



1. coin change

[1, 2, 5]

amount 11

$$\textcircled{3} \quad \textcircled{5 \ 5 \ 1} = 11$$

$$\textcircled{2 \ 2 \ 5 \ 2} = 11$$

$$\textcircled{1 \ \dots \ 1} = 11$$

~~1, 2, 3, 4, 6~~

[1, 3, 4, 5]

7

$$\textcircled{5, 1, 1} = 3 \text{ coins}$$

2 coins
 $\textcircled{3, 4}$

We have to do exhaustive search

com '[1, 3, 5]

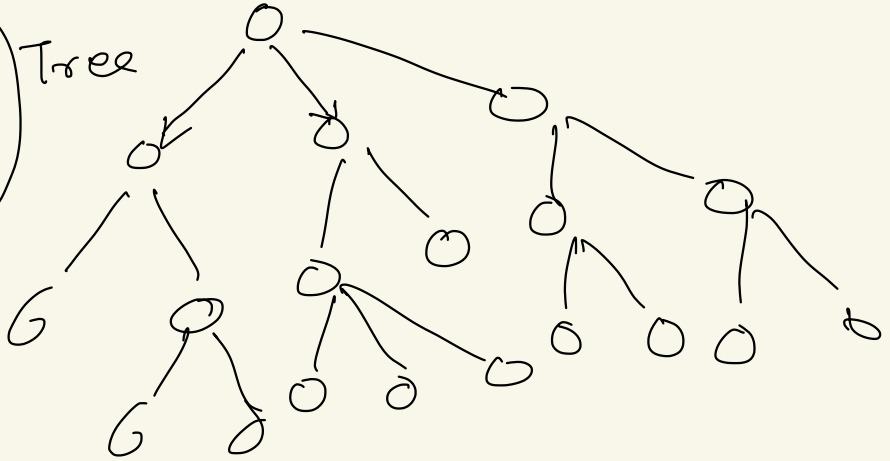
15

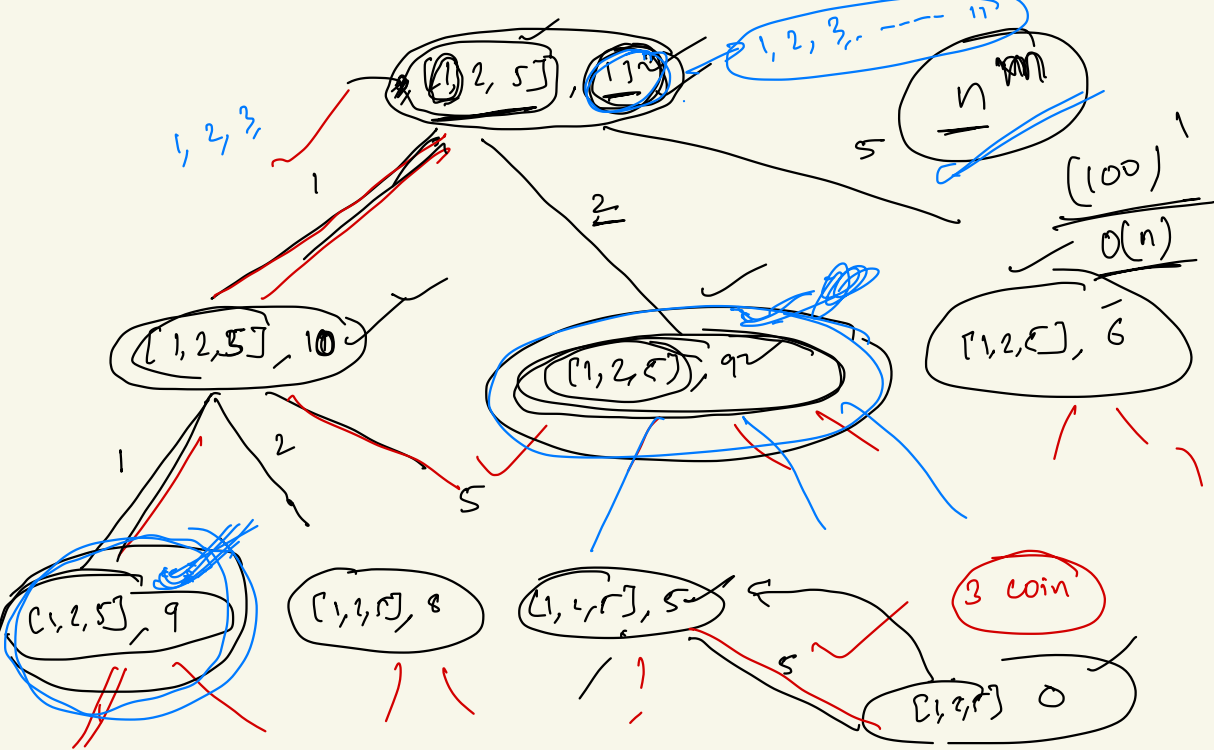
backtracking

DAG

Directed
Acyclic
Graph

Tree





```
int dfs (int[] coins, int amount) { O(amount)
```

```
    if (amount == 0) return 0;
```

```
    if (amount < 0) return Integer.MAX_VALUE;
```

```
    int res = Integer.MAX_VALUE;
```

```
    if (hm.containsKey(amount))  
    {  
        hm.get(amount)  
    }  
    for (int i = 0; i < coins.length; i++)
```

```
        int curres = dfs (coins, amount - coins[i]);
```

```
        if (curres == Integer.MAX_VALUE)  
            continue;
```

```
        res = Math.min (res, 1 + curres)
```

```
    }
```

```
    return res
```

```
}
```

```
hm.put (amount, res);
```

$[1, 1, 1, 1, 1]$ target = 3

$$+1 + 1 + 1 + 1 + 1 = 5$$

$$\cancel{-1} \cancel{+1} + 1 + 1 + 1 = 3$$

$$+1 - 1 + 1 + 1 + 1 = 3$$

$$\left. \begin{array}{l} - + + + + \\ + - + + + \\ + + - + + \\ + + + - + \\ + + + + - \end{array} \right\}$$

$$\begin{array}{ccccccc} & & & \downarrow & \downarrow & & \\ +1 & -1 & +1 & +1 & & \Rightarrow & 1 \\ \hline & & & & \searrow & & 2 \end{array}$$

```
dfs ( int[] nums , int i , int sum , int target )  
{
```

```
    if ( i == nums.length )
```

```
    {  
        if ( sum == target ) ans++;
```

```
    }  
    return;
```

```
    dfs ( num , i+1 , sum + nums[i] , target )
```

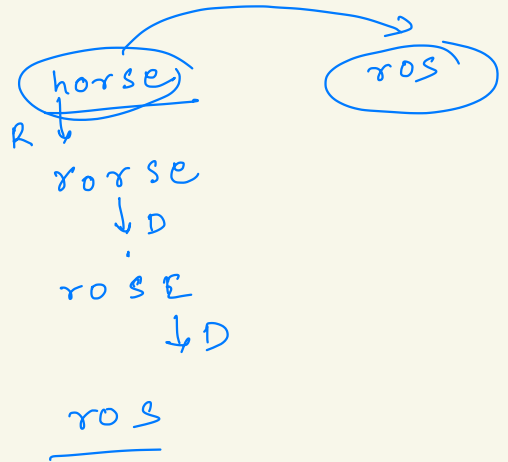
```
    dfs ( num , i+1 , sum - nums[i] , target )
```

```
}
```

```
dfs ( nums , 0 , 0 , target )
```

Edit distance
 cost
 Insert — 1
 Delete → 1
 Replace —

 —





```
int dfs ( string p , string q , int i , int j )
```

```
{
  if ( i == p.length )
  {
    return q.length - j ;
```

"abc" → "abc"

3 insert

```

  if ( j == q.length ) {
    return p.length - i ;
```

"abc" → "xabc"

3 delete

```

  if ( p.charAt(i) == q.charAt(j) )
  {
    return dfs ( p , q , i+1 , j+1 ) ;
```

```

  }
  int cost1 = dfs ( p , q , i+1 , j+1 ) ;
```

```

  int cost2 = dfs ( p , q , i+1 , j ) ;
  int cost3 = dfs ( p , q , i , j+1 ) ;
```

```

  memo[i][j] = 1 + min ( cost1 , cost2 , cost3 ) ;
  return min ( cost1 , cost2 , cost3 )
```

3

~~$O(p.length \times q.length)$~~

~~$O(3^{min(p.length, q.length)})$~~

~~abc~~

~~pqr~~