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General Setup

We ran our batch job on two nodes (2x12 cores, 2x24 when considering hyper-threading) in the Cerrado cluster. All experiments were executed three times and then the average execution time and the standard deviation were calculated. Efficiency and speedup were based on the execution time reported by the sequential execution of the bubble sort algorithm.

For the implementation using MPI, we used the domain decomposition philosophy. In short, each process sorts 1/n of the vector using the bubble sort algorithm and shares its lowest values with the left neighbor. The piece of the vector shared is interleaved with the vector held by the left neighbor, and the same process is repeated until the vector is sorted. In this report, we discuss three optimization that we perform in this workflow.

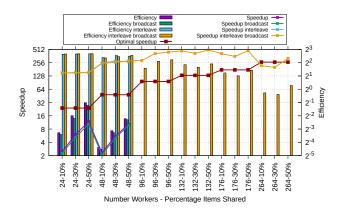


Figure 1: Speedup x Efficiency

Bubble Sort without optimizations

The bubble sort problem addressed here consists of sorting one vector with 1000032 integers. This vector is divided among the processes. Therefore, each process have n/processes integers. As we are sorting a vector in descending order, each process can generate its own vector, without the need to create the entire vector and share it between the processes.

The first phase of the bubble sort algorithm using domain decomposition structure is the application of the bubble sort algorithm over the part of the vector held by each process. After that, each processes communicates with all other processes to test whether they are sorted or not with their neighboring processes. Otherwise, the processes send their lowest numbers to the process on left and receive the highest values from the process on the right. This steps is repeated until the vector is sorted.

According to the results seen in Figure 1, the speedup of this implementation is deeply related to the percentage of numbers that are shared between the processes. It is important to note that we cannot shared more than 50% of the vector between processes, since processes other than 0 and processes-1 will send and receive numbers from the left and right.

Broadcast optimization

The first optimization was to reduce the amount of broadcast messages sent by processes to check whether they are all sorted or not when compared with the other processes. Therefore, as soon as a broadcast message returns that a process is not sorted in relation to the left neighbor, we stop sending and receiving broadcast messages.

As shown in Figure 1, the results using this optimization, compared to results without optimization, were in the range of the standard deviation. Even when the percentage of numbers shared between the processes were higher, which results in faster convergence, the reduction in broadcast messages was not significant. TALK ABOUT THE STRESS TEST.

Interleave instead of bubble sort

The second optimization was focused on reducing the use of the bubble sort algorithm as much as possible, since this algorithm has a time complexity of O(n). Thus, as we can interleave the vector with the part of the vector shared between the processes, it is possible to execute the bubble sort algorithm only once in each process. To use interleaving instead of bubble sort, we first interleave the vector with the percentage of numbers received from right, ignoring the percentage of numbers received from the left. Finally, we interleave the ignored part with the entire vector. It is not possible to call just once the interleave method, as we can end up with three vector pieces in a single process.

This optimization lead to a speedup higher than the optimal speedup. As the interleave algorithm has a linear time complexity, the percentage of items shared between the processes does not have a high impact on speedup or efficiency when using all physical cores or hyper-threading.

Broadcast and interleave

We also tested using both optimization discussed above at the same time. The results showed that this can lead to almost the same results as using just the interleaving optimization. However, when using more process than hyperthreading limit, the results shows that sharing a larger percentage of number is better. Despite this, there is a loss of efficiency and, at some point, a lost of speedup. We believe that this is due to the number of broadcast messages that must be used to synchronize all of these processes.

Discussion

Finally, the broadcast messages, even when widely required, have no significant impact on the domain decomposition performance with MPI. The main bottleneck in this process is the bubble sort algorithm.

Comparing the domain decomposition, with its better optimization, with the divide and conquer approach shows that divide and conquer has a much better speedup and efficiency when using more processes than hyper-threading.

Listing 1: Dataset generator

```
1 #include <stdio.h>
3 int *get_vector(int vector_size, int *v) {
       for (int i = 0; i < vector_size; i++) {</pre>
 5
           v[i] = vector_size - i;
 6
 7
       return v;
 8 }
9
10 int *get_vector_offset(int vector_size, int subvector_size, int *v,
11
                        int offset) {
       int init = subvector_size * offset;
12
1.3
       int end = init + subvector_size;
       for (int i = init; i < end; i++) {</pre>
14
15
           v[i - init] = vector_size - i;
16
17
       return v;
18 }
                                              Listing 2: Bubble Sort Sequential
 1 #include "dataset-generator.h"
2 #include <stdio.h>
3 #include <stdlib.h>
 4 #include <sys/time.h>
 6 float time_difference_msec(struct timeval t0, struct timeval t1) {
7
       return (t1.tv_sec - t0.tv_sec) * 1000.0f +
8
              (t1.tv_usec - t0.tv_usec) / 1000.0f;
9 }
10
11 int is_vector_sorted(int *vector, int vector_size) {
12
      int last_element = -1;
13
       for (int i = 0; i < vector_size; i++) {</pre>
14
           if (last_element > vector[i]) {
15
              return 0;
17
           last_element = vector[i];
18
       }
19
       return 1;
20 }
21
22 int *bubble_sort(int vector_size, int *vector_unsorted) {
       int swapped = 1;
23
24
       int i = 0;
       while ((i < (vector_size - 1)) & swapped) {</pre>
27
           swapped = 0;
28
           for (int j = 0; j < vector_size - i - 1; j++)</pre>
               if (vector_unsorted[j] > vector_unsorted[j + 1]) {
29
30
                  int temp = vector_unsorted[j];
31
                  vector_unsorted[j] = vector_unsorted[j + 1];
32
                  vector_unsorted[j + 1] = temp;
33
                  swapped = 1;
34
              }
           i++;
35
36
37
38
       return vector_unsorted;
39 }
40
41 int main(int argc, char **argv) {
42
       int vector_size = atoi(argv[1]);
43
44
       int vector_unsorted[vector_size];
45
       get_vector(vector_size, vector_unsorted);
       struct timeval t0;
```

```
48
       struct timeval t1;
49
50
       gettimeofday(&t0, 0);
51
       int *vector_sorted = bubble_sort(vector_size, vector_unsorted);
       gettimeofday(&t1, 0);
52
53
54
       float total_time = time_difference_msec(t0, t1);
55
       printf("Vector sorted: %d\n", is_vector_sorted(vector_sorted, vector_size));
57
       printf("Vector size: %d\n", vector_size);
58
       printf("Time sort (ms): %f\n", total_time);
59
60
       return 0;
61 }
                                                 Listing 3: Bubble Sort MPI
 1 #include "dataset-generator.h"
   #include <mpi.h>
   #include <stdio.h>
 4 #include <stdlib.h>
 5 #include <sys/time.h>
 6 #define DEBUG 0
7 #define OPTIMIZE_BROADCAST 1
8 #define BUBBLE_SORT_ONLY_ONCE 1
10 void interleave_vector(int *vector, int a_init_index, int a_end_index,
11
                         int b_init_index, int b_end_index, int *result) {
       if (a_end_index - a_init_index > b_end_index - b_init_index) {
12
13
           int temp = a_init_index;
           a_init_index = b_init_index;
15
           b_init_index = temp;
16
           temp = a_end_index;
17
           a_end_index = b_end_index;
18
           b_end_index = temp;
       }
19
20
21
       int i = 0, a = a_init_index, b = b_init_index;
22
       while (a <= a_end_index b <= b_end_index) {</pre>
23
           if (a <= a_end_index && (vector[a] < vector[b] b > b_end_index)) {
24
              result[i] = vector[a];
25
               a++;
26
           } else {
27
              result[i] = vector[b];
28
              b++;
29
           }
30
           i++;
31
       }
32 }
33
34 void bubble_sort(int vector_size, int *vector_unsorted) {
35
       int swapped = 1;
36
37
       int i = 0;
38
       while ((i < (vector_size - 1)) & swapped) {</pre>
39
           swapped = 0;
40
           for (int j = 0; j < vector_size - i - 1; j++)
               if (vector_unsorted[j] > vector_unsorted[j + 1]) {
41
42
                  int temp = vector_unsorted[j];
43
                  vector_unsorted[j] = vector_unsorted[j + 1];
                  vector_unsorted[j + 1] = temp;
45
                  swapped = 1;
46
47
           i++;
48
49 }
50
51 int is_vector_sorted(int *vector, int vector_size) {
52
       int last_element = -1;
53
       for (int i = 0; i < vector_size; i++) {</pre>
           if (last_element > vector[i]) {
              return 0;
```

```
56
            }
57
            last_element = vector[i];
58
59
        return 1;
60 }
61
62 int main(int argc, char **argv) {
63
        int vector_size = atoi(argv[1]);
        float percentage_items_exchange = atof(argv[2]);
 64
 65
 66
        MPI_Status status;
67
        int my_rank;
68
        int num_processes;
69
 70
        MPI_Init(&argc, &argv);
 71
        MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);
 72
        MPI_Comm_size(MPI_COMM_WORLD, &num_processes);
 73
74
        if (vector_size % num_processes) {
 75
            printf("Error: vector size must be a multiple of the number of "
 76
                  "processes.\n");
 77
            MPI_Abort(MPI_COMM_WORLD, -1);
 78
        }
 79
80
        double t0;
81
        double t1;
82
        t0 = MPI_Wtime();
 83
        int subvector_size = vector_size / num_processes;
        int number_items_shared = subvector_size * percentage_items_exchange;
 85
86
        int subvector[subvector_size + number_items_shared];
87
        get_vector_offset(vector_size, subvector_size, subvector, my_rank);
88
89
        // Avoid allocating a new vector in each iteration.
90
        int process_status[num_processes];
91
        int interleaved_shared_vector_pre_defined[number_items_shared * 2];
    #if BUBBLE_SORT_ONLY_ONCE == 1
92
93
        int interleaved_subvector_pre_defined[subvector_size];
94
        int bubble_sort_executed = 0;
95 #endif
96
97 #if DEBUG == 1
98
        int loop_index = 0;
99 #endif
100
101
        int done = 0;
102
        while (!done) {
103
                           -----FIRST PHASE-----
           // ----
104 #if BUBBLE_SORT_ONLY_ONCE == 1
105
            if (!bubble_sort_executed) {
106
               bubble_sort(subvector_size, subvector);
107
               bubble_sort_executed = 1;
108
            } else {
109
                interleave_vector(subvector, number_items_shared,
110
                                subvector_size - number_items_shared - 1,
                                subvector_size - number_items_shared,
111
                                subvector_size - 1,
112
113
                                interleaved_subvector_pre_defined);
               for (int i = 0; i < subvector_size - number_items_shared; i++) {</pre>
114
115
                   subvector[i + number_items_shared] =
116
                       interleaved_subvector_pre_defined[i];
117
               }
118
119
                interleave_vector(subvector, 0, number_items_shared - 1,
120
                                number_items_shared, subvector_size - 1,
121
                                interleaved_subvector_pre_defined);
                for (int i = 0; i < subvector_size; i++) {</pre>
122
123
                   subvector[i] = interleaved_subvector_pre_defined[i];
124
                }
125
            }
126 #else
```

```
127
           bubble_sort(subvector_size, subvector);
128 #endif
           // -----FIRST PHASE-----
129
130
           // -----SECOND PHASE-----
131
132
           if (my_rank < num_processes - 1) {</pre>
133
              MPI_Send(&subvector[subvector_size - 1], 1, MPI_INT, my_rank + 1, 0,
134
                      MPI_COMM_WORLD);
           }
135
136
           if (my_rank > 0) {
137
               int largest_number_left;
138
               MPI_Recv(&largest_number_left, 1, MPI_INT, my_rank - 1, 0,
139
                     MPI_COMM_WORLD, &status);
               process_status[my_rank] = subvector[0] > largest_number_left;
140
141
           } else {
               process_status[my_rank] = 1;
142
143
144
           for (int i = 0; i < num_processes; i++) {</pre>
145
              MPI_Bcast(&process_status[i], 1, MPI_INT, i, MPI_COMM_WORLD);
147 #if OPTIMIZE_BROADCAST == 1
148
               if (!process_status[i]) {
149
                  break;
150
151 #endif
152
           }
153
154
           int vector_sorted = 1;
155
           for (int i = 0; i < num_processes; i++) {</pre>
156
               vector_sorted &= process_status[i];
157
               if (!vector_sorted) {
158
                  break;
159
               }
160
           }
161
           if (vector_sorted) {
162
               done = 1;
163
               break;
164
165
           // -----SECOND PHASE-----
           // -----THIRD PHASE-----
           if (my_rank > 0) {
168
169
               MPI_Send(&subvector[0], number_items_shared, MPI_INT, my_rank - 1,
170
                      0, MPI_COMM_WORLD);
171
           }
172
           if (my_rank < num_processes - 1) {</pre>
               MPI_Recv(&subvector[subvector_size], number_items_shared, MPI_INT,
173
174
                      my_rank + 1, 0, MPI_COMM_WORLD, &status);
175
176
               interleave_vector(subvector, subvector_size - number_items_shared,
177
                              subvector_size - 1, subvector_size,
178
                              subvector_size + number_items_shared - 1,
179
                              interleaved_shared_vector_pre_defined);
180
181
               MPI_Send(
182
                  &interleaved_shared_vector_pre_defined[number_items_shared],
183
                  number_items_shared, MPI_INT, my_rank + 1, 0, MPI_COMM_WORLD);
184
185
               for (int i = 0; i < number_items_shared; i++) {</pre>
186
                  subvector[subvector_size - number_items_shared + i] =
187
                      interleaved_shared_vector_pre_defined[i];
188
               }
189
           }
190
           if (my_rank > 0) {
191
               MPI_Recv(&subvector[0], number_items_shared, MPI_INT, my_rank - 1,
192
                       0, MPI_COMM_WORLD, &status);
193
           }
           // -----THIRD PHASE-----
194
195 #if DEBUG == 1
196
           if (loop_index == 0) {
197
               for (int i = 0; i < subvector_size; i++) {</pre>
```

```
198
                   printf("%d ", subvector[i]);
199
200
                printf("---- %d", my_rank);
                printf("\n");
201
202
                fflush(stdout);
203
204
            loop_index++;
205
    #endif
206
207
208
        t1 = MPI_Wtime();
209
        double total_time = (t1 - t0) * 1000;
210
211 #if DEBUG == 1
212
        if (my_rank > 0) {
213
            MPI_Send(&subvector[0], subvector_size, MPI_INT, 0, 0, MPI_COMM_WORLD);
214
        } else {
215
            int final_vector[vector_size];
216
            for (int i = 0; i < subvector_size; i++) {</pre>
217
                final_vector[i] = subvector[i];
218
219
220
            for (int i = 1; i < num_processes; i++) {</pre>
221
                int subvector_received[subvector_size];
222
                MPI_Recv(&subvector_received[0], subvector_size, MPI_INT, i, 0,
223
                        MPI_COMM_WORLD, &status);
224
                for (int j = 0; j < subvector_size; j++) {</pre>
225
226
                    final_vector[subvector_size * i + j] = subvector_received[j];
227
228
            }
229
230
            printf("Final vector:\n");
231
            for (int i = 0; i < vector_size; i++) {</pre>
232
                printf("%d ", final_vector[i]);
233
234
            printf("\n");
235
            printf("DEBUG: %d\n", DEBUG);
236
237
            printf("OPTIMIZE_BROADCAST: %d\n", OPTIMIZE_BROADCAST);
238
            printf("BUBBLE_SORT_ONLY_ONCE: %d\n", BUBBLE_SORT_ONLY_ONCE);
239
            printf("Vector sorted: %d\n",
240
                  is_vector_sorted(subvector, subvector_size));
241
            printf("Vector size: %d\n", vector_size);
242
            printf("Time sort (ms): %f\n", total_time);
243
        }
244 #else
245
        if (my_rank == 0) {
246
            printf("DEBUG: %d\n", DEBUG);
247
            printf("OPTIMIZE_BROADCAST: %d\n", OPTIMIZE_BROADCAST);
248
            printf("BUBBLE_SORT_ONLY_ONCE: %d\n", BUBBLE_SORT_ONLY_ONCE);
249
            printf("Vector sorted: %d\n",
250
                   is_vector_sorted(subvector, subvector_size));
251
            printf("Vector size: %d\n", vector_size);
252
            printf("Time sort (ms): %f\n", total_time);
        }
253
254 #endif
255
256
        MPI_Finalize();
257
258
        return 0;
```

259 }