set of similar atlas patches. Mathematically, the optimization of  $\boldsymbol{\alpha}_{v}$  can be formulated as the sparse representation problem below:

$$\alpha_{v} = \arg\min_{\alpha_{v}} \frac{1}{2} \| f_{s}(v) - A_{v} \alpha_{v} \|_{2}^{2} + \eta \| \alpha_{v} \|_{1} \quad \text{s.t. } \alpha_{v} \ge 0$$
 (9.4)

The first term is the data fitting term, which measures difference between the target feature vector  $f_s(v)$  and the linearly combined feature representation  $A_v\alpha_v$  from all atlas image patches. The second term is the sparsity term, which attributes to the sparsity property of the weighting vector  $\alpha_v$ .  $\eta$  controls the strength of sparsity constraint on the weighting vector  $\alpha_v$ . If  $\eta$  is larger, the number of nonzero elements in  $\alpha_v$  will be smaller. In this way, only a few patches in patch dictionary  $A_v$  will be selected to reconstruct the target features  $f_s(v)$  in a nonparametric fashion, thus reducing the risk of including those misleading atlas patches in the likelihood estimation.

Based on the derived weighting vector  $\alpha_v$ , the prostate likelihood  $Q_s(v)$  for a target point v can be estimated by Eq. (9.3). Since the weighting vector  $\alpha_v$  is sparse, the prostate likelihood  $Q_s(v)$  is finally determined by the linear combination of labels corresponding to atlas patches with nonzero elements in vector  $\alpha_v$ . After estimating the prostate likelihood for all voxels in the target image  $I_s$ , a likelihood map  $Q_s$  is generated, which can be used to robustly locate the prostate region (as shown in Fig. 9.9). Usually, a simple thresholding or level set method [42,43] can be applied to binarize the likelihood map for segmentation. However, since each voxel in the target image is independently estimated in the multi-atlas segmentation method, the final segmentation could be weird as no shape prior is considered. To robustly and accurately estimate the final prostate region from the prostate likelihood map, it is necessary to take into account the prostate shape prior during the segmentation.

**Data and Shape Driven Deformable Model.** The main purpose of this section is to segment the prostate region based on the prostate likelihood map estimated in the previous section. The likelihood map can be used in two aspects of deformable model construction. First, the initialization of deformable model can be easily built by thresholding the likelihood map. In this way, the limitation of model initialization problem in the traditional deformable segmentation can be naturally relieved. Second, the likelihood map can be used as the appearance force to drive the evolution of the deformable model. Besides, in order to deal with large inter-patient shape variation, we propose to use sparse shape prior for deformable model regularization.

Here, our deformable model is represented by a 3D surface, which is composed of K vertices  $\{d_k \mid k = 1, ..., K\}$ . After concatenating these K vertices  $\{d_k \mid k = 1, ..., K\}$  into a vector d, each deformable model can be represented as a shape vector with length of  $3 \cdot K$ . Let D denote a large shape dictionary that includes prostate shape vectors of all training subjects. Each column of shape dictionary D

corresponds to the shape vector of one subject. The shape dictionary can be used as a shape prior to constrain the deformable model in a learned shape space. Instead of assuming the Gaussian distribution of shapes and then simply using PCA for shape modeling as done in the Active Shape Model [44], we adopt a recently proposed method, named sparse shape composition [45], for shape modeling. In the sparse shape composition, the shapes are sparsely represented by shape instances in the shape dictionary without the need of the Gaussian assumption. Specifically, given a new shape vector d and shape dictionary D, sparse shape composition method reconstructs shape vector d as the sparse representation of shape dictionary D by minimizing the following objective function:

$$(\boldsymbol{\varepsilon}, \psi) = \arg\min_{\boldsymbol{\varepsilon}, \psi} \|\psi(\boldsymbol{d}) - \boldsymbol{D}\boldsymbol{\varepsilon}\|_{2}^{2} + \mu \|\boldsymbol{\varepsilon}\|_{1}$$
 (9.5)

where  $\psi(d)$  denotes the target shape d that is affine aligned onto the mean shape space of shape dictionary D.  $\varepsilon$  indicates the sparse coefficient for the linear shape combination. Once  $(\varepsilon, \psi)$  are estimated by Eq. (9.5), the regularized shape can be computed by  $\psi^{-1}(D\varepsilon)$ , where  $\psi^{-1}$  is the inverse affine transform of  $\psi$ .

For each target image, the segmentation task is formulated as the deformable model optimization problem. During the optimization procedure, each vertex of deformable model  $d_k$  is driven iteratively by the information from both prostate likelihood map and shape model until converged at the prostate boundaries. Mathematically, the evolution of the deformable model can be formulated as the minimization of an energy function, which contains a data energy  $E_{\rm data}$  and a shape energy  $E_{\rm shape}$  as in Eq. (9.6):

$$E = E_{\text{data}} + \lambda E_{\text{shape}}.$$
 (9.6)

The data term  $E_{\text{data}}$  is used to attract the 3D surface toward the object boundary based on the likelihood map. Specifically, each vertex  $d_k$  is driven by the force related to the gradient vector of prostate likelihood map. Denote  $\overrightarrow{\nabla Q}_s(d_k)$  as the gradient vector at vertex  $d_k$  in the prostate likelihood map, and  $\vec{n}_s(d_k)$  as the normal vector on the vertex  $d_k$  of surface. When vertex  $d_k$  deforms exactly to the prostate boundary and also its normal direction aligns with the gradient direction of prostate boundary, the local matching term  $\langle \overrightarrow{\nabla Q}_s(d_k), \vec{n}_s(d_k) \rangle$  is maximized. In this way, we formulate to minimize the data energy  $E_{\text{data}}$  as

$$E_{\text{data}} = -\sum_{k} \langle \overrightarrow{\nabla Q}_{s}(\boldsymbol{d}_{k}), \overrightarrow{n}_{s}(\boldsymbol{d}_{k}) \rangle. \tag{9.7}$$

Since all the vertices on the deformable model are jointly evolved during the deformation, the matching of the deformable model with the prostate boundary will be robust to possible incorrect likelihood on some vertices, as well as inconsistency between neighboring vertices.

The shape term  $E_{\text{shape}}$  is used to encode the geometric property of the prostate shape based on the estimated coefficient  $\varepsilon$  and the transformation  $\varphi$  in Eq. (9.5).

Specifically, the shape term is formulated as follows:

$$E_{\text{shape}} = \left\| \boldsymbol{d} - \psi^{-1}(\boldsymbol{D}\boldsymbol{\varepsilon}) \right\|_{2}^{2} + \beta \sum_{k} \left\| \boldsymbol{d}_{k} - \frac{\sum_{d_{j} \in \mathbb{N}(\boldsymbol{d}_{k})} \boldsymbol{d}_{k}}{\sum_{d_{j} \in \mathbb{N}(\boldsymbol{d}_{k})} \boldsymbol{1}} \right\|_{2}^{2}$$
(9.8)

where the first term constrains the deformed shape d to be close to the regularized shape  $\psi^{-1}(\mathbf{D}\varepsilon)$  by the sparse shape composition, and the second term imposes the smoothness constraint on shape, which prevents large deviations between each vertex  $d_k$  and the center of its neighboring vertices  $d_i \in \mathbb{N}(d_k)$ .

By combining Eq. (9.7) and Eq. (9.8) into Eq. (9.6), the vertices of the deformable model are iteratively driven toward the prostate boundary while constraining the shape in a nonparametric shape space.

## 9.3 EXPERIMENTS

We evaluate our method on the dataset, which includes 66 T2-weighted MR images from the University of Chicago Hospital. The images are acquired with 1.5 T magnetic field strength from different patients under different MR image scanners (34 images from Philips Medical Systems and 32 images from GE Medical Systems). Under this situation, the difficulty for the segmentation task increases since both shape and appearance differences are large. In Fig. 9.10, images B and E were acquired from a GE MRI scanner, while the other three were acquired from a Philips MRI scanner. As shown in Fig. 9.10, image C was obtained without the endorectal coil. It has a different prostate shape with other four images acquired with the endorectal coil. Besides, the prostate appearance suffers from the inhomogeneity (as in B and D) and noise (as in D and E), which further result in large variations. The image dimension and spacing are different from image to image. For example, the image dimension varies from  $256 \times 256 \times 28$  to  $512 \times 512 \times 30$ . The image spacing varies from  $0.49 \times 0.49 \times 3$  mm to  $0.56 \times 0.56 \times 5$  mm. The manual delineation of the prostate in each image is provided by a clinical expert as the ground truth for quantitative evaluation. As the preprocessing of the dataset, the bias field correction [46] and histogram matching [47] are applied to each image successively. We adopted a two-fold cross-validation. Specifically, in each case, the images of one fold are used for training the models, while the images of the other fold are used for testing the performance.

The parameters for deep feature learning are listed below. The patch size is  $15 \times 15 \times 9$ . The number of layers in SSAE framework is 4. The number of nodes in each layer of SSAE is 800, 400, 200, and 100, respectively. Thus, the deep-learned features have the dimensionality of 100. The target activation  $\rho$  for the hidden units is 0.15. The sparsity penalty  $\beta$  is 0.1. The Deep Learning Toolbox [48] is used for training our SSAE framework.

The searching neighborhood  $\mathbb{N}(v)$  is defined as the  $7 \times 7 \times 7$  neighborhood centered at voxel v. For sparse patch matching, the parameter  $\eta$  in Eq. (9.4), which con-











Five typical T2-weighted MR prostate images acquired from different scanners, showing large variations of both prostate appearance and shape, especially for the cases with or without using the endorectal coils.

**Table 9.1** Definitions of four evaluation measurements

Dice ratio	$\frac{2 \cdot V(S \cap F)}{V(S) + V(F)}$
Precision	$\frac{V(S \cap F)}{V(F)}$
Hausdorff distance	$\max(H(e_S, e_F), H(e_S, e_F)),$
	$H(e_S, e_F) = \max_{d_i \in e_S} \left\{ \min_{d_j \in e_F} \operatorname{dist}(d_i, d_j) \right\}$
Average surface distance	$\frac{1}{2} \left( \frac{\sum_{d_i \in e_S} \min_{d_j \in e_F} \operatorname{dist}(d_i, d_j)}{\sum_{d_i \in e_S} 1} + \frac{\sum_{d_j \in e_F} \min_{d_i \in e_S} \operatorname{dist}(d_j, d_i)}{\sum_{d_j \in e_F} 1} \right)$

S, ground truth segmentation; F, automatic segmentation; V, volume size;  $e_S$ , surfaces of ground-truth segmentation;  $e_F$ , surface of automatic segmentation;  $d_i$ , vertices on the surfaces  $e_S$ ;  $d_j$ , vertices on the surfaces  $e_F$ ;  $\operatorname{dist}(d_i, d_j)$ , Euclidean distance between vertices  $d_i$  and  $d_j$ .

trols the sparsity constraint, is 0.001. For the final deformable model segmentation, the parameter  $\lambda$  in Eq. (9.6), which weights the shape energy during deformation, is 0.5, and the parameter  $\mu$  in Eq. (9.5) is 0.5.

Given the ground-truth segmentation S and the automatic segmentation F, the segmentation performance is evaluated by four metrics: Dice ratio, precision, Hausdorff distance, and average surface distance. Dice ratio and precision measure the overlap between two segmentations. Hausdorff distance and average surface distance measure the boundary distance between two surfaces of segmentation. Detailed definitions are given as Table 9.1.

# 9.3.1 EVALUATION OF THE PERFORMANCE OF DEEP-LEARNED FEATURES

Inspired by [49], we plot the PCA-projected features to show the effectiveness of different features in separating voxels from different classes (e.g., the prostate class and the non-prostate class). After mapping each feature vector to the subspace spanned by the first three principal components, the effective features would (i) cluster the voxels with the same class label as close as possible and (ii) separate the voxels with different class labels as far as possible. First, we demonstrate the discrimination power of our deep learning features in Fig. 9.11, by visualizing the PCA-projected feature dis-

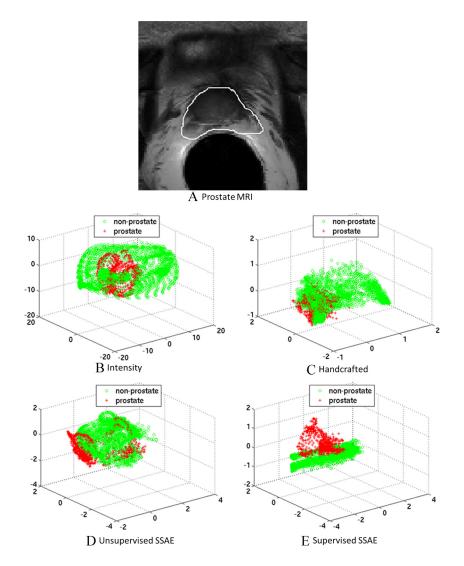
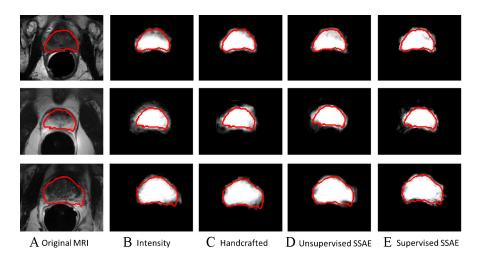


FIGURE 9.11

Distributions of voxel samples by using four types of features: (A) a typical slice of prostate MRI with white contour as ground truth, (B) intensity, (C) handcrafted, (D) unsupervised SSAE, and (E) supervised SSAE. Red crosses and green circles denote prostate and non-prostate voxel samples, respectively.

tributions of different feature representations of a typical prostate MRI (Fig. 9.11A), i.e., intensity patch (Fig. 9.11B), handcrafted (Fig. 9.11C), features learned by unsupervised SSAE (Fig. 9.11D), and features learned by supervised SSAE (Fig. 9.11E).



**FIGURE 9.12** 

(A) Typical slices of T2 MR images with manual segmentations. The likelihood maps produced by sparse patch matching with four feature representations: (B) intensity patch, (C) handcrafted, (D) unsupervised SSAE, and (E) supervised SSAE. Red contours indicate the manual ground-truth segmentations.

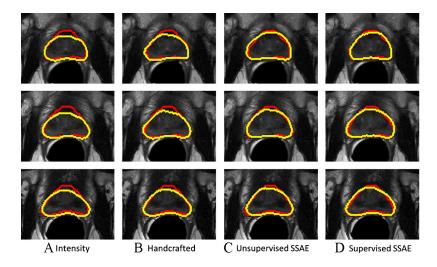
Specifically, for the case of handcrafted features, we include three commonly used features, i.e., Haar [50], HoG [47], and LBP [21]. The same patch size is used for computing all features under comparison. It can be seen that the deep-learned features from supervised SSAE have better clustering results in the projected feature space, and thus better discriminative power than other two predefined features (i.e., intensity and handcrafted), as well as deep-learned features by unsupervised SSAE. The superior performance of supervised SSAE over the unsupervised SSAE indicates the necessity of utilizing label information to improve the discrimination power of learned features.

Next, we evaluate the segmentation accuracy of different feature representations in the context of sparse patch matching. Table 9.2 lists the quantitative results (Dice ratio, precision, Hausdorff distance, and average surface distance) for all feature representations. The *p*-values (computed with paired t-test at 5% significance level), comparing the supervised SSAE with all other methods, are provided below each quantitative result. It can be observed that our supervised SSAE method significantly outperforms all the intensity and handcrafted feature methods. According to the paired t-test at 5% significance level, both our proposed methods (unsupervised and supervised SSAE) outperform the rest of competing method, but the supervised SSAE is not statistically superior to the unsupervised SSAE.

Fig. 9.12 further shows the typical likelihood maps estimated by four different feature representations for three different patients. It can be observed that the features learned from supervised SAE can better capture the prostate boundary, especially on

**Table 9.2** The mean and standard deviation of quantitative results for MR prostate segmentation with different feature representations. Best performance is indicated by bold font

Method	Intensity	Haar	HOG	LBP	Handcraft	Unsupervised SSAE	Supervised SSAE
Dice (%)	$85.3 \pm 6.2$	$85.6 \pm 4.9$	$85.7 \pm 4.9$	$85.5 \pm 4.3$	$85.9 \pm 4.5$	$86.7 \pm 4.4$	$\textbf{87.1} \pm \textbf{4.2}$
	(1.1e-04)	(2.2e-05)	(6.1e-05)	(5.5e-05)	(7.0e-06)	(2.1e-01)	(NA)
Precision (%)	$85.1 \pm 8.3$	$85.9 \pm 8.5$	$85.3 \pm 8.7$	$83.7 \pm 7.7$	$87.3 \pm 7.4$	$\textbf{87.3} \pm \textbf{7.3}$	$87.1 \pm 7.3$
	(1.9e-03)	(3.63e-02)	(4.5e-03)	(1.3e-06)	(7.0e-01)	(7.3e-01)	(NA)
Hausdorff	$8.68 \pm 4.24$	$8.50 \pm 2.86$	$8.51 \pm 2.69$	$8.59 \pm 2.38$	$8.55 \pm 2.91$	$8.65 \pm 2.69$	$\textbf{8.12} \pm \textbf{2.89}$
	(1.8e-01)	(1.9e-01)	(1.6e-01)	(1.1e-01)	(1.5e-01)	(6.3e-02)	(NA)
ASD	$1.87 \pm 0.93$	$1.76 \pm 0.52$	$1.74 \pm 0.50$	$1.75 \pm 0.44$	$1.77 \pm 0.54$	$1.68 \pm 0.49$	$\boldsymbol{1.66 \pm 0.49}$
	(6.0e-03)	(8.9e-03)	(3.1e-02)	(2.5e-02)	(5.0e-04)	(5.8e-01)	(NA)

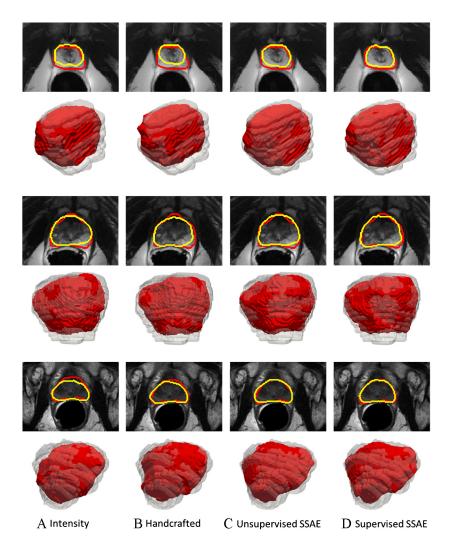


Typical prostate segmentation results of the same patients produced by four different feature representations: (A) intensity, (B) handcrafted, (C) unsupervised SSAE, and (D) supervised SSAE. Three rows show the results for three different slices of the same patient, respectively. Red contours indicate the manual ground-truth segmentations, and yellow contours indicate the automatic segmentations.

the anterior and right posterior parts of the prostate. Fig. 9.13 shows some typical segmentation results obtained by the sparse label matching method with four different feature representations, respectively. Similarly, the proposed method (i.e., supervised SSAE) achieves the best segmentation, especially on the anterior parts of the prostate, which demonstrates the effectiveness of our proposed method. Moreover, Fig. 9.14 gives the typical prostate segmentation results of different patients produced by four different feature representations, respectively. 3D visualization of the segmentation result has been provided below each segmentation result shown in 2D. For 3D visualization in each row, the red surface indicates automatic segmentation results with different features, such as intensity, handcrafted, unsupervised SSAE and supervised SSAE, respectively. The transparent gray surfaces indicate the ground-truth segmentations. Our proposed supervised SSAE method improves the segmentation accuracy on both the anterior and posterior parts of prostates.

## 9.3.2 EVALUATION OF THE PERFORMANCE OF DEFORMABLE MODEL

In this section, we further evaluate our deformable model to show its effectiveness. The comparison methods contain three different deformable model based methods. The first one is the conventional Active Shape Model (ASM). The second one uses intensity features for multi-atlas label fusion and then finalizes the segmentation by



Typical prostate segmentation results of three different patients produced by four different feature representations: (A) intensity, (B) Handcrafted, (C) unsupervised SSAE, and (D) supervised SSAE. The three odd rows show the results for three different patients, respectively. Red contours indicate the manual ground-truth segmentations, and yellow contours indicate the automatic segmentations. The three even rows show the 3D visualization of the segmentation results corresponding to the images above. For 3D visualizations in each row, the red surfaces indicate the automatic segmentation results using different features, such as intensity, handcrafted, unsupervised SSAE and supervised SSAE, respectively. The transparent gray surfaces indicate the ground-truth segmentations.

**Table 9.3** Mean and standard deviation of quantitative results for the segmentations obtained by supervised SSAE with/without using deformable model (DM). The best performance is indicated by bold font. \* denotes the statistically best performance among all the methods with/without deformable model (according to the paired t-test at 5% significant level)

Method	ASM	Intensity		Handcrafted		Supervised SSAE	
		w/o DM	w/ DM	w/o DM	w/ DM	w/o DM	w/ DM*
Dice (%)	$78.4 \pm 9.7$	$85.3 \pm 6.2$	$86.0 \pm 4.3$	$85.9 \pm 4.5$	$86.4 \pm 4.4$	$87.1 \pm 4.2$	$\textbf{87.8} \pm \textbf{4.0}^*$
	(2.7e-11)	(3.0e-06)	(7.3e-10)	(7.7e-08)	(5.1e-06)	(2.6e-03)	(NA)
Precision (%)	$71.9 \pm 13.8$	$85.1 \pm 8.3$	$89.3 \pm 7.4$	$87.3 \pm 7.4$	$92.3 \pm 7.3$	$87.1 \pm 7.3$	$91.6 \pm 6.5$
	(1.3e-21)	(8.0e-17)	(4.5e-07)	(1.4e-11)	(7.7e-02)	(5.7e-20)	(NA)
Hausdorff	$11.50 \pm 5.48$	$8.68 \pm 4.24$	$7.72 \pm 2.90$	$8.55 \pm 2.91$	$7.97 \pm 2.92$	$8.12 \pm 2.89$	$\textbf{7.43} \pm \textbf{2.82}^*$
	(8.5e-07)	(3.6e-04)	(2.5e-02)	(3.8e-05)	(1.2e-04)	(7.4e-03)	(NA)
ASD	$3.12 \pm 1.71$	$1.87 \pm 0.93$	$1.78 \pm 0.55$	$1.77 \pm 0.54$	$1.71 \pm 0.50$	$1.66 \pm 0.49$	$\textbf{1.59} \pm \textbf{0.51}^*$
	(9.4e-10)	(6.4e-04)	(2.0e-07)	(2.0e-05)	(1.3e-03)	(1.6e-02)	(NA)

adopting a deformable model on the produced likelihood map, similar to our proposed method. The second method follows the same procedure as the first one except using the handcrafted features, such as Haar, HOG, and LBP, instead of intensity patch for multi-atlas label fusion. Table 9.3 shows the segmentation results of intensity, handcrafted and supervised SSAE with/without deformable model and the *p*-value (with paired t-test at 5% significance level) between the supervised SSAE with deformable model and all other methods. According to the paired t-test at 5% significance level on Dice ratio, our proposed deformable model is statistically the best among all the competing methods. Specifically, our proposed supervised SAE outperforms the ASM, the intensity based deformable model, and the handcrafted based deformable model by DSC 10.7%, 2.1%, and 1.6%, respectively. Besides, it can be seen that, after adopting the second level of deformable segmentation, the segmentation accuracy can be further improved for all the comparing methods.

## 9.4 CONCLUSION

In this book chapter, we present an automatic segmentation algorithm for T2 MR prostate images. To address the challenges of making the feature representation robust to large appearance variations of the prostate, we propose to extract the deep-learned features by the SSAE framework. Then, the learned features are used under sparse patch matching framework to estimate the prostate likelihood map of the target image. To further relieve the impact of large shape variation in the prostate shape repository, a deformable model is driven toward the prostate boundary under the guidance from the estimated prostate likelihood map and sparse shape prior. The proposed method is extensively evaluated on the dataset containing 66 prostate MR images. By comparing with several state-of-the-art MR prostate segmentation methods, our method demonstrates superior performance in term of segmentation accuracy.

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