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What I Wish I Knew When Learning Picat: Introduction

August 2025

I have long been interested in constraint programming, which has been referred to as the "Holy Grail" of programming where the user states the problem and the computer solves it. https://dl.acm.org/doi/fullHtml/10.1145/24224.242304

While this is far from reality, constraint programming can reduce and scan the search space for NP dynamic programming problems without the user having to explicitly code the backtracking/search algorithm. Examples include: shortest path, knapsack, n-queens, Sudoku and so on.

Picat is a great language for learning these concepts and also an interesting general purpose programming language.

My background in programming is mostly procedural (Python) and pure functional (Haskell). So my challenge with Picat is multi-faceted: 1. Learn how constraint programming works in general, 2. Learn how constraint programming works in Picat, 3. Learn how Picat works.

Because Picat is a descendent of Prolog, it's core is a logic programming paradigm. And while the Picat manual is excellent, it moves along a quick clip and I had to read it very carefully to understand what I

didn't understand. Think Calculus textbook. It's all documented, but makes sense sometimes only after you've learned it.

Also, because it's a niche language, there's a limited amount of online support. There's no StackExchange/Picat. (There are a few Picat questions there though!) I was lucky to get in contact with one of the key developers/users of the language, Håkan Kjellerstrand, who kindly helped me through many a head scratching moment. His website is invaluable: https://hakank.org/picat/.

He also made a customized ChatGPT with Picat's documentation that has helped me as well, although like all LLMs, it can hallucinate solutions that don't work and has a tiny training dataset compared with JavaScript. But it has been more useful than not as I bang my head against the wall of knowledge.

This document is my attempt to share what I learned and is intended for programmers who have similar experience to me: a reasonable grasp of a common language such as Python, C, JavaScript, etc or a background with a functional language such as Haskell or OCaml, but not much use of Prolog or other logic programming language, and possibly no idea what constraint programming is.

Consider this a rough draft representing my personal learning curve. This document is not intended to be read top to bottom, but rather to help you if you get stuck where I did and hopefully give you the insight to move forward. As such, there's some redundancy between sections because I'm trying to make them self-contained as much as possible.

Notes:

I am much indebted to Advent of Code for providing a wealth of puzzles that have helped me learn Picat (and other languages).

Title inspired by What I Wish I Knew When I was Learning Haskell, which helped me learn that language.

Many extra thanks to Håkan Kjellerstrand for editing a draft of this document, and always being ready to answer any question on Picat.

A Motivating Example

Remember simultaneous linear equations? For example, here's a problem from Reddit's Learn Math:

 $$$ x + y = 2 \ y + z = 7 \ z + w = 13 \ w + x = 8 \ w \ge 0 \ s$ Think how you might solve this with any programming languages you know. Maybe nested for loops over possible values? Or a filter with conditions? Or just do it in your head?

With Picat, this is straightforward:

```
import cp. % the constraint solver module

main =>
    X + Y #= 2, % #= means RHS equals LHS in valid solutions
    Y + Z #= 7,
    Z + W #= 13,
    W + X #= 8,
    W #>= 0, X #>= 0,
```

```
Sols = solve_all([W,X,Y,Z]), % find all solutions

foreach (S in Sols)
   [W1,X1,Y1,Z1] = S, % pattern match on the variables
   println([w=W1,x=X1,y=Y1,z=Z1]) % print them out
end.
```

This outputs:

```
[w = 0, x = 8, y = -6, z = 13]
[w = 1, x = 7, y = -5, z = 12]
[w = 2, x = 6, y = -4, z = 11]
[w = 3, x = 5, y = -3, z = 10]
[w = 4, x = 4, y = -2, z = 9]
[w = 5, x = 3, y = -1, z = 8]
[w = 6, x = 2, y = 0, z = 7]
[w = 7, x = 1, y = 1, z = 6]
[w = 8, x = 0, y = 2, z = 5]
```

Nice!

My Personal Vendetta With Optimization

My interest in optimization goes back to when I worked on the Optimization Subroutine Library at IBM Kingston in my first job out of college in 1989. IBM needed a technical writer for the manual who had a background in computing and math, and as a dual CS/Math major with a writing minor, who also happened to have a father who worked at IBM for 30 years, I was the perfect person.

OSL was a cutting edge Simplex and interior-point barrier method linear optimization library of subroutines for IBM mainframes that worked with Fortran, APL, and hard-core 360 Assembly. It could also take advantage of the "vector processing facility" to do multiple operations simultaneously. Today we call that SIMD.

This was software that cost in the hundreds of thousands of dollars and ran on machines that cost millions. But it was in great demand nonetheless: Airlines and trucking companies used OSL for scheduling, oil and gas companies for evaluating the potential of drill sites.

Nowadays, you can just download for free any of a number of linear programming libraries and run them on your laptop with more compute than any 1990s mainframe.

However, at the time, and still today, the math at the center of this is over my head, and I never really understood how the optimization worked or how to use it myself. Which is why I find Picat so appealing. Picat enables learning about constraint programming and optimization with the linear algebra and discrete mathematics quietly in the background.

Fun fact: A couple the researchers from IBM who wrote much of OSL, John Forrest and John Tomlin, were and are instrumental in COIN-OR, an open source optimization software initiative. John Forrest was not the friendliest to a young technical writer, but John Tomlin was as kind as possible.

https://www.informs.org/Recognizing-Excellence/Award-Recipients/John-Forrest https://www.coin-or.org/coinCup/coinCup2007Winner.html

My Beef With Prolog

I learned programming on a Radio Shack Color Computer in 1972 and then the first IBM PC a few years later. BASIC and then Pascal were the only languages I had for many years. In those days, before the Internet, any other language, even assembly, were hundreds of dollars (thousands in today's money) and essentially unobtainium.

Pascal was an option because of Borland's \$49.99 Turbo Pascal. And so when Borland released a similarly priced Turbo Prolog, I was all in. I attempted to write an Othello program as my project for a CS class in college. And, apologies to Prof. Barry Burd, I got exactly nowhere. With no Stack Overflow or ChatGPT, I was unable to even figure out how to set up the data structure for the board.

So logic programming is also an long time foe I have been wanting to win at least one or two rounds with.

Note: I have since managed to write a version of Othello in Haskell. But not yet Prolog or Picat.

Note: APL is another monster from those days. For now though, it remains left to sleep.

How This Document Is Organized

This document has the following primary sections:

- Introduction. (you are here!), which includes some high level information about Picat.
- Constraint and Planner Programming, these capabilities are the reason I wanted to learn Picat and are a central strength of the language. If you are familiar with Prolog then start here.
- Picat is not Python. This is the section if you're unfamiliar with Prolog and logic programming concepts. I had always struggled with these, so I share what I found challenging and helpful. There's also some neat tricks here such as dynamic dispatch.
- Resources. Links to more information about Picat and example code.
- Appendix: Using Picat In Class. Some ideas for how to autograde Picat student assignments.
- Appendix: My Errors. The things I always get wrong, although I'm doing it less now that I've written this!
- Appendix: Debugging. Some ideas for debugging that I rely on.
- Appendix: Stuff I Don't Know. Things that I don't fully understand about Picat.

About Picat

What is Picat?

- 1. A dynamically typed hybrid of imperative, logic, functional and constraint programming.
- 2. A programming language with support for Boolean Satisfiability (SAT), Mixed-Integer Programming (MIP), Satisfiability Modulo Theories (SMT), and Finite Domain (FD) Constraint Programming (CP) solvers.
- 3. Combines some of the best ideas of Prolog, Python, Haskell, MiniZinc/z3, OR-Tools.
- 4. A wonderful resource for learning logic and constraint programming.

Answer: all of the above.

Picat vs. Other Languages

Let's look at how Picat stacks up against some programming languages you may know.

Other Language	Picat
Imperative: Python, JavaScript	Straightforward syntaxPrint from any statement to debugLibraries are limitedCommunity is small
Functional: Haskell, OCaml	= Functional concepts - No lambdas
Solvers: Z3, MiniZinc	+ Full programming language vs. just a solver
Logic: Prolog	+ Functions = Unification, non-determinism, tabling = Most "standard" Prolog features

⁺ Advantage, = Similar, - Disadvantage

Picat Has Common Programming Concepts

Concept	Picat
Comments	`% percent sign for comments. /* */ for block comments
Variables	A=5, B=3.4, C=(1234 mod 7). Note: Variables start with a capital letter in Picat.
Numeric Separator	A=1_000_000. This is syntactic sugar.
Strings	<pre>println("Hello World.")</pre>
Linked Lists	MyList =[3,4,6,1,56,123.65,"a string?",[a,sub,list]]
Arrays (O(n) access)	$My2DArray = \{\{1,2\},\{3,4\}\}, println(My2dArray[1,2]).$
List Comprehension.	Xs = [X : X in 15, X != 2].
Pattern Matching	head([H\ T])=H.
Loops	<pre>foreach (X in MyList) Y=X*X,println(X) end.</pre>
Recursion	fib(0)=1. $fib(1)=1$. $fib(N)=fib(N-1)+fib(N-2)$ member(X,[X
Functions	$myfunc(X) = R \Rightarrow if X>0 then R=X*X else R=X*X*X end.$
Output	<pre>print(), println(), printf()</pre>
Input	read_file_lines("datafile.txt").
Higher Order Functions	<pre>map(reverse, MyStringList). or MyStringList.map(reverse).</pre>

Also: Hashmaps, Sets, Ordered Sets and Binary Heaps.

Things Picat Has In Common With Logic Programming (Prolog)

- Variables start with a Capital Letter.
- Atoms
- Unification
- · Finite Domain Variables
- Tabling (Automatic Memoization)
- Non-Determinism
- Definite Clause Grammar (DCG) (Although I don't know how to use them. So if you do, please let me know.)

Things Picat Has Uniquely (I think)

Planner

There is a planner definition language, PDDL, but it is not a general programming language like Picat, and I did not find it very easy to learn.

• Solver polymorphism + Turing Complete

There are DSL languages such as MiniZinc are designed to work with multiple backend solvers. Also languages such as Prolog, Python, Java, C++, etc. are Turing Complete with library bindings to solvers, from-the-bottom-up integrated nature of Picat's solvers, the planner module, while being a full programming language does stand out from the crowd.

Things Picat Doesn't Come With

- · Classes, Objects
- Lambdas/Anonymous Functions
- · Strong Typing, Type Hinting
- Monads

More at: https://picat-lang.org/download/picat_compared_to_prolog_haskell_python.html

Using the Manual

https://picat-lang.org/download/picat_guide.pdf

- The manual is the single most important document for learning Picat. It has everything, but can be very terse, and so must be read closely.
- The index at the back lists all the commands and hyperlinks to them. I use this more than any other method when programming in Picat.

Some Notes About Example Code

Clauses and Scope

Each clause in Picat ends with a .. In example code each line is fully distinct for variable scope. % begins a comment.

For example:

```
A=5. % A=5.
```

But A is only 5 in this clause. After the ., A goes out of scope.

And if you prefer spaces around your operators, please go ahead.

```
A="A Wildebeest!". % A is a string.
```

Again, A is in scope only until the . and doesn't exist after.

```
B=A+A. %** Error : Free variable in expression: '+'
```

A hasn't been defined in this clause.

But using a , provides a continuous scope for A.

```
A=5,B=A+A. %A=5 and B=10.
```

Arity and /x notation in predicates and functions

In Prolog and Picat, it's common to refer to a function by the number of arguments it has. This is known as the functions' *arity*. For example, new_list/1 as in:

```
A=new_list(5). % make a list of 5 things
```

Why? Because often there's a version of the predicate or function with a different number of arguments.

```
A = new\_list(5,0). \ \% \ make \ a \ list \ of \ 5 \ things \ and \ initialize \ them \ all \ to \ 0.
```

Constraint Programming and the Planner

Constraint programming let's you solve problems that require searching through possible solutions. How can you place queens on a chessboard so that no queen is able to take another? (N-queens) Can a knight on chessboard visit every square once and end by returning to its starting square? (Knights tour) The best route for a traveling salesman? (Traveling Salesman) The quickest way out of a maze? (Shortest Path) How best to choose items to fill a suitcase? (Knapsack) How to complete a partially filled Sudoku puzzle? (Sudoku)

All of these, and many many more can be found via the links in the resources section.

The main concept here is the satisfaction and sometimes optimization of a function defined by a set of rules aka constraints. The function has variables whose values are not known, but can be defined to be within a given range. These are called "decision variables," and differ from normal variables.

Decision variables can be real/floating point values or integers, and in most most cases, there's no closed form solution to obtain their values. Constraint programming is NP-Hard. https://en.wikipedia.org/wiki/Integer_programming#Heuristic_methods

There are many applicable techniques you may have seen in a CS algorithms class: Dijkstra's algorithm, A*, recursion/induction, A/B pruning, branch-and-bound, fail first, breadth first search, depth first search, simplex, gradient descent, satisfiability solver, memoization/tabling or just brute force.

A solution using these algorithms is found through iteration and any efficiency over brute force is through careful selection of which potential solution to try next, when to give up and try a different one, and identification of when a given search location is the same as a previous one. This last item is also known as symmetry breaking, that is, if a state is identical/symmetrical to a previous one, don't do the calculations all over again.

These algorithms can reduce the time to find a solution from hours to fractions of a second, but learning all of them and implementing them for a specific problem can be challenging. Enter Picat!

Picat has multiple built-in solvers: Boolean Satisfiability (SAT), Mixed-Integer Programming (MIP), Satisfiability Modulo Theories (SMT), and Finite Domain (FD) Constraint Programming (CP). Incredibly, the interface to all of them is largely the same. This lets you switch between CP and SAT, for example by just changing and import statement.

There's also the amazing a Planner for finding minimum cost solutions to problems expressed via actions on a global state.

Fibonacci and Tabling

Let's take a the example every dynamic programming text begins with, Fibonacci numbers. $F_n = F_{n-1} + F_{n-2}$. In Picat:

```
fib(0) = 1.

fib(1) = 1.

fib(N) = fib(N-1)+fib(N-2).
```

Run this with and we quickly see a problem with compute time.

```
1346269 CPU time 0.042 seconds.
165580141 CPU time 4.755 seconds.
```

fib is recalculating every value of N-1 and N-2 for each N. At fib(40) that's 331,160,281 recursive calls. https://cboard.cprogramming.com/c-programming/168662-fibonacci-how-long-would-take.html

The solution is to memoize the values into a hash table after they are computed so that they can be looked up rather than brute forced on subsequent calls.

Picat (and many Prolog solutions) make this ridiculously easy. Here's the revised code.

```
main =>
    time(println(fib(5))),
    time(println(fib(30))),
    time(println(fib(40))),
    time(println(fib(4000))).
table
fib(0) = 1.
fib(1) = 1.
fib(N) = fib(N-1) + fib(N-2).
8 CPU time 0.0 seconds.
1346269 CPU time 0.0 seconds.
165580141 CPU time 0.0 seconds.
645748844909481735313769490153695956444139006401513427084075775981772103590
340889144494778072872417437607415237838188974992270097421831524820190627635
507987437042751068564702163075936230573885067767672020696704775060888952943
005092911660239478668417638539538139822817039366653699227090953080068213995
247807210499558291914070299436220877792964591740126101486595203811704525911
413319493360805771417086457836066360819419152173551158109939739457834939838
445927496726613615480616157565958189443176199220973699176769740582063418920
881445493379744229521401326215683407010162734227278277627261530663030930529
820517574447424280331075224194662196557804131017595052316172225782924860810
023912187851892996757577669202694023487336446627257747177409240688283001864
394259217610825454631646288077026537526196161573244340403420573366832792840
98590801501
CPU time 0.013 seconds.
```

Domain/Decision Variables and Constraints, cp::, #=

The core idea of constraint programming are decision variables, which are variables that have a range of potential values that are then solved by adding conditions/constraints they must meet.

Terminology Note: the Picat manual calls these *domain* variables and the common term of art is *decision* variable. According to IBM, a decision variable has a domain. So there you go. I will largely use *domain* because I cut-and-pasted a good bit from the manual.

Here's an example. Note that the module cp must be imported to use domain variables.

```
import cp. % needed for ::/2
A :: 1..10 % A is a number between 1 and 10
```

If you type this into the interactive Picat REPL, you get:

```
A = DV_0104d8_1..10
```

Let's modify this so that A must be even. We do this by adding a constraint with #=.

```
A :: 1..10, A mod 2 #= 0.
% REPL says: A = DV_010970_2_4_6_8_10
```

This shows the power of a constraint solver: Sometimes the domain can be reduced directly, i.e. the domain if A is now only the even numbers. This is discussed more in the Picat Constraint Programming book, chapter 2-3.

Constraint Example: Some Numbers that Multiply

It's also easy to make a list or array of domain variables. Here's a contrived problem:

- 5 increasing numbers that differ by 1,2,3, and 4
- The product of the numbers is less than 100000
- The first number is as large as possible Let's say we want to find a sequence of 5 numbers between 1 and 100 where their product is less than 100000, but where the first number is as large as possible (but between 1 and 100).

```
println(x=X),
println(n=N).
```

Output is:

```
y = 72577
x = [6,7,9,12,16]
n = 5
```

What Constraints are there?

There's lots of constraints that can be applied to via a constraint operator or to a list or expression of domain variables and global constraints.

Picat has implemented quite a few constraints, but there are so, so, so many more. Hakan has implemented more of them here: https://www.hakank.org/picat/#global.

Rabbit Hole: There's even a Global Constraint Catalog! Take a look at your own peril to your free time. And should you want to go down this hole, perhaps try to implement one of these constraints in Picat!

Constraint Operators

Numeric: ::, notin, #=, #=, #=, #=, #=, #= Logical: #= (not), #= (and), #= (XOR), #= (implication, left side implies right), #= (equivalence, left and right are equivalent)

Arithmetic on Lists and Expressions

- cond(BoolConstr, ThenExp, ElseExp): if the Boolean constraint is true, then the ThenExp else ElseExp
- count(*V*,*List*): The number of times *V* occurs in a list of variables
- max(List): The maximum a list of domain variables
- max(Exp1,Exp2): The maximum of Exp1 and Exp2
- min(List): The minimum of a list of domain variables
- min(Exp1,Exp2): The minimum of Exp1 and Exp2
- prod(*List*): The product of a list of domain variables
- sum(*List*): The sum of a list of domain variables

I often think I need to constrain on the length of a list, but that's because I'm thinking about the problem from my Python/Haskell view. What I really want is usually count or max or sum.

For example, in this Advent of Code problem, I want to minimize the number of items in the list Bins assigned to bin 1. Item $\mathscr{D} = 0$ for an assignment of that element to bin 1 and $\mathscr{D} != 0$ for any other bin.

My initial thought: Bins should be shortest. Therefore, filter Bins and then minimize len(Bins). But this is me thinking like an imperative or functional programmer. What I really needed was to get the count of items in Bins equal to 0. I could do this a few ways:

```
L1 #= sum([(Bins[I] #= 0) : I in 1..N]), % L1 = Bin 1 size
L1 #= sum([1 : I in 1..N, Bins[I]] #= 0) % condition on right hand side of
list comprehension
L1 #= count(0,Bins)
% and then in when we invoke solve, we use min
solve($[min(L1)],Bins).
```

Global Constraints

I copied this list (and the majority of the text) from the Picat manual, but reduced to the high-level points. This means I removed some detail and for the more complex constraints, refer to the manual! https://picat-lang.org/download/picat_guide.pdf

Note: In all cases where there list *List* it can also be an *Array*.

- acyclic(Vs, Es): The undirected graph represented by Vs and Es contains no cycles. [see hcp for how the graph is defined]
- acyclic_d(Vs, Es): The directed graph represented by Vs and Es contains no cycles.
- all_different(List): All variables in the list or array are different.
- all_distinct(List): The same as all_different, but for the cp module it maintains a higher level of consistency. For some problems, this is faster, and, for some other problems, it is slower.
- all_different_except_0(*List*): This constraint is true if all non-zero values in the *List* are different.
- assignment(*List 1,List 2*): This constraint ensures that the first *List* is a dual or the second. i.e., if the *ith* element of the first is *j*, then the *jth* element of the second is *i*.
- at_least(N,L,V): There are at least N elements in L that are equal to V, all must be integers.
- at_most(N,L,V): There are at most N elements in L that are equal to V, all must be integers.
- circuit(List): The List forms a Hamiltonian cycle. This constraint ensures that each variable has a different value, and that the graph formed by the assignment does not contain any sub-cycles.

```
For example, for the constraint circuit([X1, X2, X3, X4]), [3,4,2,1] is a solution, but [2,1,4,3] is not, because 1->2, 2->1, 3->4, 4->3 contains two sub-cycles.
```

count(*V,List,Rel,N): The number of elements of List where V Rel N is true. Rel is one of #=, #!=, #>,
 #>=, #<, or #<=. This constraint can be defined as:

```
count(V,L,Rel,N) =>
  sum([V #= E : E in L]) #= Count,
  call(Rel,Count,N).
```

count(V,List,N): The same as count(V,List,#=,N).

• cumulative(Starts, Durations, Resources, Limit): This constraint is for describing and solving time-based scheduling problems. The arguments Starts, Durations, and Resources are lists of integer-domain variables of the same length, and Limit is an integer-domain variable.

```
Let Starts be [S1, S2, ..., Sn], Durations be [D1, D2, ..., Dn], and Resources be [R1, R2, ..., Rn].
```

For each job *i*, *Si* represents the start time, *Di* represents the duration, and *Ri* represents the units of *Resources* needed. *Limit* is the limit on the units of *Resources* available at any time. This constraint ensures that the limit cannot be exceeded at any time.

- decreasing(List): The List is in (non-strictly) decreasing order.
- decreasing_strict(*List*): The *List* is in strictly decreasing order.
- diffn(*RectangleList*): This constraint ensures that no two rectangles in *RectangleList* overlap with each other. A rectangle in an n-dimensional space is represented by a list of 2 × n elements [X1, X2, . . ., Xn, S1, S2, . . ., Sn], where Xi is the starting coordinate of the edge in the *ith* dimension, and Si is the size of the edge.
- disjunctive_tasks(Tasks): Tasks is a list of terms. Each term has the form
 disj_tasks(S1,D1,S2,D2), where S1 and S2 are integer-domain variables, and D1 and D2 are
 positive integers. This constraint is equivalent to posting the disjunctive constraint S1+D1 #=< S2
 #\/ S2+D2 #=< S1 for each term in Tasks; the constraint converts the disjunctive tasks into global
 constraints.
- element(*I,List,V*): The *Ith* element of *List* is *V*, where all are integer-domain variables.
- element(I,List,V): The same as element(I,List,V), except 0-based, rather than 1-based, indexing is used.
- exactly(N,List,V): This constraint succeeds if there are exactly N elements in L that are equal to V, all must be integer-domain variables.
- global_cardinality(*List,Pairs*): *List* is a list of integer-domain variables [X1,..., Xd], and *Pairs* is a list of pairs [K1-V1,..., Kn-Vn], where each key Ki is a unique integer, and each Vi is an integer-domain variable.

The constraint is true if every element of L*ist is equal to some key, and, for each pair *Ki-Vi*, exactly *Vi* elements of *List* are equal to *Ki*. This constraint can be defined as follows:

```
global_cardinality(List,Pairs) =>
  foreach ($Key-V in Pairs)
  sum([B : E in List, B#<=>(E#=Key)]) #= V
  end.
```

• hcp(Vs, Es): The directed graph represented by Vs and Es forms a Hamiltonian cycle.

Vs is a list of pairs of the form {V,B}, and Es is a list of triplets of the form {V1,V2,B}.

A pair $\{V,B\}$ in Vs, where V is a ground term and B is a Boolean variable, denotes that V is in the graph if and only if B=1.

A triplet $\{V1, V2, B\}$ denotes that V1 is connected to V2 by an edge in the graph if and only if B = 1.

The circuit and subcircuit constraints can be implemented as follows by using hcp:

```
circuit(L) =>
    N = len(L),
    L :: 1..N,
    Vs = [{I,1} : I in 1..N],
    Es = [\{I,J,B\} : I in 1..N,
    J in fd_dom(L[I]),
    J !== I,
    B #<=> L[I] #= J],
    hcp(Vs,Es).
subcircuit(L) =>
    N = len(L),
    L :: 1..N,
    Vs = [\{I,B\} : I in 1..N,
    B #<=> L[I] #!= I],
    Es = \{\{I,J,B\} : I \text{ in } 1..N,
    J in fd_dom(L[I]),
    J !== I,
    95B #<=> L[I] #= J],
    hcp(Vs, Es).
```

- hcp(Vs,Es,K): The same as hcp(Vs,Es), except that it also constrains the number of vertices in the graph to be K.
- hcp_grid(A): This constraint ensures that the grid graph represented by A, which is a two-dimensional array of Boolean (0/1) variables, forms a Hamiltonian cycle.

In a grid graph, each cell is directly connected horizontally and vertically, but not diagonally, to its neighbors. Only cells labeled 1 are considered as vertices of the graph. This constraint is implemented as follows by using hcp:

```
hcp_grid(A) =>
    NRows = len(A),
    NCols = len(A[1]),
    Vs = [{(R,C), A[R,C]} :
    R in 1..NRows,
    C in 1..NCols],
    Es = [{(R,C), (R1,C1), _} :
    R in 1..NRows,
    C in 1..NCols,
    (R1,C1) in neibs(A,NRows,NCols,R,C)],
    hcp(Vs,Es).
```

```
neibs(A,NRows,NCols,R,C) =
    [(R1,C1) : (R1,C1) in [(R-1,C), (R+1,C),
    (R,C-1), (R,C+1)],
    R1 >= 1, R1 =< NRows,
    C1 >= 1, C1 =< NCols,
    A[R1,C1] !== 0].</pre>
```

• hcp_grid(A, Es): The same as hcp_grid(A), except that it also restricts the edges to Es, which consists of triplets of the form {V1,V2,B}.

In a triplet in *Es*, *V1* and *V2* take the form (R,C), where R is a row number and C is a column number, and B is a Boolean variable, which denotes that V1 is connected to V2 by an edge in the graph if and only if B = 1. If Es is a variable, then it is bound to the edges of the grid graph.

- hcp_grid(A, Es, K): The same as hcp_grid(A, Es), except that it also constrains the number of vertices in the graph to be K.
- increasing(*List*): The *List* is in (non-strictly) increasing order.
- increasing_strict(*List*): The *List* is in strictly increasing order.
- lex_le(List 1,List 2): List 1 is lexicographically less than or equal to List 2.
- lex_lt(L1,L2): (List 1,List 2): List 1 is lexicographically less than to List 2.
- matrix_element(Matrix,I,J,V): True if the entry at <I,J> in Matrix is V, where all are integer-domain variables.
- matrix_element0(*Matrix,I,J,V*): The same as matrix_element, except that it uses 0-based, rather than 1-based, indexing.
- neqs(NeqList): NeqList is a list of inequality constraints of the form X #!= Y, where X and Y are integer-domain variables. This constraint is equivalent to the conjunction of the inequality constraints in NeqList, but it extracts all_distinct constraints from the inequality constraints
- nvalue(N,List): The number of distinct values in List is N, where List is a list of integer-domain variables.
- path(Vs*, Es, Src, Dest): The undirected graph represented by Vs and Es has a path from Src to Dest. [see hcp for how the graph is defined]

Note that the graph is assumed to be undirected. If there exists a triplet {V1,V2,B} in Es, then the triplet {V2,V1,B} will be added to Es if it is not specified.

- path_d(Vs,Es,Src,Dest): The same as path(Vs,Es,Src,Dest), except that the graph is directed.
- regular(List, Q, S, M, Q0, F): Given a finite automaton (DFA or NFA) of Q states numbered 1, 2,...,Q with input 1...S, transition matrix M, initial state Q0 ($1 \le Q0 \le Q$), and a list of accepting states F, True if the List is accepted by the automaton.

The transition matrix M represents a mapping from $1..Q \times 1..S$ to 0..Q, where 0 denotes the error state. For a DFA, every entry in M is an integer, and for an NFA, entries can be a list of integers.

The regular constraint is covered in the Constraint book

• scalar_product(A,X,Product): The scalar product of A and X is Product, where A and X are lists or arrays of integer-domain variables, and Product is an integer-domain variable. A and X must have the same length.

- scalar_product(A,X,Rel,Product): The scalar product of A and X has the relation Rel with Product, where Rel is one of the following operators: #=, #!=, #>=, #>, #=< (or #<=), and #<.
 - scc(Vs, Es): The undirected graph represented by Vs and Es is strongly connected. [see hcp for how the graph is defined]

Note that the graph is assumed to be undirected. If there exists a triplet {V1,V2,B} in Es, then the triplet {V2,V1,B} will be added to Es if it is not specified

- scc(Vs, Es, K): The same as scc(Vs, Es), except that it also constrains the number of vertices in the graph to be K.
- scc_grid(A): This constraint ensures that the grid graph represented by A, which is a two-dimensional array of Boolean variables, forms a strongly connected undirected graph.

In a grid graph, each cell is directly connected horizontally and vertically, but not diagonally, to its neighbors. Only cells labeled 1 are considered as vertices of the graph.

This constraint is implemented as follows by using scc:

```
scc_grid(A) =>
    NRows = len(A),
    NCols = len(A[1]),
    Vs = \{\{(R,C), A[R,C]\}\}:
    R in 1..NRows,
    C in 1..NCols],
    Es = [\{(R,C), (R1,C1), _\} :
    R in 1...NRows,
    C in 1..NCols,
    (R1,C1) in neibs(A,NRows,NCols,R,C),
    (R,C) @< (R1,C1)],
    scc(Vs, Es).
neibs(A,NRows,NCols,R,C) =
    [(R1,C1):(R1,C1) in [(R-1,C),(R+1,C),
    (R,C-1), (R,C+1)],
    R1 >= 1, R1 =< NRows,
    C1 >= 1, C1 =< NCols,
    A[R1,C1] !== 0].
```

Note that there is an edge between each pair of neighboring cells in the resulting graph as long as the cells are in the graph.

• scc_grid(A,K): The same as scc_grid(A,Es), except that it also constrains the number of vertices in the graph to be K.

• scc_d(Vs,Es): The directed graph represented by Vs and Es is strongly connected, where Vs and Es are the same as those in scc(Vs,Es), except that the graph is directed.

- scc_d(Vs,Es,K): The same as scc_d(Vs,Es), except that it also constrains the number of vertices in the graph to be K.
- serialized(Starts, Durations): This constraint describes a set of non-overlapping tasks, where Starts and Durations are lists of integer-domain variables, and the lists have the same length. Let Os be a list of 1s that has the same length as Starts. This constraint is equivalent to cumulative(Starts, Durations, Os, 1).
- subcircuit(*List*): This constraint is the same as circuit(*List*), except that not all of the vertices are required to be in the circuit. If the *ith* element of *List* is *i*, then the vertex *i* is not part of the circuit.
- subcircuit_grid(A): The grid graph represented by A, which is a two-dimensional array of Boolean (0/1) variables, forms a Hamiltonian cycle.

In a grid graph, each cell is directly connected horizontally and vertically, but not diagonally, to its neighbors. Only non-zero cells are considered as vertices of the graph.

- subcircuit_grid(A, K): The same as subcircuit_grid(A), except that it also constrains the number of vertices in the graph to be K.
- tree(Vs,Es): This constraint ensures that the undirected graph represented by Vs and Es is a tree. [see hcp for how the graph is defined]

Note that the graph to be constructed is assumed to be undirected. If there exists a triplet {V1,V2,B} in Es, then the triplet {V2,V1,B} will be added to Es if it is not specified.

• tree(*Vs*, *Es*, *K*): The same as tree(*Vs*, *Es*), except that it also constrains the number of vertices in the tree to be *K*.

Using solve and solve_all with cp, sat, mip and smt

Let's go back to the example I used in the intro. I fibbed a little. Yes, it's easy to solve this toy problem and yes it can be done with all the solvers, but using each solver is slightly different. They aren't fully "hot swappable".

Here's the full version of that code where all the solvers are specified. You can try this by uncommenting a different solver from the one in the code.

```
% import cp. % solve with cp
% import sat. % solve with sat
% import mip. % solve with mip, you need to install cbc, glpk, gurobi or compile Picat from scratch for scip
import smt. % solve with smt, you need to install cvc or z3
main =>
```

```
% for sat and smt, need to explictly make new dvars
    % also works for cp and mip,
    % but cp can figure out the domain without new dvar/0
    % but if you want non-integer solutions for mip
    % need to specify they can be real numbers with something after the
decimal point
    % for example, instead of new_dvar use W :: 0.0..100.0
    W = new dvar(), % ideally set to a more limited doman
    X = new_dvar(), % new_dvar allows for any +/- integer value
    Y = new_dvar(), % based on architecture: either 32-bit or 64-bit
    Z = new_dvar(),
    X + Y #= 2,
   Y + Z #= 7,
    Z + W \# = 13,
    W + X \# = 8,
    W \#>= 0, X \#>= 0,
   Sols = solve_all([W,X,Y,Z]), % cp, sat or smt which defaults to calling
z3
   % Sols = solve_all($[cbc],[W,X,Y,Z]), % one option for mip
    foreach (S in Sols)
        [S1, S2, S3, S4] = S,
        println([w=S1, x=S2, y=S3, z=S4])
    end.
```

solve(Vars) finds one solution and solve_all = Sols finds, well, all the solutions.

solve is a predicate and the domain variables in Vars will be replaced with a valid soution after the call to solve.

solve_all = Sols is a function and the list of valid solutions is bound to Sols. Sols will be a list even if there's only one solution.

Common Options Across All Solvers

When calling solve and solve_all there's some common options you can select, regardless of which solver you use.

- \$limit(N): Search up to N solutions.
- \$max(Var): Maximize the variable Var.
- \$min(Var): Minimize the variable Var.
- \$report(Call): Execute Call each time a better answer is found while searching for an optimal answer. (Not available with mip.) I used this for debugging in this program.

Options are the first argument in a solve call and have to be inside a list, even if there's only one. For example, in the above we could write:

```
Sols = solve_all([$min(W)],[W,X,Y,Z]).
```

or

```
Sols = solve_all($[limit(3),report(printf("Got one! %w",W))],[W,X,Y,Z]).
```

Note the use of \$. This means that Picat should not attempt to evaluate the term as an immediate function call. Also note that the \$ can be outside of the list for multiple options. Or inside on both options. More on \$ here.

The Four Solver Modules

Let's look at the four solver modules and what makes them different from each other, and the options you can provide to the solver for them.

Note: Picat is primarily focused on problems with integer aka finite-domain solutions. (Yes, integers are infinite, but not in computer programs that are expected to halt.) MIP provides the ability to have real-valued solutions.

On the other hand, Picat does have a neural network modules that interfaces to the FAAN neural network library. I'm sure someone could use it for non-linear optimization, given that this is exactly what neural networks do. However, that person is not me. Hakan, of course, has some example code.

CP, Constraint Programming or Constraint Logic Programming (Integer)

CP finds feasible values for decision variables by searching through and reducing the domains of those variables via algorithmic techniques such as: breadth and depth-first search, tabling (memoization), backtracking, refinement, perturbation, constraint propagation, combinatorics, unification, and other heuristics.

*Note: The cp module has been more the sufficient for all of the Advent of Code problems in this text and it's been the main one I use for constraints. It also has the most options to adjust the search strategy. However, because cp has been so quick, I have not tried the other solvers very much, but that doesn't mean you shouldn't try them. *

Also, I have also started to see many Advent of Code days as being alilgned to planner because there's such a plethora of shortest path or action-next action problems.

Here's the scoop copied right out of the manual:

- backward: The list of variables is reversed first.
- constr: Variables are first ordered by the number of attached constraints.
- degree: Variables are first ordered by degree, i.e., the number of connected variables.
- down: Values are assigned to variables from the largest to the smallest.
- ff: The first-fail principle is used: the leftmost variable with the smallest domain is selected.
- ffc: The same as with the two options: ff and constr.
- ffd: The same as with the two options: ff and degree.
- forward: Choose variables in the given order, from left to right.

• inout: The variables are reordered in an inside-out fashion. For example, the variable list [X1,X2,X3,X4,X5] is rearranged into the list [X3,X2,X4,X1,X5].

- label\$(CallName)\$: This option informs the cp solver that once a variable \$V\$ is selected, the user-defined call \$CallName(V)\$ is used to label \$V\$, where \$CallName\$ must be defined in the same module, an imported module, or the global module.
- leftmost: The same as forward.
- max: First, select a variable whose domain has the largest upper bound, breaking ties by selecting a variable with the smallest domain.
- min: First, select a variable whose domain has the smallest lower bound, breaking ties by selecting a variable with the smallest domain.
- rand: Both variables and values are randomly selected when labeling.
- rand_var: Variables are randomly selected when labeling.
- rand_val: Values are randomly selected when labeling.
- reverse_split: Bisect the variable's domain, excluding the lower half first.
- split: Bisect the variable's domain, excluding the upper half first.
- updown: Values are assigned to variables from the values that are nearest to the middle of the domain.

I say this later on, but it bears repeating: The search and labeling methods can greatly affect solution time. See pgs 59-61 in the Picat constraint book for an example of trying all the combinations of solve options on a Magic Squares problem. Results there range from essentially instaneous to more than the author's set limit of 10 seconds.

SAT, Boolean Satisfiability (Integer)

SAT converts a constraint problem into propositional logic via a Boolean algebra expression composed of *ands* and *ors*. This representation of the problem with only ^ (and) and v (or) is known as Conjunctive Normal Form or Clause Normal Form (CNF).

SAT solvers rely on an extensive body of computer science research that shows the equivalence of many NP-Hard problems to both each other and to SAT. And that according to the Cook-Levin theorem, "Any problem in NP can be reduced in polynomial time by a deterministic Turing machine to the Boolean satisfiability problem."

Here's an example of a Sudoku rule that each row has all numbers in CNF from an Aalto University course. C_3 is one rule and $x_{r,c,v}$ is a matrix of variables where r is the row, t is the column, and t is the value at that row and column.

 $S = \sum_{r,n,v} | x_{r,1,v} | x_{r,2,v} | x_{r,n,v} | s$

The full example at the link has 6 rules:

 $$$ \phi C_1 \ C_2 \ C_3 \ C_4 \ C_5 \ C_6$

The CNF is run through the SAT solver to determine if the there's an assignment of the variables (in the above \$x\$) that satisfies the combination of the rules \$\phi\$. If so, we have a Sudoku solution.

Picat manages the conversion of a constraint program and its domain variables into CNF and then runs its internal SAT solver. However, if you want to use your own, you can have Picat save (dump) the CNF file.

Here's a link to a bunch of SAT solvers and more tutorials.

Here's Picat's options when using sat:

- dump: Dump the CNF code to stdout.
- dump\$(File)\$: Dump the CNF code to \$File\$.
- seq: Use sequential search to find an optimal answer.
- split: Use binary search to find an optimal answer (default).
- \$nvars\$(NVars)\$: The number of variables in the CNF code is \$NVars\$.
- \$ncls\$(NCls)\$: The number of clauses in the CNF code is \$NCls\$.

I believe \$nvars and \$ncls provides access to the number of variables and clauses should you need them.

SMT, Satisfiability Modulo Theories (Integer)

SMT are built on the ideas of SAT and include additional methods and data structures such as bitvectors. Many SMT solvers make use of DPLL(T).

Davis–Putnam–Logemann–Loveland (DPLL) algorithm is a complete, backtracking-based search algorithm for deciding the satisfiability of propositional logic formulae in conjunctive normal form, i.e. for solving the CNF-SAT problem. https://en.wikipedia.org/wiki/DPLL_algorithm

SMT solvers are also closely related to automated theorem provers, and one of the main SMT solver, Z3 from Microsoft Research, states on its web page, "A theme shared among many of the algorithms is how they exploit a duality between finding satisfying solutions and finding refutation proofs."

To use the smt module in Picat, you need to install an external SMT solver and invoke solve with the name of the solver. Picat will export a file with the appropriate format and then call the external solver. Picat uses the SMT-LIB2 format for output. SMT options are:

SMT solver	License	solve	Picat System Call or Interface	Link
cvc4	open source	solve([cvc4],Vars)	cvc4 TempFile > SolFile	link
z3	open source	solve([z3],Vars)	Picat calls z3. This is the default.	link
other	n/a	<pre>solve([dump],Vars) solve([dump\$(File)\$],Vars)</pre>	Dump the constraints in SMT-LIB2 format to stdout or to \$File\$	n/a

Two other options are:

- logic\$(Logic)\$: Instruct the SMT solver to use \$Logic\$ in the solving, where \$Logic\$ must be an atom or a string, and the specified logic must be available in the SMT solver. The default logic for Z3 is "LIA", and another suggestion is "QF_FD". The default logic for CVC4 is "NIA".
- tmp\$(File)\$: Dump the SMT-LIB2 format to \$File\$ rather than the default file "_tmp.smt2", before calling the SMT solver. The name File must be a string or an atom that has the extension name

".smt2". When this file name is specified, the SMT solver will save the solution into a file name that has the same main name as \$File\$ but the extension name ".sol".

Rabbit hole (the biggest): The world of theorem provers associated research into the boundaries of NP and decidability is about as big a rabbit hole as possible and sweeps in all the big names of Turing, Curry, Howard, Gödel, Russell, Frege, and many more.

Here's a sample program in Lean, a theorem proving programming language, for solving some linear inequalty constraints. Gotta love the keyword grind for searching the solution space:

```
example (x y : Int) :  27 \le 11*x + 13*y \rightarrow 11*x + 13*y \le 45   \rightarrow -10 \le 7*x - 9*y \rightarrow 7*x - 9*y > 4 := by  grind
```

Should you wish to see into the current state of the related P vs. NP problem, may I recommend this book by Avi Wigderson that I made it halfway through: https://www.math.ias.edu/avi/book.

MIP, Mixed-Integer Programming (Integer and Real)

MIP solves problems with real (continuous), integer, or binary decision variables or any mixture of these. This is as opposed to LP, linear programming, which only allows for continuous solutions. Both, howerver, are based on numerical linear algebra techniques. MIP algorithms for finding solutions in the search space include branch-and-bound, branch-and-cut, cutting plans, interior-point methods, Lagrangian relaxation, and Simplex.

To use the mip module in Picat, you need to install an external MIP solver and invoke solve with the name of the solver. Picat will export a file with the appropriate format and then call the external solver. Options are:

MIP solver	Licencse	solve	Picat System Call or Interface	Link
cbc	open source	solve([cbc],Vars)	cbc TempFile solve -solu SolFile	link
glpk	open source	<pre>solve([glpk],Vars)</pre>	glpsol -lp -o SolFile TempFile	link
scip	open source	<pre>solve([scip],Vars)</pre>	Internal C interface that requires you to build Picat from source with SCIP enabled	
gurobi	paid	solve([gurobi],Vars)	<pre>gurobi_cl ResultFile=SolFile TempFile</pre>	link
CPLEX	paid	<pre>solve([dump\$(File)\$], Vars)</pre>	You have load the <i>File</i> into CPLEX	link

When using mip, if you want real valued solutions (non-integer), then you need to specify an interval for the domain variable in the form \$L..U\$, where \$L\$ and \$U\$ are real values. That is, there must be something after the decmial. For example 1.34 or 2.0.

Also, nonlinear constraints are not allowed. For example, you can't do this:

```
import mip.

main =>
    X :: 0.0..100.0,
    2**X #= 31,

solve([glpk],X),
    println(x=X).
```

results in

```
*** error(dvar_expected(_a18),nonlinear_constraint)
```

Fun fact: Simplex and interior-point were the two algorithms that IBM's OSL software implemented and I documented in 1989. CPLEX is OSL's "descendant" sort of. OSL is more directly an ancestor of the open source COIN-OR tools and CPLEX was an IBM acquisition in 2009. I fear a rabbit hole coming on....

Constraint and Planner Example Programs

Constraint Example: Advent of Code 2016 Day 15

https://adventofcode.com/2016/day/15

The problem from AOC:

When a button is pressed, a capsule is dropped and tries to fall through slots in a set of rotating discs to finally go through a little hole at the bottom and come out of the sculpture. If any of the slots aren't aligned with the capsule as it passes, the capsule bounces off the disc and soars away. You feel compelled to get one of those capsules.

The discs pause their motion each second and come in different sizes; they seem to each have a fixed number of positions at which they stop. You decide to call the position with the slot 0, and count up for each position it reaches next.

Furthermore, the discs are spaced out so that after you push the button, one second elapses before the first disc is reached, and one second elapses as the capsule passes from one disc to the one below it. So, if you push the button at time=100, then the capsule reaches the top disc at time=101, the second disc at time=102, the third disc at time=103, and so on.

The button will only drop a capsule at an integer time - no fractional seconds allowed.

For example, at time=0, suppose you see the following arrangement:

Disc #1 has 5 positions; at time=0, it is at position 4.

Disc #2 has 2 positions; at time=0, it is at position 1.

If you press the button exactly at time=0, the capsule would start to fall; it would reach the first disc at time=1. Since the first disc was at position 4 at time=0, by time=1 it has ticked one position forward. As a five-position disc, the next position is 0, and the capsule falls through the slot.

Then, at time=2, the capsule reaches the second disc. The second disc has ticked forward two positions at this point: it started at position 1, then continued to position 0, and finally ended up at position 1 again. Because there's only a slot at position 0, the capsule bounces away.

If, however, you wait until time=5 to push the button, then when the capsule reaches each disc, the first disc will have ticked forward 5+1 = 6 times (to position 0), and the second disc will have ticked forward 5+2 = 7 times (also to position 0). In this case, the capsule would fall through the discs and come out of the machine.

However, your situation has more than two discs; you've noted their positions in your puzzle input. What is the first time you can press the button to get a capsule?

```
--- Part Two ---
```

After getting the first capsule (it contained a star! what great fortune!), the machine detects your success and begins to rearrange itself.

When it's done, the discs are back in their original configuration as if it were time=0 again, but a new disc with 11 positions and starting at position 0 has appeared exactly one second below the previously-bottom disc.

With this new disc, and counting again starting from time=0 with the configuration in your puzzle input, what is the first time you can press the button to get another capsule?

This puzzle is perfect for Picat. Some things to notice:

- Look how long the description is versus the code!
- The use of parallel lists to encode the problem variables. The first list has the number of positions for each disc, DPos, and the second list has the position of the disk at time zero, DTZ. This is a common approach.
- As the capsule falls, the equation for \$T_{start}\$ for a given \$Disc\$ is:

```
$(T_{start}+ Distance + Disc_{time-zero}) \mod Disc_{num-positions} = 0$
```

We could code this as a foreach loop:

```
foreach (D in 1..DPos.len)
    0 #= (T+D+DTZ[D]) mod DPos[D]
```

end,

But because each is zero, the sum is zero, and one line of code looks cooler than three. So we used
 sum(...) #= 0.

- Because we are looking to know the time to press the button, the variable T is set to a range of
 possible values.
- The notation :: means that the variable is within the set of values of the list on the right side of the expression.
- The notation 1..5 means "a list with items 1 to 5 i.e., [1,2,3,4,5]"
- We aren't given a range of times, so the program sets the range of the solution T to between 0 and maxint_small(), which is not very small: it's 72,057,594,037,927,935, aka \$2^{56}-1\$, and it the largest possible value that's allowed in a decision variable, and the smallest value is \$-2^{56}-1\$.
- solve is a predicate and unifies T with the solution.
- If you wanted all the solutions, solve_all is a function and looks like Sols = solve_all(T).
- On this problem the cp solver is the fastest, but that's not always the case.

Solver	Part1	Part2
ср	0.04	0.25
sat*	1.88	7.32
mip	0.40	2.40

- The reason SAT is so much slower is because the domain of T is so large. To get these results the domain was reduced to 10_000_000 to get it to work.
- Important: In general usage, CP solver tends to be faster than SAT for easy problems, but for harder problem SAT tends to be faster. But whether a problem is "easy" or "hard" often can only be determined by testing it.
- In section "2.4 Minesweeper Using SAT" in the Picat constraint programming book, CP beats SAT for \$N \le 430\$ and above that SAT wins.

```
go(DPos,DTZ) = T =>
    %(Time + Dist + Time Zero Position) mod Disc Positions
    T :: 0..maxint_small(), % 72_057_594_037_927_935
    T :: 0..10_000_000, % for SAT also note use of _ sugar to make large
number readable
    sum([(T+D+DTZ[D]) mod DPos[D] : D in 1..DPos.len]) #=0,
    solve([$min(T)],T).
```

Constraint Example: Jane Street Bug

https://www.janestreet.com/bug-byte/

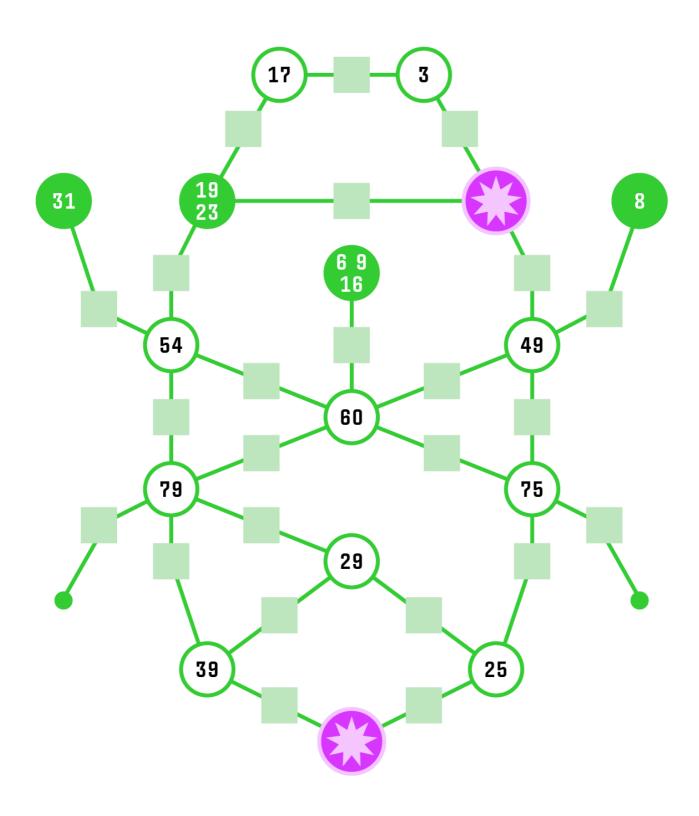
Bug Byte

Fill in the edge weights in the graph below with the numbers 1 through 24, using each number exactly once. Labeled nodes provide some additional constraints:

The sum of all edges directly connected to this node is M.

There exists a non-self-intersecting path starting from this node where N is the sum of the weights of the edges on that path. Multiple numbers indicate multiple paths that may overlap.

Once the graph is filled, find the shortest (weighted) path from to and convert it to letters (1=A, 2=B, etc.) to find a secret message.



In Picat, here's a solution. The nodes and edges are defined and then the constraints about the known values of nodes and possibly values for the edge weights. Each constraint reduces the search space.

The constraint in this program are all_distinct, #=, #^ and #<=.

all_distinct means that the values of the list of edges are all different from each other. When combined with the previous line that puts them in the range of 1 to 24, that means the edges will contain every possible value between 1 and 24.

The #= constraint syntax ensures that the left and right side are equal. Another way to look at this is that the constraint tells the solver module (in this case cp) to try to find a set of values of left and right that are equal.

#<= is less than or equal and #^ is the logical XOR.

Some more notes:

V:: 1..24 means that V is a variable that could be set to any number between 1 and 24, inclusive. Further constraints will limit this, but initially each V is open to all possible values in this range.

The line EdgeVars = [(Edge, V) : Edge in Edges, V :: 1..24] results initially in this:

```
[((A,B),_09b8::[1 ..24]),((A,D),_0a80::[1 ..24]),((B,S),_0b48::[1 ..24]),
((C,H),_0c10::[1 ..24]),((D,S),_0cd8::[1 ..24]),((D,H),_0da0::[1 ..24]),
((S,I),_0e68::[1 ..24]),((F,I),_0f30::[1 ..24]),((G,J),_0ff8::[1 ..24]),
((H,J),_010c0::[1 ..24]),((H,K),_01188::[1 ..24]),((I,J),_01250::[1 ..24]),
((I,L),_01318::[1 ..24]),((J,K),_013e0::[1 ..24]),((J,L),_014a8::[1 ..24]),
((K,M),_01570::[1 ..24]),((K,P),_01638::[1 ..24]),((K,N),_01700::[1 ..24]),
((L,0),_017c8::[1 ..24]),((M,N),_01890::[1 ..24]),((M,0),_01958::[1 ..24]),
((N,E),_01a20::[1 ..24]),((0,E),_01ae8::[1 ..24]),((Q,L),_01bb0::[1 ..24])]
```

The _xxxx is a unique identifier for the individual decision variable V and the :: [1..24] shows that it has a range of possible values that will have to be constrained.

If we added a sum constraint:

```
EdgeVars = [(Edge, V) : Edge in Edges, V :: 1..24],
sum([V : (_, V) in EdgeVars]) #= 30
```

The result would be:

```
[((A,B),_09b8::[1 ..7]),((A,D),_0a80::[1 ..7]),((B,S),_0b48::[1 ..7]),
((C,H),_0c10::[1 ..7]),((D,S),_0cd8::[1 ..7]),((D,H),_0da0::[1 ..7]),
((S,I),_0e68::[1 ..7]),((F,I),_0f30::[1 ..7]),((G,J),_0ff8::[1 ..7]),
((H,J),_010c0::[1 ..7]),((H,K),_01188::[1 ..7]),((I,J),_01250::[1 ..7]),
((I,L),_01318::[1 ..7]),((J,K),_013e0::[1 ..7]),((J,L),_014a8::[1 ..7]),
((K,M),_01570::[1 ..7]),((K,P),_01638::[1 ..7]),((K,N),_01700::[1 ..7]),
((L,0),_017c8::[1 ..7]),((M,N),_01890::[1 ..7]),((M,0),_01958::[1 ..7]),
((N,E),_01a20::[1 ..7]),((0,E),_01ae8::[1 ..7]),((Q,L),_01bb0::[1 ..7])]
```

Given the limit of 30 for the sum of all of the decision variables, the constraint solver has determined that the maximum value of each variable now is 7. Note: sometimes the solver cannot do this domain reduction before the call to solve.

We will need a different set of constraints to solve the bug byte, and they are in the code below. But before you look at it, some things to note:

- The comments say that we only need C, F, and G to solve. How was this determined? Through trial and error! Someone smarter than me may have been able to figure it out, but I had to go and manually try and figure out combinations to solve.
- This was one of my first Picat programs and it took me a long time and a lot of confusion to start to understand what exactly I was "solving" and how to represent the problem in code.
- The shortest path code was lifted right out of the Picat book, with a slight modification for this problem.
- The shortest path uses table and the (+,+,+,-,min) indicates that the first three arguments, Graph,X,Y, are inputs, the fourth, Path, is an output, and fifth, WL, aka weight, is to be minimized.
- This Prolog-style shortest path is a mind bender for me still, and it really shows how odd logic programming can feel. The code says:
 - If X and Y have an edge between them, that's the shortest path.
 - If not, the ?=> on the first rule, then the shortest path is from X to Z and then Z to Y.
 - What? Huh? How?
 - Yes, that's it. Picat searches over the entire space and returns the one with the minimum W

```
import cp.
main =>
    % Define the graph with nodes and edges
    Nodes = ['A', 'B', 'C', 'D', 'E', 'F', 'G', 'H', 'I', 'J', 'K', 'L',
'M', 'N', 'O', 'P', 'Q', 'S'],
    Edges = [('A', 'B'), ('A', 'D'),
             ('B', 'S'),
             ('C', 'H'),
             ('D', 'S'), ('D', 'H'),
             ('S', 'I'),
             ('F', 'I'),
             ('G', 'J'),
             ('H', 'J'), ('H', 'K'),
                  'J'), ('I', 'L'),
             ('I',
             ('J', 'K'), ('J', 'L'),
             ('K', 'M'), ('K', 'P'), ('K', 'N'),
             ('L', 'O'),
             ('M', 'N'), ('M', 'O'),
             ('N', 'E'),
             ('0', 'E'),
             ('Q', 'L')],
    % Edges are tuples of nodes and weights in range 1..24
    EdgeVars = [(Edge, V) : Edge in Edges, V :: 1..24],
    % Unique edge weights
    % Reduce search space to 24! = 6,204,484,903,168,028,160
    all_distinct([V : (_, V) in EdgeVars]),
    % Constraint to enforce known edge weights
```

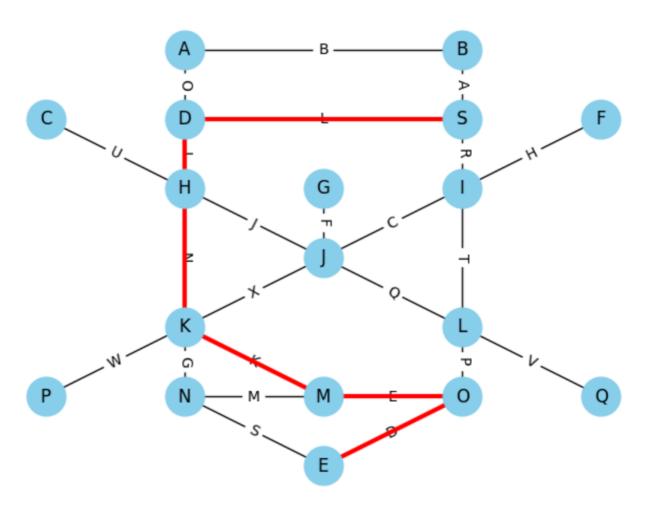
```
% Reduce search space to 19! = 121,645,100,408,832,000
         KnownWeights = [(('D', 'S'), 12),
                                               (('J', 'K'), 24),
                                               (('K', 'N'), 7),
                                               (('I', 'L'), 20)],
         foreach((Edge, Weight) in KnownWeights),
                  member((Edge, Weight), EdgeVars)
         end,
         % Constraint to enforce known sum of weights for nodes
         % Reduce search space to 48
         KnownSums = [('A', 17),
                                       ('B', 3),
                                        ('H', 54),
                                        ('I', 49),
                                        ('J', 60),
                                        ('K', 79),
                                        ('L', 75),
                                        ('M', 29),
                                        ('N', 39),
                                        ('0', 25)],
         foreach((Node, Sum) in KnownSums),
                  NodeEdges = [(N1, N2) : (N1, N2) in Edges, (N1 = Node ; N2 = Node = No
Node)],
                  NodeVars = [V : (Edge, V) in EdgeVars, Edge in NodeEdges],
                  sum(NodeVars) #= Sum
         end,
         % Constraint that sum of weight on an edge = KnownPathSum OR
         % sum of weight plus min edge on neighbor is <= to KnownPathSums
         % only need C, G, and F to reduce search space to 2
         KnownPathSums = \Gamma
                                               ('C', 31),
                                               % ('D', 19),
                                               % ('D', 23),
                                                 ('G', 6),
                                               % ('G', 9),
                                               % ('G', 16),
                                                 ('F', 8)],
         foreach((Node, Sum) in KnownPathSums),
                  NodeEdges = [(N1, N2) : (N1, N2) in Edges, N1 = Node],
                  NodeVars = [V : (Edge, V) in EdgeVars, Edge in NodeEdges],
                  Neighbors = [N2 : (N1, N2) in Edges, N1 = Node],
                  NodeOneHopEdges = [(N1, N2) : (N1, N2) in Edges, N1 in Neighbors],
                  NodeOneHopVars = [V : (Edge, V) in EdgeVars, Edge in
NodeOneHopEdges],
                  (sum(NodeVars) #= Sum) #^ (sum(NodeVars) + min(NodeOneHopVars) #=<</pre>
Sum)
         end,
         Solutions = solve_all([ffc], EdgeVars),
         printf("Number of solutions: %d\n", length(Solutions)),
         foreach(Solution in Solutions)
                  AllEdges = Solution ++ [((Y,X), Weight) : ((X,Y), Weight) in
```

```
Solution],
        sp(AllEdges, 'S', 'E', Path, _),
        Message = [chr(W+64) : ((X,Y), W) in Path],
        println('======""),
        println(Path),
        println("Message is: "++Message),
    end,
    save solution(Solutions),
    println("Done!").
% shortest path adapted from Picat Manual
table (+,+,+,-,min)
sp(Graph,X,Y,Path,WL) ?=>
    Path = [((X,Y),Wxy)],
    WL = Wxy,
    member(((X,Y), Wxy), Graph).
sp(Graph,X,Y,Path,WL) =>
    Path = [((X,Z), Wxz)|Path1],
    member(((X,Z), Wxz), Graph),
    sp(Graph,Z,Y,Path1,WL1),
    WL1 = Wzy,
    WL = Wxz+Wzy.
% Save to file for use with Python to make a graph
save_solution(Solutions) =>
    Out = open("solutions.txt", write),
    foreach(Solution in Solutions)
        println(Out, Solution)
    end,
    close(Out).
```

The output is two potential solutions. Which is close enough for a person to figure out which the right one is. (It's the one that's a word.)

Here's a visual of the shortest path made with Python. The edges are labelled in order from node S to node E: LINKED.

LINKED



Constraint Example: Santa's Knapsack

https://adventofcode.com/2015/day/24

Advent of Code 2015 day 24 is a knapsack problem. Typically AOC problems get harder from day 1 to day 25, but day 24 is a breeze in Picat! Here's the instructions:

Part 1

It's Christmas Eve, and Santa is loading up the sleigh for this year's deliveries. However, there's one small problem: he can't get the sleigh to balance. If it isn't balanced, he can't defy physics, and nobody gets presents this year.

No pressure.

Santa has provided you a list of the weights of every package he needs to fit on the sleigh. The packages need to be split into three groups of exactly the same weight, and every package has to fit. The first group goes in the passenger compartment of the sleigh, and the second and third go in containers on either side. Only when all three groups weigh exactly the same amount will the sleigh be able to fly. Defying physics has rules, you know!

Of course, that's not the only problem. The first group - the one going in the passenger compartment - needs as few packages as possible so that Santa has some legroom left over. It doesn't matter how many packages are in either of the other two groups, so long as all of the groups weigh the same.

Furthermore, Santa tells you, if there are multiple ways to arrange the packages such that the fewest possible are in the first group, you need to choose the way where the first group has the smallest quantum entanglement to reduce the chance of any "complications". The quantum entanglement of a group of packages is the product of their weights, that is, the value you get when you multiply their weights together. Only consider quantum entanglement if the first group has the fewest possible number of packages in it and all groups weigh the same amount.

For example, suppose you have ten packages with weights 1 through 5 and 7 through 11. For this situation, some of the unique first groups, their quantum entanglements, and a way to divide the remaining packages are as follows:

Group 1	Group 2	Group 3
11 9 (QE=99)	10 8 2	75431
10 9 1 (QE=90)	11 7 2	8543
10 8 2 (QE=160)	11 9	75431
10 7 3 (QE=210)	11 9	85421
10 5 4 1 (QE=200)	11 9	8732
10 5 3 2 (QE=300)	11 9	8741
10 4 3 2 1 (QE=240)	11 9	875
9 8 3 (QE=216)	11 7 2	10 5 4 1
9 7 4 (QE=252)	11 8 1	10 5 3 2
9 5 4 2 (QE=360)	11 8 1	10 7 3
8 7 5 (QE=280)	11 9	10 4 3 2 1
8 5 4 3 (QE=480)	11 9	10 7 2 1
7 5 4 3 1 (QE=420)	11 9	10 8 2

Of these, although 10 9 1 has the smallest quantum entanglement (90), the configuration with only two packages, 11 9, in the passenger compartment gives Santa the most legroom and wins. In this situation, the quantum entanglement for the ideal configuration is therefore 99. Had there been two configurations with only two packages in the first group, the one with the smaller quantum entanglement would be chosen.

What is the quantum entanglement of the first group of packages in the ideal configuration?

Part 2

That's weird... the sleigh still isn't balancing.

"Ho ho ho", Santa muses to himself. "I forgot the trunk".

Balance the sleigh again, but this time, separate the packages into four groups instead of three. The other constraints still apply.

Given the example packages above, this would be some of the new unique first groups, their quantum entanglements, and one way to divide the remaining packages:

Group 1	Group 2	Group 3	Group 4
11 4 (QE=44)	10 5	9321	8 7
10 5 (QE=50)	11 4	9321	8 7
9 5 1 (QE=45)	11 4	10 3 2	8 7
9 4 2 (QE=72)	11 3 1	10 5	8 7
9 3 2 1 (QE=54)	11 4	10 5	87
8 7 (QE=56)	11 4	10 5	9321

Of these, there are three arrangements that put the minimum (two) number of packages in the first group: 11 4, 10 5, and 8 7. Of these, 11 4 has the lowest quantum entanglement, and so it is selected.

Now, what is the quantum entanglement of the first group of packages in the ideal configuration?

And here's the code. Some things to note:

- There are two parts and two solution algorithms per part.
- Bins are represented by a list of 1s and 0s to indicate if a particular weight is in bin 1 or either of bin 2 or bin 3.
- It doesn't matter which items are in bin 2 vs. bin 3, only that bin 1 represents \$\frac{1}{3}\$ of the total
- In my initial attempts on the problem I solved for bin 2 and bin3 and it took an order of magnitude longer to solve.
- Faster solving depends very much on selecting the right problem to solve!
- The first algorithm go_kn uses a modified version of the knapsack algorithm from the Picat book about constraint solving. It does not use the cp solver module. It a standard BFS (or is it DFS) with the amazing table to memoize and speed up.
- The second algorithm is uses cp and #= to constrain the solution to the problem statement.
- Algorithm 1 (tabling) is much faster than algorithm 2 (CP), but both are pretty fast. Interestingly part 1 shows a bigger difference in times than part 2.

	Knapsack	CP default	CP degree/updown
Part 1	0.010s	1.6s	0.263s
Part 2	0.001s	0.5s	0.019s

• The table has two columns for CP. One is the default search strategy solve(), the second specifies degree and updown, which mean, according to the Manual.

- degree: Variables are first ordered by degree, i.e., the number of connected variables.
- updown: Values are assigned to variables from the values that are nearest to the middle of the domain.
- A full list of the possible search strategies is on page 100 of the Manual.
- This is where a *little bit of the magic wears off*. Having some sense of your problem and how to search it best does help. On the other hand, you can just try all the methods and see which works best.
- It is not usually clear at the outset which will be the fastest method. See pgs 59-61 in the Picat constraint book for an example of trying all the combinations of solve options on a Magic Squares problem.
- Regardless, I found the CP version of the problem easier to grok and less CS major than the recursive graph search of the standard knapsack. And that's why we're using Picat, right? For the magic of letting the computer search.
- I used println via report inside of solve to track what's going on because I was having a hard time to get this code to work.
- As I understand it, Picat does not really support multi-objective optimization with two min/1. So I'm not sure how I got this to work!

```
import cp.
main =>
   % Weights = {1, 2, 3, 4, 5, 7, 8, 9, 10, 11}, % example
   Weights =
{1,2,3,7,11,13,17,19,23,31,37,41,43,47,53,59,61,67,71,73,79,83,89,97,101,10
3,107,109,113}, % problem
    time(go_kn(Weights,sum(Weights)//3, 1)),
    printf("\n"),
    time(go(Weights, sum(Weights)//3, 1)),
    printf("\n"),
    time(go_kn(Weights, sum(Weights)//4, 2)),
    printf("\n"),
    time(go(Weights, sum(Weights)//4, 2)).
go(Weights, Target, Q) =>
    assign_bin1(Weights, Target, Bins, QE, L1),
    % solve($[min(L1), min(QE), % using degree and updown is faster
    solve($[degree,updown,min(L1), min(QE),
              report(printf("Found %w, %w %w\n", L1, QE, Bins))], % debug
info from inside solve!
              Bins),
    Bin1Weights = [Weights[I]: I in 1..Weights.length, Bins[I]==0],
    printf("Bin 1: %w\n",Bin1Weights),
    printf("CP Answer Part %d: %w\n",Q,prod(Bin1Weights)).
assign_bin1(Weights, Target, Bins, QE, L1) =>
    N = length(Weights),
```

```
Bins = new_array(N),
    Bins :: 0..1,
    Bin1Sum #= sum([Weights[I]*(Bins[I] #= 0) : I in 1..N]),
    Bin1Sum #= Target,
    L1 \# sum([(Bins[I] \# 0) : I in 1..N]), \% Minimize L1 = Bin 1 length
    QE \#= prod([max(1,W*(Bins[I]\#=0)) : I in 1..N, W = Weights[I]]). %
Minimize QE = product of weights in bin 1
go_kn(Weights, Target, Q) =>
    knapsack(to_list(Weights), Target, Sack, Val),
    printf("Bin 1: %w\n", Sack),
    printf("Table Answer Part %d: %w\n",Q,second(Val)).
% knapsack modified from https://picat-
lang.org/picatbook2015/constraint_solving_and_planning_with_picat.pdf
% Val = (Length of Sack, QE)
% Item is a list of weights
% for the table + is input, - is output, and min is the objective
table(+,+,-,min)
knapsack(_,C,Sack,Val), C<=0 =>
    Sack = [], Val = (1,1).
knapsack([\_|L],C,Sack,Val),C>0?=>
    knapsack(L,C,Sack,Val).
knapsack([IWeight|L],C,Sack,Val), C >= IWeight =>
    Sack = [IWeight|Sack1],
    knapsack(L,C-IWeight,Sack1,Val1),
    Val = (first(Val1)+1, second(Val1)*IWeight).
```

Here's some of the output:

The Planner

The planner module is, as far as I know, unique to Picat. It lets you define a starting state, action to create the next state, the final/goal state, and then just solve it. It's quite amazing!

Planner acts as high-level interface to the underlying solver and mechanics of tabling and goal state checking.

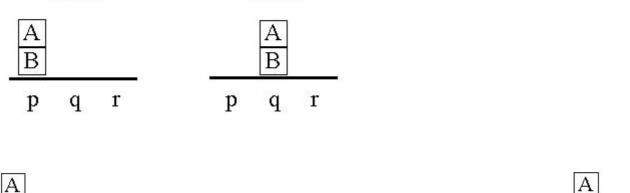
Planner Example: Blocks World

Start

Here's an example from the documentation for the programming language Curry, which combines functional and logic paradigms. https://curry-lang.org/docs/tutorial/html/curry-tutorial.Ch6.S1.html#SS3

The "blocks world" consists of 3 possibly empty piles, labeled p, q and r, of unique blocks labeled A, B, C, etc. "Start" and "Final" below are two examples from blocks world.

Final



A blocks world "problem" consists of two worlds, like Start and Final above. Its solution consists in the moves that produce the second world from the first one. A "move" transfers the block on top of a pile to the top of another pile. No other blocks are affected by the move.

Here's a solution with the Picat planner.

Note: A neat trick here is the use of () and; (meaning "or") to create the equivalent of a case statement in another language. Although it's not really a case statement. More detail on this here.

```
import planner.

main =>
    problem(S),
    best_plan(S,Plan), % solves the problem S
    println(S[1]), % prints the first state
    foreach (Step in Plan)
        println(Step) % prints each state
    end,
    printf("Solution cost: %w\n", length(Plan)).

% uncomment an S to run it
problem(S) =>
    % S = [[[a,b],[],[]], [[],[a,b],[]]]. % simple
```

```
% S = [[[a,b],[],[]], [[],[b,a],[]]]. % simple
    S = [[[a,b,c,d,e],[],[]], [[],[c,b,a,d,e],[]]]. % difficult
% the goal state
final(State), State[1] == State[2] => true.
% action predicate defines how to go to the next state: NextS
% Action variable is used to write the chosen step to the log
action([[S1,S2,S3],G],NextS,Action,Cost) =>
    % pattern match on all the possible moves
    % this works like a case statement although all options are evaluated
    % Goal is G and is passed through as part of the state
    S1 = [H1|T1],
        NewS1 = T1,
        NewS2 = [H1|S2],
        NewS3 = S3,
        Action = ("1->2", NewS1, NewS2, NewS3)
    S1 = [H1|T1],
        NewS1 = T1,
        NewS2 = S2,
        NewS3 = [H1|S3],
        Action = ("1->3", NewS1, NewS2, NewS3)
    S2 = [H2|T2],
        NewS1 = S1,
        NewS2 = T2,
        NewS3 = [H2|S3],
        Action = ("2->3", NewS1, NewS2, NewS3)
    S2 = [H2|T2],
        NewS1 = [H2|S1],
        NewS2 = T2,
        NewS3 = S3,
        Action = ("2->1", NewS1, NewS2, NewS3)
    S3 = [H3|T3],
        NewS1 = [H3|S1],
        NewS2 = S2,
        NewS3 = T3,
        Action = ("3->1", NewS1, NewS2, NewS3)
    S3 = [H3|T3],
        NewS1 = S1,
        NewS2 = [H3|S2],
        NewS3 = T3,
        Action = $("3->2", NewS1, NewS2, NewS3)
    ),
    Cost = 1, % the cost for a given step
```

```
NextS = [[NewS1,NewS2,NewS3],G]. % the next state.
```

This outputs:

```
[abcde,[],[]]
(1->2,bcde,a,[])
(1->2,cde,ba,[])
(1->3,de,ba,c)
(2->3,de,a,bc)
(2->3,de,[],abc)
(1->3,e,[],dabc)
(1->2,[],e,dabc)
(3->2,[],de,abc)
(3->2,[],bade,c)
(3->2,[],cbade,[])
Solution cost: 11
```

Planner Example: Wizards!

https://adventofcode.com/2015/day/22

Advent of Code 2015 day 22. This has a long description, sorry! But hopefully helpful in understanding what's needed.

```
--- Day 22: Wizard Simulator 20XX ---
```

Little Henry Case decides that defeating bosses with swords and stuff is boring. Now he's playing the game with a wizard. Of course, he gets stuck on another boss and needs your help again.

In this version, combat still proceeds with the player and the boss taking alternating turns. The player still goes first. Now, however, you don't get any equipment; instead, you must choose one of your spells to cast. The first character at or below 0 hit points loses.

Since you're a wizard, you don't get to wear armor, and you can't attack normally. However, since you do magic damage, your opponent's armor is ignored, and so the boss effectively has zero armor as well. As before, if armor (from a spell, in this case) would reduce damage below 1, it becomes 1 instead - that is, the boss' attacks always deal at least 1 damage.

On each of your turns, you must select one of your spells to cast. If you cannot afford to cast any spell, you lose. Spells cost mana; you start with 500 mana, but have no maximum limit. You must have enough mana to cast a spell, and its cost is immediately deducted when you cast it. Your spells are Magic Missile, Drain, Shield, Poison, and Recharge.

Magic Missile costs 53 mana. It instantly does 4 damage. Drain costs 73 mana. It instantly does 2 damage and heals you for 2 hit points. Shield costs 113 mana. It starts an effect that lasts for 6 turns. While it is active, your armor is increased by 7. Poison costs 173 mana. It starts an effect that lasts for 6 turns. At the start of each turn while it is active, it deals the boss 3 damage. Recharge costs 229

mana. It starts an effect that lasts for 5 turns. At the start of each turn while it is active, it gives you 101 new mana. Effects all work the same way. Effects apply at the start of both the player's turns and the boss' turns. Effects are created with a timer (the number of turns they last); at the start of each turn, after they apply any effect they have, their timer is decreased by one. If this decreases the timer to zero, the effect ends. You cannot cast a spell that would start an effect which is already active. However, effects can be started on the same turn they end.

For example, suppose the player has 10 hit points and 250 mana, and that the boss has 13 hit points and 8 damage:

- -- Player turn --
 - Player has 10 hit points, 0 armor, 250 mana
 - Boss has 13 hit points Player casts Poison.
- -- Boss turn --
 - Player has 10 hit points, 0 armor, 77 mana
 - Boss has 13 hit points Poison deals 3 damage; its timer is now 5. Boss attacks for 8 damage.
- -- Player turn --
 - Player has 2 hit points, 0 armor, 77 mana
 - Boss has 10 hit points Poison deals 3 damage; its timer is now 4. Player casts Magic Missile, dealing 4 damage.
- -- Boss turn --
 - Player has 2 hit points, 0 armor, 24 mana
 - Boss has 3 hit points Poison deals 3 damage. This kills the boss, and the player wins. Now, suppose the same initial conditions, except that the boss has 14 hit points instead:
- -- Player turn --
 - Player has 10 hit points, 0 armor, 250 mana
 - Boss has 14 hit points Player casts Recharge.
- -- Boss turn --
 - Player has 10 hit points, 0 armor, 21 mana
 - Boss has 14 hit points Recharge provides 101 mana; its timer is now 4. Boss attacks for 8 damage!
- -- Player turn --
 - Player has 2 hit points, 0 armor, 122 mana
 - Boss has 14 hit points Recharge provides 101 mana; its timer is now 3. Player casts Shield, increasing armor by 7.
- -- Boss turn --
 - Player has 2 hit points, 7 armor, 110 mana

• Boss has 14 hit points Shield's timer is now 5. Recharge provides 101 mana; its timer is now 2. Boss attacks for 8 - 7 = 1 damage!

-- Player turn --

- Player has 1 hit point, 7 armor, 211 mana
- Boss has 14 hit points Shield's timer is now 4. Recharge provides 101 mana; its timer is now 1. Player casts Drain, dealing 2 damage, and healing 2 hit points.

-- Boss turn --

- Player has 3 hit points, 7 armor, 239 mana
- Boss has 12 hit points Shield's timer is now 3. Recharge provides 101 mana; its timer is now 0. Recharge wears off. Boss attacks for 8 7 = 1 damage!

-- Player turn --

- Player has 2 hit points, 7 armor, 340 mana
- Boss has 12 hit points Shield's timer is now 2. Player casts Poison.

-- Boss turn --

- Player has 2 hit points, 7 armor, 167 mana
- Boss has 12 hit points Shield's timer is now 1. Poison deals 3 damage; its timer is now 5. Boss attacks for 8 7 = 1 damage!

-- Player turn --

- Player has 1 hit point, 7 armor, 167 mana
- Boss has 9 hit points Shield's timer is now 0. Shield wears off, decreasing armor by 7. Poison deals 3 damage; its timer is now 4. Player casts Magic Missile, dealing 4 damage.

-- Boss turn --

- Player has 1 hit point, 0 armor, 114 mana
- Boss has 2 hit points Poison deals 3 damage. This kills the boss, and the player wins. You start with 50 hit points and 500 mana points. The boss's actual stats are in your puzzle input. (see code below) What is the least amount of mana you can spend and still win the fight? (Do not include mana recharge effects as "spending" negative mana.)

--- Part Two ---

On the next run through the game, you increase the difficulty to hard.

At the start of each player turn (before any other effects apply), you lose 1 hit point. If this brings you to or below 0 hit points, you lose.

With the same starting stats for you and the boss, what is the least amount of mana you can spend and still win the fight?

Like I said, that was a lot of instruction. Here's a short table with the spells summarized.

Spell	Mana	Damage	Heal	Effect
Missile	53	4		
Drain	73	2	2	
Shield	113			+7 armor for 6 turns
Poison	173			3 damage for 6 turns
Recharge	229			+101 mana for 5 turns

The code is below. Some things to note:

- The problem state is expressed with a nested list that includes all of the elements, even if they don't get modified, such as the boss' damage to the player.
- This state is passed from each action to the next and modified as needed based on the chosen action.
- There are two action predicates, which are pattern matched on whose turn it is. 0 for the player and 1 for the boss. (And why is Bruce Springsteen always the enemy?)
- The notation State@[0,[MaxHP, HP, Mana, BHP, BDamage], Shield, Poison, Recharge, Mode] binds the variable State to all of the list after the @ sign. This way it can be referenced in whole in the Action variable rather than having to retype all of that.
- The notation _ for variables in the final predicate mean that the variable isn't being used and this is simply a placeholder. The term of art here is *anonymous variable*. Which is weird to think about. It's still variable, but no one cares.
- Like Blocks World, this code uses a construct similar to a case statement formed through clauses separated by; meaning "or". (It's not exactly a case statement because backtracking/failure will automatically evaluate the other alternatives. Logic programming! See this section.)
- sign is used to avoid having an if. For example, NBHP = BHP (3 * sign(Poison)) means that if Poison is 0, then sign(Poison) is 0, but if Poison is greater than 0, sign returns 1. It didn't run any faster, but I felt like a boss for writing it this way.
- The list of possible spells is built up by addition, ++, rather than starting with all and removing. At first I tried removing, but the logic was complex to use delete and hard to implement. Accumulating allowed spells was much more straightforward to code.
- Also, the ability to reassign, :=, or what the functional people call *mutability*, can be very handy. *Impure* as the functional crowd calls it, yes, but oh so nice. However, like any good weapon, one must be careful to not cut off your own foot, so be careful when reassigning variable values. Standard Prolog, fyi, has only immutable variables.
- The key to this problem is trying all of the possible spells that are available. That's where member comes in. This line

member([Spell, SpellMana], Spells

means: non-deterministically select a pair of values from the Spells list and then try all the other ones. Or at least all the other ones that meet the criteria of the solver. **And this is the holy grail.** While I have some sense of which values will be picked and how the selection happens, and while to really get the most out of Picat I do need to know this, I also kind of don't need to know.

• member means not having to learn how to write my own depth-first (DFS) or breadth-first search (BFS). **How cool is this?**

```
import planner.
import math.
main =>
    problem(S),
    Initial1 = [0,S,0,0,0,0], % Turn, [Player, Boss], Shield, Poison,
Recharge, Mode
    % time2(best_plan_unbounded(Initial1,Plan1,PlanCost1)), % 3.33 s
    % time2(best_plan(Initial1,Plan1,PlanCost1)), % 1.72 s
    time2(best_plan_bb(Initial1,Plan1,PlanCost1)), % 0.06 s
    foreach (Step in Plan1)
        println(Step)
    end,
    printf("Part 1 solution length: %w\n", length(Plan1)),
    printf("Part 1 answer = mana cost: %w\n", PlanCost1),
    Initial2 = [0,S,0,0,0,1],
    time2(best plan bb(Initial2,Plan2,PlanCost2)), % fastest
    printf("Part 2 solution length: %w\n", length(Plan2)),
    printf("Part 2 answer = mana cost: %w\n", PlanCost2).
problem(S) =>
    % S = [10,10,250,13,8]. % Example 1: 10 Max HP, 10 HP, 250 mana, boss
13 HP and 8 damage
   % S = [10,10,250,14,8]. % Example 2: 10 Max HP, 10 HP, 250 mana, boss
14 HP and 8 damage
    S = [50,50,500,55,8]. % Puzzle: 10 Max HP, 10 HP, 250 mana, boss 14 HP
and 8 damage
final(State@[_,[_, HP, Mana, BHP, _], _, _, _, _]), HP > 0, BHP <= 0 =>
true.
% Play Turn 0
action(State@[0,[MaxHP, HP, Mana, BHP, BDamage], Shield, Poison, Recharge,
Mode], NextS, Action, Cost) =>
   HP := HP - Mode,
    Mana := Mana + (101 * sign(Recharge)), % apply recharge
    Spells = [["missile", 53], ["drain", 73]],
    if (Shield <= 1) then (Spells := Spells ++ [["shield", 113]]) end,
    if (Poison <= 1) then (Spells := Spells ++ [["poison", 173]]) end,
    if (Recharge <= 1) then (Spells := Spells ++ [["recharge", 229]]) end,
```

```
member([Spell,SpellMana],Spells),
    SpellMana <= Mana,
    NMana := Mana - SpellMana,
     Spell == "missile" , BHP := BHP - 4;
     Spell == "drain" , BHP := BHP - 2, HP := min(HP+2, MaxHP);
     Spell == "shield" , Shield := 6;
     Spell == "poison" , Poison := 6;
     Spell == "recharge" , Recharge := 5 + 1
    NBHP = BHP - (3 * sign(Poison)), % apply poison
    Action = [State, Spell],
    Cost = SpellMana,
    NextS = [1,[MaxHP, HP, NMana, NBHP, BDamage], max([Shield-1,0]),
max([Poison-1,0]), max([Recharge-1,0]), Mode].
% Boss Turn 1
action(State@[1,[MaxHP, HP, Mana, BHP, BDamage], Shield, Poison, Recharge,
Mode],NextS,Action,Cost) =>
    Mana := Mana + (101 * sign(Recharge)), % apply recharge
    NBHP = BHP-(3 * sign(Poison)), % apply poison
    NHP = HP - max([BDamage-(7 * sign(Shield)),1]), % min damage = 1
    NHP > 0,
    Action = [State, boss],
    Cost = 0,
    NextS = [0,[MaxHP, NHP, Mana, NBHP, BDamage], max([Shield-1,0]),
max([Poison-1,0]), max([Recharge-1,0]), Mode].
```

And here's the output:

```
% Searching with the bound 268435455
% Searching with the bound 3518
% Searching with the bound 3405
% Searching with the bound 2970
% Searching with the bound 2917
% Searching with the bound 2482
% Searching with the bound 2296
% Searching with the bound 2001
% Searching with the bound 1928
% Searching with the bound 1742
% Searching with the bound 1460
% Searching with the bound 1347
% Searching with the bound 1294
% Searching with the bound 952
CPU time 0.09 seconds. Backtracks: 0
[[0,[50,50,500,55,8],0,0,0,0],missile]
[[1,[50,50,447,51,8],0,0,0,0],boss]
[[0,[50,42,447,51,8],0,0,0,0],poison]
```

```
[[1,[50,42,274,48,8],0,5,0,0],boss]
[[0,[50,34,274,45,8],0,4,0,0],recharge]
[[1,[50,34,45,42,8],0,3,5,0],boss]
[[0,[50,26,146,39,8],0,2,4,0],missile]
[[1,[50,26,194,32,8],0,1,3,0],boss]
[[0,[50,18,295,29,8],0,0,2,0],shield]
[[1,[50,18,283,29,8],5,0,1,0],boss]
[[0,[50,17,384,29,8],4,0,0,0],poison]
[[1,[50,17,211,26,8],3,5,0,0],boss]
[[0,[50,16,211,23,8],2,4,0,0],missile]
[[1,[50,16,158,16,8],1,3,0,0],boss]
[[0,[50,15,158,13,8],0,2,0,0],missile]
[[1,[50,15,105,6,8],0,1,0,0],boss]
[[0,[50,7,105,3,8],0,0,0,0],missile]
Part 1 solution length: 17
Part 1 answer = mana cost: 953
% Searching with the bound 268435455
% Searching with the bound 1500
% Searching with the bound 1460
% Searching with the bound 1407
% Searching with the bound 1294
% Searching with the bound 1288
CPU time 0.045 seconds. Backtracks: 0
Part 2 solution length: 17
Part 2 answer = mana cost: 1289
```

Planner Example: Moving Stuff

https://adventofcode.com/2016/day/11

Advent of Code 2016 day 11 has you moving stuff up and down with an elevator based on constraints. So perfect for Planner! Apologies again for the length of the description.

```
--- Day 11: Radioisotope Thermoelectric Generators ---
```

You come upon a column of four floors that have been entirely sealed off from the rest of the building except for a small dedicated lobby. There are some radiation warnings and a big sign which reads "Radioisotope Testing Facility".

According to the project status board, this facility is currently being used to experiment with Radioisotope Thermoelectric Generators (RTGs, or simply "generators") that are designed to be paired with specially-constructed microchips. Basically, an RTG is a highly radioactive rock that generates electricity through heat.

The experimental RTGs have poor radiation containment, so they're dangerously radioactive. The chips are prototypes and don't have normal radiation shielding, but they do have the ability to generate an electromagnetic radiation shield when powered. Unfortunately, they can only be powered by their corresponding RTG. An RTG powering a microchip is still dangerous to other microchips.

In other words, if a chip is ever left in the same area as another RTG, and it's not connected to its own RTG, the chip will be fried. Therefore, it is assumed that you will follow procedure and keep chips connected to their corresponding RTG when they're in the same room, and away from other RTGs otherwise.

These microchips sound very interesting and useful to your current activities, and you'd like to try to retrieve them. The fourth floor of the facility has an assembling machine which can make a self-contained, shielded computer for you to take with you - that is, if you can bring it all of the RTGs and microchips.

Within the radiation-shielded part of the facility (in which it's safe to have these pre-assembly RTGs), there is an elevator that can move between the four floors. Its capacity rating means it can carry at most yourself and two RTGs or microchips in any combination. (They're rigged to some heavy diagnostic equipment - the assembling machine will detach it for you.) As a security measure, the elevator will only function if it contains at least one RTG or microchip. The elevator always stops on each floor to recharge, and this takes long enough that the items within it and the items on that floor can irradiate each other. (You can prevent this if a Microchip and its Generator end up on the same floor in this way, as they can be connected while the elevator is recharging.)

You make some notes of the locations of each component of interest (your puzzle input). Before you don a hazmat suit and start moving things around, you'd like to have an idea of what you need to do.

When you enter the containment area, you and the elevator will start on the first floor.

For example, suppose the isolated area has the following arrangement:

The first floor contains a hydrogen-compatible microchip and a lithium-compatible microchip. The second floor contains a hydrogen generator. The third floor contains a lithium generator. The fourth floor contains nothing relevant. As a diagram (F# for a Floor number, E for Elevator, H for Hydrogen, L for Lithium, M for Microchip, and G for Generator), the initial state looks like this:

```
F4 . . . . . .
F3 . . . LG .
F2 . HG . . .
F1 E . HM . LM
```

Then, to get everything up to the assembling machine on the fourth floor, the following steps could be taken:

Bring the Hydrogen-compatible Microchip to the second floor, which is safe because it can get power from the Hydrogen Generator:

```
F4 . . . . . F3 . . . LG . F2 E HG HM . . F1 . . . LM
```

Bring both Hydrogen-related items to the third floor, which is safe because the Hydrogen-compatible microchip is getting power from its generator:

Leave the Hydrogen Generator on floor three, but bring the Hydrogen-compatible Microchip back down with you so you can still use the elevator:

```
F4 . . . . . . F3 . HG . LG . F2 E . HM . . F1 . . . LM
```

At the first floor, grab the Lithium-compatible Microchip, which is safe because Microchips don't affect each other:

```
F4 . . . . . . F3 . HG . LG . F2 . . . . . . F1 E . HM . LM
```

Bring both Microchips up one floor, where there is nothing to fry them:

```
F4 . . . . . . F3 . HG . LG . F2 E . HM . LM F1 . . . . .
```

Bring both Microchips up again to floor three, where they can be temporarily connected to their corresponding generators while the elevator recharges, preventing either of them from being fried:

```
F4 . . . . . . F3 E HG HM LG LM
F2 . . . . . .
F1 . . . . .
```

Bring both Microchips to the fourth floor:

```
F4 E . HM . LM
F3 . HG . LG .
F2 . . . .
F1 . . . .
```

Leave the Lithium-compatible microchip on the fourth floor, but bring the Hydrogen-compatible one so you can still use the elevator; this is safe because although the Lithium Generator is on the destination floor, you can connect Hydrogen-compatible microchip to the Hydrogen Generator there:

```
F4 . . . LM
F3 E HG HM LG .
F2 . . . .
F1 . . . .
```

Bring both Generators up to the fourth floor, which is safe because you can connect the Lithium-compatible Microchip to the Lithium Generator upon arrival:

```
F4 E HG . LG LM
F3 . . HM . .
F2 . . . .
F1 . . . .
```

Bring the Lithium Microchip with you to the third floor so you can use the elevator:

```
F4 . HG . LG .
F3 E . HM . LM
F2 . . . .
F1 . . . .
```

Bring both Microchips to the fourth floor:

```
F4 E HG HM LG LM
F3 . . . . .
F2 . . . . .
F1 . . . .
```

In this arrangement, it takes 11 steps to collect all of the objects at the fourth floor for assembly. (Each elevator stop counts as one step, even if nothing is added to or removed from it.)

In your situation, what is the minimum number of steps required to bring all of the objects to the fourth floor?

--- Part Two ---

You step into the cleanroom separating the lobby from the isolated area and put on the hazmat suit.

Upon entering the isolated containment area, however, you notice some extra parts on the first floor that weren't listed on the record outside:

- An elerium generator.
- An elerium-compatible microchip.
- A dilithium generator.
- A dilithium-compatible microchip.

These work just like the other generators and microchips. You'll have to get them up to assembly as well.

What is the minimum number of steps required to bring all of the objects, including these four new ones, to the fourth floor?

Phew! Here's the code. And some things to note:

- The problem state is represented by two lists: one with the floor each molecule is on and one with the floor each generator is on.
- These two arrays are parallel so that the same molecule and generator are paired by index in the problem setup.
- The names of the molecules/generators are not stored. It is inferred by the index into the list, but as you will see, we play fast and loose with this.
- The solution speed is very dependent on how the search space is reduced through the constraints. My initial version took 45 seconds for part 1 and 245 seconds for part 2. After many enhancements, the time was reduced to 0.02 and 0.09 seconds, respectively.
- Here's what made the code run faster:
 - unbounded search (depth first)
 - Item2 < Item1 removes the symmetric solutions where Item1 >= Item2
 - extract get_move into its own function
 - precompute the number of items and pass as state (MolE.len for example)
 - Action is set to []
 - ++[0] instead of [0]++ when setting Item2
 - counter function instead of membchk
 - try to bring up two whenever possible and only down one
 - only go down if items are on floors below the elevator
 - *Biggest gain* zipped pairs of {Mol, Gen} sorted rather than [Mol ++ Gen] this allows for symmetry breaking meaning that moving a pair {2,0}, for example, doesn't matter if it's one molecule or another, the move is identical.
 - remove table. I tried adding table everywhere, but it's built into the planner and just slowed things down
- I also tried adding a heuristic function. In this case it didn't make any difference.
- In terms of the search method, best_plan_unbounded was the fastest. The other methods were about twice as long to complete: best_plan, best_plan_bin, best_plan_bb and best_plan_nondet.

There a great explanation of how to solve efficiently on Reddit.
 https://www.reddit.com/r/adventofcode/comments/5hoia9/comment/db1v1ws/

• In case you didn't see this syntax elsewhere here S@[A,B,C] means that S is bound to the list [A,B,C] and that it can be referenced wherever you want to use the entire list without decomposing it.

```
import planner.
import util.
main =>
   % example, requires 11 moves
   MolE = [1,1], %H, Li
    GenE = [2,3], %HGen, LiGen
    ProbE = [1,MolE.len,zip(MolE,GenE).sort], % elevator on ground floor
    time2(best_plan_unbounded(ProbE,PlanE)),
    printf("Example solution length: %w\n", length(PlanE)),
    % part 1
    Mol1 = [2,1,2,1,1], %Po, Tm, Pm, Ru, Co
    Gen1 = [1,1,1,1,1], %Po, Tm, Pm, Ru, Co
    Prob1 = [1,Mol1.len,zip(Mol1,Gen1).sort], % elevator on ground floor
    time2(best_plan_unbounded(Prob1,Plan1)),
    printf("Part 1 solution length: %w\n", length(Plan1)),
    % part 2
    Mol2 = [2,1,2,1,1,1,1], Po, Tm, Pm, Ru, Co, El, Di
    Gen2 = [1,1,1,1,1,1,1], %Po, Tm, Pm, Ru, Co, El, Di
    Prob2 = [1,Mol2.len,zip(Mol2,Gen2).sort], % elevator on ground floor
    time2(best_plan_unbounded(Prob2,Plan2)),
    printf("Part 2 solution length: %w\n", length(Plan2)).
final(State@[E,N,Items]),Items.map(sum).sum == 4*2*N => true. % all 4th
floor
action(State@[E,N,Items],NextS,Action,Cost) =>
    [NewE, NewItems] = get_move(E, N, Items),
    Action = [],
    % 30x speedup pairs/sort and action memoizes duplicate states
    NextS = [NewE,N,NewItems.pairs.sort],
    Cost = 1.
get_move(E,N,Items) = [NewE,NewItems] =>
    N2 = N*2
    FlatItems = Items.map(to_list).flatten,
    % .001 sec speedup
    if min(FlatItems) >= E % don't move to emptied bottom floors
        then Move = 1
        else member(Move,[-1,1]) end,
    NewE = E+Move, NewE >0, NewE <=4, % elevator moves
    FloorItems = [I : I in 1..N2, FlatItems[I] == E], % pick item from
```

```
current floor
    member(Item1, FloorItems),
    NewItems = copy_term(FlatItems),
    NewItems[Item1] := FlatItems[Item1]+Move,
    % 0.3x speedup
    if Move = 1 % always try to bring up two / down one item
    then member(Item2, FloorItems++[0]),
         Item2 < Item1,</pre>
         if Item2 > 0 then
            NewItems[Item2] := FlatItems[Item2]+Move end
    end,
    NewGBF = counter(NewItems), % GBF means generators by floor
    foreach (I in 1..2..N2) % step 2.
       NewItems[I] = NewItems[I+1]; % mol attached to its generator OR
       NewGBF[NewItems[I]] = 0 % no other gen on floor
    end.
% would be nice if this were builtin, but easy enough to code
pairs(L) = [\{L[I], L[I+1]\} : I in 1..2..L.len].
% counter is O(n)
counter(L) = R =>
    R = [0,0,0,0],
    foreach(I in 2..2..L.len)
        R[L[I]] := 1
    end.
```

Planner Example: Twisty Passages All The Same

https://adventofcode.com/2016/day/13

Advent of Code 2016 day 13 has another good candidate for the planner.

```
--- Day 13: A Maze of Twisty Little Cubicles ---
```

You arrive at the first floor of this new building to discover a much less welcoming environment than the shiny atrium of the last one. Instead, you are in a maze of twisty little cubicles, all alike.

Every location in this area is addressed by a pair of non-negative integers (x,y). Each such coordinate is either a wall or an open space. You can't move diagonally. The cube maze starts at 0,0 and seems to extend infinitely toward positive x and y; negative values are invalid, as they represent a location outside the building. You are in a small waiting area at 1,1.

While it seems chaotic, a nearby morale-boosting poster explains, the layout is actually quite logical. You can determine whether a given x,y coordinate will be a wall or an open space using a simple system:

```
Find x*x + 3*x + 2*x*y + y + y*y.
```

Add the office designer's favorite number (your puzzle input).

Find the binary representation of that sum; count the number of bits that are 1.

If the number of bits that are 1 is even, it's an open space.

If the number of bits that are 1 is odd, it's a wall.

For example, if the office designer's favorite number were 10, drawing walls as # and open spaces as ., the corner of the building containing 0,0 would look like this:

```
0123456789
0 .#.###.##
1 ..#..#
2 #....##...
3 ###.###.
4 .##..#..
5 ..##...#.
6 #...##.##
```

Now, suppose you wanted to reach 7,4. The shortest route you could take is marked as O:

```
0123456789
0 .#.###.##
1 .0#..#..#
2 #000.##...
3 ###0#.###.
4 .##00#00#.
5 ..##000.#.
6 #...##.###
```

Thus, reaching 7,4 would take a minimum of 11 steps (starting from your current location, 1,1).

What is the fewest number of steps required for you to reach 31,39?

--- Part Two --- How many locations (distinct x,y coordinates, including your starting location) can you reach in at most 50 steps?

Here's the code. Items of note:

• The biggest gain is from tabling the function f which indicates if a given coordinate is a wall or open space.

- Tabling action also gives a small speedup.
- The planner will use the function named heuristic, if provided, as an aid in finding the solution. Here this approach helped by providing the "Manhattan distance" to the solution for part 1.
- For part 2 there are two algorithms, a standard breadth first search (BFS) which does not use the solver and a "brute force" approach of just calling the solver on every possible coordinate that's up to 50 steps away from the start.
- I couldn't wrap my head around BFS and had to turn to ChatGPT, which, except for some syntax errors, provided the code. This runs super fast, 0.001 seconds.
- For the brute force solution, Picat is fast enough to get it done in less than 0.4 seconds.

```
import planner.
main =>
   % End = [7,4], % example
    I = 1358, % puzzle
    End = [31,39], % part 1
    Start = [1,1],
    print_maze(9,9,I),
    time(best_plan([Start,End,I],Plan,Cost)), % .007 sec
    printf("Answer Part 1: %w\n",Cost),
    time(Part2Alt = part2alt(50,Start,I)), % 0.4 sec
    printf("Answer Part 2 Alt: %w\n",Part2Alt.len),
                                           % 0.001 sec
    time(Part2 = paths(50,Start,I)),
    printf("Answer Part 2: %w\n",Part2.len).
% Part 1
final([Loc,End,_]), Loc = End => true.
action(S@[[X,Y],End,I],NextS,Action,Cost) =>
    member([DX,DY],[[1,0],[0,1],[-1,0],[0,-1]]),
    NewX = X + DX, NewY = Y + DY,
    NewX >= 0, NewY >= 0,
    f(NewX, NewY, I), % no moving into a wall
    NextS = [[NewX, NewY], End, I],
    Action = [NewX, NewY],
    Cost = 1.
% 4x speedup
heuristic([[X,Y],[EX,EY],_]) = abs(X-EX)+abs(Y-EY).
% table 10x speedup
table
f(X,Y,I) = even((X*X + 3*X + 2*X*Y + Y + Y*Y +
I).to_binary_string.map(to_int).sum).
```

```
% Part 2
paths(Steps, Start, I) = Visited =>
    Visited = bfs(Steps, [Start],[Start], I).
% ChatGPT BFS
bfs(0, _Frontier, Visited, _I) = Visited.
bfs(Steps, Frontier, VisitedO, I) = VisitedFinal =>
    Next := [],
    Vacc := Visited0,
    foreach ([X,Y] in Frontier)
        foreach ([DX,DY] in [[1,0],[0,1],[-1,0],[0,-1]])
            NX = X + DX, NY = Y + DY,
            if NX \ge 0, NY \ge 0 then
                if f(NX,NY,I), not membchk([NX,NY], Vacc) then
                    Vacc := Vacc ++ [[NX,NY]],
                    Next := Next ++ [[NX,NY]]
                end
            end
        end
    VisitedFinal = bfs(Steps-1, Next, Vacc, I).
part2alt(Steps,Start,I) = R =>
    Poss = possible(Steps, Start, I),
    Visited = [],
    while (Poss != [])
        if best_plan([Start,Poss.head,I],Steps,Plan,Cost)
            then Visited := (Visited ++ [Poss.head]) end,
        Poss := Poss.tail,
    end,
    R = Visited.
possible(Steps,[X1,Y1],I) = R =>
    R = sort_remove_dups([[X+DX,Y+DY] : X in 0..Steps+1, Y in 0..Steps+1,
X+Y<=Steps+1,
                       [DX,DY] in [[1,0],[0,1],[-1,0],[0,-1]],
                       X+DX>=0, Y+DY>=0, f(X+DX,Y+DY,I).
% Helpers
print_maze(MX,MY,I) =>
    printf(" %w\n", stringify(0..MX)),
    foreach(Y in 0..MY)
        printf("%w ",Y),
        foreach(X in 0..MX)
            if f(X,Y,I) then Wall = "." else Wall = "#" end,
            printf("%w",Wall)
        end,
        printf("\n")
    end.
% My maze, upper corner
```

```
% 0123456789
% 0 .#.####.##
% 1 ..#..#
% 2 #....##...
% 3 ###.#.##
% 4 .##..#..
% 5 ..##...#.
% 6 #...##.##
stringify([]) = "".
stringify([H|T]) = to_string(H)++stringify(T).
```

Planner Example: Shortest and Longest Path

https://adventofcode.com/2016/day/17

```
--- Day 17: Two Steps Forward ---
```

You're trying to access a secure vault protected by a > 4x4 grid of small rooms connected by doors. You start in the top-left room (marked S), and you can access the vault (marked V) once you reach the bottom-right room:

Fixed walls are marked with #, and doors are marked with - or |.

The doors in your current room are either open or closed (and locked) based on the hexadecimal MD5 hash of a passcode (your puzzle input) followed by a sequence of uppercase characters representing the path you have taken so far (U for up, D for down, L for left, and R for right).

Only the first four characters of the hash are used; they represent, respectively, the doors up, down, left and right from your current position. Any b, c, d, e, or f means that the corresponding door is open; any other character (any number or a) means that the corresponding door is closed and locked.

To access the vault, all you need to do is reach the bottom-right room; reaching this room opens the vault and all doors in the maze.

For example, suppose the passcode is hijkl. Initially, > you have taken no steps, and so your path is empty: you simply find the MD5 hash of hijkl alone. The first four characters of this hash are ced9, which indicate that up is open (c), down is open (e), left is open (d), and right is closed and locked (9).

Because you start in the top-left corner, there are no "up" or "left" doors to be open, so your only choice is down.

Next, having gone only one step (down, or D), you find the hash of hijklD. This produces f2bc, which indicates that you can go back up, left (but that's a wall), or right. Going right means hashing hijklDR to get 5745 - all doors closed and locked. However, going up instead is worthwhile: even though it returns you to the room you started in, your path would then be DU, opening a different set of doors.

After going DU (and then hashing hijklDU to get 528e), only the right door is open; after going DUR, all doors lock. (Fortunately, your actual passcode is not hijkl).

Passcodes actually used by Easter Bunny Vault Security do allow access to the vault if you know the right path. For example:

If your passcode were ingpwlah, the shortest path would be DDRRRD.

With kglvqrro, the shortest path would be DDUDRLRRUDRD.

With ulgzkmiv, the shortest would be DRURDRUDDLLDLUURRDULRLDUUDDDRR.

Given your vault's passcode, what is the shortest path > (the actual path, not just the length) to reach the vault?

Your puzzle input is awrkjxxr.

--- Part Two ---

You're curious how robust this security solution really is, and so you decide to find longer and longer paths which still provide access to the vault. You remember that paths always end the first time they reach the bottom-right room (that is, they can never pass through it, only end in it). For example:

If your passcode were ingpwlah, the longest path would take 370 steps.

With kglvqrro, the longest path would be 492 steps long.

With ulqzkmiv, the longest path would be 830 steps long.

What is the length of the longest path that reaches the vault?

Notes on the solution code below:

- This is much like the other planner examples and the only challenge is that determining if a path from one location to another exists is based on the MD5 hash of a string based on the current path.
- planner is great in part 1 for shortest path and makes for very straightforward code. But it doesn't lend itself to solving for the worst case of the longest path.
- To solve part 2, we need to explore all paths until every choice and its children are explored. We stop at any solution where we get to the vault at location (4,4).
- A recursive, tabled, path predicate modeled on the shortest-path from the Picat manual solves part 2.
- Picat doesn't have an inbuilt MD5 function or available module. My choices were calling the Linux md5show command line utility or creating a binding to an MD5 library and recompiling Picat. I chose the command line.

• I thought I would be able to set and read an environment variable, but this did not work. The context was lost after making the shell command and could not be read. So I wrote the MD5 to a file and read it. This was, of course, quite slow. Here's the code:

```
table
system_md5(String) = MD5 =>
   Ret = command("echo -n "++String++ " | md5sum | awk '{print $1}' >
temp_md5"),
   MD5 = read_file_chars("temp_md5").
```

- For part 1, the limited number of calls to get MD5 didn't impact performance. Part 1 took less than 0.01 seconds. But part 2 took 300 seconds.
- Thus I explored option 3, have ChatGPT write an MD5 in pure Picat. ChatGPT was reluctant and initial refused to do the hard work of writing the full algorithm, and then preferred to give me ISO Prolog. ChatGPT and I then pair programmed our way to a Picat version.
- Part 2 time was reduced to 12 seconds.
- I put the MD5 in this appendix. There are a non-zero number of Advent of Code problems that require MD5, so it's available as a module for your use, should you need it.

```
import util.
import planner.
import md5. % homemade MD5 with ChatGPT
main =>
    % Code = "hijkl", % test case, fails as expected
    % Code = "ihgpwlah", % test case
    % Code = "kglvqrro", % test case
    % Code = "ulgzkmiv", % test case
    Code ="awrkjxxr", % RDURRDDLRD
    % part 1: .005 sec
    time(best_plan([Code,1,1],Plan,Cost)),
    printf("Answer Part 1: %w\n",Plan.join('')),
    % part 2: with chatGPT MD5 in Picat, 12 seconds
    path(Code, [1, 1], [4, 4], CostSP),
    printf("Answer Part 2: %w\n", CostSP-1).
% part 1 using planner
table
final(S@[Code,Row,Col]) =>
    Row == 4, Col == 4, true.
table
action(S@[Code,Row,Col],NextS,Action,Cost) =>
    Deltas = get_deltas(Code),
    member([DCode,DRow,DCol],Deltas),
    NRow = Row + DRow, between(1, 4, NRow),
    NCol = Col + DCol, between(1, 4, NCol),
```

```
NextS = [Code++DCode, NRow, NCol],
    Action = DCode,
    Cost = 1.
table
get_deltas(Code) = Deltas =>
    MD5 = md5(Code).take(4),
    Opts = [X : I in 1..4, X = cond(membchk(MD5[I], "bcdef"), 1, 0)],
    Deltas = [],
    if Opts[1] == 1 then Deltas := Deltas ++ [["U",-1, 0]] end,
    if Opts[2] == 1 then Deltas := Deltas ++ [["D", 1, 0]] end,
    if Opts[3] == 1 then Deltas := Deltas ++ [["L", 0,-1]] end,
    if Opts[4] == 1 then Deltas := Deltas ++ [["R", 0, 1]] end.
% Part 2 using recursive search and table
table(+,+,+,max)
path(Code,S@[Row,Col],Goal@[GRow,GCol],Cost),
    S = Goal
    Cost = 1,
    printf("%w\r",Code.len-8). % get some output to see progress
path(Code,S@[Row,Col],Goal@[GRow,GCol],Cost) =>
    Deltas = get_deltas(Code),
    member([DCode,DRow,DCol],Deltas),
    NRow = Row + DRow, between(1, 4, NRow),
    NCol = Col + DCol, between(1, 4, NCol),
    path(Code++DCode, [NRow, NCol], Goal, Cost1),
    Cost = 1 + Cost1.
```

Planner and Constraint Example: Traveling Salesperson

https://adventofcode.com/2016/day/24

Advent of Code has a challenge that is a classic traveling salesperson who has to visit multiple locations and take the overall shortest path.

```
--- Day 24: Air Duct Spelunking ---
```

You've finally met your match; the doors that provide access to the roof are locked tight, and all of the controls and related electronics are inaccessible. You simply can't reach them.

The robot that cleans the air ducts, however, can.

It's not a very fast little robot, but you reconfigure it to be able to interface with some of the exposed wires that have been routed through the HVAC system. If you can direct it to each of those locations, you should be able to bypass the security controls.

You extract the duct layout for this area from some blueprints you acquired and create a map with the relevant locations marked (your puzzle input). 0 is your current location, from which the cleaning robot embarks; the other numbers are (in no particular order) the locations the robot needs to visit at least once each. Walls are marked as #, and open passages are marked as .. Numbers behave like open passages.

For example, suppose you have a map like the following:

To reach all of the points of interest as quickly as possible, you would have the robot take the following path:

```
0 to 4 (2 steps)
4 to 1 (4 steps; it can't move diagonally)
1 to 2 (6 steps)
2 to 3 (2 steps)
```

Since the robot isn't very fast, you need to find it the shortest route. This path is the fewest steps (in the above example, a total of 14) required to start at 0 and then visit every other location at least once.

Given your actual map, and starting from location 0, what is the fewest number of steps required to visit every non-0 number marked on the map at least once?

Your puzzle answer was 412.

```
--- Part Two ---
```

Of course, if you leave the cleaning robot somewhere weird, someone is bound to notice.

What is the fewest number of steps required to start at 0, visit every non-0 number marked on the map at least once, and then return to 0?

Your puzzle answer was 664.

My initial solution took over 4 minutes, and by the time I was done optimizing, it was down to just over 4 seconds. How did I achieve such wizardry?

Note: 4 seconds is actually pretty slow compared to the solutions others came up with for this problem. But we aren't in this to win, or because we know how to solve this kind of problem with known algorithms, but because we wanted to solve it with the holy grail!

Attempts and speed:

- 1. A planner based solution with the option to move from a given Maze location to another if it's in a precomputed set of valid neighbors. As we go, add each Visited required location to a list and compare against the total required list. Reqs.
- 2. Don't compare the list of visited required locations with Reqs, just check its length. (20% speedup)
- 3. Rather than building a list of visited, delete from Regs as we visit one. (20% speedup)

4. Pre-compute dead ends, those locations with only one valid neighbor, and prune them if they aren't in Reqs. (25% speedup)

5. Use planner to find all the shortest paths and compute a Dists table of distances between all pairs of Reqs. Then use cp to get the minimum path that meets constraints of the problem. The bulk of the time is the planner loop, everything else runs almost instantaneously. (50% speedup)

Attempt 5 eliminated any checks in the action predicate. It just finds a path from a given Start to End. Look how short it is!

• A note on the use of a list element or matrix element as a constraint where the list or matrix is consists of decision variables. In order to constrain on the value of an element in Dists we have to use matrix_element. Not regular index notation. This had me stuck for a while.

```
matrix_element(Dists,Path[I+1],Path[I],D) % works
Dists[[Path[I+1],Path[I]] : I in 1..N-1] % does not work
```

- Similarly, for a list of decision variables you will want to use element(I, List, V) and not V
 #= List[I]. If V is a list of non-decision variables, say integers, then you can use a regular list comprehension.
- And one more note, look at the giant condition in the parse function foreach. I had originally constructed that with some nested if statements, but the conditions take care of that all and the body of the loop is just one statement. No difference in performance, but it's so cool!

Note: I had problems with the repeated use/abuse of planner. Hakan did some research and suggested to add table in front of the action, which confused me because I thought action was already tabled. But without this extra table the code would get stuck somewhere in the loop. Another option is initialize_table, which is commented out, but can also "unstick" the completion of the code. I am using version 3.8#7. By the time you read this, a future version may have fixed it. The beta version notes, "+ Avoid segfault caused by c_INITIALIZE_TABLE." which may or may not be related to what's happening here.

```
import planner.
import cp.

main =>
    cl_facts([$show(true)]), % globally control progress printing, see
my_println
    % cl_facts([$show(false)]),

% Maze = read_file_lines("test24_2016.data").to_array,
    Maze = read_file_lines("day24_2016.data").to_array,
    save_maze(Maze,"day24_2016_pruned.data"),

% Neibs are the neighbors of each [Y,X] Maze location
    % Reqs are the required [Y,X] coordinates to visit
    [Neibs,Reqs] = prune(Maze),
    N = Reqs.len,
```

```
% Dists is a table of distances between each pair of regs
    Dists = new_array(N,N), bind_vars(Dists,999),
    foreach (I in 1..N-1, J in I+1..N)
        % initialize_table, % this can also fix if Picat gets "stuck" on
repeated calls
        best_plan([Reqs[I], Neibs, Reqs[J]],_,C),
        Dists[I,J] := C,
        Dists[J,I] := C,
        my_println([i=I,j=J,c=C]) % see progress
    end,
    foreach (Row in Dists) my_println(Row) end, % show Dists
    % find the best Path from Reqs[1] that includes all other Reqs
    Path = new list(N),
    Path :: 1..N,
    all_different(Path),
    Path[1] #= 1, % start at Reg[1]
    Part1 #= sum([D : I in 1..N-1,
matrix_element(Dists,Path[I+1],Path[I],D)]),
    solve([$min(Part1)],Path),
    my_println(Path), % show Path
    printf("Answer Part 1: %w\n",Part1),
    % find the best Path from Reqs[1], visit all Reqs, return to Reqs[1]
    Path2 = new_list(N+1),
    Path2 :: 1..N,
    Path2[1] #= 1, Path2[N+1] #= 1,
    all_different(slice(Path2,1,N)), % neat use of slice
    Part2 #= sum([D : I in 1..N,
matrix element(Dists,Path2[I+1],Path2[I],D)]),
    solve([$min(Part2)],Path2),
    my_println(Path2),% show Path
    printf("Answer Part 2: %w\n",Part2).
% Planner final and action states
final(S@[CurYX,_Neibs,End]), CurYX=End => true.
% multiple calls to planner cause Picat to freeze
% adding table seems to eliminate
table
action([[Y,X],Neibs,End],NextS,_,Cost) =>
    member(MoveTo, Neibs[Y,X]),
    NextS = ([MoveTo, Neibs, End]),
    Cost = 1.
% Parse maze and prune dead ends
prune(Maze) = [Neibs,Reqs] =>
    Regs = parse_regs(Maze),
    Neibs = parse(Maze),
    my_println(vsize_no_prune=get_size(Neibs)), % see progress
    Flag := true, % flag to keep doing this until no more prunes
```

```
while (Flag)
        Flag := false,
        % if a [Y,X] has only one neighbor, and it isn't in Reqs
        % the neighbor can be pruned
        foreach(Y in 1..Neibs.len, X in 1..Neibs[1].len,
                not member([Y,X],Reqs),
                len(Neibs[Y,X]) == 1)
            Maze[Y,X] := '$', % mark pruned with $
            Flag := true,
        end,
        Neibs := parse(Maze),
        my_println(vsize_prune=get_size(Neibs)), % see progress
    end.
parse(Maze) = Neibs =>
    MaxY = Maze.len, MaxX = Maze[1].len,
    Neibs = new_array(MaxY,MaxX), bind_vars(Neibs,[]),
    foreach (Y in 1..MaxY, X in 1..MaxX,
            MYX = Maze[Y,X],
            [DY,DX] in [[-1,0],[1,0],[0,1],[0,-1]],
            NX = X+DX, NY = Y+DY,
            between(1, MaxY, NY), between(1, MaxX, NX),
            not member(Maze[NY,NX],['#','$']), % $ is a pruned location
            not member(MYX,['#','$']))
        Neibs[Y,X] := Neibs[Y,X] ++ [[NY,NX]]
    end.
parse regs(Maze) = Regs =>
    NumLocs = [[Maze[Y,X].to\_int,[Y,X]] : Y in 1..Maze.len, X in
1..Maze[1].len, not member(Maze[Y,X],['.','#','$'])],
    Reqs = [[Y,X] : [\_,[Y,X]] in NumLocs.sort(1)].
% Utility functions
get_size(Neibs) = S =>
    S = 0,
    foreach(Y in 1..Neibs.len, X in 1..Neibs[1].len)
        S := S + len(Neibs[Y,X])
    end.
my_println(X) =>
    show(Show), % global fact for printing progress info
    if Show then println(X) end.
save_maze(Maze,File) =>
    show(Show),
    if Show then
        FD = open(File,write),
        foreach (Row in Maze)
            println(FD,Row)
        end,
        close(FD)
    end.
```

Here's the upper corner of the "pruned" maze:

The output of the above code, with the show predicate set to true is:

```
vsize_no_prune = 9944
vsize_prune = 9516
vsize_prune = 9124
vsize_prune = 8980
vsize_prune = 8836
vsize_prune = 8782
vsize_prune = 8728
vsize prune = 8698
vsize_prune = 8672
vsize_prune = 8656
vsize_prune = 8640
vsize_prune = 8632
vsize_prune = 8624
vsize_prune = 8618
vsize_prune = 8612
vsize_prune = 8606
vsize_prune = 8600
vsize_prune = 8596
vsize_prune = 8592
vsize_prune = 8590
vsize_prune = 8588
vsize_prune = 8586
vsize_prune = 8584
vsize_prune = 8584
[i = 1, j = 2, c = 92]
[i = 1, j = 3, c = 30]
[i = 1, j = 4, c = 288]
[i = 1, j = 5, c = 66]
[i = 1, j = 6, c = 234]
[i = 1, j = 7, c = 224]
[i = 1, j = 8, c = 270]
[i = 2, j = 3, c = 82]
[i = 2, j = 4, c = 204]
[i = 2, j = 5, c = 86]
[i = 2, j = 6, c = 154]
[i = 2, j = 7, c = 148]
[i = 2, j = 8, c = 190]
[i = 3, j = 4, c = 278]
[i = 3, j = 5, c = 48]
[i = 3, j = 6, c = 224]
```

```
[i = 3, j = 7, c = 214]
[i = 3, j = 8, c = 260]
[i = 4, j = 5, c = 258]
[i = 4, j = 6, c = 70]
[i = 4, j = 7, c = 84]
[i = 4, j = 8, c = 34]
[i = 5, j = 6, c = 200]
[i = 5, j = 7, c = 190]
[i = 5, j = 8, c = 236]
[i = 6, j = 7, c = 22]
[i = 6, j = 8, c = 44]
[i = 7, j = 8, c = 58]
{999,92,30,288,66,234,224,270}
{92,999,82,204,86,154,148,190}
{30,82,999,278,48,224,214,260}
{288,204,278,999,258,70,84,34}
{66,86,48,258,999,200,190,236}
{234,154,224,70,200,999,22,44}
{224,148,214,84,190,22,999,58}
{270,190,260,34,236,44,58,999}
[1,3,5,2,7,6,8,4]
Answer Part 1: 412
[1,2,4,8,6,7,5,3,1]
Answer Part 2: 664
```

Picat Isn't Python (or Exactly Prolog)

My primary programming languages are Python and Haskell. I often make syntax errors or have problems because I forget about these items below. If you come from these or a C-syntax style language, you may also need to read this.

Maybe You Already Know Prolog?

This whole section is *predicated* on the idea that you are largely unfamiliar with the concepts of Prolog and other logic programming languages. But maybe you already know Prolog? If that's the case, did you see what I did with predicated? Ha! Hahahahah. Ahem. Yes. Anyway...

If you do know Prolog you should know that Picat supports:

- Horn clauses using the Prolog syntax of : -/2. This makes it straightforward to port Prolog programs.
- Prolog style *if-then-else* in the form (*If -> Then; Else*) and mandates the presence of the else-part.
- The! cut operator, however because Picat has =>/2 (deterministic) and ?=>/2 (non-deterministic) (in contrast to just Horn clauses with:-/2), the!/0 is unnecessary in Picat. In other words,!/0 is only used with:-/2, but not with =>/2 and ?=>/2.

Note: For me, I find! confusing and have managed to completely avoid it with Picat. Should you wish, here's some slides about cut from a class I took:

https://courses.grainger.illinois.edu/cs421/sp2020/slides/11.2.1-prolog-cut.pdf and the SWI-Prolog manual's explanation: https://www.swi-prolog.org/pldoc/doc_for?object=!/0. God speed.

- cl_facts for adding facts to the database, but it doesn't have Prolog's clause/2 or the assert and retract family of predicates for metaprogramming.
- Definite Clause Grammar (DCG) rules for parsing strings with -->, but does not have the phrase predicate for processing them.

Should you want to use DCGs in Picat:

- Here's an introduction
- And some examples which require this module
- And more examples: search for "dcg" or "DCG" at https://hakank.org/picat/.
- is/2 for unifying on numeric values. It allows binding across integer and float numeric data types.

In Prolog, there a big difference between is/2 and =/2: is/2 requires a numerical context "LHS is RHS", and requires that RHS is a numerical evaluation. In Prolog X = 2+2 means that X is unified with 2+2, i.e. does not do any evaluation. Picat blurs this difference by evaluating 2+2. If you wanted to delay the evaluation to work like Prolog, it would be X=\$2+2 in Picat, where \$ indicates a literal.

```
A is 5. % A is bound to 5.

4 is A. % Error, "Free variable in expression: is"

5.0 is 5 % Succeds/true/yes. Equivalent to Picat's =:=.
```

I have never found a reason to use is instead of =.

Note: For a more in-depth comparison of Picat and Prolog, look here.

Rabbit Hole: Picat is a descendent of the B-Prolog language, and therefore is part of the whole Prolog family and also logic programming family.

Giant Rabbit Hole: Logic programming dates back to 1972, but its roots go deep into the math of predicate/symbolic logic and it was central to the first wave of Artificial Intelligence (AI). The idea was to encode knowledge into systems of rules sometimes known as "expert systems". And this is also why the Picat constraint programming book's cover says "Springer Briefs in Intelligent Systems: Artificial Intelligence, Multiagent Systems and Cognitive Robotics".

This is in contrast to the "AI" people talk about today, which is statistically based and in common parlance refers mainly to Large Language Models (LLMs). Someday someone may find a way to unite these two branches of thought: encoded knowledge and statistically inferred likelihood, but until then, Prolog and its ilk have been pushed somewhat aside by the neural networks and transformers...and now we might consider all of concepts of epistemology and what it is to "know" and if knowledge graphs and ontologies hold the key. But was Plato right that all knowledge is subjective? Perhaps dependent type systems should be considered as solutions for encoding high order kinds, if these levels of logic really are necessary in the real world, and...um...where was I?

If none of this makes any sense, then the rest of this section is for you.

Variables

- Variable names must have an initial capital letter or underscore.
- Like Prolog, Picat programmers tend towards short, often single character variable names.
- Long variable names tend to be bi-capitalized, but this is just a style recommendation.

Personally, I find the whole "Prolog, we don't use variables more than a two characters long" a little hard to follow. I can see where it comes from the history of logic programming coming from symbolic logic, but for reading other people's code, somewhat longer names would be perfectly fine by me.

```
A = 5. % OK

_A = 5. % OK

a = 5. % Parses, but the result is 'false'. Because the atom 'a' does not unify with the number 5.

A=5,b=4. % Parses, but fails because the atom b!=4, and therefore A does not get bound to 5.

b=4;A=5. % A is bound to 5. because b!=4 and ';' means 'or'.

NoJavScriptVariableNamesHere=true. % OK, but this is not normal Picat style, but you do you however you want.
```

Multidimensional Lists and Arrays

Do you wonder what the syntax is for referencing the elements of a multidimensional list or array? Wonder no more! Here's code from Rosetta Code.

The structure is row major. Meaning I is each row and J is each column. While this is only 2D, it generalizes to more dimensions.

```
main =>
    % 2D arrays
A2 = new_array(4,4),
    foreach(I in 1..4, J in 1..4)
        A2[I,J] := (I-1)*4+J
end,
    foreach(Row in A2) println(Row) end,

% These functions are defined in the util module.
% They returns lists so we have to convert them to arrays.
    println('rows '=to_array(A2.rows)),
    println('columns '=A2.columns.to_array),
    println(diagonal1=A2.diagonal1.to_array),
    println(diagonal2=A2.diagonal2.to_array).
```

Output

```
{1,2,3,4}

{5,6,7,8}

{9,10,11,12}

{13,14,15,16}

rows = {{1,2,3,4},{5,6,7,8},{9,10,11,12},{13,14,15,16}}

columns = {{1,5,9,13},{2,6,10,14},{3,7,11,15},{4,8,12,16}}

diagonal1 = {1,6,11,16}

diagonal2 = {4,7,10,13}
```

Indexing a Range with Steps

For a range with steps use *start..step..end*. For example:

```
A=1..9. % A = [1,2,3,4,5,6,7,8,9]
A=1..2..9. % A = [1,3,5,7,9]
```

Note: no brackets around the range. It's a list already. In Haskell this would need to be [1..9] and [1,3..9]. If you type A=[1..9] into Picat you get a nested list: [[1,2,3,4,5,6,7,8,9]].

Assignment (Binding) vs. Unification (Bind or Fail) vs. Equality (Only Numbers)

Here be dragons. Or at least a sharp corner to hit your head on when you realize your program is failing because you used the wrong one.

Logic programming uses the concepts of binding and unification. Binding is similar to assignment in other programming languages. Unification attempts to validate if the left and right side are the same, and if not either binds one side to the other or fails. Examples will help here.

Default binding

When a variable is first parsed by Picat, it is in an uninstantiated state. Trying to use it will result in an error.

```
A. % in the REPL: *** error(instantiation_error,call).
A. % as a standalone predicate in a program *** SYNTAX ERROR *** (22-22)
wrong head.
A = B+3. % ** Error : Free variable in expression: '+'
```

"Wrong head" here means that Picat is expecting either a predicate or a function that have a =, =>, or ?=>, not a standalone variable reference.

"Free variable" means that B has not been defined yet, so A cannot be bound to the value of B+3 because the + cannot be evaluated.

However, when it's first referenced the variable will be given a unique identifier, which can be seen if we try to print an unbound variable:

```
println(A). % If A hasn't been defined/bound then \_3d084e8 (or some other unique identifier)
```

Unification: the = operators

It is always tricky to try to explain unification, which is expressed by the = operator. It performs one thing that looks like two. The Picat manual says, "The unification T1 = T2 is true if term T1 and term T2 are already identical, or if they can be made identical by instantiating the variables in the terms." Which, in my opinion, feels a bit like "a monad is a monoid in the category of endofunctors". True, but useful only once you already know what the concept means.

Assigning a variable to an expression for it's first use and checking the equality of a variable and an expression on subsequent uses are both aspects of unification.

Unification is also, central to its functioning, bidirectional, for example:

```
[A,3] = [hello,B] % A becomes hello and B becomes 3.
```

Unification is at the heart of logic programming, but it also underlies type inference, type checking and pattern matching in functional programming languages such as Haskell and OCaml. However, unless you have tried to build a type inference engine, you are unlikely to have heard the term used in functional programming.

Unification results either in success/true/yes or fail/false/no. The slash here indicates these are the synonyms. The evaluation results in success or failure, the logical value of the evaluation for each respectively is true/false and the Picat interpreter will output yes or no to indicate this.

Key point: a successful unification results in an unbound variable being bound. Let's look at some examples.

VERY IMPORTANT: The explicit and central use of unification is the main difference between Prolog and almost all other programming languages.

Picat makes it easier for people coming from non-logic programming backgrounds by including functions (see below), foreach loops and list comprehensions.

However, Picat is still a member of the Prolog family and as such, understanding how unification works is required for anything but the simplest program.

Rabbit Hole: Unification is central to type inference in languages such as Haskell. There's the Hindley-Milner algorithm W, for example, which use unification to determine if the type of an expression. Here's a link to algorithm W. Someone even made a t-shirt!

Rabbit Hole: Mercury is a functional/logic language that includes unification. Unlike Picat, it is purely function and strongly typed. https://mercurylang.org/ Verse is also functional/logic, but is not yet publicly

available except for programming games such as Fortnight. Yes, really. https://files.gotocon.com/uploads/slides/conference_65/2896/original/GOTO.pdf

```
A=5, println(A). % A is bound to the value 5, and the unification succeeds allowing the statement to print 5.
```

5=A, println(A). % A is bound to 5 because unification is bidirectional. <- IMPORTANT

Read the above as

1. A is given a unique identifier as a default binding.

From the Picat manual "A variable gets a type once it is bound to a value. Variables in Picat, like variables in mathematics, are value holders. Unlike variables in imperative languages, Picat variables are not symbolic addresses of memory locations. A variable is said to be free if it does not hold any value. A variable is instantiated when it is bound to a value."

- 2. The default binding can be made/shown to be equivalent to 5 through unification.
- 3. Unification binds 5 to A's unique identifier.
- 4. , means the logical "and" operation.
- 5. Because the left side of the , is true we can output the value of A with a println.
- 6. As noted above A=5 is identical to 5=A because unification is bidirectional. <- Important

Compare this with:

```
A=5, A=3, println(A). % Fails/false/no.
```

Read the above as:

- 1. A=5 binds/unifies/assigns 5 to A.
- 2. A=3 attempts to unify A with 3. This fails 5 cannot be made to equal 3.
- 3. Because step 2 is false, the overall, clause is false and the println doesn't happen.
- 4. The entire clause fails. A will not be bound to 5 after this clause! ** <- Important**

```
A=5, A!=3, println(A). % Succeeds/true/yes.
A!=3, A=5, println(A). % Fails/false/no.
```

!= is "not unifiy". In the first line above A does get bound to 5. The second line fails because for A!=3 the variable A has not been instantiated or bound to a value and therefore cannot be unified with 3.

Now look at this. Did you expect it?

```
A=B, println([A,B]). % A and B point to the same unique identifier ->
[_10a58,_10a58]
B=5,A=B, println(A). % B unifies/binds to 5, A binds to B, A is 5 -> 5.
A=B,B=5, println(A) % B unifies with A, B binds to 5, A is now 5. <-
Important</pre>
```

Above is a two variable example. Both left and right in A=B are unbound variables, which means the unification points them to same unique identifier. Therefore whenever A or B gets bound to a value A will be also.

```
Equality: the == and = := operators
```

If you want to test equality without unifying or binding, then == does this, just like Python or JavaScript. Well, not like JavaScript, which has === and more rabbit holes about equality. Why is equality so complex? Because it's both about the value and type of the objects on the left and right-hand sides.

```
A=5,A==5. % Succeeds/true/yes
A==5. % Fails/false/no. Picat provides the amusing error: ** Warning:
superfluous call to ==
A=3,A!==5. % Succeeds/true/yes
A=5,A!==5. % Fails/false/no. A is not bound to 5. <- Important</pre>
```

Note: Two terms can be equivalent with == even if they don't point to the same unique identifier.

Numerical equality can also be checked with = :=, which considers float and interger types the same and allows for a difference of 0.00000001. Also, not numerically equal is = \=. For example:

```
5=5.0 % Fails/false/no
5=:=5.0 % Succeeds/true/yes
5=:=5.1 % Fails/false/no
5=:=5.000001 % Fails/false/no
5=:=5.000000000001 % Succeeds/true/yes
5=\=6 % Succeeds/true/yes
```

Assignment and Re-assignment: =, := and bind_vars()

In logic programming, as noted above, = is unification, binding, and initial assignment. And for initial assignment of a structure such as a list or array there is bind_vars().

However, variables in Picat are re-assignable, meaning := overwrites the previous value. The manual says, "In order to simulate imperative language variables, Picat provides the assignment operator :=."

Note: Using A := 5 for the first occurrence of A is considering bad style. To force the re-binding of a value to a variable, := is the operator.

*Note: It's not really correct to say that variables are "mutable". What is happening with :=/2 is that a new variable is created under the hood, and then is given the same variable name. More info here.

This matters because backtracking can undo this re-assignment when evaluating alternatives. Which means it will work the way you expect it to. The manual says, "When LHS is an access in the form X[I], the component of X indexed I is updated. This update is undone if execution backtracks over this assignment."

And while I find this confusing, it also seems to "just work the way I expect" so I've stopped worrying about it.*

Anyway, here's some examples!

```
A:=5. % A is re-assigned to 5, we assume that A was already bound previously.

A=3,A:=5. % A is re-assigned to 5.

A:=5,A=3. % Fails/false/no. A is not bound to 5.

A=new_list(5), bind_vars(A,"b"). % A = [[b],[b],[b],[b],[b]]

A=new_list(5), bind_vars(A,"b"), A[1]:="c". % A = [[c],[b],[b],[b],[b]]

A=new_array(2,3), bind_vars(A,0). % A = {{0,0,0},{0,0,0}}
```

Reassignment via Predicate and Function Arguments

The statement above about Picat "just works the way I expect" remains true, but what you expect needs to be what's going to happen. Lists, arrays, and maps passed as arguments to predicates and functions can have their values modified through reassignment inside the predicate or function, but cannot change in size.

In other words, don't think of arguments being passed by value or by reference, but there being a context to what can be reassigned via a predicate or function argument and what cannot.

Here's some example code:

```
main =>
    A = 0,
    println(a=A), % a = 0
```

```
p0(A),
    println(a=A), % a = 0
    L = [0,0,0],
    println(1=L), % 1 = [0,0,0]
    p1(L),
    println([p1,l=L]), % [p1,l = [0,0,0]]
    p2(L),
    println([p2,l=L]), % [p2,l = [3,0,0]]
    p3(L),
    println([p3,l=L]), % [p3,l = [3,0,0]]
    p4(L),
    println([p4,l=L]), % [p4,l = [3,3,0]]
    R = f1(L),
    println([f1,l=L]). \% [f1,l = [3,3,3]]
p0(X) => X := 3.
p1(X) => X := [].
p2(X) \Rightarrow X[1] := 3.
p3(X) \Rightarrow X := [4,4,4], X[2] := 3.
p4(X) \Rightarrow X[2] := 3, X := [4,4,4].
f1(X) = R \Rightarrow R = 1, X[3] := 3.
```

Reassignment vs Unificiation and Backtracking

Keep repeating: this works the way I expect it to. Anyway, here's what backtracking can do with reassignment versus unification.

Take a look at this code below. member /2 assigns a single value from the list 1...3 to T and S. member is non-deterministic and on a *fail* condition, it will backtrack and select a different value from the list.

The *fail* condition can be forced by the fail/0 predicate or through another failure, such as a failed unification or equivalence test.

```
go1 is using unification with =/2 and go2 is using reassignment with :=/2.
```

In go1, unification fails at X = T*2 forcing backtracking at that line because X already is bound to T*1.

In go2, Y := S*2 does not force backtracking because := causes reassignment of Y.

Note: the use of ?=> on main allows backtracking on the overall main predicate. And two top-level main functions where the second one succeeds after all options for backtracking on the first are used. This has nothing to do with the output of go1 or go2, but does prevent the overall program from finishing with *** error(failed, main/0). See more about ?=> here.

```
main ?=> % allows backtracking of main
    (member(T,1..3),
    X = T*1,
    println([go1,x=X,t=T]),
    X = T*2,
    println([go1,x=X,t=T]),
    X = T*3,
    println([go1,x=X,t=T])
    % fail
);
   (nl,
     member(S,1..3),
    Y := S*1,
    println([go2,y=Y,s=S]),
    Y := S*2,
    println([go2,y=Y,s=S]),
    Y := S*3,
    println([go2,y=Y,s=S]),
    fail % fail forces backtracking
).
main => true. % when main ?=> fails, go here
```

Outputs

```
[go1,x = 1,t = 1]

[go1,x = 2,t = 2]

[go1,x = 3,t = 3]

[go2,y = 1,s = 1]

[go2,y = 2,s = 1]

[go2,y = 3,s = 1]

[go2,y = 2,s = 2]

[go2,y = 4,s = 2]

[go2,y = 6,s = 2]

[go2,y = 3,s = 3]

[go2,y = 6,s = 3]

[go2,y = 6,s = 3]
```

Global Maps

Picat has "prebuilt maps" which are accessible globally. This is something I've only just begun to learn about and haven't used them myself. Instead I was using cl_facts to create global information on a small scale here and here.

Note: Some langauges call these data structures dictionaries (Python) or hash maps (Haskell) or key-value pairs (Java).

Global data makes function and predicate definitions shorter because you don't have to pass global state via arguments, and global state can be updated at anytime and anywhere in the code.

However, global data is, by definition, not local and therefore makes programs absolutely not-pure because functions and predicates operations can be affected by the side effect of the global value. And by being impure it can make the code harder to reason about and debug.

On the other hand, do you enjoy the State Transformer Monad in Haskell to preserve purity?

Moving on, here's an example of a global map:

```
main =>
  Map = get_global_map(),
  Map.put(counter,0),
  Map.put(a_list,[1,2,3,4,5,6,7]),
  println([counter=Map.get(counter),a_list=Map.get(a_list)]),
  my_func.

my_func =>
  Map2 = get_global_map(),
  Map2.put(counter,Map2.get(counter)+1),
  Map2.put(a_list,Map2.get(a_list)++[8]),
  println([counter=Map2.get(counter),a_list=Map2.get(a_list)]).
```

Outputs:

```
[counter = 0,a_list = [1,2,3,4,5,6,7]]
[counter = 1,a_list = [1,2,3,4,5,6,7,8]]
```

Picat has three kinds of prebuilt maps: heap maps, global maps, and table maps. These differ in the way they handle backtracking. Following is an excerpt from the manual:

Heap maps: Changes to a heap map up to a choice point are undone when execution backtracks to that choice point. There are an unlimited number of prebuilt heap maps.

Global maps: A big difference between a global map and a heap map is that changes to the global map are not undone upon backtracking. The number of prebuilt global maps is 97, and the system halts if a program requests more than 97 global maps.

Table maps: Like the global map, changes to a table map are not undone upon backtracking. Unlike the global map, however, keys and values are hash-consed so that common ground sub-terms are not replicated in the table area. The number of prebuilt table maps is 97, and the system halts if a program requests more than 97 table maps. In tabled programs, using prebuilt maps is discouraged because it may cause unanticipated effects.

Note: I have no idea what hash-consed means.

Program Structure and Control Flow

Picat programs consist of statements which can be combined into longer clauses inside procedures or functions. Picat statements are either rules or facts. This is more correct than thinking of them as statements because all of the rules and facts are stored in a database of the program. This is also how Prolog works.

Fun fact: Because a program is a database, you can alter the rules and facts on the fly with cl_facts . See this section and also this for perfectly legitimate abuses of cl_facts .

The main predicate and Picat file extension.

The default entry point for a Picat program is a main predicate. (Similar to C, Haskell, etc.). If you call a Picat program from the command line, main will be run unless you override it (with -g on the command line). I am happy to always use main.

Also, the mandatory file extension for Picat programs and modules is .pi.

```
% hello.pi
main => println("Hello Picat!").
```

Then run it from a terminal.

```
picat hello.pi
Hello Picat!
```

Whitespace

Whitespace does not matter except for one space needed after the end of clauses because Picat doesn't care if you smush everything together.

Anonymous Variables: _ aka underscore

_ is used when you have a variable in a function or predicate and don't need to use it. The _ can be used by itself of in the front of a name to help code-readability; but the meaning is the same. For example, _A or _ThisVariableIsNotNeededHere.

Here's an example from the Picat manual with a definition of zip for combinging two lists into pairs of elements from each list. The result is the same length as the shorter list and any extra is thrown away. Thus,

we don't care about what the other list contains if one of the lists is [].

```
zip([],\_) = []. % don't care about the 2nd list if first is empty zip(\_,[]) = []. % visa versa zip([X|Xs],[Y|Ys]) = [\{X,Y\}|zip(Xs,Ys)]. % recursive zip if both are non-empty A = zip(1...2,3...6). % A = [\{1,3\},\{2,4\}]
```

Of course, you could also just list the variables and not use them, but the use of the _ helps clarify that the variable isn't being used.

```
zip([],Ys) = []. % works the same.
zip(Xs,[]) = [].
zip([X|Xs],[Y|Ys]) = [{X,Y}|zip(Xs,Ys)].
```

Predicates and Logic Programming "Weirdness": append/3

In Prolog, everything is a predicate with arguments. Some arguments are considered "input" and others "output" or both, it's not like imperative or functional languages where we always think about a function that has a "returned value".

Let's look at the classic example of a predicate: Prolog's append/3 predicate, which Picat also has and it let's you join two lists.

It takes the form append(L1, L2, L3). Note the standard use of terse variable names.

```
append([1,2],[3,4],L3). % L3 = [1,2,3,4].
```

But L1, L2, and L3 are not the "output" of the predicate. You can also write this:

```
append(L1,[3,4],[1,2,3,4]). % L1 = [1,2].
```

OK, that's not like Python at all. And it gets weirder. Type this into the Picat interpreter.

```
Picat> append(L1,L2,[1,2,3,4]).
L1 = '[]'
L2 = [1,2,3,4] ?
```

This means [1,2,3,4] can be formed by an empty L1 and L2 being the same as L3. And then there's this ?. Picat is asking if you want more. If you enter ;, which means "or", the output continues with all

possibilities until there are no more, which is indicated with no.

```
Picat> append(L1,L2,[1,2,3,4]).

L1 = '[]'

L2 = [1,2,3,4] ?;

L1 = [1]

L2 = [2,3,4] ?;

L1 = [1,2]

L2 = [3,4] ?;

L1 = [1,2,3]

L2 = [4] ?;

L1 = [1,2,3,4]

L2 = '[]' ?;

no
```

You can even have all arguments be variables!

```
Picat> append(L1,L2,L3).
L1 = '[]'
L3 = L2 ?;
L1 = [_113c0]
L3 = [_113c0|L2] ?;
L1 = [_113c0,_113e0]
L3 = [_113c0,_113e0|L2] ?;
L1 = [_113c0,_113e0,_11400]
L3 = [_113c0,_113e0,_11400|L2] ?;
L1 = [_113c0,_113e0,_11400,_11420]
L3 = [_113c0,_113e0,_11400,_11420]
```

Technically what is happening here is unification, which we discussed earlier. Unification allows for non-deterministic behavior, which we will go into further later. But the key point here is what would it be like to write a program with nothing but predicates that work this way?

append/4 for parsing

Since we brought up append/3 there's also append/4 which splits up a list into multiple parts. The manual says:

```
append(W,X,Y,Z) (nondet): This predicate is defined as: append(W,X,Y,Z) =>
append(W,X,WX), append(WX,Y,Z).
```

Which is true, but also, hey, how about an example? Since the manual doesn't give one, I went to ChatGPT, which helpfully gave this for parsing all occurrences of a pattern from a list.

```
main =>
List = [a,b,c,d,b,c],
```

```
Pattern = [b,c],
  append(Left, Pattern, Right, List),
  println([Left, Right]),
  fail
;
true.
```

Note the use of fail, ; and true to extract all possible unifications/solutions. We will also cover this here. This code outputs:

```
[a,dbc]
[abcd,[]]
yes
```

Functions!

A key difference/advantage of Picat vs. Prolog is the inclusion of functions. With functions it's more explicit what the input and output of a called object are. You can use append as above or, if you just want to join two lists, you can do this:

```
L3 = L1 ++ L2.

L3 = [1,2] ++ [3,4]. % L3 = [1,2,3,4].

[1,2] ++ [3,4] = L3. % L3 = [1,2,3,4].

L3 := [1,2] ++ [3,4]. % L3 = [1,2,3,4].
```

This is deterministic and unifies or explicitly assigns L1 followed by L2 to L3. Again note that unification is bidirectional. For example:

```
A = append(1,2,3). % *** Undefined procedure: append/3
[3,4] = [1,2] ++ L2. println(L2). % Fails/false/no.
```

While ++/2 is absolutely a function, an example you're more likely to think of is something like our Fibonacci function earlier, or here's a function that returns the longer of two lists. Here we use the notation = R to identify a return value that will be set inside the body of the function.

```
longer(L1,L2) = R \Rightarrow if len(L1) \Rightarrow len(L2) then R = L1 else R = L2 end.
```

If you want to return two or more values, you can pack them into a list, array, etc.

```
longer(L1,L2) = [R,Len(R)] \Rightarrow if len(L1) \Rightarrow len(L2) then R = L1 else R = L2 end.
```

Note: An argument of a function can also be updated just like in the predicate append/3 allowing for more than just the explicitly returned function value to be updated. See this example.

Is it a Predicates or a Function?

Key point: The Picat manual identifies functions with the notation = Val, = ResList or similar. If you try to call a predicate like a function or visa-versa you will get an error an undefined procedure or a fail that you didn't expect. Use picat -log to get more descriptive error messages.

This seems like a simple error to avoid, but the distinction between a function that returns a value versus a predicate that unifies one or more of its arguments was, and is, something I stumble on.

As one example Len = length(L) in Picat. That's a function. In standard Prolog it's a predicate, length(L, Len).

As another example to get a single solution or all solutions to a constraint programming problem the manual says:

- solve(Vars): This predicate ... a single solution
- solve_all(Vars) = Solutions ... all solutions

solve is a predicate, and it's input and output/return value are both in the variable Vars. solve_all doesn't change Vars. The output/return of solve_all is put into the variable Solutions.

This mixing of Prolog-style predicates "the return value is in the argument list" and "normal" programming language style functions where "the return value is on the other side of an =" can be confusing when first encountered. I always check the manual to see if a predicate/function uses a = in the definition.

```
=> vs = and conditions
```

Functions can be defined with = if they are simply a single expression or => if there are multiple clauses in the body. When using => you can add a condition after the assignment of the result. For example.

(The non-deterministic/backtracking ?=> is described here.)

```
main =>
    println(double(5)),
    println(double2(5)),
    println(double3(5)),
    println(double3(15)).

double(X) = X*2.
double2(X) = R => R = X*2.
double3(X) = R, X<10 => R = X*2.
double3(X) = R => R = "not today my friend"
```

The output is:

```
10
10
10
not today my friend
```

Pattern matching and @

Pattern matching is too big a topic to cover fully. But here's an example of how you can decompose a compound object, such as a list, into its parts.

```
main =>
    A = [1,2,3],
    [L2,L3] = last_two_of_three(A), % pattern match left side
    println([L2,L3]).

last_two_of_three([L1,L2,L3]) = [L2,L3] => % pattern match argument
    printf("What's wrong with %w?\n",L1).
```

Outputs

```
What's wrong with 1?
[2,3]
```

To pattern match on the head and tail of a list, the syntax is [Head|Tail]. Note that Head is an individual item and Tail is a list. Combining Head with a list requires putting it inside []. For example:

```
main =>
    A = "A string of characters!",
    println(cipher(A)).

cipher([]) = [].
cipher([H|T]) = [chr(ord(H)+1)] ++ cipher(T). % note [] around H term
```

Outputs:

```
B!tusjoh!pg!dibsbdufst"
```

@ lets you reference an entire pattern matched object without having to deal with the decomposed parts. That sounds complicated. It's not. @ is just syntactic sugar.

```
some_predicate(All@[X,Y,Z]), % All is bound to [X,Y,Z]
L1 = length([X,Y,Z]),
L2 = length(All). % L1 is identical L2,
```

When to use \$ and when not to

\$ is used to denote a literal. This instructs Picat to not treat the token after the \$ as something to interpret right then and there.

For example:

```
solve([$min(Part1)],Path) % pass the argument "min(Part1)" as an option to
solve. Don't attempt to evaluate the min of Part1 here.
```

Or if we want to add a fact to the global environment and not call the predicate when it's added.

```
cl_facts([$part(1)]) % adds the fact part(1) to the global environment.
cl_facts([part(1)]) %tries to call part(1) here and errors: *** Undefined
procedure: part/1

part(Part), % if we used $part(1) above, then this works later in the code
if Part = 1 then println("Yes") end % and we can test the Part variable now
```

And sometimes we can use \$ or not and both are ok. For example when assigning an action for the planner.

```
Action = $("1->2",NewS1,NewS2,NewS3) % works
Action = ("1->2",NewS1,NewS2,NewS3) % also fine, nothing in here will be
evaluated
```

Another use of \$ is here.

Function call syntax: () and .

Functions can be called by placing arguments in parenthesis or by using dot notation. This is just syntactic sugar. The . notation makes the code a little shorter (1 character versus 2), and looks more like functional programming, Rust, JavaScript. This syntax is used in lots of languages and commonly referred to as *method chaining*. You may find it easier to follow the logic with the dot notation, and you can mix-and-match the notations however you like.

Personally, I find the dot notation easier to understand if there's more than function being applied. Many nested parenthesis feels more like Lisp to me. For example:

Parentheses form:

```
Steps = map(my_parser,map(split,read_file_lines("day.txt"))),
init_bots(Steps,Bots,Bins),
Answer = prod(map(dec,take(3,(to_list(step([S : S in Steps,
S[1]=$gives],Bots,Bins)))))),
```

Dot notation form:

```
Steps = ("day.txt").read_file_lines.map(split).map(my_parser),
init_bots(Steps,Bots,Bins),
Answer = step([S : S in Steps,
S[1]=$gives],Bots,Bins).to_list.take(3).map(dec).prod,
```

A mixture of both:

```
Steps = read_file_lines("day.txt").map(split).map(my_parser),
% etc.
```

Note: Obligatory xkcd reference. Or where you expecting this?

Statement delimiters

All statements have to end in ,, ; or . , means "and", ; means "or" and . means "end of statement".

() are used to mark a block of code as separate from the code around it. They are often optional, but using them will help make sure the compiler and you don't get confused.

```
A=2, B=3.
Name.length > 0; Name := "I'll just call you Larry.".
```

Control flow: if and foreach

- if ... then is exactly what you think it is, but there's required syntax that took me a while to get used to.
- if requires an end. The statement just before this end doesn't need a ,. Picat used to enforce this syntax, but doesn't anymore.

```
curve(Grade) = (Letter,Comment) =>
  if Grade > 50
    then (Letter = A, Comment="Nice.")
    else (Letter = F, Comment="See me.")
end.
```

The then keyword is optional if you enclose the condition in ()

```
curve(Grade) = Letter =>
  if (Grade > 50) Letter = 'A' else Letter = 'F' end.
```

Picat also allow Prolog style if statements with -> and ;. The syntax is \$if -> then ; else\$.

Note: Parentheses are **highly** recommended around these constructs to be explicit about what statements are can be "or" with each other and thereby avoid having Picat to do something you didn't intend.

```
(A>5 -> println("Big"); println("small")).
```

foreach is a loop structure like any other programming language. Picat also has while and do ... while. The condition in foreach has to be enclosed in (). And, like if, you need an end at the end.

```
% multiple iterators are allowed, they are treated like nested loops
foreach(X in 1..10, Y in 1..10)
    A[X,Y] := my_hash_function(X,Y) % <- line end comma optional
end.</pre>
```

You can also put a condition inside the foreach, similar to list comprehension in Haskell and other languages. For example:

```
foreach(X in 1..10, Y in 1..10, X + Y mod 4 <= 2)
% ...
end.</pre>
```

You can have as many conditions as you like and thereby remove having any if statements in your loop body. Here's an example below from one of my programs to get the valid neighbors of a given 2 dimensional array item.

Neighbors are those coordinates that do not have a # or \$ in them and are within the bounds of the array. Look at all those conditions and only one line in the loop body!

```
not member(Maze[NY,NX],['#','$']), % $ is a pruned location
    not member(MYX,['#','$']))
    Neibs[Y,X] := Neibs[Y,X] ++ [[NY,NX]]
end.
```

Control flow: the ; aka "or" operator

if ... then ... else are familiar control flow for almost all programming languages. Prolog/Picat can also use the concept of "or". There's an example of this in Blocks World.

The structure is similar to a case statement in other languages: (A; B; C; D), which reads as perform A, if it fails, perform B, etc. Enclose these in () to make sure that the options doesn't get mixed up with other parts of the predicate or function.

However, it's not exactly a case statement. For example, (A = 3 ; A = 4 ; A = 5) will bind A to 3, 4, and 5 respectively on backtracking/failure.

Control flow: cond and compare_terms

Another way to do an if is with cond. While it's not listed in the Picat manual index, it does define the function in this example:

```
The fib function can also be defined as follows: fib(N) = cond((N = 0; N = 1), 1, fib(N-1) + fib(N-2)). The conditional expression returns 1 if the condition (N = 0; N = 1) is true, and the value of fib(N-1) + fib(N-2) if the condition is false.
```

Another option is compare_terms. It outputs -1, 0, or 1 if the first term is less than, equal to, or greater than the second term. For example.

```
A = compare_terms(5,2). % A = 1
B = compare_terms(2,2). % B = 0
C = compare_terms(2,5). % C = -1
```

Note: For constraint programming cond/3 is also available as a constraint, for example: C # = cond(A#>3, A+B, A-B).

Control flow: call and apply

You can invoke any Picat predicate or function with predicate call or the function apply. For example, the below calls println with the single argument, "hello".

```
call(println,"hello") % println("hello")
A=apply(head,"hello"). $ A = h
```

This can be used to do what other programming languages call *eval*. It can also be used to dynamically choose which code to execute based on the values of variables. See here.

```
Control flow: list_to_and
```

Let's say you had a bunch of boolean statements in a list and you wanted to evaluate them. You could write a parser and run them through a list comprehension or, you could invoke the power of Picat!

Here's a list of statements we may have in a file. (A new Advent of Code challenge perhaps?)

```
main =>
   Conds = "[A=5,B=3,A!=B]", % pretend we read this from a file
   AndList = list_to_and(parse_term(Conds)),
   println([a=A,b=B,andList=AndList]),
   Ans = AndList.cond(true,false),
   println(ans=Ans).
```

Outputs:

```
[a = _114b0,b = _114c8,andList = (_11260 = 5,_11328 = 3,_11260 != _11328)]
ans = true
```

Note that the A and B in Conds don't escape the scope of Conds. That is, we can't access them in the println.

Nevertheless, the evaluation of Conds with cond works. Change A!=B to A=B and you will see that Ans now equals false.

Example: Global fact = Global state

The below code recursively parses parenthesis but has different requirements for part 1 and part 2. To do this it uses a global fact: part(n) to change the behavior of parse1 function. The fact is changed from part(1). to part(2). with the cl_facts() command that updates and overwrites the global fact dictionary.

Probably unsafe, but quite neat!

I could have used a global map instead to do this, but I didn't know about them at the time I wrote this code.

https://adventofcode.com/2016/day/9

```
main =>
    % Data = "A(1x5)BC",
    % Data = "A(2x2)BCD(2x2)EFG",
    % Data = "(25x3)(3x3)ABC(2x3)XY(5x2)PQRSTX(18x9)(3x2)TWO(5x7)SEVEN",
    Data = read_file_lines("day.txt").head,
```

```
cl_facts([$part(1)]), % a global fact
printf("Part 1 Answer: %w\n",parse(Data).sum),

cl_facts([$part(2)]), % override global fact
printf("Part 2 Answer: %w\n",parse(Data).sum).

parse([]) = [].
parse([H|T]) = R =>
    if H = '(' then (R = parse1(T)) else (R = [1]++parse(T)) end.

parse1(L) = R =>
    Ix = find_first_of(L,'x'), Ip = find_first_of(L,')'),
    M = take(L,Ix-1).to_int, N = slice(L,Ix+1,Ip-1).to_int,
    TT = slice(L,Ip+1+M), % tail to leave
    part(Part),
    (Part = 1, R = [M*N]++parse(TT);
    Part = 2, R = [N*sum(parse(slice(L,Ip+1,Ip+M)))]++parse(TT)).')'
```

Example: Dynamic Dispatch with apply and call

While Picat doesn't have lambda expressions, it does allow for code execution based on the value of a variable.

Here's an example that simulates a simple assembly language. It invokes the correct operation based on the parsed input strings via the apply function. apply and call are able to transfer operation to another function or predicate that is passed as an argument.

call and apply both *call* the parameters given. call requires a predicate as the first term, whereas apply requires a function as the first term (and then returns the results of that call).

The interesting thing in the example below is that the name of the function is identical to the string in the input. The *cpy* command is performed by the *cpy* function.

The code also makes use of a hash map to store the value of registers and passes state back and forth via unification. Note how S isn't explicitly returned. It's a mutable map and it is both an input and output just like any predicate in Prolog. This is just like append/3, as discussed here.

This is true even though S is an argument to a function, which has an explicit return value namely the program counter, PC which is updated using the function syntax and :=.

One more thing to notice here: the code for converting strings to integers. You may find it useful when parsing input yourself.

https://adventofcode.com/2016/day/12

- cpy x y copies x (either an integer or the value of a register) into register y.
- inc x increases the value of register x by one.
- dec x decreases the value of register x by one.
- jnz x y jumps to an instruction y away (positive means forward; negative means backward), but only if x is not zero.

Here's a couple of possible programs:

```
|-----|
| Program 1| Program 2|
|-----|
| cpy 41 a | cpy 1 a |
| cpy a b | cpy 1 b
| inc a
         | cpy 26 d |
| inc a
         | jnz c 2
| dec a
        | jnz 1 5
| jnz a 2 | cpy 7 c
| dec a
        | inc d
         | dec c
         | jnz c -2 |
         | сру а с
         | inc a
         | dec b
         | jnz b -2 |
         | cpy c b |
         | dec d
         | jnz d -6 |
         | cpy 13 c |
         | cpy 14 d |
         | inc a
         | dec d
         | jnz d -2 |
         | dec c |
         | jnz c -5 |
  -----|----|
```

And here's the code. The list index of each program serves as the program counter reference for the jnz, jump not zero command.

```
% Advent of Code 2016 Day 12

import util.

main =>
    % Program = read_file_lines("test").map(split).map(parse),
    Program = read_file_lines("day.txt").map(split).map(parse),

Part1 = run(Program,new_map(["a"=0,"b"=0,"c"=0,"d"=0]),1),
    printf("Answer Part 1: %w\n",get(Part1, "a")),

Part2 = run(Program,new_map(["a"=0,"b"=0,"c"=1,"d"=0]),1),
    printf("Answer Part 2: %w\n",get(Part2, "a")).

run(Program,S,PC) = NewS =>
    while (between(1,Program.len,PC))
```

```
[Op,Args] = Program[PC],
        % here's the dynamic dispatch
        % apply calls the function stored in the variable Op
        % with the arguments: Args, S and PC.
        PC := apply(Op,Args,S,PC),
    end,
    NewS = S.
% extract the op code as an atom
% convert numbers in the argument into the correct int type.
parse([H|T]) = [(H).to_atom, T.map(parse_n)].
parse_n(X) = Xn \Rightarrow if between(97,122,ord(X[1])) then Xn = X else Xn =
X.to_int end.
cpy([X,Y],S,PC) = NPC => NPC = PC+1,
    if number(X) then put(S,Y,X) else V = get(S,X), put(S,Y,V) end.
inc([X],S,PC) = NPC \Rightarrow NPC = PC+1, V = get(S,X), put(S,X,V+1).
dec([X],S,PC) = NPC = NPC = PC+1, V = get(S,X), put(S,X,V-1).
jnz([X,Y],S,PC) = NPC =>
    if number(X) then Xn = X else Xn = get(S,X) end,
    if Xn != 0 then NPC = PC+Y else NPC = PC+1 end.
```

More apply and call

A couple more examples of call and apply.

```
A = pend(X,Y,1..4), A.call
```

When input in the Picat REPL outputs:

```
A = append('[]',[1,2,3,4],[1,2,3,4])
X = '[]'
Y = [1,2,3,4] ?;
A = append([1],[2,3,4],[1,2,3,4])
X = [1]
Y = [2,3,4] ?;
A = append([1,2],[3,4],[1,2,3,4])
X = [1,2]
Y = [3,4] ?;
A = append([1,2,3],[4],[1,2,3,4])
X = [1,2,3]
Y = [4] ?;
A = append([1,2,3,4],'[]',[1,2,3,4])
X = [1,2,3,4]
Y = '[]' ?;
```

```
no
```

Another way of manipulation is Univ (= . . /2) which converts a term to/from a list. It's mentioned in the Picat Guide (page 35) but there's no example. Here's a simple one. Also, here's the Prolog documentation of = . . .

```
L = [1,2,3,4], Goal =.. [sum,L], Res = Goal.apply.
```

Outputs:

```
L = [1,2,3,4]
Goal = sum([1,2,3,4])
Res = 10
```

Non-determinism: ?=> and more table

A key feature of logic programming languages is explicit and implicit backtracking from failure to try and achieve success. We talked a little about backtracking here.

But let's now recall our friends append/3 and append/4.

Picat predicates/rules, but not functions, can be defined as backtrackable with ?=>. The manual provides an example for determining if a a node Y is reachable from a node X in a graph.

```
reach(X,Y) ?=> edge(X,Y). % if this fails, try the next rule
reach(X,Y) => reach(X,Z), edge(Z,Y).
```

The manual notes that this takes exponential time to compute and by applying table, Picat can memoize the redundant calls to already seen nodes.

```
table % so much faster
reach(X,Y) ?=> edge(X,Y).
reach(X,Y) => reach(X,Z), edge(Z,Y).
```

Note: If the data given by edge/2 represents a circular graph, e.g. edge(1,2) and edge(2,1), then without table/0 it will go into an infinite loop (if that is not handled in some way). With table/0 this is handled neatly since it caches the nodes that's are visited before.

reduce for functional folds

Haskell (and other languages) have the concept of a *fold* to apply an operation to pairs of elements in a list and accumulate the result. For example:

```
(Haskell)
foldl (+) 0 [1..10] -- outputs 55
-- we can also use an anonymous lambda function for x - y
foldl (\x y -> x - y) 30 [1..10] -- outputs -25
```

And you can leave out the base case with foldl1 or foldr1.

```
(Haskell)
foldl1 (+) [1..10] -- still 55
foldl1 (\x y -> x - y) [1..10] -- 53
```

While Picat doesn't have anonymous lambda functions, we can accomplish the same thing with a named function.

```
main =>
    L = 1..10,
    P = reduce(+,L), % standard +
    println(p=P),
    D = reduce(diff,L), % user defined function, diff
    println(d=D),
    D30 = reduce(diff,L,30), % initial value of 30
    println(d30=D30).

diff(X,Y) = R =>
    R = X-Y,
    println([x=X,y=Y,r=R]).
```

Outputs:

```
p = 55
[x = 1,y = 2,r = -1]
[x = -1,y = 3,r = -4]
[x = -4,y = 4,r = -8]
[x = -8,y = 5,r = -13]
[x = -13,y = 6,r = -19]
[x = -19,y = 7,r = -26]
[x = -26,y = 8,r = -34]
[x = -34,y = 9,r = -43]
[x = -34,y = 10,r = -53]
d = -53
[x = 30,y = 1,r = 29]
[x = 29,y = 2,r = 27]
[x = 27,y = 3,r = 24]
```

```
[x = 24, y = 4, r = 20]
[x = 20, y = 5, r = 15]
[x = 15, y = 6, r = 9]
[x = 9, y = 7, r = 2]
[x = 2, y = 8, r = -6]
[x = -6, y = 9, r = -15]
[x = -15, y = 10, r = -25]
d30 = -25
```

Note: while the Haskell and Picat versions do the same thing, it's so much easier to add a debugging println to Picat. And yes, I know you can use trace from Debug.Trace, but it's not as straightforward.

Helper functions for accumulators

When doing arbitrary recursion with accumulation you either need to include the accumulator in the arguments or call a helper function with the default base case, often 0 or [].

The Picat manual gives this example:

```
min_max([H|T],Min,Max) =>
    min_max_helper([H|T],H,Min,H,Max).

min_max_helper([],CMin,Min,CMax,Max) => Min = CMin, Max = CMax.
min_max_helper([H|T],CMin,Min,CMax,Max) =>
    min_max_helper(T,min(CMin,H),Min,max(CMax,H),Max).
```

This is not unique to Picat and is common in functional programming with the use of functions named go or aux often used. Here's an example from an old version of the Haskell compiler code.

```
(Haskell)
    foldr k z = go
        where
        go [] = z
        go (y:ys) = y `k` go ys
```

More Haskell Functions in Picat

If you have a Haskell background and want to see what it's like to implement much of the Haskell Prelude in Picat, the amazing Hakan has you covered here as well.

His port most of the Haskell Prelude function to Picat: https://hakank.org/picat/haskell_prelude.pi

Some examples below. I quite like the run length encoding one.

```
% 15 foldl
foldl(_F,E,[]) = E.
```

```
foldl(F,E,[X|Xs]) = foldl(F, apply(F,E,X), Xs).
foldl1(F,[]) = _ => throw $error(empty_list,foldl1,F, []).
foldl1(F,[X|Xs]) = foldl(F,X,Xs).
% Run Length Encoding
% http://www.shlomifish.org/lecture/Perl/Haskell/slides/basic/lists.html
rle([]) = [].
rle([A|[]]) = [(A=1)].
rle([X|Xs]) = cond(X == A,
                    [(A=Count+1)|As],
                    [(X=1),(A=Count)|As]) \Rightarrow [(A=Count)|As] = rle(Xs).
% Haskell's group/1:
% Groups together consecutive elements of L into sublists.
     Picat> G = grouph([1,2,3,2,1,2,2,2,3,3,21])
%
     G = [[1], [2], [3], [2], [1], [2,2,2], [3,3], [21]]
grouph(L) = Group =>
    Group = [],
    Tmp = [L[1]],
    foreach(I in 2..L.length)
       if L[I] == L[I-1] then
          Tmp := [L[I]|Tmp]
       else
          Group := Group ++ [Tmp],
          Tmp := [L[I]]
       end
    end,
    Group := Group ++ [Tmp].
```

Using Picat For Instruction

To use Picat with an autograder, the student code can be imported as a module into the grader. For example, students could be given the magic square problem from the Picat Constraint Solving book.

Here's a sample assignment.

A magic square is one where the columns, rows and diagonals sum to the same number. https://en.wikipedia.org/wiki/Magic_square You are to code a constrain solving solution in Picat that has that sum be the "magic sum" of N*(N*N+1)//2. https://en.wikipedia.org/wiki/Magic_constant Be sure to not change the code that says module student. at the top.

Use this code as your template:

```
module student.
import cp.

magic(N) = Square =>
    NN = N*N,
```

```
Sum = N*(NN+1)//2, % ensures consistency of solve
Square = new_array(N,N),
Square :: 1..NN,
% your code here
solve(Square)
```

Here's a potential full solution, this is from the Picat book. https://picat-lang.org/picatbook2015/constraint_solving_and_planning_with_picat.pdf

```
module student.
import cp.

magic(N) = Square =>
    NN = N*N,
    Sum = N*(NN+1)//2,
    Square = new_array(N,N),
    Square :: 1..NN,
    all_different(Square.vars()),
    foreach (I in 1..N)
        Sum #= sum([Square[I,J] : J in 1..N]), % rows
        Sum #= sum([Square[J,I] : J in 1..N]) % columns
end,
    % diagonal sums
    Sum #= sum([Square[I,I] : I in 1..N]),
    Sum #= sum([Square[I,I] : I in 1..N]).
```

And the associated grader that puts the result into a file. Consistency in grading is ensured by using the combination of the magic sum and the set solve search method, in this case: [ffd,down]. (Fail first with variable ordered by degree and down variables from largest to smallest.)

```
% grader.pi
import student.
import cp.

main =>
    Writer = open("grade_file.txt", write),
    Square = magic(5),
    solve([ffd,down],Square), % tell students the solve method
    if
        Square == {{3,9,14,15,24},{10,20,22,2,11},{19,17,1,21,7},
        {8,13,16,23,5},{25,6,12,4,18}}
        then println(Writer,"Correct!") % or write to a file
        else println(Writer,"Wrong!")
    end,
    close(Writer).
```

Errors I Always Make and How I Compensate

Type Errors, Numbers and Characters, println vs writeln

Since Picat isn't strongly typed, the programmer has to keep track of what's what. Also, lists and arrays can be heterogeneous, meaning you can mix types freely in them.

For example, Picat doesn't show the difference between a string and an integer when printing output of a list or array. Here's some code:

```
main =>
    D = "12345",
    C = 1..5,
    E = D++C,
    println(printlnE=E), % [1,2,3,4,5,1,2,3,4,5]
    writeln(writelnE=E), % ['1','2','3','4','5',1,2,3,4,5]
    E[6]:=E[6]+10,
    println(printlnE=E), % [1,2,3,4,5,11,2,3,4,5]
    writeln(writelnE=E), % ['1','2','3','4','5',11,2,3,4,5]
    E[1]:=E[1]+10. % *** error(type_error(number,1),(+)/2)
```

Output is below. There's no quote marks around the strings when using println so it's not clear that the first 5 items are strings and the second 5 are integers.

You can use writeln instead, which puts quotes around atoms and strings. This was not something I realized until it was pointed out to me that write is different than print!

More Type Errors: Lists and Arrays

Lists are denoted with [] and arrays with {}. Lists dynamically allocate memory and accessing elements takes \$O(N)\$ time. Arrays take a fixed amount of memory and accessing elements is \$O(1)\$.

Most Picat functions and predicates are overloaded to work seamlessly on arrays, but not all! And the error isn't always clear that it's a type error.

```
A = [1,2,3,4], AL = len(A), B=head(A).
% AL = 4
% B = 1

A = {1,2,3,4}, AL = len(A), B=head(A).
% AL = 4
% *** unresolved_function_call(head({}(1,2,3,4)))
```

I sometimes switch my code between lists and arrays for the advantages one gives over the other, such as in access time. But refactoring isn't as simple as just making the variables into lists.

List Ranges With []

List made with ranges don't use [] like Haskell does. I noted this here. But I keep forgetting and using A = [1..10] when I should have written A=1..10. Unfortunately for me, the former is not a syntax error, but results in a nested list: A=[[1,2,3,4,5,6,7,8,9,10]].

And More Type Errors: "" vs ' ' aka Atoms and Strings, Oh My

In some programming languages double and single-quoted strings are synonymous. (Python) In others, strings are double-quoted and individual characters are single-quoted.

In Picat, "" means string, which is a list of characters. For example:

```
A = "hello world". % A = [h,e,l,l,o,' ',w,o,r,l,d]
```

And '' means "atom". Atom is a concept from Prolog, which is kind of like an enumerated type, and I'm not going to do justice to explaining it (see below), but basically any lowercase string (less than 1000 characters!) is an atom. So you can do this:

```
N=5, println(n=N). % output n=5
N=3, println(my_n_is_set_to_N). % output my_n_is_set_to_3
```

Note that in the above, the = is binding/unification!

This bites me when I'm pattern matching on a string. For example, the below took me some trial and error to get right. The '0' is an atom, but works here like a character, and the "0" is a string, which could also have been written as ['0'].

```
swap10([]) = [].
swap10(['0'|T]) = "1" ++ swap10(T).
swap10(['1'|T]) = "0" ++ swap10(T).
```

Rabbit Hole: In Prolog-land all is not so simple with strings and quote marks. Here's what SWI-Prolog says about strings. It's 8 pages long!

And here's the SWI-Prolog definition of an atom:

Atoms are identifiers. They are typically used in cases where identity comparison is the main operation and that are typically not composed nor taken apart. Examples are RDF resources (URIs that identify something), system identifiers (e.g., 'Boeing 747'), but also individual words in a natural language processing system.

They are also used where other languages would use enumerated types, such as the names of days in the week. Unlike enumerated types, Prolog atoms do not form a fixed set and the same atom can represent different things in different contexts.

Another Rabbit Hole: Despite the fact that one of Prolog's origins is in translation of English weather forecasts to French (look for METEO), it originally represented strings as lists of ASCII values. SICStus Prolog and B-Prolog both do this:

```
B-Prolog Version 8.1, All rights reserved, (C) Afany Software 1994-2014.
| ?- X = "Picat".
X = [80,105,99,97,116]
```

Predicate vs Function (sort of a type error)

I still use predicates and expect a return value and functions and don't assign the return value to a variable. I mentioned this here.

If you (or I) use picat -log to call the program, there's more descriptive error messages. For example, the call:

```
reduce(1..4,4)
```

Gives the following warnings (but not errors):

```
undefined_assumed_global_predicate: reduce / 2
defined_as_function_in(basic): reduce / 2
```

Unification vs Assignment

Invariably I make an error where I use = when I need to use :=. This happens when I am editing code and moving things around and lose track of the first time I bind a variable versus when I either test it or update it.

And thus, when I think I'm assigning/initial binding, Picat is actually unifying and therefore failing because the new value doesn't equal the old value.

It's "frowned upon" to use := for initial assignment, and under the covers, Picat is doing unification anyway. Yes, unification is hard for imperative/functional programmers, but it is the engine powering non-determinism in logic programming.

So it's really a matter of knowing when to use =: bind/unify, :=: reassign, and == to test equality. And thereby remembering that this error might be what's causing your bug.

Forgetting a comma or a period (or having an extra one)

Some people like to put the ,, ; and . at the start of lines.

^{*}More Rabbit Hole: There's also GNU Prolog, YAP Prolog, Strawberry Prolog,..."

```
main =>
    A = 5
    , B = 10
    , if A > B
        then println("Yoo")
        else println("Hoo")
    end
.
```

This can make it easier to move lines around, but I think it looks weird and it doesn't work in all cases.

Invariably, I add a new line of code and forget the comma or I accidentally add a period. Picat is improving in its ability to locate the error, but it can be vague and give a large range of possible lines to check.

I compensate by adding only a few lines at a time and always saving and rerunning so that I don't have far to hunt for the most recent edit that broke syntax rules.

Don't use list indexing with decision/domain variables

When solving constraint problems, if the list contains decision variables use element(I, List, V) and not V #= List[I]. Also $matrix_element$ for 2D arrays/lists. I noted this in this example code.

Debugging

Picat has a debugger, and it works as advertised and if you want to use it I will point you at the Manual. But for me the key has been println, printf, and, in extreme cases, readchar.

*Note: For strange error messages Hakan says:

What I tend to do is to run the program debugger with the -d flag, and the press "r":

```
$ picat program.pi -d
Call: (1) main ? r
```

Sometimes this works, but sometimes this doesn't give a clue about the error (or why the program is not doing what I want). It might give a *huge* output.

Print and Printf are Your Friends

Picat lets you put a println anywhere. You can even put a println in a condition in a function definition! As such, I make extensive use of my friend println when debugging.

println only has one argument. To print more than one variable, they can be enclosed in () or []. And a literal, that starts with \$, can be added to give some extra info about where in the code the print is coming from and eliminates the risk that the atom has some specific meaning.

```
println(A). % nice and simple
A=5, println(a=A). % outputs "a=5"
println([[a=A,b=B,l=L,t=T,s=S]]). % multiple variables we are wondering
about
println(a=A=b=B=c=C). % doesn't require []
println([$parser,slice(A,1,5),A.len]). % where are we? and a piece of A and
A's length
my_func(A,B,C) = Result, println([$my_func_call,A]) => ...
```

printf is also good, but it requires formatting codes and the newline \n has to be added. There's a full list of formatting codes in the manual, but I just use \%w because I'm lazy.

```
printf("Answer is: %w, %w, %w\n",A,B,C).
```

Print within solve!

You can use println to see what's going on inside the constrain solver. Very handy when things aren't going as expected. Also just super cool. Here's an example from my code here.

Globally Control Progress/Debug Println

Using my "trick" for setting global state variables, you can turn and and off progress/debug print statements.

```
% use my_println instead of println
main =>
    cl_facts([$show(true)]),
    % or cl_facts([$show(false)]),

    my_println("Hello World").

my_println(X) =>
    show(Show),
    if Show then println(X) end.
```

Or you can use a global map instead.

```
% use my_println instead of println
main =>
```

```
Map = get_global_map(),
    Map.put(show,true),
    % or Map.put(show,false),
    my_println("Hello World").

my_println(X) =>
    Map = get_global_map(),
    if Map.get(show)==true then println(X) end.
```

Hakan's version of this is below. "Calling p(X) does not print anything, but p(X,true) does."

```
p(X) :- p(X,false). % default debug printing is off
p(X,Print) :- if Print then println(x=X) end,
```

readchar for single step execution

If I'm really lost as to what's going on in a big loop or recursion, single step debugging can be emulated with read_char, which defaults to taking a character from stdin.

This can be adjusted to only fire on a given condition and further limit the stream of output to be focused on for debugging.

```
R = 0,
foreach (I in 1..100_000_000)
    R := do_thing(R) % mutations, yikes!
    if (I mod 10000 = 0) % stop every 10,000 loops
        then println([$r,R]), read_char() % wait for enter key
    end
end.
```

time to calculate execution time

Wrapping predicates and function calls in time() will print out the CPU time required. This is more useful for locating more efficient algorithms than basic debugging; after all, I can tell when my fans turn on and there is no output for 5 minutes. For example,

```
...a bunch of code...
time(solve(DVars),
println(DVars).)
```

time2 will also calculate backtracks, but it doesn't count backtracks from within the planner module.

Things I Still Don't Fully Understand or Wish Had More Example

The Picat manual can be succinct and doesn't provide examples for everything. Here's some stuff I don't know how to use or where I still get confused.

Functions and Predicates I Don't Understand

```
acyclic_term
```

The manual says: "This predicate is true if Term is acyclic, meaning that Term does not contain itself." I don't know what this means in terms of a term (how is a term a graph?) or when I would use it.

Hakan notes: "Beside from porting some Prolog programs that use this, I've never used it."

Hillel says: "As far as I can tell it probably matters for people using LP for theorem proving and mathematics? Example of a cyclic term:

```
A = $struct(A), acyclic_term(A).
no
```

Constraints I Don't Understand

neqs

The manual says, "This constraint is equivalent to the conjunction of the inequality constraints in *NeqList*, but it extracts all_distinct constraints from the inequality constraints." I find this explanation confusing. There's an example of it here: https://www.hakank.org/picat/color_neqs.pi. Perhaps it will make sense to you?

regular, circuit and table_in constraints

These are covered in the [Picat Constraint book]h(ttps://picat-

lang.org/picatbook2015/constraint_solving_and_planning_with_picat.pdf), but I haven't come up with a use case on my own yet, so I'm not feeling very confident in my understanding.

The examples from the book are here: - https://www.hakank.org/picat/knight_tour_circuit.pi - https://www.hakank.org/picat/circuit.pi, in this Hakan defines circuit_path/2, which also extracts the path taken.

Conceptual Areas I'm Not Comfortable With

I haven't used these much, or at all, which makes me less confident about them.

DCGs

The manual says Picat supports DCG (Definite Clause Grammar) rules with -->, but provides no examples. (Although there's copious resources referenced here)

In general, I find parsing libraries, regardless of the language, both very useful and hard to learn. I feel like DCGs and parsing in Picat could be a chapter.

Global maps

The section on global maps in the manual is very short and the few examples don't show how to access the contents of a global map. I'd like more examples and to better understand the differences between global, heap and table maps and why to use one over another.

Ţ

Aka Prolog cut operator, is something I think I understand and then when I think more, I don't. Luckily Picat seems to obviate the need for! through the much more straight forward?=> for backtrackable rules.

Event Driven Actors

Picat has the capability to be reactive and respond to trigger events. This is cool, and the reason I've listed it here is that I haven't even tried to use event driven actors.

Hakan has the following note about Event Driven Actors:

I haven't use this very much, but it helped me writing a tracer for constraint models. See this code and test example.

Also this program was used for the discussion on constraint propagation in the Picat book section "2.3.3 Constraint Propagation - Example".

Things I Would Like Added to the Index

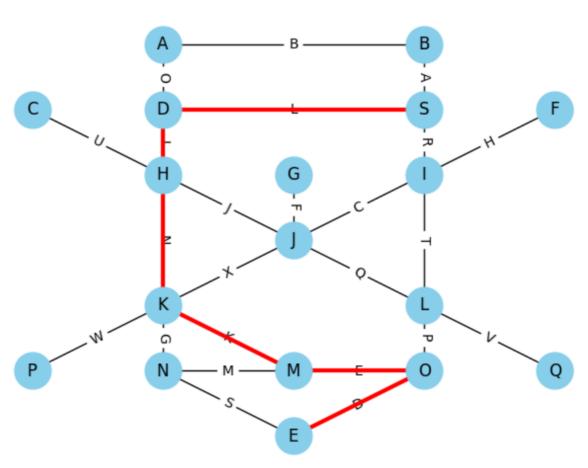
- The notation (If -> Then; Else) is in a footnote and one example, but it's not in the index, which is my go to resource.
- cond when not used as a constraint.

Enhancements I'd Like

• Graphics. When I did the Jane Street Bug to help me visualize the problem I used Python and the networkx and matplotlib libraries. It would be great to be able to call graphics libraries from

Picat.

LINKED



• Planner with negative costs. Advent of Code 2016 day 17 requires the shortest and longest paths. planner makes the shortest path nearly trivial. But longest path required me to write a tabled search. Looking for the worst solution with planner would have been more fun.

Resources

- Picat website https://picat-lang.org/
- The Manual https://picat-lang.org/download/picat_guide.pdf
- Constraint Solving and Planning with Picat book https://picatlang.org/picatbook2015/constraint_solving_and_planning_with_picat.pdf
- Karlova University Course https://jbulin.github.io/teaching/fall/nopt042/
- A ChatGPT version that knows something about Picat. Warning: It can get confused between Picat, Prolog, Python and Haskell. https://chatgpt.com/g/g-EEpNUZ9H1-picat-prodigy
- The SWI-Prolog manual for Prolog-related concepts. https://www.swi-prolog.org/pldoc/doc_for? object=!/0
- Learn Prolog Now! for learning Prolog for beginners, which has applicability for Picat given its logic programming roots: https://lpn.swi-prolog.org/lpnpage.php?pageid=online

Code Examples

- Rosetta Code. Useful to compare to a language you know https://rosettacode.org/wiki/Category:Picat
- The **best** resource https://hakank.org/picat/

- Hakan's global constraint implementations: https://www.hakank.org/picat/#global
- Constraint Programming Problems (multiple programming languages) https://www.csplib.org
- Claudio Cesar de Sá's Github Picat directory: https://github.com/claudiosa/CCS/tree/master/picat (comments tend to be in Portuguese)
- · Advent of Code solutions
 - Neng-Fa Zhou, Håkan Kjellerstrand, Cristian Grozea, Oisín Mac Fhearaí, Picat Through the Lens of Advent of Code https://arxiv.org/html/2507.11731
 - Neng-Fa Zhou https://github.com/nfzhou/aoc/tree/main
 - https://github.com/cgrozea/AdventOfCode2024
 - https://hakank.org/advent-of-code-2024/
 - https://github.com/DestyNova/advent_of_code_2024
- My Advent of Code (examples also in the example code in this repository: https://github.com/dsagman/picat/tree/main/example%20code)
 - 2016 https://github.com/dsagman/advent-of-code/tree/main/2016
 - Planner https://github.com/dsagman/advent-of-code/blob/main/2015/day22/day22.pi
 - Knapsack https://github.com/dsagman/advent-of-code/blob/main/2015/day24/day24.pi

Modules

• JSON encoder https://github.com/nfzhou/json-picat

Editor Plugins

- VS Code https://marketplace.visualstudio.com/items?itemName=arthurwang.vsc-picat
- Emacs https://github.com/nfzhou/emacs-picat-mode/tree/main
- Jupyter Kernel ipicat https://pypi.org/project/picat-kernel/

ipicat has a bug. change

```
from IPython.core.display import display, HTML, Javascript
```

to

from IPython.display import display, HTML, Javascript

Optimization/Constraint Programming Resources

- COIN-OR open source https://github.com/coin-or/COIN-OR-OptimizationSuite
- Z3 (Microsoft) https://microsoft.github.io/z3guide/docs/logic/intro/
- OR-Tools (Google) https://developers.google.com/optimization
- CPLEX (IBM) https://ibmdecisionoptimization.github.io/tutorials/html/Linear_Programming.html
- Global Constraint Catalog https://sofdem.github.io/gccat/gccat/index.html
- SAT Solvers https://github.com/urbanophile/awesome-sat-solvers

Appendix: MD5 in Pure Picat

```
% ------ MD5 in native Picat-----
% Written by ChatGPT in Prolog
% Some back and forth with ChatGPT to get it working in Picat
module md5.
import util.
md5(String) = HexDigest =>
    Padded = md5_pad(String.to_codes),
    Blocks = map(block to words, Padded.chunks of(64)),
    State0 = [0x67452301, 0xefcdab89, 0x98badcfe, 0x10325476],
    FinalState = md5_compress_blocks(Blocks, State0),
    HexDigest = state to hex(FinalState).to lowercase.
% Bitwise and modular helpers
private
mod32(X) = X \mod 4294967296.
private
left_rotate(X, N, R) =>
    L1 = (X << N) /  0xFFFFFFF,
    L2 = X \gg (32 - N),
    R = (L1 \setminus / L2) / \setminus 0xFFFFFFFF.
% MD5 core functions
private
f(X,Y,Z) = R \Rightarrow A = X / Y, B = \sim X / Z, R = A / B.
g(X,Y,Z) = R \Rightarrow A = X / Z , B = ~Z / Y, R = A / B.
h(X,Y,Z) = R \Rightarrow A = X \wedge Y, R = A \wedge Z.
i(X,Y,Z) = R \Rightarrow A = ~Z \setminus / X, R = A \wedge Y.
% Shift amounts (S[i]) and index schedule (K[i])
private
md5_shifts([
    7,12,17,22, 7,12,17,22, 7,12,17,22, 7,12,17,22,
    5, 9,14,20, 5, 9,14,20, 5, 9,14,20, 5, 9,14,20,
    4,11,16,23, 4,11,16,23, 4,11,16,23, 4,11,16,23,
    6,10,15,21, 6,10,15,21, 6,10,15,21, 6,10,15,21
]).
private
md5_indexes([
     0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15,
     1, 6,11, 0, 5,10,15, 4, 9,14, 3, 8,13, 2, 7,12,
     5, 8, 11, 14, 1, 4, 7, 10, 13, 0, 3, 6, 9, 12, 15, 2,
     0, 7,14, 5,12, 3,10, 1, 8,15, 6,13, 4,11, 2, 9
]).
% Precomputed T[i] = floor(abs(sin(i + 1)) * 2^32)
```

```
private
md5 constants([
  0xd76aa478, 0xe8c7b756, 0x242070db, 0xc1bdceee,
  0xf57c0faf, 0x4787c62a, 0xa8304613, 0xfd469501,
  0x698098d8, 0x8b44f7af, 0xffff5bb1, 0x895cd7be,
  0x6b901122, 0xfd987193, 0xa679438e, 0x49b40821,
  0xf61e2562, 0xc040b340, 0x265e5a51, 0xe9b6c7aa,
  0xd62f105d, 0x02441453, 0xd8a1e681, 0xe7d3fbc8,
  0x21e1cde6, 0xc33707d6, 0xf4d50d87, 0x455a14ed,
  0xa9e3e905, 0xfcefa3f8, 0x676f02d9, 0x8d2a4c8a,
  0xfffa3942, 0x8771f681, 0x6d9d6122, 0xfde5380c,
  0xa4beea44, 0x4bdecfa9, 0xf6bb4b60, 0xbebfbc70,
  0x289b7ec6, 0xeaa127fa, 0xd4ef3085, 0x04881d05,
  0xd9d4d039, 0xe6db99e5, 0x1fa27cf8, 0xc4ac5665,
  0xf4292244, 0x432aff97, 0xab9423a7, 0xfc93a039,
  0x655b59c3, 0x8f0ccc92, 0xffeff47d, 0x85845dd1,
  0x6fa87e4f, 0xfe2ce6e0, 0xa3014314, 0x4e0811a1,
  0xf7537e82, 0xbd3af235, 0x2ad7d2bb, 0xeb86d391
1).
% Pad message
private
md5_pad(Bytes) = Padded =>
    % Pad with 0x00 until length mod 64 = 56
    pad_zeroes(Bytes ++ [0x80], 56, PaddedPre),
    % Append 64-bit length (little endian)
    BitLenBytes = word64_le(Bytes.len * 8),
    Padded = PaddedPre ++ BitLenBytes.
% Pad with zeroes until modulo condition met
private
pad_zeroes(List, TargetMod, Padded) =>
    R = List.len \mod 64,
    PadLen = (TargetMod - R + 64) \mod 64,
    Padded = List ++ new_list(PadLen,0).
% Encode a 64-bit value as 8 bytes little endian
private
word64_le(N) = [B0,B1,B2,B3,B4,B5,B6,B7] =>
    B0 = (N \gg 0) / \Omega FF
    B1 = (N \gg 8) / \Omega FF
    B2 = (N >> 16) /  0xFF,
    B3 = (N \gg 24) / \ 0xFF,
    B4 = (N >> 32) /  0xFF,
    B5 = (N >> 40) /  0xFF,
    B6 = (N >> 48) / \ 0xFF,
    B7 = (N >> 56) /  0xFF.
% Convert 64-byte block to 16 32-bit words
% private % has to be public
block_{to}words([]) = [].
block_to_words([B0,B1,B2,B3|Rest]) = [W|Ws] =>
    % Convert 4 bytes to a little-endian 32-bit word
    W = B0 + (B1 << 8) + (B2 << 16) + (B3 << 24),
```

```
Ws = block_to_words(Rest).
% One block transforms the current A,B,C,D
private
md5_process_block([A0,B0,C0,D0], BlockWords) = [Aout,Bout,Cout,Dout] =>
    md5 constants(Ts),
    md5_shifts(Shifts),
    md5 indexes(Ks),
    [A1,B1,C1,D1] = loop steps(0, A0, B0, C0, D0, BlockWords, Ts, Shifts,
Ks),
    Aout = mod32(A0 + A1),
    Bout = mod32(B0 + B1),
    Cout = mod32(C0 + C1),
    Dout = mod32(D0 + D1).
% Recursive 64-step loop
private
loop_steps(64, A,B,C,D, _{-,-,-,-}) = [A,B,C,D].
loop_steps(I, A,B,C,D, BlockWords, [Ti|Tt], [Si|St], [Ki|Kt]) = State =>
    Mi = BlockWords[Ki+1],
    F = step_function(I,B,C,D),
    Temp = mod32(A + F + Ti + Mi),
    left_rotate(Temp, Si, Rot),
    NewA = D, NewD = C,
    NewC = B, NewB = mod32(B + Rot),
    I2 = I + 1,
    State = loop_steps(I2, NewA, NewB, NewC, NewD, BlockWords, Tt, St, Kt).
% Step function chooser by round
private
step function(I,B,C,D) = R=>
         I < 16 then R = f(B,C,D)
    elseif I < 32 then R = g(B,C,D)
    elseif I < 48 then R = h(B,C,D)
    else
                       R = i(B,C,D)
    end.
% Process all blocks, folding the state
private
md5_compress_blocks([], State) = State.
md5_compress_blocks([Block|Rest], StateIn) = StateOut =>
    StateNext = md5_process_block(StateIn, Block),
    StateOut = md5_compress_blocks(Rest, StateNext).
% Convert 32-bit word to 4 little-endian bytes
private
word_to_bytes_le(Word) = [B0,B1,B2,B3] =>
    B0 = (Word >> 0) /  0xFF,
    B1 = (Word >> 8) /  0xFF,
    B2 = (Word >> 16) /  0xFF,
    B3 = (Word \gg 24) /\ 0xFF.
% Use to_hex_string with zero-pad, no byte_to_hex needed
private
```

```
hex2(B) = S =>
    T = B.to_hex_string,
    if T.len == 1 then S = "0" ++ T else S = T end.

private
state_to_hex([A,B,C,D]) = HexStr =>
    Ab = word_to_bytes_le(A), Bb = word_to_bytes_le(B),
    Cb = word_to_bytes_le(C), Db = word_to_bytes_le(D),
    Bytes = Ab ++ Bb ++ Cb ++ Db,
    Parts = [hex2(X) : X in Bytes],
    HexStr = Parts.join('').
```

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