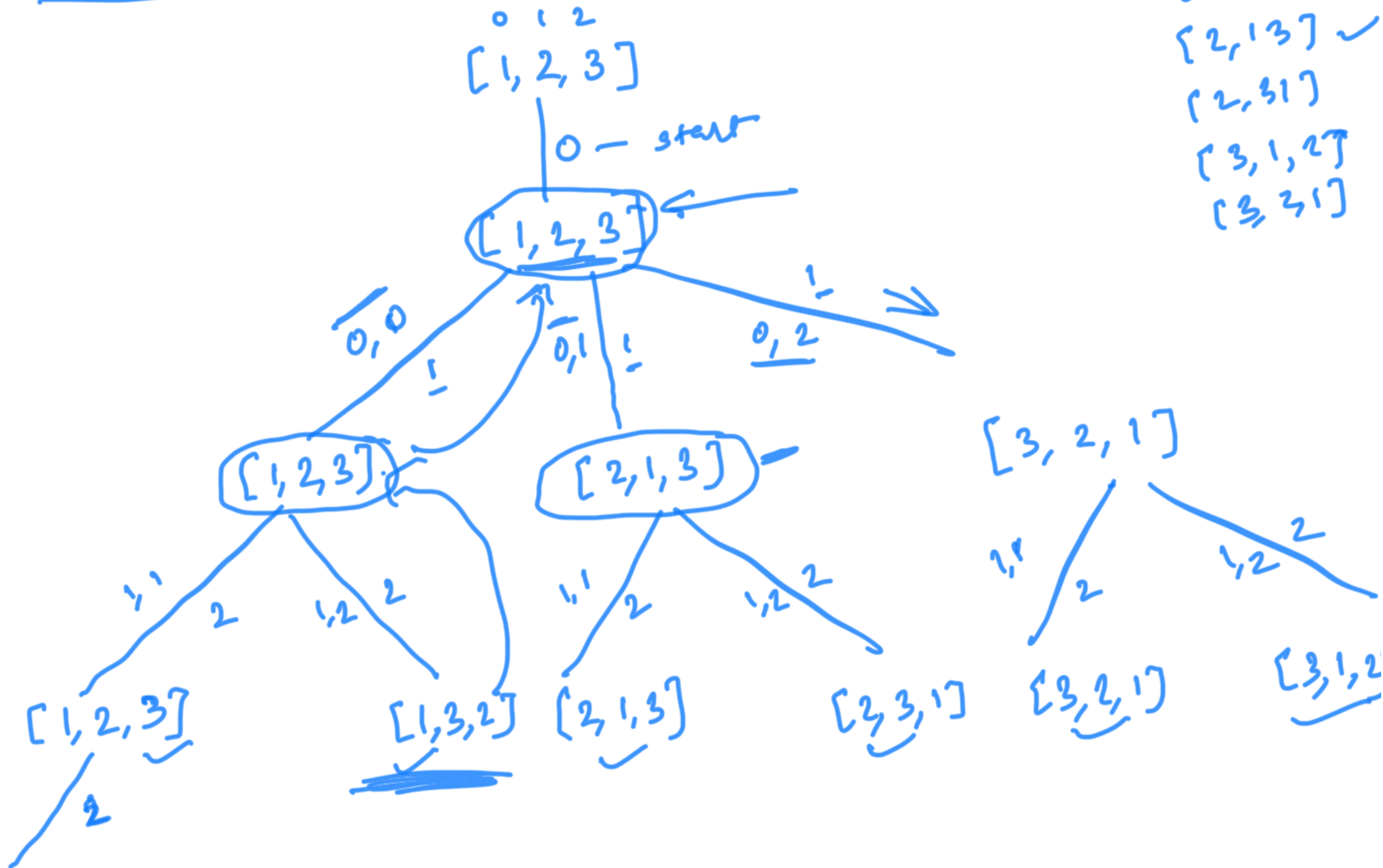


# Recursion

# Permutation

[1, 2, 3] — [1, 2, 3]  
 [1, 3, 2]  
 [2, 1, 3] ✓  
 [2, 3, 1]  
 [3, 1, 2]  
 [3, 2, 1]



void dfs ( list <Integer> nums, int start )

```

if ( start == nums.size() - 1 )
{
    print (nums);
    return;
}

```

```

for ( int i = start ; i < nums.size() ; i++ )

```

```

{
    swap ( nums, start, i ); // do

```

```

    dfs ( nums, start + 1 );

```

```

    swap ( nums, start, i ); // undo

```

```

}

```

```

}

```

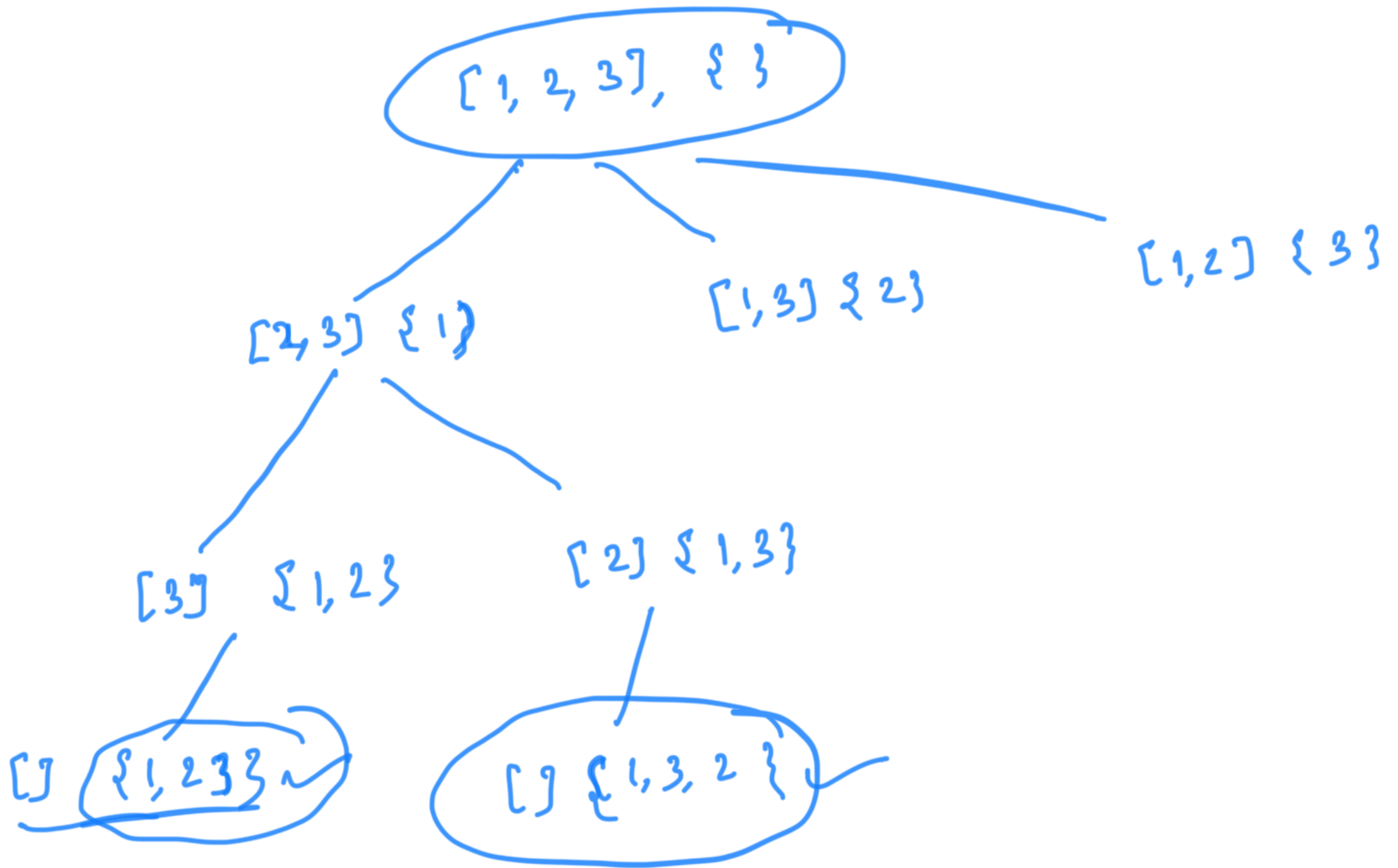
[ 1, 2, 3 ]

temp list

1 — [ 2, 3 ]

2 — [ 1, 3 ]

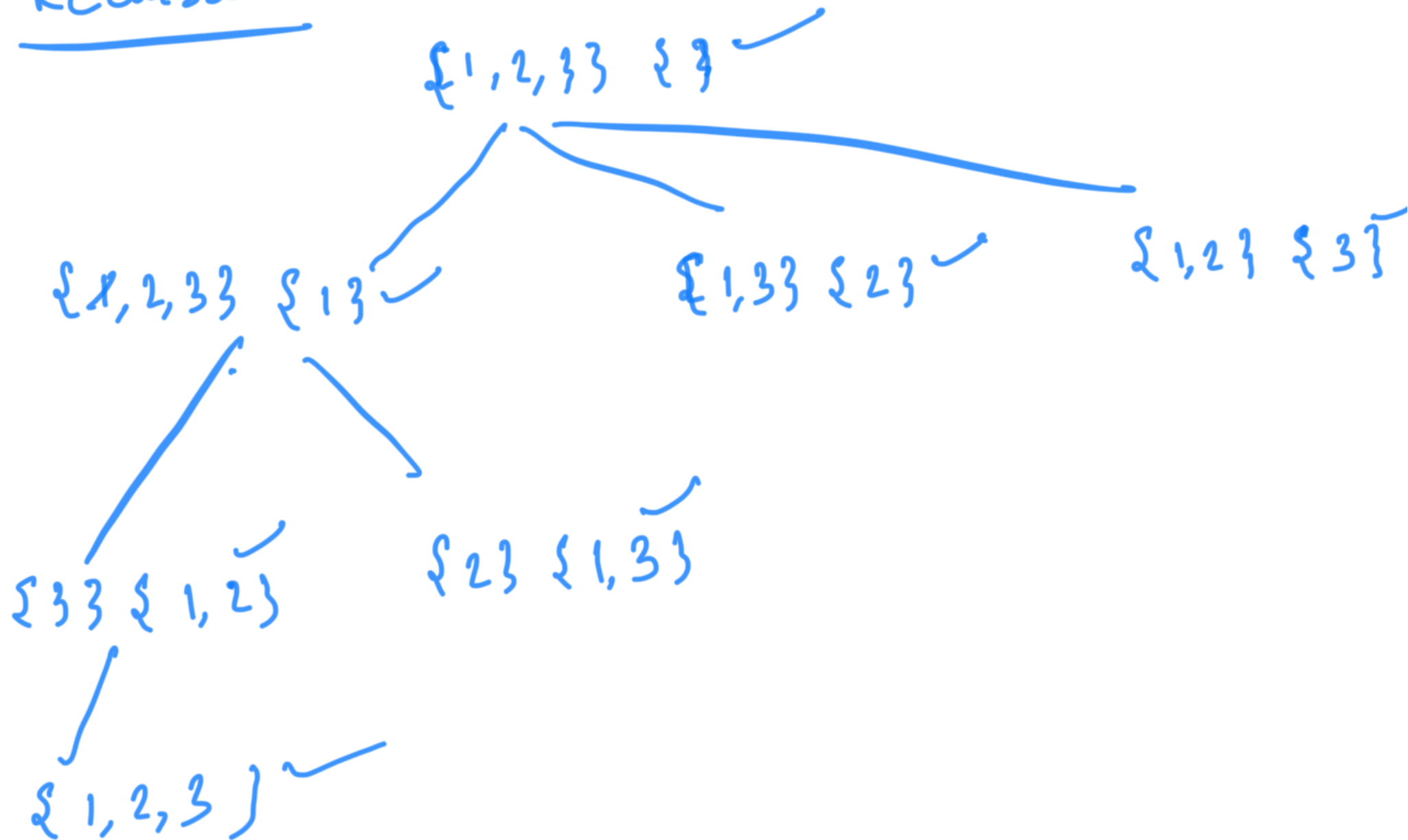
3 — [1, 2]



permutation  
combination }

subset

Recursion



Bit masking

n element  $\frac{2^n}{1}$

0 1 2 ...  $2^{n-1}$

0, 1, 2, 3

{1, 2, 3}

0	0 0 0	→	{ }
1	0 0 1	→	{ 3 }
2	0 1 0	→	{ 2 }
3	0 1 1	→	{ 2, 3 }
4	1 0 0	→	{ 1 }
5	1 0 1	→	{ 1, 3 }
6	1 1 0	→	{ 1, 2 }
7	1 1 1	→	{ 1, 2, 3 }

Iterative solution

{1, 2, 3}

{ }, {1}, {2}, {3} . . . }

{ { } }

{ { } } → { { }, { 1 }, { 2 }, { 3 } }

{ { 1 }, { 1 1 }, { 2 2 }, { 3 3 } }

{ { 1 2 }, { 1 3 }, { 1, 2 3 }, { 1, 3 3 } }

N number

[ 1, 1, 1, 2 ]

[ 1, 1, 1, 2 ]

[ 1, 2, 1, 1 ]

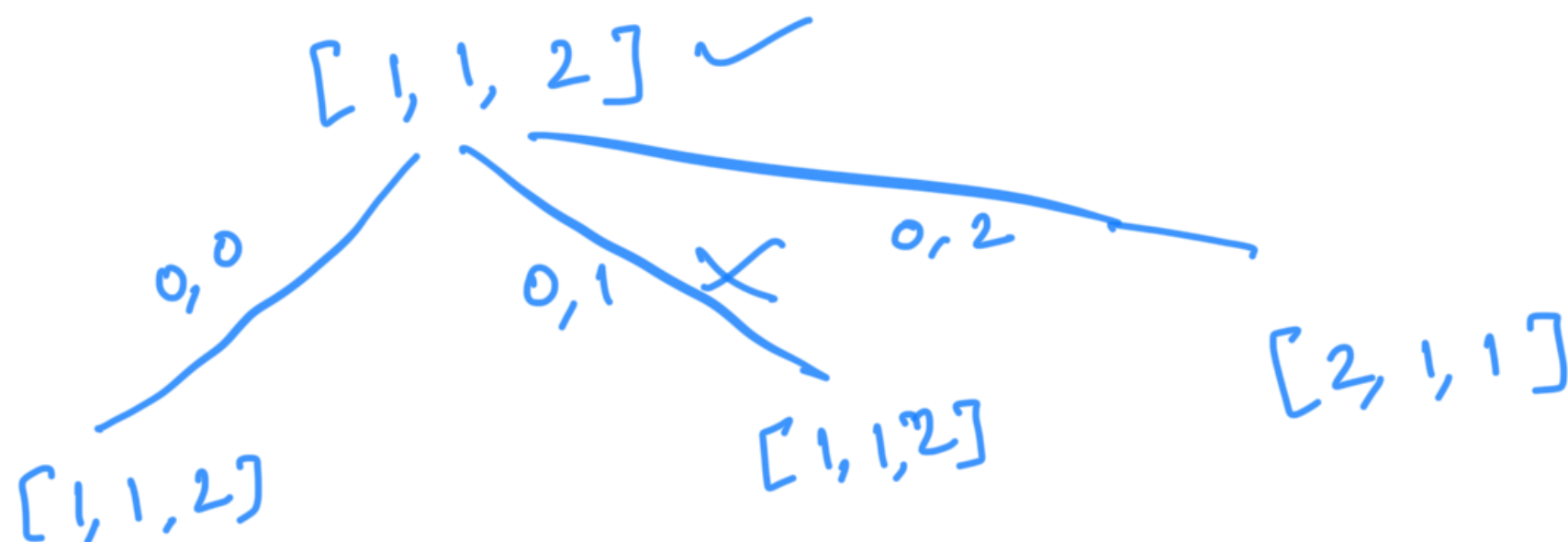
[ 1, 1, 2, 1 ]

$$\frac{4!}{3!} = \frac{4 \times 3!}{3!}$$

$[2, 1, 1, 1]$  /

$[1, 1, 1, 2, 2, 3, 3, 3, 4]$  ✓

$$\frac{9!}{3! 2! 3!} =$$



Combination sum

$[2, 3, 5, 8], 8$

$[2, 2, 2, 2] ✓$

$[2, 2, 2, 2] ✓$



8, 6, 4 ... 0

2, 4, 6, (8)

[3, 5] ✓

[8] ✓

Start

0

take the number and  
go to next

or

do not take this no.  
go to next.

dfs ( arr[], int start, int target, list )

{

if (target == 0) ✓

{

print list;

return;

}

if (target < 0) return;

if (start == arr.length) return;

list.add(arr[start]);

taken ——— dfs(arr, start, target - arr[start], list);

list.remove(list.size() - 1);

not taken ——— dfs(arr, start + 1, target, list)

{ 2, 3, 5, 8 }

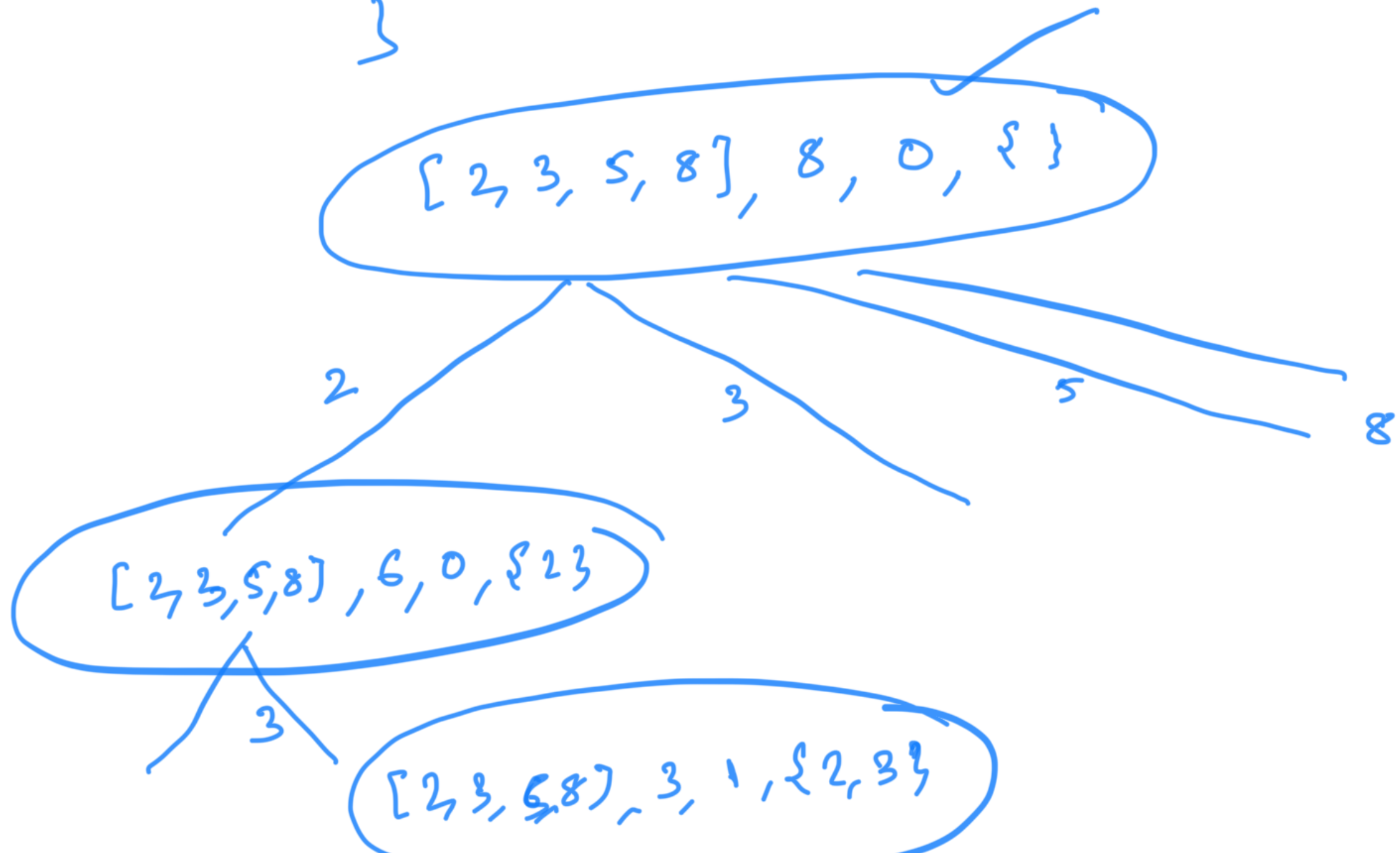
dfs (

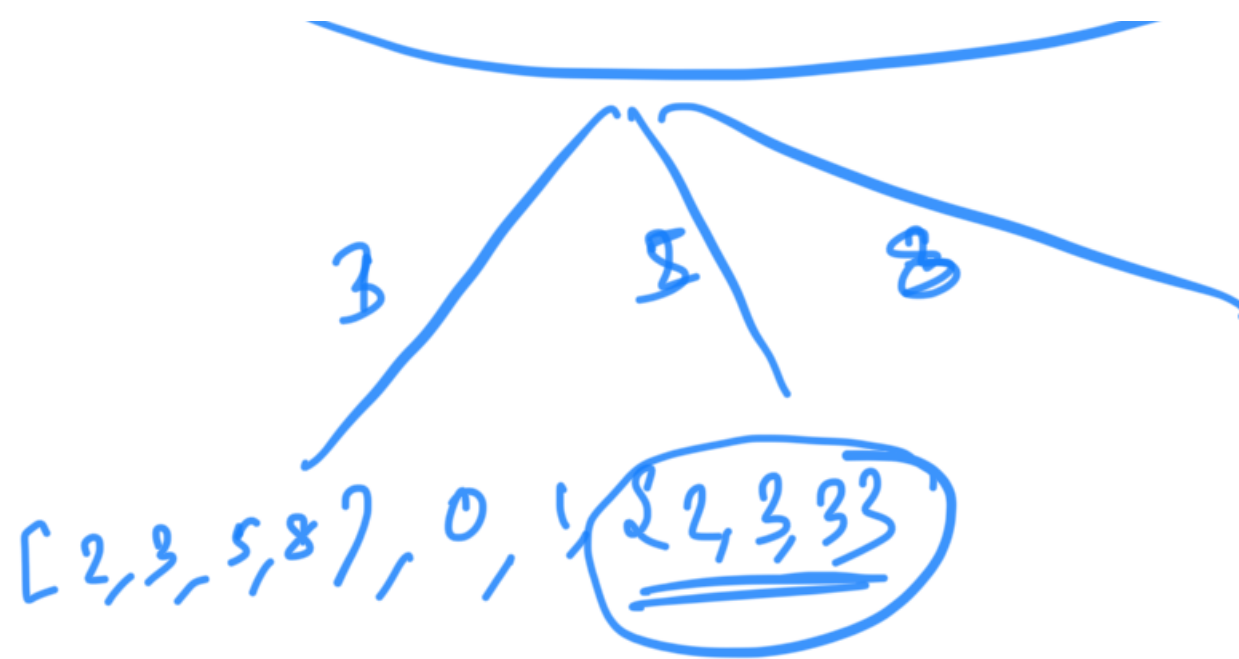
{

```

for (i = start ; i < arr.length; i++)
{
    list.add(arr[start]);
    dfs(arr, i, target - arr[start],
        list.remove());
}

```





Time complexity



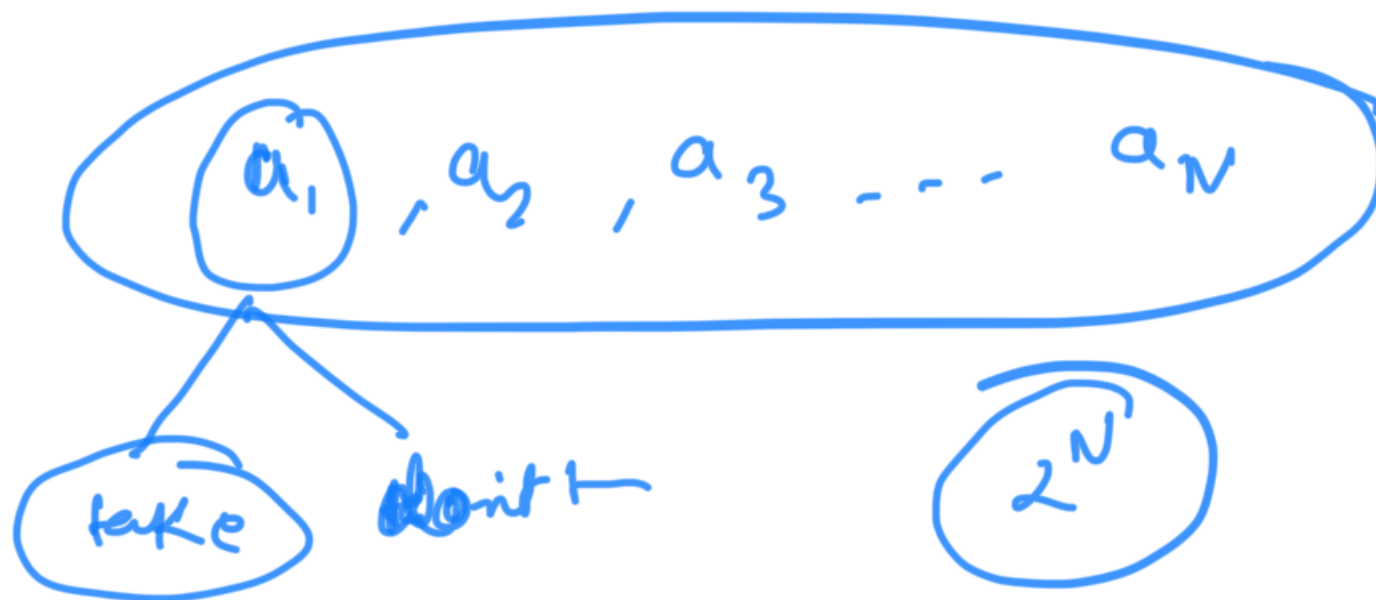
target = 140

$2^N$  ↙

140

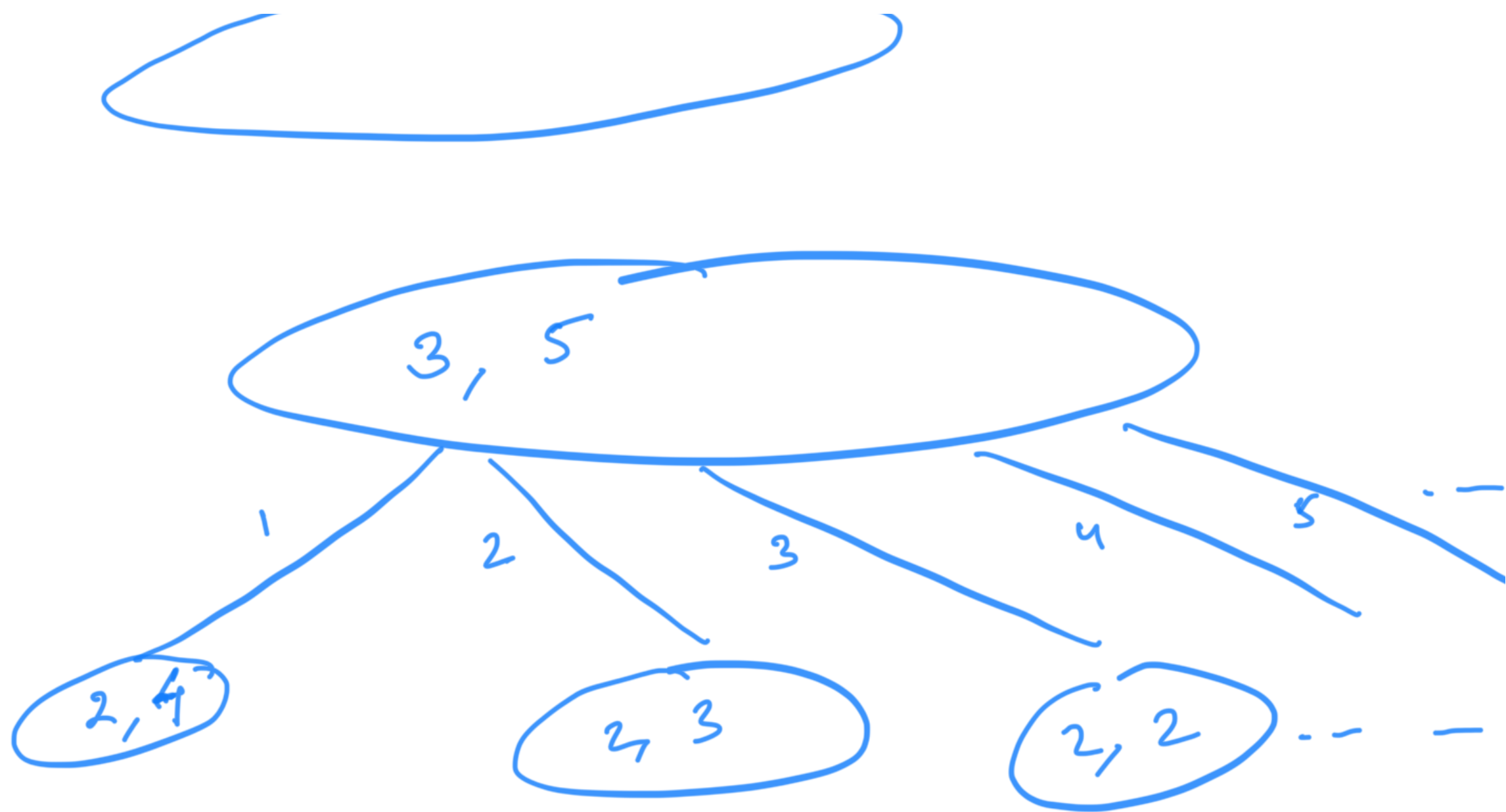
140

$[1, \dots, 140]$



$2^N$  and target

$O(2^N)$



$q$		
.	.	
	$q$	

$R_1 \rightarrow$

$R_2 \rightarrow$

$R_3 \rightarrow$

$R_4 \rightarrow$

$a_{11}$	$a_{12}$		
$a_{21}$		.	$a_{24}$
$a_{31}$		.	
$x$	$x$	$a_{33}$	$a_{34}$

$4 \times 4$

$x$

Co

$00$	$01$	$02$	$03$
$10$	$11$	$12$	$13$
$20$	$21$	$22$	$23$
$30$	$31$	$32$	$33$

$n \times n$

$(i, j) \rightarrow$

boolean[] isQATCOL =  $\left[ \begin{array}{cccc} \underline{(3,0)} & \underline{(2,1)} & (1,2) & (0,3) \end{array} \right]$

$\left[ \begin{array}{cccc} 0,0 & (1,1) & (2,2) & \overset{3}{(3,3)} \end{array} \right] \rightarrow 3$

$\downarrow \quad \downarrow \quad \downarrow \quad \downarrow$

3 map to same value

$\left[ \begin{array}{ccc} (0,1) & (1,2) & (2,3) \end{array} \right]$

$i+$

$(i,j) \rightarrow \begin{cases} (i+j) \\ (j-i) \end{cases}$

$\begin{array}{cc} \underline{(2,0)} & \underline{(3,1)} \\ -2 & -2 \\ \hline & \hline \end{array}$

col  $\rightarrow$

$(i,j)$

$\left. \begin{array}{l} j \rightarrow \text{true} \\ i+j \rightarrow \text{true} \end{array} \right\} \checkmark$



i

j+i

j-i

dfs (u

$j-i \rightarrow \text{true}$

[

dfs( row, N )

{

if ( row == N )

{ print ans ; return  
}

for ( col = 0 ; col < N ; col++ )

{ // try to put q at (row, col)

if ( hm1.get( col ) == true

|| hm2.get( col + row ) == true

|| hm3.get ( row - col ) != true  
continue ;