Linear Algebra Done Right

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June 27, 2021

1 Vector Spaces

Linear algebra is the study of linear maps on finite-dimensional vector spaces. Vector spaces are defined in this chapter, and their basic properties are developed. Vector spaces are a generalization of the description of a plane using two coordinates, as published by Descartes in 1637.

1.1 R^n , C^n , and F^n

Definition: Complex Number

A complex number is an ordered pair $(a, b) \in \mathbb{R}^2$, denoted a + bi.

• The set of all complex numbers is denoted by **C**:

$$\mathbf{C} = \{a + bi : a, b \in \mathbf{R}\}\$$

• Addition and multiplication on C are defined by

$$(a+bi) + (c+di) \equiv (a+c) + (b+d)i$$

$$(a+bi) \cdot (c+di) \equiv (ac-bd) + (ad+bc)i$$

Theorem: Complex Number

A complex number is an ordered pair $(a, b) \in \mathbf{R}^2$, denoted a + bi.