

# Algorithms for Modern Processor Architectures

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All software for this talk: <https://github.com/lemire/talks/tree/master/2025/sea/software>

# Disk at gigabytes per second

[PC Components](#) > [Storage](#) > [SSDs](#)

## Micron shows off world's fastest PCIe 6.0 SSD, hitting 27 GB/s speeds — Astera Labs PCIe 6.0 switch enables impressive sequential reads

News

By [Sunny Grimm](#) published March 8, 2025

The next-gen of networking and storage is hitting the trade shows

# Input/Output

- PCI Express 4.0 (2011) : 31.5 GB/s (16 lanes)
- PCI Express 5.0 (2017) : 63 GB/s (16 lanes)
- PCI Express 6.0 (2019) : 128 GB/s (16 lanes)
- PCI Express 7.0 (2022) : 242 GB/s (16 lanes)

# High Bandwidth Memory

- Xeon Max processors contain 64 GB of HBM
- Bandwidth 800 GB/s

# Some numbers

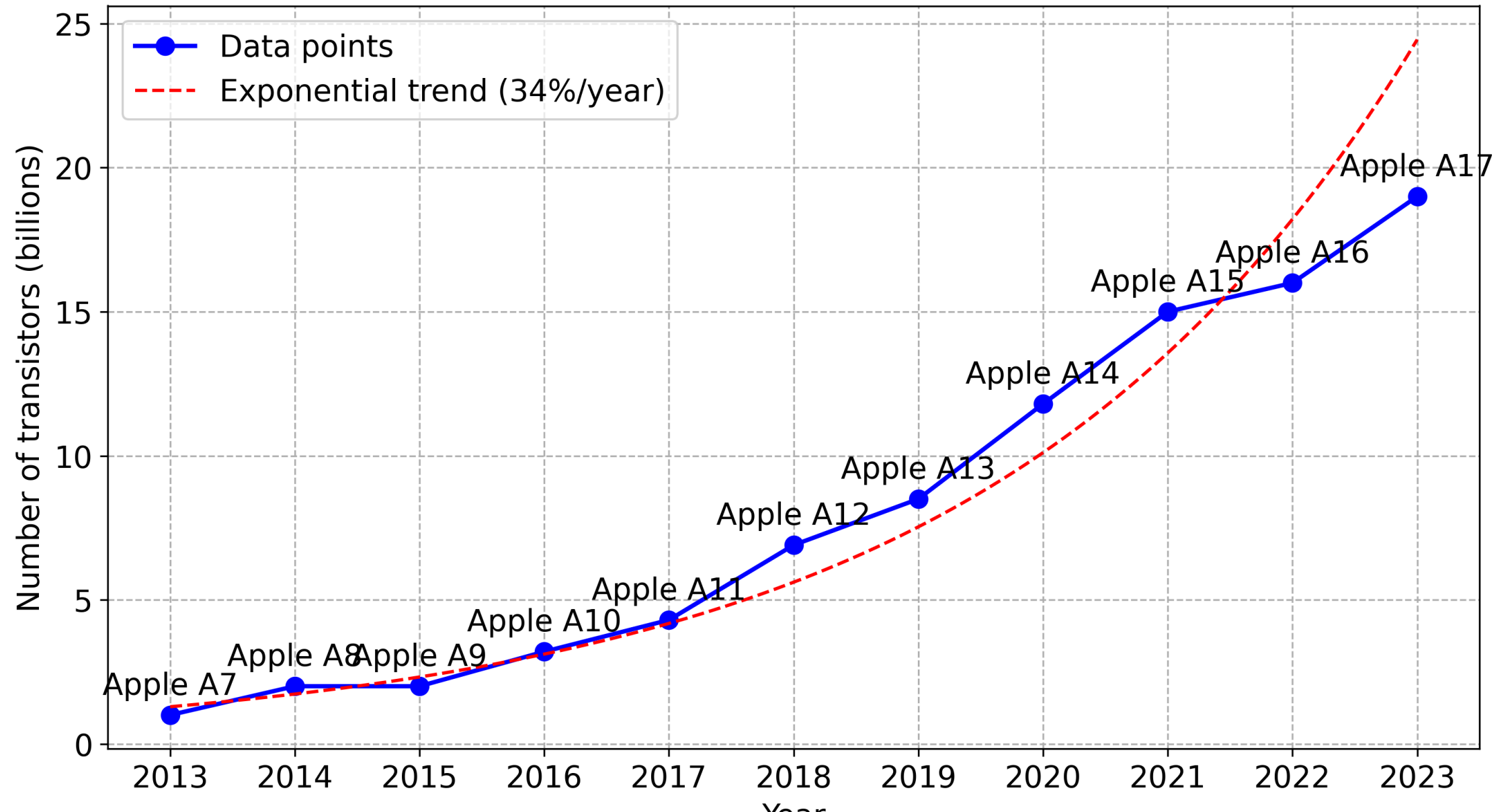
- Time is discrete: clock cycle
- Processors: 4 GHz ( $4 \times 10^9$  cycles per second)
- One cycle is 0.25 nanoseconds
- light: 7.5 centimeters
- One byte per cycle: 4 GB/s

**Easily CPU bound**

# Frequencies and transistors

processor	year	frequency	transistors
Pentium 4	2000	3.8 GHz	0.040 billions
Intel Haswell	2013	4.4 GHz	1.4 billions
Apple M1	2020	3.2 GHz	16 billions
Apple M2	2022	3.49 GHz	20 billions
Apple M3	2024	4.05 GHz	25 billions
Apple M4	2024	4.5 GHz	28 billions
AMD Zen 5	2024	5.7 GHz	50 billions

Year vs number of transistors



# Where do the transistors go?

- More cores
- More superscalar execution
- Better speculative execution
- More cache, more memory-level parallelism
- Better data-level parallelism (SIMD)



# Where do the transistors go?

- More cores
- More superscalar execution (more instructions per cycle)
- Better speculative execution (→ more instructions per cycle)
- More cache, more memory-level parallelism (→ more instructions per cycle)
- Better data-level parallelism (SIMD) (→ fewer instructions)

# Superscalar execution

processor	year	arithmetic logic units	SIMD units
Pentium 4	2000	2	$2 \times 128$
AMD Zen 2	2019	4	$2 \times 256$
Apple M*	2019	6+	$4 \times 128$
Intel Lion Cove	2024	6	$4 \times 256$
AMD Zen 5	2024	6	$4 \times 512$

Moving to up to 4 load/store per cycle

# Parsing a number

- `1.3321321e-12` to `double`

```
double result;  
fast_float::from_chars(  
    input.data(), input.data() + input.size(), result);
```

*Reference:* Number Parsing at a Gigabyte per Second, Software: Practice and Experience  
51 (8), 2021

## Parsing a number

processor	instructions	instructions/cycle	cycles
Apple M4	211	7.5	25
Intel Ice Lake	191	5	39

# Lemire's Rule 1

Modern processors execute *nearly* as many instructions per cycle as you can supply.

- with caveats: branching, memory, and input/output

# Lemire's Corrolary 1

In computational workloads (batches), minimizing instruction count is critical for achieving optimal performance.

## Lemire's Tips

1. Batch your work in larger units to save instructions.
2. Simplify the processing down to as few instructions as possible.

# Going back to number parsing

- Our number parser is everywhere: major browsers (Safari, Chrome), GCC (12+), C#, Rust
- About  $4\times$  faster than the conventional alternatives.
- How did we do it?



We massively reduced the number of CPU instructions required.

function	instructions
strtod	$> 1000$
our parser	$\approx 200$

*Reference:*

Number Parsing at a Gigabyte per Second, Software: Practice and Experience 51 (8), 2021

# SWAR

- Stands for SIMD within a register
- Use normal instructions, portable (in C, C++,...)
- A 64-bit registers can be viewed as 8 bytes
- Requires some cleverness

## Check whether we have a digit

In ASCII/UTF-8, the digits 0, 1, ..., 9 have values 0x30, 0x31, ..., 0x39.

To recognize a digit:

- The high nibble should be 3.
- The high nibble should remain 3 if we add 6 (0x39 + 0x6 is 0x3f)

## Check whether we have 8 consecutive digits

(You are not supposed to understand this:)

```
bool is_made_of_eight_digits_fast(const char *chars) {  
    uint64_t val;  
    memcpy(&val, chars, 8);  
    return (((val & 0xF0F0F0F0F0F0F0F0) |  
            (((val + 0x0606060606060606) & 0xF0F0F0F0F0F0F0F0) >> 4))  
            == 0x3333333333333333);  
}
```

(Works with ASCII, harder if input is UTF-16 as in Java/C#)

# Batching (unrolling)

6 to 7 instructions per multiplication

```
uint64_t sum = 0;
for (size_t i = 0; i < length; i++)
    sum += (uint64_t)x[i] * y[i];
```

3 to 5 instructions per mutiplication

```
uint64_t sum = 0;
for (; i < length - 3; i += 4)
    sum += (uint64_t)x[i] * y[i]
           + (uint64_t)x[i + 1] * y[i + 1]
           + (uint64_t)x[i + 2] * y[i + 2]
           + (uint64_t)x[i + 3] * y[i + 3];
```

# Results

processor	instructions	instructions/cycle	cycles
Apple M4	6	5.2	1.2
	3.5	3.4	1.0
Intel Ice Lake	7	4.4	1.6
	5	4.5	1.1

With unrolling, you can get close to 1 product+store per cycle

# Knuth's random shuffle

```
for (size_t j = array.size() - 1; j > 0; --j) {  
    size_t k = random_bounded(j + 1);  
    std::swap(array[j], array[k]);  
}
```

# Batched random shuffle

- Draw one random number
- Compute two indices (with high proba)
- Reduces the instruction count
- Reduces the number of branches

*Reference:* Batched Ranged Random Integer Generation, Software: Practice and Experience 55 (1), 2025



## Results (Apple M4)

Use a large array of 64-bit keys (8 MB).

technique	instructions	instructions/cycle	cycles
Standard	20	3.8	5.2
Batched (2)	15	4.8	3.1

# Branching

Hard-to-predict branches can derail performance

# Unicode (UTF-16)

- Code points from U+0000 to U+FFFF, a single 16-bit value.
- Beyond: a surrogate pair [U+D800 to U+DBFF] followed U+DC00 to U+DFFF

# Validate

- Check whether we have a lone code unit ( $x \leq 0xD7FF \vee x \geq 0xDBFF$ ), if so ok
- Check whether we have the first part of the surrogate ( $0xD800 \leq x \leq 0xDBFF$ ) and if so check that we have the second part of a surrogate

# Validate

```
size_t i = 0;
for (i < code_units.size()) {
    uint16_t unit = code_units[i];
    if (unit <= 0xD7FF || unit >= 0xE000) { ++i; continue; }
    if (unit >= 0xD800 && unit <= 0xDBFF) {
        if (i + 1 >= code_units.size()) { return false; }
        uint16_t next_unit = code_units[i + 1];
        if (next_unit < 0xDC00 || next_unit > 0xDFFF) { return false; }
        i += 2; // Valid surrogate pair
        continue;
    }
    return false;
}
```

## Performance results (Apple M4)

input type	cycles	instructions	instructions/cycle
ASCII	1	7	7
Alternate	1	8	8

1 character per second might be just 4 GB/s (slower than disk)

## Performance results (Apple M4)

input type	cycles	instructions	instructions/cycle
ASCII	1	7	7
Alternate	1	8	8
Random	7	8	1.1

We are now barely at 1 GB/s!

# Speculative execution

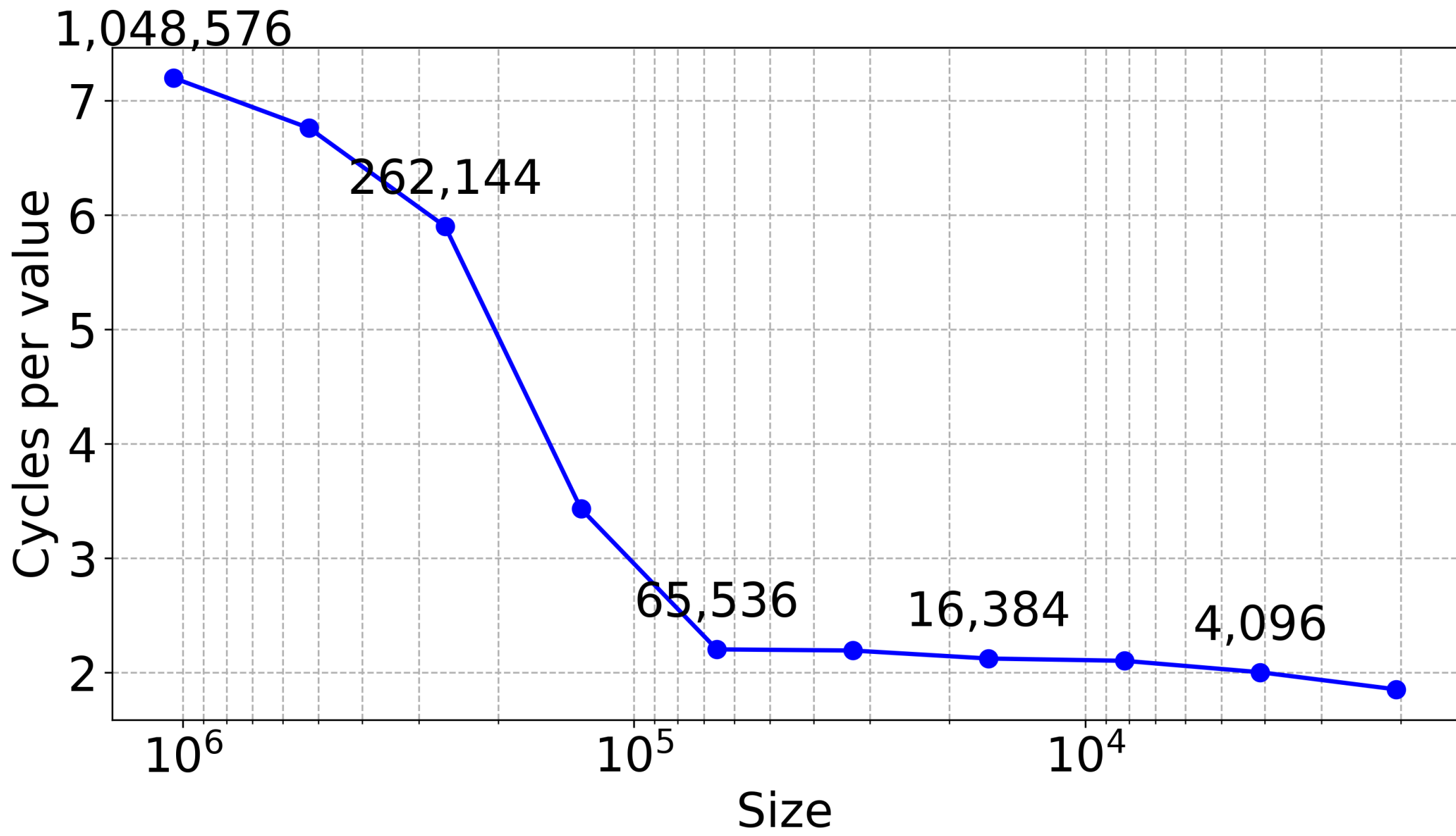
- Processors *predict* branches
- They execute code *speculatively* (can be wrong!)



**How much can your processor learn?**

# How much can your processor learn?

size	ns/value	GHz	cycles/value	instr/value	i/c
1048576	1.59	4.51	7.20	8.01	1.11
524288	1.50	4.51	6.76	8.01	1.19
262144	1.31	4.51	5.90	8.01	1.36
131072	0.76	4.52	3.43	8.01	2.34
65536	0.49	4.52	2.20	8.01	3.64
32768	0.49	4.52	2.19	8.02	3.66



# Finite state machine to the rescue

- Can identify characters by the most significant 8 bits.
- Trivial finite state machine: default, has just encountered a high surrogate, or error.

```

static uint8_t transition_table[3][256] = {
    {...},
    {...},
    {...}
};

bool is_valid_utf16_ff(std::span<uint16_t> code_units) {
    uint8_t state = 0; // Start in Initial state
    for (auto code_unit : code_units) {
        uint8_t high_byte = code_unit >> 8;
        state = transition_table[state][high_byte];
    }
    return state == 0; // Valid only if we end in Initial state
}

```

## Performance results (Apple M4)

input type	cycles	instructions	instructions/cycle
branchy	7	8	1.1
finite-state	1.1	7	6.4

The finite-state approach can be  $7\times$  faster!

# Rules of thumb

1. Processors can 'learn' thousands of branches: benchmark over massive inputs.
2. Pick a solution without branches when it provides the same performance.

A modern processor like the Apple M4 can learn to predict nearly perfectly 10,000 random (0/1) branches.

<b>entries</b>	<b>% branch misses</b>
4096	0.2
8192	0.4
16384	4.4
32768	33.5
65536	41.7
524288	48.2



# Pipelining

How does the processor manage to validate one UTF-16 character per cycle when it takes **many cycles** just to *load* the character?

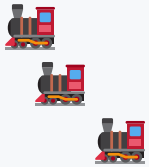
# Cycle 1



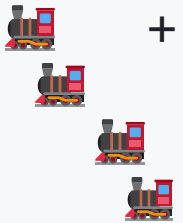
## Cycle 2



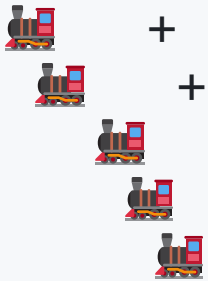
## Cycle 3



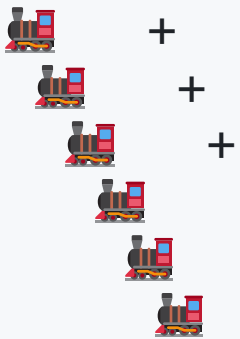
# Cycle 4



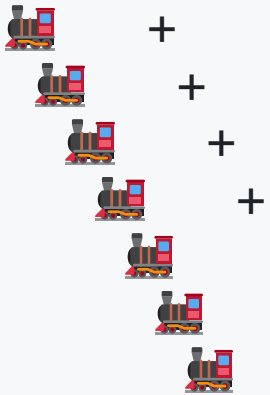
# Cycle 5



# Cycle 6



# Cycle 7





# Little's Law

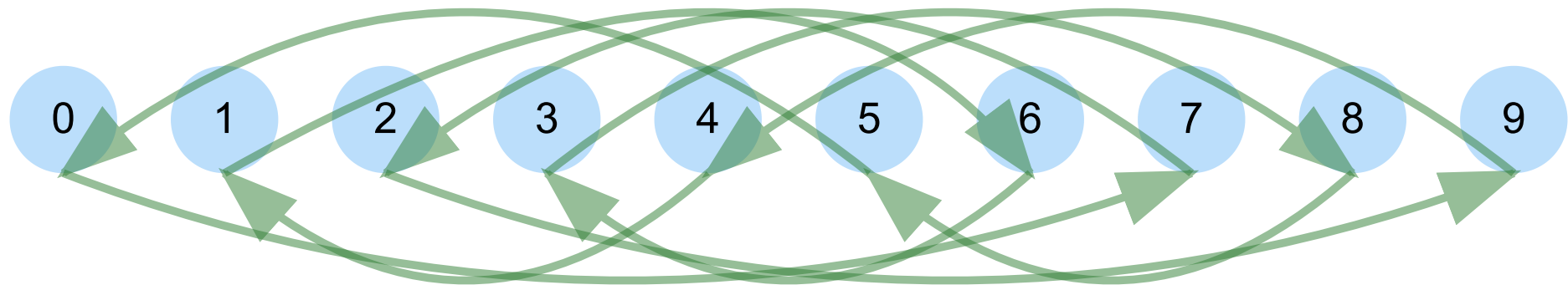
- Latency harms throughput
- Parallelism hides latency

$$\text{throughput} = \frac{\text{parallelism}}{\text{latency}}$$

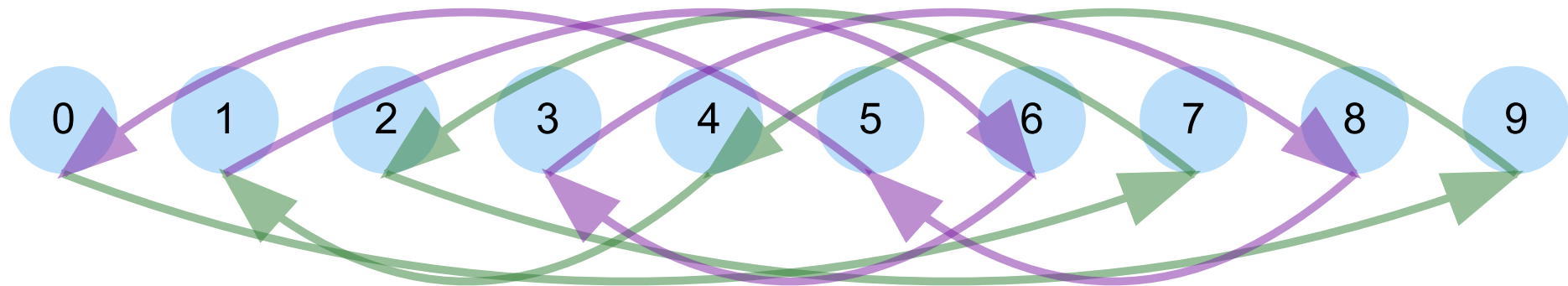
# Memory-level parallelism

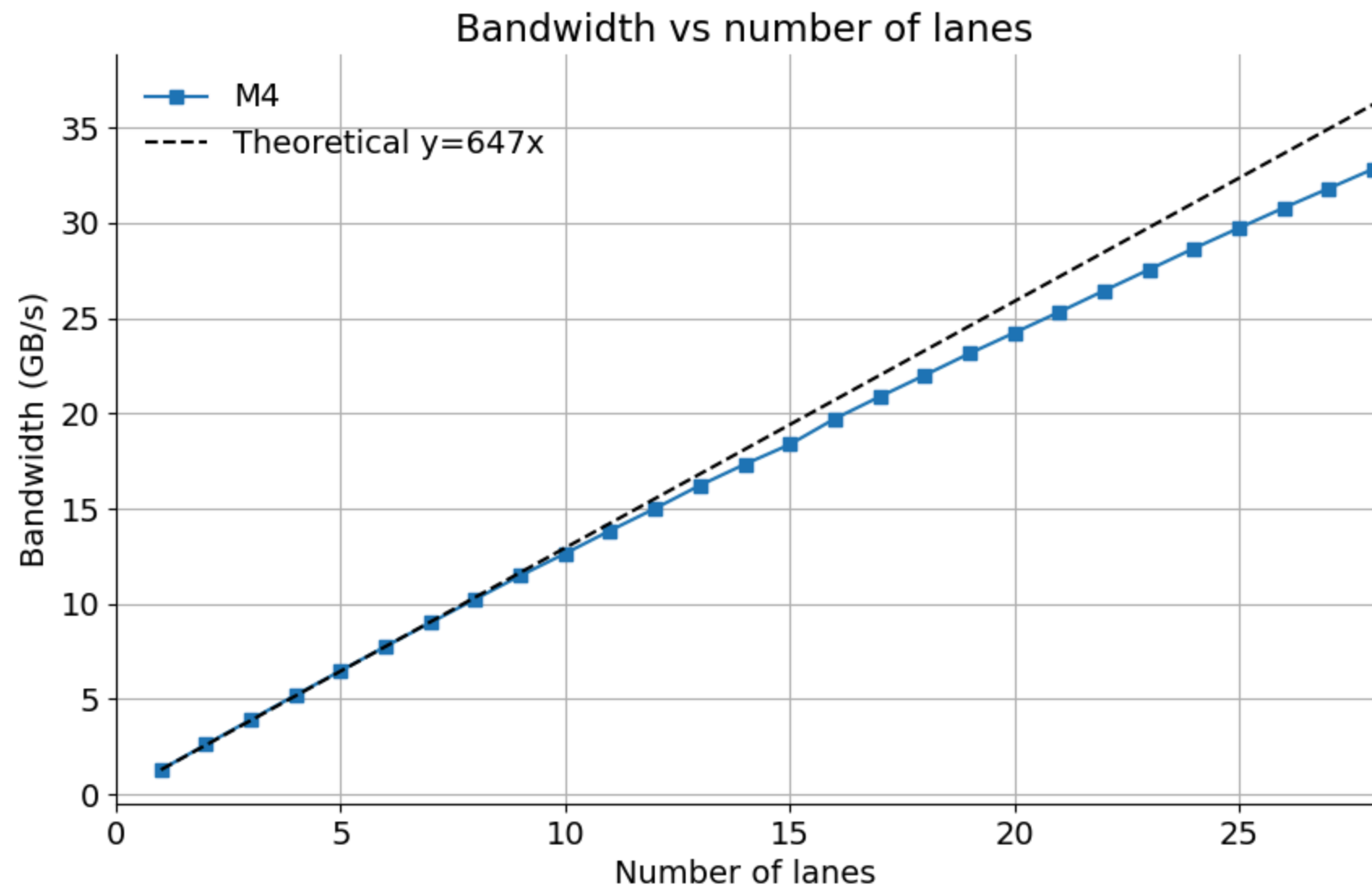
- Create large array of indices forming a cycle
- Start with [0,1,2,3,4]
- Shuffle so that no index can remain in place.
- Start with [4,0,3,2,1]
- Sandra Sattolo's algorithm
- This forms a random path

1 lane



# 2 lanes





# Consequence

An algorithm that hits 2 or 3 memory areas instead of just 1 is not necessarily 2 or 3 times slower! Might be just as fast!

# Bloom filter

8 hash functions

	not in set	in set
cache misses	3.5	7.5

(Intel Ice Lake processor, out-of-cache filter)

**Less than half the cache misses**

# Bloom filter

8 hash functions

	not in set	in set
cache misses	3.5	7.5
cycles	135	170

(Intel Ice Lake processor, out-of-cache filter)

**Only a 25% difference in speed**



# Data-level parallelism



# SIMD

- Stands for Single instruction, multiple data
- Allows us to process 16 (or more) bytes or more with one instruction
- Supported on all modern CPUs (phone, laptop)

# Deltas (C)

successive difference:

```
for (size_t i = 1; i < n; ++i) {  
    dst[i] = src[i] - src[i - 1];  
}
```

prefix sum:

```
for (size_t i = 1; i < n; ++i) {  
    dst[i] = dst[i - 1] + src[i];  
}
```

# Apple M4

algorithm	cycles	instructions	ins/cycle
successive difference	1	6	6
prefix sum	1	5	5

## Now allow SIMD!

algorithm	cycles	instructions	ins/cycle
successive difference	0.25	0.9	3.8
prefix sum	1	5	5

Autovectorization worked for differences, but failed for the prefix sum

**Need to learn SIMD design magic !**

## UTF-16, random (adversarial), Apple M4

input type	cycles	instructions	instructions/cycle
branchy	7	8	1.1
finite-state	1.1	7	6.4
SIMD	0.3	0.4	4.6

- SIMD *correction* function (which copies the data) faster than the non-SIMD validation



## Interested, check these projects

- simdjson: fastest JSON parser in the world <https://simdjson.org>

ClickHouse, Microsoft, Shopify, Intel, Meta Velox, Google Pax, the Node.js runtime,

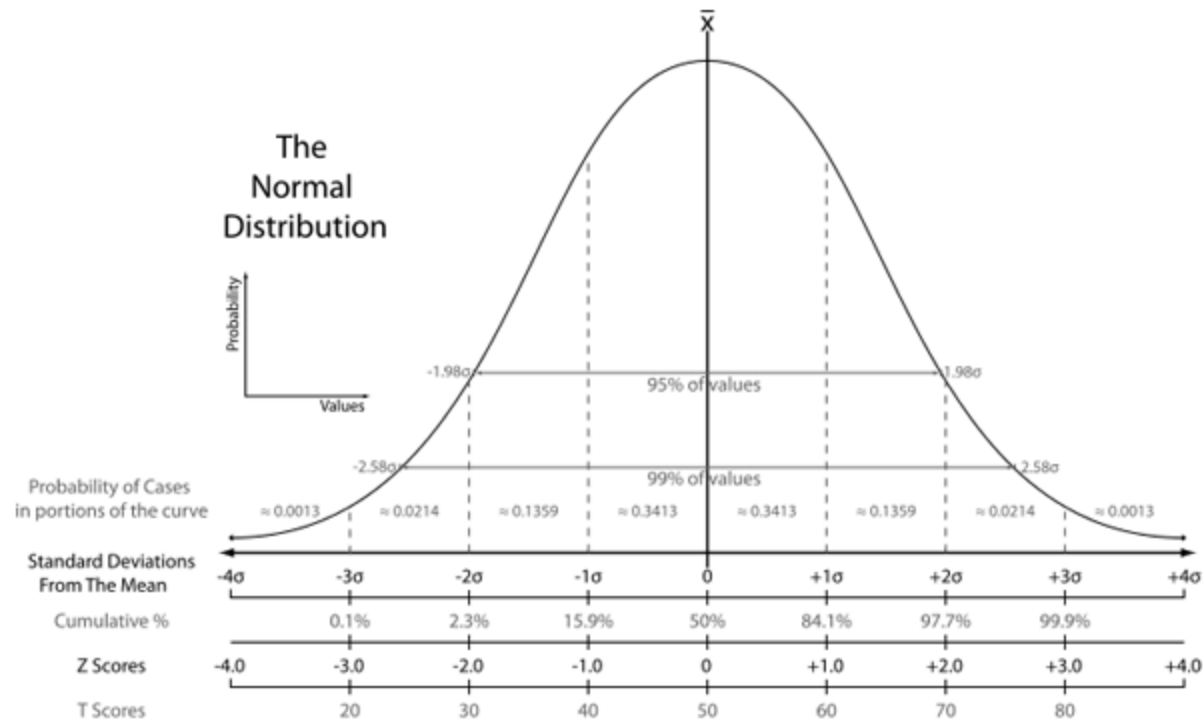
- simdutf: Unicode routines (UTF8, UTF16, UTF32) and Base64  
<https://github.com/simdutf/simdutf>

Node.js, WebKit/Safari, Ladybird, Chromium, Cloudflare Workers and Bun

# Measurements

- We often assume that measurements (timings) are normally distributed.
- It is often an incorrect assumption.

# Sigma events

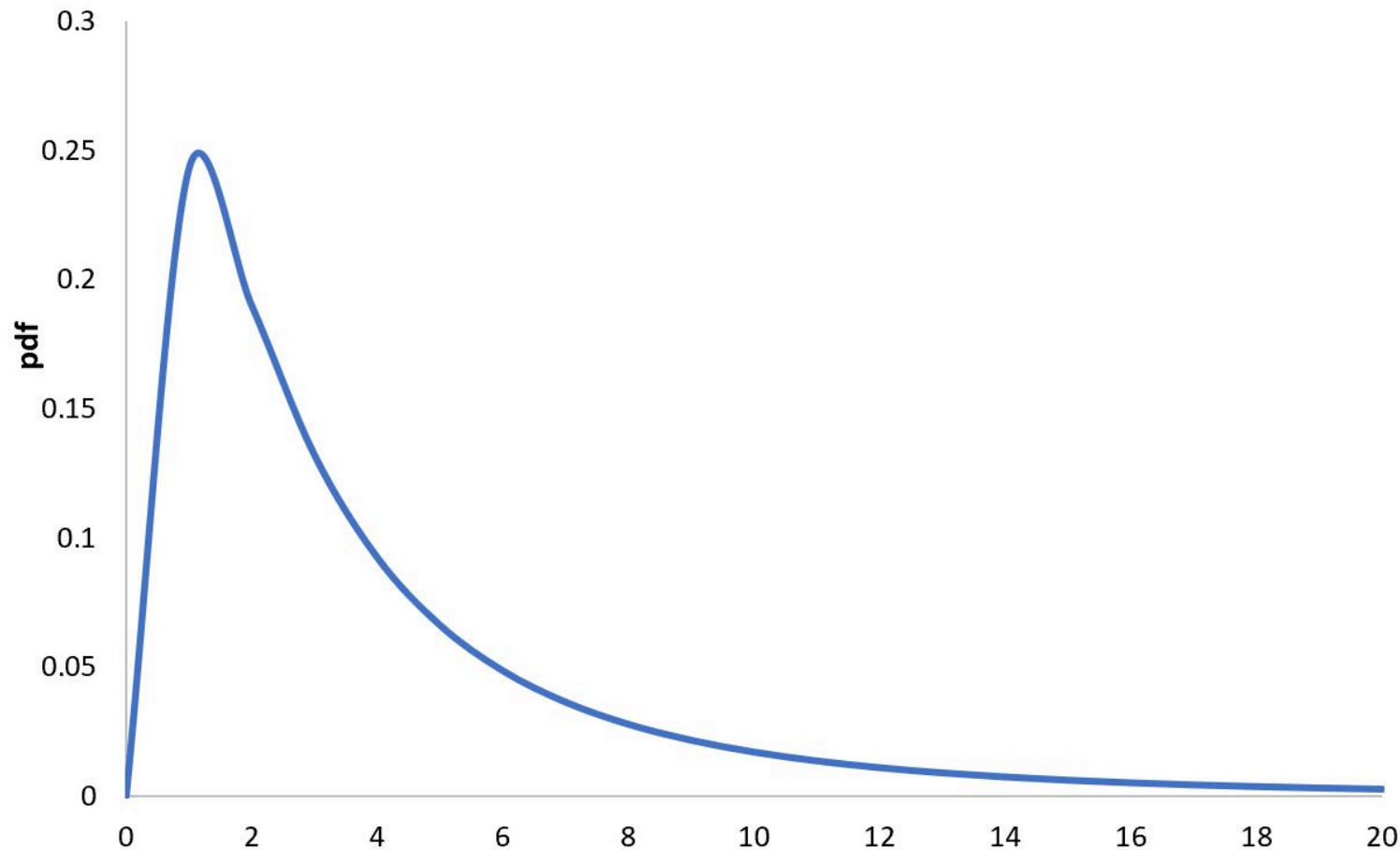


- 1-sigma is 32%
- 2-sigma is 5%
- 3-sigma is 0.3% (once ever 300 trials)
- 4-sigma is 0.00669% (once every 15000 trials)
- 5-sigma is 5.9e-05% (once every 1,700,000 trials)
- 6-sigma is 2e-07% (once every 500,000,000)

$$e^{-n^2/2} / (n * \sqrt{\pi/2}) \times 100 \text{ for } n > 3$$

# What if we dealt with log-normal distributions?

Log-Normal Distribution ( $\mu=1, \sigma=1$ )



# Consequences

- If your measurements are normally distributed, the 'error' falls off as  $1/\sqrt{N}$
- Reality: often does not work at all.

# Consequences

- If your measurements are normally distributed, the 'error' falls off as  $1/\sqrt{N}$
- Reality: often does not work at all.
- If your measurements are normally distributed, the absolute minimum is meaningless.
- Reality: the absolute minimum is a often a reliable metric.

# Conclusion

- Processors are get much better! Wider!
- 'hot spot' engineering can fail, better to reduce overall instruction count.
- Branchy code can do well in synthetic benchmarks, but be careful.