

Pythagorean Identities:

$$\sin^2(\theta) + \cos^2(\theta) = 1$$

$$\sin^2(\theta) = 1 - \cos^2(\theta) \qquad 1 + \tan^2(\theta) = \sec^2(\theta) \qquad 1 + \cot^2(\theta) = \csc^2(\theta)$$

$$\cos^2(\theta) = 1 - \sin^2(\theta)$$

Even/Oddness Symmetry Identities:

$$\sin(-\theta) = -\sin(\theta) \qquad \csc(-\theta) = -\csc(\theta) \qquad [\sin \text{ and } \csc \text{ are odd functions}]$$

$$\cos(-\theta) = \cos(\theta) \qquad \sec(-\theta) = \sec(\theta) \qquad [\cos \text{ and } \sec \text{ are even functions}]$$

$$\tan(-\theta) = -\tan(\theta) \qquad \cot(-\theta) = -\cot(\theta) \qquad [\tan \text{ and } \cot \text{ are odd functions}]$$

Cofunction Relationships:

$$\sin(\theta) = \cos\left(\frac{\pi}{2} - \theta\right) \quad \sec(\theta) = \csc\left(\frac{\pi}{2} - \theta\right) \quad \tan(\theta) = \cot\left(\frac{\pi}{2} - \theta\right)$$

Sum and Difference formulas:

$$\sin(A + B) = \sin(A)\cos(B) + \cos(A)\sin(B)$$

$$\sin(A - B) = \sin(A)\cos(B) - \cos(A)\sin(B)$$

$$\tan(A + B) = \frac{\tan(A) + \tan(B)}{1 - \tan(A)\tan(B)}$$

$$\cos(A + B) = \cos(A)\cos(B) - \sin(A)\sin(B)$$

$$\cos(A - B) = \cos(A)\cos(B) + \sin(A)\sin(B)$$

$$\tan(A - B) = \frac{\tan(A) - \tan(B)}{1 + \tan(A)\tan(B)}$$

Double Angle Formulas:

$$\sin(2\theta) = 2\sin(\theta)\cos(\theta)$$

$$\cos(2\theta) = \cos^2(\theta) - \sin^2(\theta)$$

$$= 1 - 2\sin^2(\theta)$$

$$= 2\cos^2(\theta) - 1$$

$$\tan(2\theta) = \frac{2\tan(\theta)}{1 - \tan^2(\theta)}$$

Half Angle Formulas:

$$\sin^2(\theta) = \frac{1 - \cos(2\theta)}{2} \quad \text{or}$$

$$\sin\left(\frac{\alpha}{2}\right) = \pm \sqrt{\frac{1 - \cos(\alpha)}{2}}$$

$$\cos^2(\theta) = \frac{1 + \cos(2\theta)}{2} \quad \text{or}$$

$$\cos\left(\frac{\alpha}{2}\right) = \pm \sqrt{\frac{1 + \cos(\alpha)}{2}}$$

$$\tan\left(\frac{\alpha}{2}\right) = \pm \sqrt{\frac{1 - \cos(\alpha)}{1 + \cos(\alpha)}} = \frac{\sin(\alpha)}{1 + \cos(\alpha)} = \frac{1 - \cos(\alpha)}{\sin(\alpha)}$$

[In all of the above, (\pm) determined by quad of $\frac{\alpha}{2}$]