

Tema 1 (2.9) Det CMMC al lui 90127 și 32107 fol. alg lui Euclid extins  
și det. coef. Bezout.

$$x_a = (1, 0), x_b = (0, 1)$$

$$90127 = 2 \cdot 32107 + 25913$$

$$x_n = (1, 0) - 2 \cdot (0, 1) = (1, -2)$$

$$32107 = 1 \cdot 25913 + 6194$$

$$x_n = (0, 1) - 1 \cdot (1, -2) = (-1, 3)$$

$$25913 = 4 \cdot 6194 + 1137$$

$$x_n = (1, -2) - 4 \cdot (-1, 3) = (5, -14)$$

$$6194 = 5 \cdot 1137 + 509$$

$$x_n = (-1, 3) - 5 \cdot (5, -14) = (-26, 73)$$

$$1137 = 2 \cdot 509 + 119$$

$$x_n = (5, -14) - 2 \cdot (-26, 73) = (57, -160)$$

$$509 = 4 \cdot 119 + 33$$

$$x_n = (-26, 73) - 4 \cdot (57, -160) = (-254, 713)$$

$$119 = 3 \cdot 33 + 20$$

$$x_n = (57, -160) - 3 \cdot (-254, 713) = (819, -2299)$$

$$33 = 1 \cdot 20 + 13$$

$$x_n = (-254, 713) - (819, -2299) = (-1073, 3012)$$

$$20 = 1 \cdot 13 + 7$$

$$x_n = (819, -2299) - (-1073, 3012) = (1892, -5311)$$

$$13 = 1 \cdot 7 + 6$$

$$x_n = (-1073, 3012) - (1892, -5311) = (-2965, 8323)$$

$$7 = 1 \cdot 6 + 1$$

$$x_n = (1892, -5311) - (-2965, 8323) = (4857, -13634)$$

$$6 = 6 \cdot 1 + \boxed{0}$$

$$1 = 4857 \cdot 90127 + (-13634) \cdot 32107$$

(3.9) Det inversul lui 10 modulo 37.

$$(10, 37): 37 = 3 \cdot 10 + 7$$

$$10 = 1 \cdot 7 + 3$$

$$7 = 2 \cdot 3 + \boxed{1} \Rightarrow (10, 37) = 1 \Rightarrow \exists \text{ inversul lui } 10 \text{ mod } 37$$

$$3 = 3 \cdot 1 + 0$$

$$1 = 4u + 3v \Leftrightarrow 1 = 10u + 37v \Leftrightarrow 1 \equiv 10u \pmod{37} \Leftrightarrow \boxed{u = \text{inversul}}$$

$$37 - 3 = 34 = 11 \cdot 3 + 1$$

$$\cancel{11 \cdot 3 + 1 = 34}$$

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$$37 \cdot 7 = 259$$

$$10 \cdot 26 = 260$$

$$\Rightarrow 1 + 259 = 10 \cdot 26$$

$$\equiv 0 \pmod{37}$$

$$1 = 10 \cdot 26 \pmod{37} \Rightarrow \boxed{u = 26}$$