

# CS 3753 & 5163 Data Science

## Homework 5 (100 +20 points)

### Submission:

1. The instruction is the same as the ones previous assignments. Please submit a single python script (**abc123\_hw#.ipynb**) through blackboard. All the results are outputted from your Python code.
2. For this assignment, you **are encouraged to** collaborate with up to three members in a team. You can help each other to understand the questions and discuss the issues in the assignment. However, you cannot copy solutions from your team members. You still need to submit your solution independently.

### Questions

1. (20 points) We do the linear regression on three points (0.5, 1), (2, 2.5), and (3, 3). Please calculate the SSEs of the four following linear regression based on the definition  $SSE = \sum_{i=1}^n (y_i - \hat{y}_i)^2$ . Write the Python code to output the major steps of the calculation and results.
  - (a)  $y = x + 0.5$
  - (b)  $y = x + 1$
  - (c)  $y = 0.8 * x + 0.3$
  - (d)  $y = 0.8 * x + 0.7$

Which is the best linear regression using SSE?

2. (20 points) What is the problem solved by Lasso and Ridge regression? What is the major difference between the two regression? Please discuss the advantages and disadvantages of them.
3. (30 pints) Decision Tree  
There are various ways to decide on the metric to choose the variable on which splitting for a node is done. Different algorithms deploy different metrics to decide which variable splits the dataset best.

Let's say we have a sample of 30 records. There are two classes C1 and C2. We have three possible splits a, b, and c (see figures below). The number of records in each class is shown in every node.

- a. Measure the node impurity using Gini Index, Entropy Gain, and Misclassification Error, respectively. Please output the results in the table by your Python code. In your output, you can have the following format  
Node impurities:  
Gini index: a – left: xx; right: xx; b – left: xx; right: xx; c – left: xx; right: xx;  
Entropy: ...  
Misclass error: ...

Qualities of splitting:

Gini index: a: xx; b: xx; c: xx;  
 Entropy: ...  
 Misclass error: ...

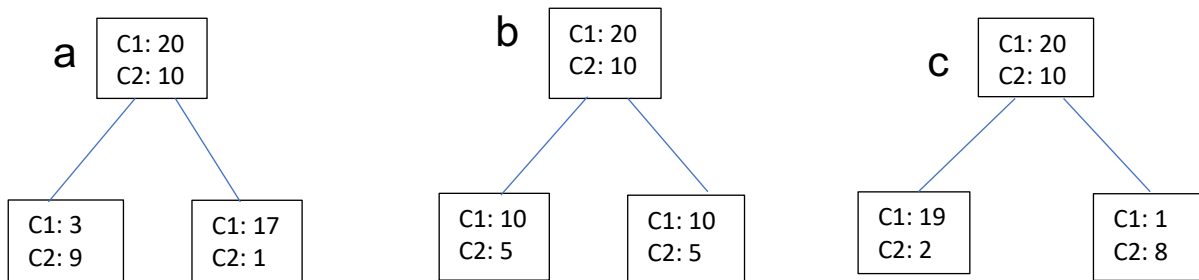
The output information of **node impurities** is in the following table. The following tables just help you understand the question. Please output the values in the above format.

Impurity	a		b		c	
	left	right	left	right	left	right
Gini index						
Entropy						
Misclass error						

- b. Evaluate the quality of the three splitting and report the best one (a, b, or c).  
 The output **qualities of the splitting** are in the following table. Please output the results by your Python code.

Splitting	a	b	c
Gini index			
Entropy			
Misclass error			

- c. Please output the best splitting (a, b, or c) using each method (Gini index, Entropy and Misclass error).  
 d. Finally, print out your conclusion about whether all three methods have the same best splitting or not.



4. (30 points) KNN: this section applies the KNN algorithm to the Iris flowers dataset. The first step is to load the dataset in “iris.csv” and convert the loaded data to numbers that we can use with the mean and standard deviation calculations. For this we will use the helper function `load_csv()` to load the file, `str_column_to_float()` to convert string numbers to floats and `str_column_to_int()` to convert the class column to integer values.

You do not need to import any libraries or modules about KNN because you will implement the KNN from scratch. The template of the code is provided and you just need to complete the functions `Euclidean_distance()`, `get_neighbors()`, and `predict_classification()`. The mean accuracy is around 96.667% ( $\approx 97\%$ ).

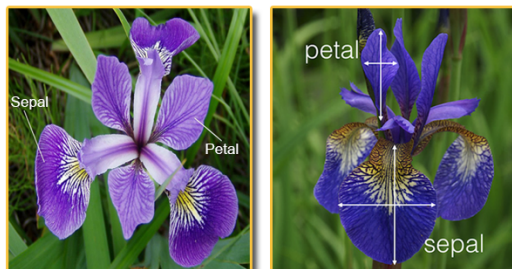
We will evaluate the algorithm using k-fold cross-validation with 5 folds. This means that  $150/5=30$  records will be in each fold. We will use the helper functions `evaluate_algorithm()` to evaluate the algorithm with cross-validation and `accuracy_metric()` to calculate the accuracy of predictions.

A new function named `k_nearest_neighbors()` was developed to manage the application of the KNN algorithm, first learning the statistics from a training dataset and using them to make predictions for a test dataset.

Download the dataset and save it into your current working directory with the filename “iris.csv”. The Iris Flower Dataset involves predicting the flower species given measurements of iris flowers.

It is a multiclass classification problem. The number of observations for each class is balanced. There are 150 observations with 4 input variables and 1 output variable. The variable names are as follows:

- a. Sepal length in cm.
- b. Sepal width in cm.
- c. Petal length in cm.
- d. Petal width in cm.
- e. Class



5. **(Extra credits: 20 pts)** Post pruning of decision tree by pessimistic approach. In this approach, the error in a leaf node is  $e'(t) = e(t) + 0.5$ , where  $e(t)$  is the training error in a node. Please calculate the pessimistic error at the parent node A and leaf nodes. Should this tree be pruned?

