

CLAUDIORDGZ

Solutions of Data Structures and Algorithms in Python

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Python Primer

The first chapter in the book is all about learning to handle Python syntax. Subjects include objects, control flow, functions, I/O operations, exceptions, iterators and generators, namespaces, modules, and scope. There is nothing regarding python packaging to redistribute your own module, which is a subject of its own.

1.1. Format

All exercises will be presented with their own Python Doctest documentation to allow testing. To run them in your own python package you can copy paste the text and add a main like the following:

```
DoctestMain
```

```
if __name__ == "__main__":
    import doctest
    doctest.testmod()
```

This is just to try to keep it as simple as possible while adding how to run the code in your own work environment.

Pro-Tip. JetBrains Pycharm is awesome, I really recommend it, plus they got a Community Edition if you are pennyless like me. The colors, the functionality it just rocks. **Plus the IDE can run the examples without the need of using a main function.**

Pro-Tip. I like to use Anaconda for my Python distro, but the standalone Python 2.7 or ≥ 3 works too.

1.1.1 Exercises

The exercises in the first chapter are fun, no joke. I've seen what's coming in chapter 2 and those exercises look terrible because they are open ended questions, but they are also important concepts.

R-1.1

Write a short Python function, `is_multiple(n, m)`, that takes two integer values and returns `True` if n is a multiple of m , that is, $n = mi$ for some integer i , and `False` otherwise.

Exercise R-1.1

```
"""Write a short Python function, is_multiple(n, m), that takes two integer
values and returns True if n is a multiple of m, that is, n = mi for some
integer i, and False otherwise.
```

```
>>> is_multiple(50,3)
False
"""
```

```
def is_multiple(n, m):
    """Return True if n is multiple of m such that n = mi
    Else returns False

    >>> is_multiple(50,3)
    False
    >>> is_multiple(60,3)
    True
    >>> is_multiple(70,3)
    False
    >>> is_multiple(-50,2)
    True
    >>> is_multiple(-60,2)
    True
    >>> is_multiple("test",10)
    Numbers must be Integer values
    >>> is_multiple(-60,"test")
    Numbers must be Integer values
    """

    try:
        return True if (int(n) % int(m) == 0) else False
    except ValueError:
        print("Numbers must be Integer values")
```

R-1.2

Write a short Python function, `is_even(k)`, that takes an integer value and returns `True` if k is even, and `False` otherwise. However, your function cannot use the multiplication, modulo, or division operators.

Exercise R-1.2

"""Write a short Python function, is_even(k), that takes an integer value and returns True if k is even, and False otherwise. However, your function cannot use the multiplication, modulo, or division operators

```
>>> is_even(127)
False
"""
```

```
def is_even(k):
    """Return True if n is even
    Else returns False

    >>> is_even(10)
    True
    >>> is_even(9)
    False
    >>> is_even(11)
    False
    >>> is_even(13)
    False
    >>> is_even(1025)
    False
    >>> is_even("test")
    Number must be Integer values
    """
```

```
try:
    return int(k) & 1 == 0
except ValueError:
    print("Number must be Integer values")
```

R-1.3

Write a short Python function, `minmax(data)`, that takes a sequence of one or more numbers, and returns the smallest and largest numbers, in the form of a tuple of length two. Do not use the built-in functions `min` or `max` in implementing your solution.

Exercise R-1.3

""" Write a short Python function, minmax(data), that takes a sequence of one or more numbers, and returns the smallest and largest numbers, in the form of a tuple of length two. Do not use the built-in functions min or max in implementing your solution.

```
>>> print(minmax([2,3,4,5,6,7,8,9,10,11,10,9,8,7,6,5,4,3,2,1]))
Min 1 - Max 11
"""
```

```
class MinMax():
```

```
    """MinMax object helper
```

```

    Attributes:
```

```
        min (int): Minimum value of attributes
```

```
        max (max): Maximum value of attributes
```

```
    """
```

```
    def __init__(self, min, max):
```

```
        """ Default Constructor
```

```

        Args:
```

```
            min (int): Number with lesser value
```

```
            max (int): Number with higher value
```

```
    """
```

```
        self.min = min
```

```
        self.max = max
```

```
    def __str__(self):
```

```
        """String representation overload
```

```
    """
```

```
        return "Min {min} - " \
               "Max {max}".format(min=str(self.min),
                                   max=str(self.max))
```

```
def minmax(data):
```

```
    """This is the algorithm to find the
```

minimum and maximum in a list.

Args:

*data (list of int): Simple array of
Integers*

Returns:

*A tuple MinMax that holds the minimum
and maximum values found in the list*

Examples:

Here are some examples!

```
>>> print(minmax([2,3,4,5,6,7,8,9,10,11,10,9,8,7,6,5,4,3,2,1]))
Min 1 - Max 11
>>> print(minmax([50,200,300,3,78,19203,56]))
Min 3 - Max 19203
>>> print(minmax([100,150,200,500]))
Min 100 - Max 500
"""

start = 0
mm = MinMax(data[start], data[start])
if len(data) & 1 == 1:
    if data[start] < data[start+1]:
        mm.max = data[start+1]
        mm.min = data[start]
        start += 2
    else:
        start += 1
for index in range(start, len(data[start:]), 2):
    if data[index] < data[index+1]:
        l_min = data[index]
        l_max = data[index+1]
    else:
        l_min = data[index+1]
        l_max = data[index]
    if mm.min > l_min:
        mm.min = l_min
    if mm.max < l_max:
        mm.max = l_max
return mm
```

R-1.4 & R-1.5

Write a short Python function that takes a positive integer n and returns the sum of the squares of all the positive integers smaller than n .

Give a single command that computes the sum from Exercise R-1.4, relying on Python's comprehension syntax and the built-in sum function.

Exercise R-1.4 & R-1.5

""" Write a short Python function that takes a positive integer n and returns the sum of the squares of all the positive integers smaller than n.

Give a single command that computes the sum from Exercise R-1.4, relying on Python's comprehension syntax and the built-in sum function.

```
>>> sum_of_squares(10)
285
"""
```

```
def sum_of_squares(n):
    """Sum of squares of positive integers
    smaller than n

    Args:
        n (int): Highest number

    >>> sum_of_squares(10)
    285
    >>> sum_of_squares(20)
    2470
    >>> sum_of_squares(500)
    41541750
    >>> sum_of_squares(37)
    16206
    >>> sum_of_squares(-1)
    False
    """
    return sum([pow(x,2) for x in range(n)]) if n > 0 else False
```


R-1.6 & R-1.7

Write a short Python function that takes a positive integer n and returns the sum of the squares of all the odd positive integers smaller than n .

Give a single command that computes the sum from Exercise R-1.6, relying on Python's comprehension syntax and the built-in sum function.

Exercise R-1.6 & R-1.7

```
"""Write a short Python function that takes a positive integer n and returns
the sum of the squares of all the odd positive integers smaller than n.
```

```
Give a single command that computes the sum from Exercise R-1.6, relying on
Python's comprehension syntax and the built-in sum function.
```

```
"""
```

```
def sum_of_odd_squares(n):
    """Sum of squares of odd postive integers
    smaller than n
```

```
    Args:
```

```
        n (int): Highest number
```

```
>>> sum_of_odd_squares(10)
```

```
165
```

```
>>> sum_of_odd_squares(20)
```

```
1330
```

```
>>> sum_of_odd_squares(500)
```

```
20833250
```

```
>>> sum_of_odd_squares(37)
```

```
7770
```

```
>>> sum_of_odd_squares(-1)
```

```
False
```

```
"""
```

```
return sum([pow(x,2) for x in range(1, n, 2)]) if n > 0 else False
```

R-1.8

Python allows negative integers to be used as indices into a sequence, such as a string. If string s has length n , and expression $s[k]$ is used for index $-n \leq k < 0$, what is the equivalent index $j \geq 0$ such that $s[j]$ references the same element?

Exercise R-1.8

```
"""Python allows negative integers to be used as indices into a sequence,
such as a string. If string s has length n, and expression s[k] is used for in-
dex -n<=k<0, what is the equivalent index j>=0such that s[j] references
the same element?
```

```
>>> l = [2,3,4,5,6,7,8,9,10,11,10,9,8,7,6,5,4,3,2,1]
>>> return_element(l, 0)
(2, -20)
>>> return_element(l, 1)
(3, -19)
>>> return_element(l, 2)
(4, -18)
"""
```

```
def return_element(data, k):
    """Tells you the equivalent negative index
```

Args:

data (list of int): Simple array
k (int): index you want to know
the equivalent negative index

Returns:

(val, index)
val (object): element at position k
index: negative index of that position

Examples:

Here are some examples!

```
>>> l = [2,3,4,5,6,7,8,9,10,11,10,9,8,7,6,5,4,3,2,1]
>>> return_element(l, 0)
(2, -20)
>>> return_element(l, 1)
(3, -19)
```

```
>>> return_element(1, 2)
(4, -18)
"""
idx = k-len(data)
return data[idx], idx if data else False
```

R-1.9

What parameters should be sent to the range constructor, to produce a range with values 50, 60, 70, 80?

Exercise R-1.9

"""What parameters should be sent to the range constructor, to produce a range with values 50, 60, 70, 80?

```
>>> range_from_fifty()
[50, 60, 70, 80]
"""
```

```
def range_from_fifty():
    """ Creates a list
    with values 50, 60, 70, 80
```

```

    Returns:
        list: [50, 60, 70, 80]
```

```
>>> range_from_fifty()
[50, 60, 70, 80]
"""
```

```
return range(50,81,10)
```

R-1.10

What parameters should be sent to the range constructor, to produce a range with values 8, 6, 4, 2, 0, -2, -4, -6, -8?

Exercise R-1.10

```
""" What parameters should be sent to the range constructor, to produce a
range with values 8, 6, 4, 2, 0, -2, -4, -6, -8?
```

```
>>> range_from_eigth()
[8, 6, 4, 2, 0, -2, -4, -6, -8]
"""
```

```
def range_from_eigth():
    """ Return the list [8, 6, 4, 2, 0, -2, -4, -6, -8]
    :return:
        the list [8, 6, 4, 2, 0, -2, -4, -6, -8]
    >>> range_from_eigth()
    [8, 6, 4, 2, 0, -2, -4, -6, -8]
    """
    return range(8, -9, -2)
```

R-1.11

Demonstrate how to use Python's list comprehension syntax to produce the list [1, 2, 4, 8, 16, 32, 64, 128, 256].

Exercise R-1.11

```
"""Demonstrate how to use Python's list
comprehension syntax to produce the list
[1, 2, 4, 8, 16, 32, 64, 128, 256].
```

```
>>> list_comprehension_example()
[1, 2, 4, 8, 16, 32, 64, 128, 256]
"""
```

```
def list_comprehension_example():
    """ Return list
    [1, 2, 4, 8, 16, 32, 64, 128, 256]

    :return:
        list: [1, 2, 4, 8, 16, 32, 64, 128, 256]
```

```
>>> list_comprehension_example()
[1, 2, 4, 8, 16, 32, 64, 128, 256]
"""
return [pow(2,x) for x in range(9)]
```

This is a random method, I usually stress test anything that is random since I am always uneasy about it.

Exercise R-1.12

```
>>> data = [2,3,4,5,6,7,8,9,10,11,10,9,8,7,6,5,4,3,2,1]
>>> results = list()
>>> for x in range(len(data)*20):
...     val = custom_choice(data)
...     results.append(val in data)
>>> print(results)
```

[illegible]

```
def custom_choice(data):
    import random
    return data[random.randrange(0, len(data))]
```


C-1.13

Write a pseudo-code description of a function that reverses a list of n integers, so that the numbers are listed in the opposite order than they were before, and compare this method to an equivalent Python function for doing the same thing.

Exercise C-1.13

"""Write a pseudo-code description of a function that reverses a list of n integers, so that the numbers are listed in the opposite order than they were before, and compare this method to an equivalent Python function for doing the same thing.

```
>>> l1 = [2,3,4,5,6,7,8,9,10,11,10,9,8,7,6,5,4,3,2,1]
>>> custom_reverse(l1)
[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 10, 9, 8, 7, 6, 5, 4, 3, 2]
"""

import cProfile

def custom_reverse(data):
    """ Reverse the data array

    :param data: a list of elements
    :return: reverse list

    >>> l1 = [2,3,4,5,6,7,8,9,10,11,10,9,8,7,6,5,4,3,2,1]
    >>> custom_reverse(l1)
    [1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 10, 9, 8, 7, 6, 5, 4, 3, 2]
    """

    return [data[len(data)-x-1] for x in range(len(data))]

def standard_reverse(data):
    return reversed(data)

def other_reverse(data):
    return data[::-1]

if __name__ == "__main__":
    l1 = [2,3,4,5,6,7,8,9,10,11,10,9,8,7,6,5,4,3,2,1]
    l2 = [2,3,4,5,6,7,8,9,10,11,10,9,8,7,6,5,4,3,2,1]
    l3 = [2,3,4,5,6,7,8,9,10,11,10,9,8,7,6,5,4,3,2,1]
    cProfile.run('custom_reverse(l1)')
```

```
cProfile.run('standard_reverse(12)')
cProfile.run('other_reverse(13)')
```

cProfile Results

Here is a simple cProfile with the results. Time shows as 0.000 but the number of function calls tell us our implementation is not that good.

25 function calls in 0.000 seconds

Ordered by: custom_reverse

ncalls	tottime	percall	cumtime	percall	filename:lineno(function)
1	0.000	0.000	0.000	0.000	<string>:1(<module>)
1	0.000	0.000	0.000	0.000	c113.py:14(custom_reverse)
21	0.000	0.000	0.000	0.000	len
1	0.000	0.000	0.000	0.000	method 'disable' of '_lsprof.Profiler' objects
1	0.000	0.000	0.000	0.000	range

3 function calls in 0.000 seconds

Ordered by: standard_reverse

ncalls	tottime	percall	cumtime	percall	filename:lineno(function)
1	0.000	0.000	0.000	0.000	<string>:1(<module>)
1	0.000	0.000	0.000	0.000	c113.py:26(standard_reverse)
1	0.000	0.000	0.000	0.000	method 'disable' of '_lsprof.Profiler' objects

3 function calls in 0.000 seconds

Ordered by: other_reverse

ncalls	tottime	percall	cumtime	percall	filename:lineno(function)
1	0.000	0.000	0.000	0.000	<string>:1(<module>)
1	0.000	0.000	0.000	0.000	c113.py:29(other_reverse)
1	0.000	0.000	0.000	0.000	method 'disable' of '_lsprof.Profiler' objects

C-1.14

Write a short Python function that takes a sequence of integer values and determines if there is a distinct pair of numbers in the sequence whose product is odd.

In this method what we do first is remove all the repeated elements, then we just extract all the odd numbers. Multiply any of the odd numbers and you get an odd number. Any even number multiplied by an odd number returns an even number.

Exercise C-1.14

```
""" Write a short Python function that takes a sequence of integer values and
determines if there is a distinct pair of numbers in the sequence whose
product is odd.
```

```
>>> data = [2,3,4,5,6,7,8,9,10,11,10,9,8,7,6,5,4,3,2,1]
>>> get_odd_numbers(data)
[1, 3, 5, 7, 9, 11]
"""
```

```
def get_odd_numbers(data):
    """ Returns all the numbers whose product is odd

    :param data: A list of integers
    :return: numbers whose product is odd
    """

    s = set(data)
    return [k for k in s if (k & 1 == 1)]
```

C-1.15

Write a Python function that takes a sequence of numbers and determines if all the numbers are different from each other (that is, they are distinct).

We just build a set from the original list, if the length of the set is smaller, we have repeated numbers. Besides this, we could also sort the elements and look for a repeated element.

Exercise C-1.15

```
""" Write a Python function that takes a sequence of numbers and determines
if all the numbers are different from each other (that is, they are distinct).
```

```
>>> data = [2,3,4,5,6,7,8,9,10,11,10,9,8,7,6,5,4,3,2,1]
>>> check_if_unique(data)
False
>>> check_if_unique(data[:9])
True
"""
```

```
def check_if_unique(data):
    """ Check if all elements in list are unique

    :param data: list of integers
    :return: True if all unique, else False
    """
    s = set(data)
    return len(s) == len(data)
```

C-1.16 & C-1.17

In our implementation of the `scale` function (page 25), the body of the loop executes the command `data[j] *= factor`. We have discussed that numeric types are immutable, and that use of the `*` operator in this context causes the creation of a new instance (not the mutation of an existing instance). How is it still possible, then, that our implementation of `scale` changes the actual parameter sent by the caller?

Had we implemented the `scale` function (page 25) as follows, does it work properly?

The incorrect_way

```
def scale(data, factor):  
    for val in data:  
        val *= factor
```

Explain why or why not.

Well... here are some immutable types in Python.

- numerical types
- string types
- types

And here are some mutable types.

- lists
- dicts
- classes

So taken by that premise, if we want a function that modifies numeric values in place, we would need a class that wraps that numeric value. This is not trivial. So we are going to take respectfully a class done by The Edwards Research group (<http://www.edwards-research.com/>), this class is presented here: <http://blog.edwards-research.com/2013/09/mutable-numeric-types-in-python/>.

It is everything you dreamed of, I give you, a mutable numeric.

Mutable Numeric

"""

MutableNum class from: <http://blog.edwards-research.com/2013/09/mutable-numeric-types-in-python/>

Allows you to pass the instance to a function, and with proper coding, allows you to modify the value of the instance inside the function and have the modifications persist.

For example, consider:

```
> def foo(x): x *= 2
> x = 5
> foo(x)
> print(x)
```

This will print 5, not 10 like you may have hoped. Now using the MutableNum class:

```
> def foo(x): x *= 2
> x = MutableNum(5)
> foo(x)
> print(x)
```

*This **will** print 10, as the modifications you made to x inside of the function foo will persist.*

*Note, however, that the following **will not** work:*

```
> def bar(x): x = x * 2
> x = MutableNum(5)
> bar(x)
> print(x)
```

*The difference being that `[x *= 2]` modifies the current variable x, while `[x = x * 2]` creates a new variable x and assigns the result of the multiplication to it.*

If, for some reason you can't use the compound operators (`+=`, `-=`, `=`, etc.), you can do something like the following:*

```
> def better(x):
>     t = x
>     t = t * 2
>     # ... (Some operations on t) ...
>
```

```

>         # End your function with a call to x.set()
>         x.set(t)

"""

class MutableNum(object):
    __val__ = None
    def __init__(self, v): self.__val__ = v
    # Comparison Methods
    def __eq__(self, x):         return self.__val__ == x
    def __ne__(self, x):         return self.__val__ != x
    def __lt__(self, x):         return self.__val__ < x
    def __gt__(self, x):         return self.__val__ > x
    def __le__(self, x):         return self.__val__ <= x
    def __ge__(self, x):         return self.__val__ >= x
    def __cmp__(self, x):        return 0 if self.__val__ == x else 1 if self.__val__ > 0 else -1
    # Unary Ops
    def __pos__(self):           return self.__class__(+self.__val__)
    def __neg__(self):           return self.__class__(-self.__val__)
    def __abs__(self):           return self.__class__(abs(self.__val__))
    # Bitwise Unary Ops
    def __invert__(self):        return self.__class__(~self.__val__)
    # Arithmetic Binary Ops
    def __add__(self, x):        return self.__class__(self.__val__ + x)
    def __sub__(self, x):        return self.__class__(self.__val__ - x)
    def __mul__(self, x):        return self.__class__(self.__val__ * x)
    def __div__(self, x):        return self.__class__(self.__val__ / x)
    def __mod__(self, x):        return self.__class__(self.__val__ % x)
    def __pow__(self, x):        return self.__class__(self.__val__ ** x)
    def __floordiv__(self, x):    return self.__class__(self.__val__ // x)
    def __divmod__(self, x):      return self.__class__(divmod(self.__val__, x))
    def __truediv__(self, x):     return self.__class__(self.__val__.__truediv__(x))
    # Reflected Arithmetic Binary Ops
    def __radd__(self, x):        return self.__class__(x + self.__val__)
    def __rsub__(self, x):        return self.__class__(x - self.__val__)
    def __rmul__(self, x):        return self.__class__(x * self.__val__)
    def __rdiv__(self, x):        return self.__class__(x / self.__val__)
    def __rmod__(self, x):        return self.__class__(x % self.__val__)
    def __rpow__(self, x):        return self.__class__(x ** self.__val__)
    def __rfloordiv__(self, x):   return self.__class__(x // self.__val__)
    def __rdivmod__(self, x):     return self.__class__(divmod(x, self.__val__))
    def __rtruediv__(self, x):    return self.__class__(x.__truediv__(self.__val__))
    # Bitwise Binary Ops
    def __and__(self, x):         return self.__class__(self.__val__ & x)

```

```

def __or__(self, x):          return self.__class__(self.__val__ | x)
def __xor__(self, x):        return self.__class__(self.__val__ ^ x)
def __lshift__(self, x):     return self.__class__(self.__val__ << x)
def __rshift__(self, x):     return self.__class__(self.__val__ >> x)
# Reflected Bitwise Binary Ops
def __rand__(self, x):       return self.__class__(x & self.__val__)
def __ror__(self, x):        return self.__class__(x | self.__val__)
def __rxor__(self, x):       return self.__class__(x ^ self.__val__)
def __rlshift__(self, x):    return self.__class__(x << self.__val__)
def __rrshift__(self, x):    return self.__class__(x >> self.__val__)
# Compound Assignment
def __iadd__(self, x):       self.__val__ += x; return self
def __isub__(self, x):       self.__val__ -= x; return self
def __imul__(self, x):       self.__val__ *= x; return self
def __idiv__(self, x):       self.__val__ /= x; return self
def __imod__(self, x):       self.__val__ %= x; return self
def __ipow__(self, x):       self.__val__ **= x; return self
# Casts
def __nonzero__(self):      return self.__val__ != 0
def __int__(self):          return self.__val__.__int__()           # XXX
def __float__(self):        return self.__val__.__float__()         # XXX
def __long__(self):         return self.__val__.__long__()          # XXX
# Conversions
def __oct__(self):          return self.__val__.__oct__()           # XXX
def __hex__(self):          return self.__val__.__hex__()           # XXX
def __str__(self):          return self.__val__.__str__()           # XXX
# Random Ops
def __index__(self):        return self.__val__.__index__()         # XXX
def __trunc__(self):        return self.__val__.__trunc__()         # XXX
def __coerce__(self, x):    return self.__val__.__coerce__(x)
# Representation
def __repr__(self):         return "%s(%d)" % (self.__class__.__name__, self.__val__)
# Define innertype, a function that returns the type of the inner value self.__val__
def innertype(self):        return type(self.__val__)
# Define set, a function that you can use to set the value of the instance
def set(self, x):
    if isinstance(x, (int, long, float)): self.__val__ = x
    elif isinstance(x, self.__class__): self.__val__ = x.__val__
    else: raise TypeError("expected a numeric type")
# Pass anything else along to self.__val__
def __getattr__(self, attr):
    print("getattr: " + attr)
    return getattr(self.__val__, attr)

```


Now onto the second question... if numeric types are not valid then of course that method is not going to work. You would need to do something **radical** like returning a **new list**. As follows:

Returning new_list

```
def scale(data, factor):
    return [x*factor for x in data]
```

We can also change the list number by replacing the value in the list, remember that lists are mutable, so we can change that, we just can't change the number.

Exercise C-1.16 & C-1.17

*""" In our implementation of the scale function (page 25), the body of the loop executes the command data[j] *= factor. We have discussed that numeric types are immutable, and that use of the *= operator in this context causes the creation of a new instance (not the mutation of an existing instance). How is it still possible, then, that our implementation of scale changes the actual parameter sent by the caller?*

Had we implemented the scale function (page 25) as follows, does it work properly?

```
def scale(data, factor):
    for val in data:
        val *= factor
```

Explain why or why not.

```
>>> import MutableNum
>>> l = [2,3,4,5,6]
>>> e = [MutableNum.MutableNum(x) for x in l]
>>> scale(e, 5)
[MutableNum(10), MutableNum(15), MutableNum(20), MutableNum(25), MutableNum(30)]
>>> scale_in_place(e,0.2)
>>> print(e)
[MutableNum(2), MutableNum(3), MutableNum(4), MutableNum(5), MutableNum(6)]
"""
```

```
def scale_in_place(data, factor):
    """scales list to factor in place

    :param data: the input list of numbers
    :param factor: product factor
```

```
:return: list with modified values
"""
for j in range(len(data)):
    data[j] *= factor

def scale(data, factor):
    """scales list to factor

    :param data: the input list of numbers
    :param factor: product factor
    :return: list with modified values
    """

    for j in range(len(data)):
        data[j] *= factor
    return data
```

C-1.18

Demonstrate how to use Python's list comprehension syntax to produce the list

Exercise C-1.18

```
"""Demonstrate how to use Python's list comprehension
syntax to produce the list
[0, 2, 6, 12, 20, 30, 42, 56, 72, 90].
```

```
>>> demonstration_list_comprehension()
[0, 2, 6, 12, 20, 30, 42, 56, 72, 90]
"""
```

```
def demonstration_list_comprehension():
    """Python List comprehension demonstration

    :return: [0, 2, 6, 12, 20, 30, 42, 56, 72, 90]
    """

    return [idx*x for idx, x in enumerate(range(1,11))]
```

C-1.19

Demonstrate how to use Python's list comprehension syntax to produce the list [a , b , c , ..., z], but without having to type all 26 such characters literally.

Exercise C-1.19

"""Demonstrate how to use Python's list comprehension syntax to produce the list [a , b , c , ..., z], but without having to type all 26 such characters literally.

```
>>> demonstration_list_comprehension_abc()
['a', 'b', 'c', 'd', 'e', 'f', 'g', 'h', 'i', 'j', 'k', 'l', 'm', 'n', 'o', 'p', 'q', 'r', 's', 't',
'''
def demonstration_list_comprehension_abc():
    """ Python list comprehension demonstration

    :return:
        ['a', 'b', 'c', 'd', 'e', 'f', 'g', 'h',
         'i', 'j', 'k', 'l', 'm', 'n', 'o', 'p',
         'q', 'r', 's', 't', 'u', 'v', 'w', 'x',
         'y', 'z']
    """
    return [chr(x) for x in range(ord('a'), ord('z')+1)]
```

C-1.20

Python's `random` module includes a function `shuffle(data)` that accepts a list of elements and randomly reorders the elements so that each possible order occurs with equal probability. The `random` module includes a more basic function `randint(a, b)` that returns a uniformly random integer from `a` to `b` (including both endpoints). Using only the `randint` function, implement your own version of the `shuffle` function.

Exercise C-1.20

"""Python's random module includes a function shuffle(data) that accepts a list of elements and randomly reorders the elements so that each possible order occurs with equal probability. The random module includes a more basic function randint(a, b) that returns a uniformly random integer from a to b (including both endpoints). Using only the randint function, implement your own version of the shuffle function.

"""

```
def sub_shuffle(data, indexlist):
    import random
    index = random.randint(0, len(indexlist)-1)
    rElement = data[indexlist[index]]
    indexlist.pop(index)
    return rElement

def custome_shuffle(data):
    indexes_of_data = range(len(data))
    return [sub_shuffle(data, indexes_of_data) for e in range(len(data))]
```

C-1.21

Write a Python program that repeatedly reads lines from standard input until an `EOFError` is raised, and then outputs those lines in reverse order (a user can indicate end of input by typing `ctrl-D`).

Exercise C-1.21

```
""" Write a Python program that repeatedly reads lines from standard input
until an EOFError is raised, and then outputs those lines in reverse order
(a user can indicate end of input by typing ctrl-D).
"""
```

```
def read_sdin(data):
    age = 1
    if age > 0:
        try:
            age = int(input( "Enter other person 's age:" ))
            data.append(age)
            if age <= 0:
                print( "Your age must be positive" )
                read_sdin(data)
        except ValueError:
            print( "That is an invalid age specification" )
            read_sdin(data)
        except EOFError:
            print(data)
            print( "There was an unexpected error reading input." )
            raise
    else:
        read_sdin(data)

if __name__ == "__main__":
    data = [2,3,4]
    read_sdin(data)
```

C-1.22

Write a short Python program that takes two arrays *a* and *b* of length *n* storing int values, and returns the dot product of *a* and *b*. That is, it returns an array *c* of length *n* such that $c[i] = a[i] \cdot b[i]$, for $i = 0, \dots, n-1$.

Exercise C-1.22

*"""Write a short Python program that takes two arrays a and b of length n storing int values, and returns the dot product of a and b. That is, it returns an array c of length n such that c[i] = a[i] * b[i], for i = 0, ..., n-1.*

```
>>> dot_product([1,3,-5],[4,-2,-1])
```

```
3
```

```
>>> dot_product_array([1,3,-5],[4,-2,-1])
```

```
[4, -6, 5]
```

```
>>> dot_product([6,1,-3],[4,18,2])
```

```
36
```

```
>>> dot_product_array([6,1,-3],[4,18,2])
```

```
[24, 18, -6]
```

```
"""
```

```
def dot_product_array(a, b):
```

```
    """return an array c of length n such
    that c[i] = a[i] * b[i], for i = 0, ..., n-1.
```

```
    :param a: int vector
```

```
    :param b: int vector
```

```
    :return: c[i] = a[i] * b[i], for i = 0, ..., n-1.
```

```
    """
```

```
    return [x*y for x,y in zip(a,b)]
```

```
def dot_product(a,b):
```

```
    """ The dot product between two vectors is based
    on the projection of one vector onto another.
```

```
    :param a: int vector
```

```
    :param b: int vector
```

```
    :return: sum(a[i] * b[i], for i = 0, ..., n-1.)
```

```
    """
```

```
    return sum(dot_product_array(a,b))
```

C-1.23

Give an example of a Python code fragment that attempts to write an element to a list based on an index that may be out of bounds. If that index is out of bounds, the program should catch the exception that results, and print the following error message:

“Don’t try buffer overflow attacks in Python!”

Exercise C-1.23

```
"""
```

Give an example of a Python code fragment that attempts to write an element to a list based on an index that may be out of bounds. If that index is out of bounds, the program should catch the exception that results, and print the following error message:

“Don’t try buffer overflow attacks in Python!”

```
>>> catch_array_out_of_bounds()
Don't try buffer overflow attacks in Python!
"""
```

```
def catch_array_out_of_bounds():
    """Exception catching example

    :return: doesn't return
    """
    try:
        l = []
        l[0] = 1
    except IndexError as ex:
        print("Don't try buffer overflow attacks in Python!")
```


C-1.24

Write a short Python function that counts the number of vowels in a given character string.

Exercise C-1.24

```
"""
```

Write a short Python function that counts the number of vowels in a given character string.

```
>>> count_vowels("onomatopeya")
{'a': 2, 'i': 0, 'e': 1, 'u': 0, 'o': 3}
>>> count_vowels("ONOMATOPEYA")
{'a': 2, 'i': 0, 'e': 1, 'u': 0, 'o': 3}
>>> count_vowels("apple")
{'a': 1, 'i': 0, 'e': 1, 'u': 0, 'o': 0}
>>> count_vowels("APPLE")
{'a': 1, 'i': 0, 'e': 1, 'u': 0, 'o': 0}
"""
```

```
def count_vowels(word):
    """counts the number of vowels in a given
    character string.
```

```
    :param word: String in which
    to search vowels
    :return: a Dictionary with the vowel and
    times appeared
    {'a': #, 'i': #, 'e': #, 'u': #, 'o': #}
    """
```

```
    counts = {}.fromkeys("aeiou", 0)
    for char in word.lower():
        if char in counts:
            counts[char] += 1
    return counts
```

C-1.25

Write a short Python function that takes a strings, representing a sentence, and returns a copy of the string with all punctuation removed. For example, if given the string “Let’s try, Mike.”, this function would return: “Lets try Mike”.

Exercise C-1.25

```
"""
```

Write a short Python function that takes a strings, representing a sentence, and returns a copy of the string with all punctuation removed. For example, if given the string "Let s try, Mike.", this function would return "Lets try Mike".

```
>>> strip_string("The litte , small , tiny , cupcake... tasted delicious!")
'The litte small tiny cupcake tasted delicious '
```

```
>>> strip_string("struct CustomerConfig { "
... "std::string hashKey; "
... "std::string productLine; "
... "std::string customerNumber;")
'struct CustomerConfig stdstring hashKey stdstring productLine stdstring customerNumber '
```

```
>>> strip_string(r'<td valign="top" bgcolor="#FFFFCC">00-03</td> <td valign="top">.50</td><td valign="top" bgcolor=FFFFCC0003td td valigntop50tdtd valigntop50td '
```

```
>>> strip_string("Let 's try , Mike.")
'Lets try Mike '
"""
```

```
def strip_string(sentence):
    """returns a copy of the string with all punctuation removed

    :param sentence: source sentence in string form
    :return: string without ' , . ; : ? ! - _ ( ) [ ] \ ' " ' / < > { } # = '
    """
    punctuation_marks = r' , . ; : ? ! - _ ( ) [ ] \ ' " ' / < > { } # ='
    for punctuation in punctuation_marks:
        sentence = sentence.replace(punctuation, "")
    return sentence
```

C-1.26

Write a short program that takes as input three integers, a , b , and c , from the console and determines if they can be used in a correct arithmetic formula (in the given order), like " $a + b = c$," " $a = b - c$," or " $a * b = c$."

Exercise C-1.26

```
"""
```

*Write a short program that takes as input three integers, a , b , and c , from the console and determines if they can be used in a correct arithmetic formula (in the given order), like " $a+b = c$," " $a = b-c$," or " $a*b = c$."*

```
>>> ordered_integers(-1,3,2)
['add']
>>> ordered_integers(1,3,2)
['sub']
>>> ordered_integers(2,2,4)
['add', 'mul']
>>> ordered_integers(78,78,156)
['add']
>>> ordered_integers(5,10,2)
['div']
"""
```

```
import operator
```

```
def ordered_integers(a,b,c):
    """ determines if the arguments can be used
    in a correct arithmetic formula (in the given
    order), like " $a+b = c$ ," " $a = b-c$ ," or " $a*b = c$ ."

    :param a: integer
    :param b: integer
    :param c: integer
    :return: list with operation names that
    give correct arithmetic formula
    """
    operator_list = [operator.add, operator.sub,
                     operator.mul, operator.div]
    result_list = list()
    for op in operator_list:
```

```
if a == op(float(b), float(c)):
    result_list.append(op.__name__)
if c == op(float(a), float(b)):
    result_list.append(op.__name__)
return result_list
```

C-1.27

In Section 1.8, we provided three different implementations of a generator that computes factors of a given integer. The third of those implementations, from page 41, was the most efficient, but we noted that it did not yield the factors in increasing order. Modify the generator so that it reports factors in increasing order, while maintaining its general performance advantages.

Exercise C-1.27

"""

In Section 1.8, we provided three different implementations of a generator that computes factors of a given integer. The third of those implementations, from page 41, was the most efficient, but we noted that it did not yield the factors in increasing order. Modify the generator so that it reports factors in increasing order, while maintaining its general performance advantages.

```
>>> for f in factors(1000):
```

```
...     f
```

```
1
```

```
2
```

```
4
```

```
5
```

```
8
```

```
10
```

```
20
```

```
25
```

```
40
```

```
50
```

```
100
```

```
125
```

```
200
```

```
250
```

```
500
```

```
1000
```

"""

```
class Stack:
```

```
    def __init__(self):
```

```

    self.items = []

def isEmpty(self):
    return self.items == []

def push(self, item):
    self.items.append(item)

def pop(self):
    return self.items.pop()

def peek(self):
    return self.items[len(self.items)-1]

def size(self):
    return len(self.items)

def factors(n):
    """generator that computes factors

    :param n: max integer
    :return: the next factor
    in increasing order
    """
    k = 1
    ss = Stack()
    while k * k < n:
        if n % k == 0:
            yield k
            ss.push(n // k)
        k += 1
    if k * k == n:
        yield k
    while not ss.isEmpty():
        yield ss.pop()

```

C-1.28

The p-norm of a vector $v = (v_1, v_2, \dots, v_n)$ in n-dimensional space is defined as:

$$\|v\| = \sqrt[p]{v_1^p + v_2^p + \dots + v_n^p}$$

For the special case of $p = 2$, this results in the traditional Euclidean norm, which represents the length of the vector. For example, the Euclidean norm of a two-dimensional vector with coordinates $(4, 3)$ has a Euclidean norm of $\sqrt{4^2 + 3^2} = \sqrt{16 + 9} = \sqrt{25} = 5$. Give an implementation of a function named `norm` such that `norm(v, p)` returns the p-norm value of v and `norm(v)` returns the Euclidean norm of v . You may assume that v is a list of numbers.

Exercise C-1.28

```
"""
The p-norm of a vector  $v = (v_{\{1\}}, v_{\{2\}}, \dots, v_{\{n\}})$ 
in n-dimensional space is defined as:

 $\|v\| = \sqrt[p]{v^{p-1} + v^{p-2} + \dots + v^{p-n}}$ 

For the special case of  $p = 2$ , this results in the traditional
Euclidean norm, which represents the length of the vector.
For example, the Euclidean norm of a two-dimensional vector
with coordinates  $(4, 3)$  has a Euclidean norm of
 $\sqrt{4^2 + 3^2} = \sqrt{16 + 9} = \sqrt{25} = 5$ 

Give an implementation of a function named norm such that
norm(v, p) returns the p-norm value of  $v$  and norm(v) returns
the Euclidean norm of  $v$ . You may assume that  $v$  is a list of numbers.

>>> norm([4, 3])
5
>>> norm([4, 3, 9, 2], 3)
9
"""

import math
```

```

def nroot(x, n):
    """ Calculates the root to a given
    radical n

    :param x: number to which we want to find
    root to n radical
    :param n: radical
    :return: the root
    """
    return int(math.pow(x, 1.0/n))

def norm(v, p=2):
    """The p-norm of a vector v

    :param v: a vector of integers
    :param p: radical of the root
    :return: p-norm of a vector v
    """
    return nroot(sum(list(map((lambda x: x **p), v))), p)

```


Object-Oriented Programming

The second chapter looks to provide a generic foundation on Object Orientation.

2.0.2 Exercises

The exercises in the first chapter mostly open questions.