

Tema 2 (3.9) a) $1000'_{(2)} = \cancel{17}_{(10)} \quad 1 \cdot 2^0 + 1 \cdot 2^9 = 17_{(10)}$

b) $3A_{(16)} = 10 \cdot 16^0 + 3 \cdot 16^1 = \cancel{58}_{(10)}$

c) $122_{(6)} = 2 \cdot 6^0 + 2 \cdot 6^1 + 1 \cdot 6^2 = 50_{(10)} = 302_{(4)}$

d) $31_{(8)} - 14_{(8)} = 15_{(8)}$

$$\begin{array}{r|l} 50 & 4 \\ \hline 48 & 12 \\ \hline =2 & 12 \\ & \hline & 3 \\ & \hline & 0 \\ & \hline & 3 \end{array}$$

(4.9) $29^{89} \bmod 97 \equiv 29 \cdot 29^{\cancel{88}} \equiv 29 \cdot (29^2)^{44} \equiv 29 \cdot (65^2)^{22} \equiv 29 \cdot (54^2)^{11} \equiv$
 $\equiv 29 \cdot 6 \cdot (6^2)^5 \equiv 29 \cdot 6 \cdot 36^5 \equiv 77 \cdot 36^5 \equiv 77 \cdot 36 \cdot (36^2)^2 \equiv 56 \cdot 35^2 \equiv$
 $\equiv 56 \cdot 61 \equiv 21 \bmod 97$

(3.23) a) $1011_{(2)} = \cancel{11}_{(10)} \cdot \cancel{10}_{(16)} = \cancel{110}_{(10)}$
 $= 1 \cdot 2^0 + 1 \cdot 2^1 + 1 \cdot 2^3 = 11_{(10)}$

b) $2B_{(16)} = 11 \cdot 16^0 + 2 \cdot 16 = 43_{(10)}$

c) $343_{(5)} = 3 \cdot 5^0 + 4 \cdot 5 + 3 \cdot 5^2 = 3 + 20 + 75 = 98_{(10)} = 1202_{(4)}$

$$\begin{array}{r|l} 98 & 4 \\ \hline 96 & 24 \\ \hline =2 & 24 \\ & \hline & 6 \\ & \hline & 4 \\ & \hline & 1 \\ & \hline & 0 \end{array}$$

d) $16_{(8)} - 5_{(8)} = 11_{(8)} = 81_{(10)}$

(4.23) $89^{163} \bmod 167 = 89 \cdot (89^2)^{81} = 89 \cdot 72 \cdot (72^2)^{40} = 62 \cdot (7^2)^{20} = 62 \cdot (49^2)^{10} =$
 $\equiv \cancel{62 \cdot 63} \cdot (65^2)^4 \cdot 62 \cdot (63^2)^5 = 62 \cdot 128 \cdot (128^2)^2 = 62 \cdot 128 \cdot 18^2 = 62 \cdot 128 \cdot 157 =$
 $= 87 \cdot 157 = 132 \bmod 167$