

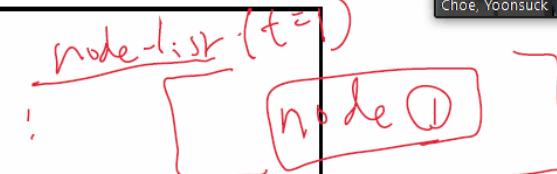
## General Search Algorithm

Pseudo-code:

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```



- node: state, plus book-keeping info (current depth, path to current state. etc.)
- Expand(node): returns Then we turn fail, so that's the one of the the first termination condition set of child nodes

state

node(0)

General Search Algorithm

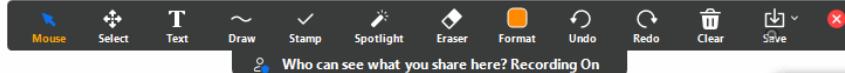
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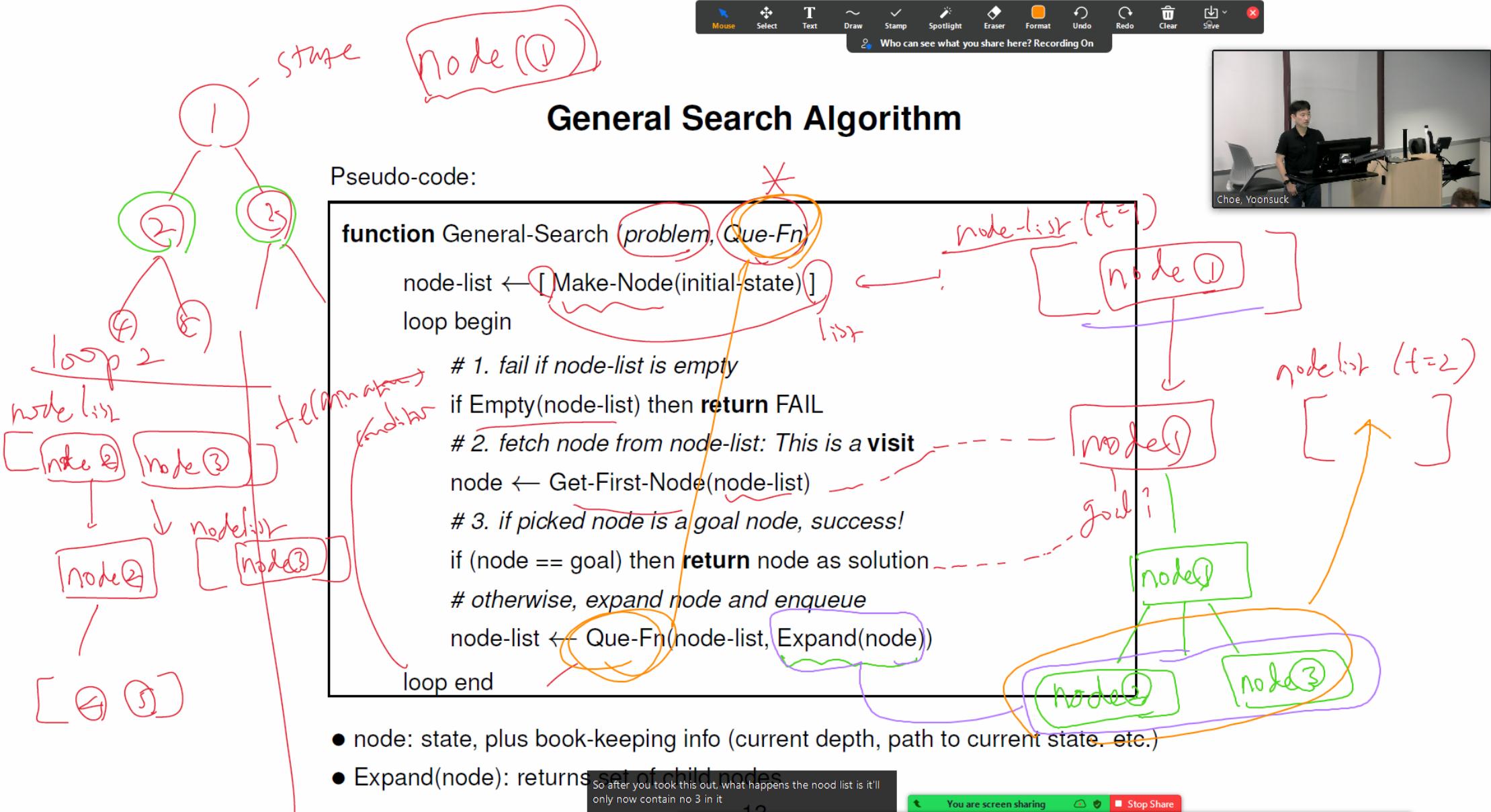
## General Search Algorithm

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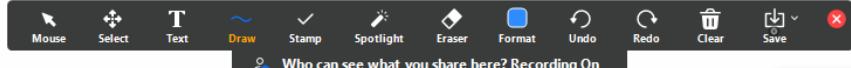
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state  
node(0)

## General Search Algorithm

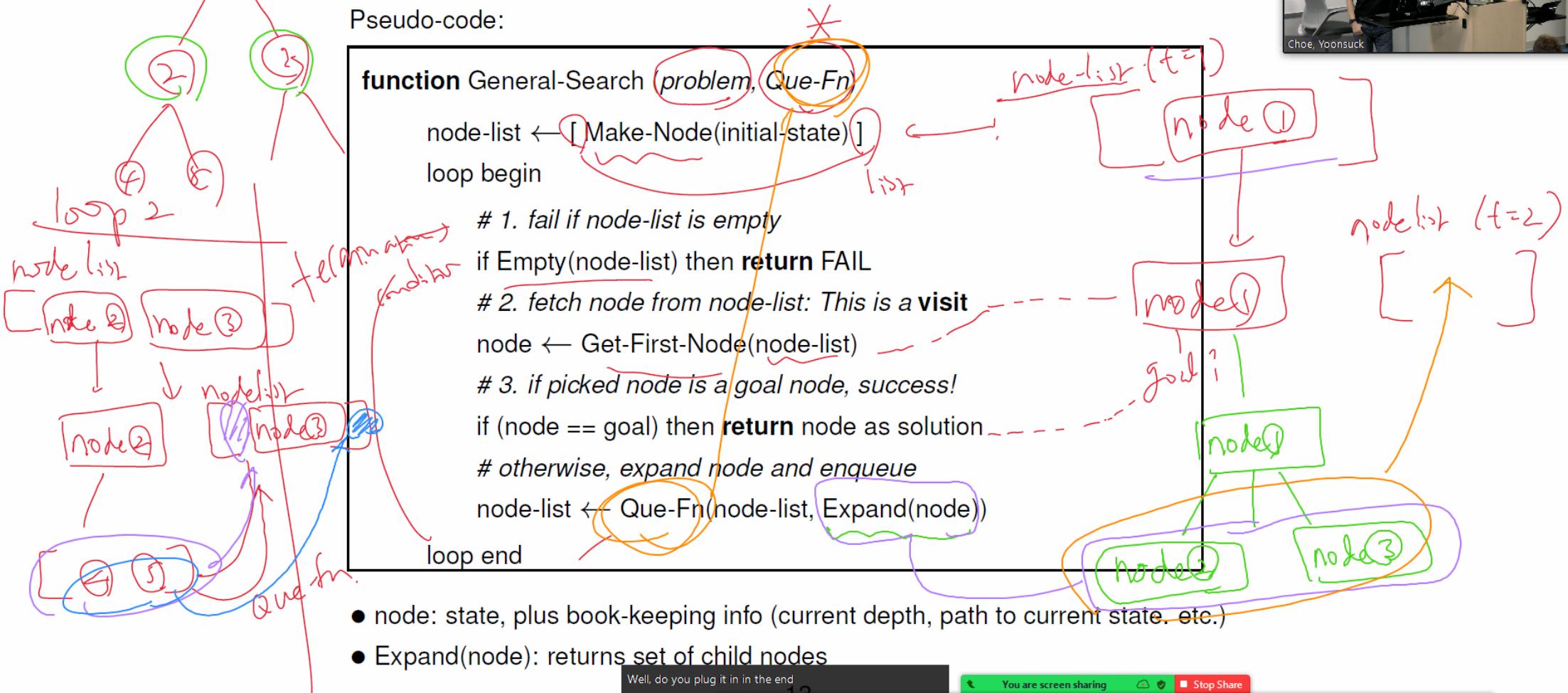


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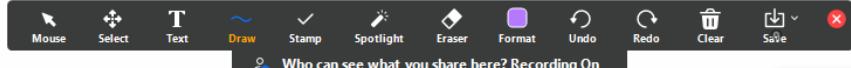
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node(0)

## General Search Algorithm

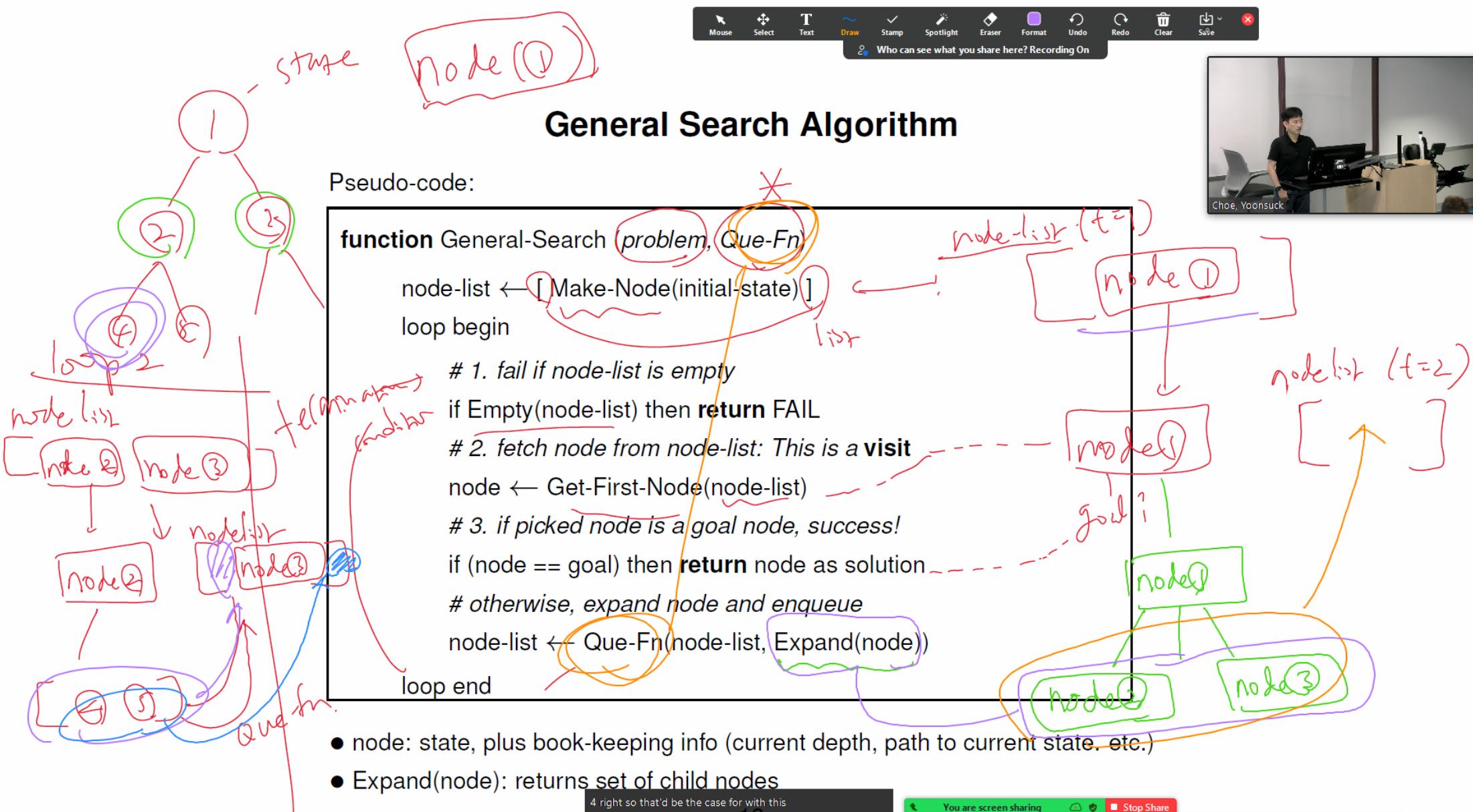


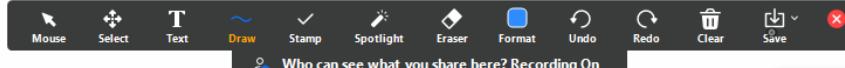
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Who can see what you share here? Recording On



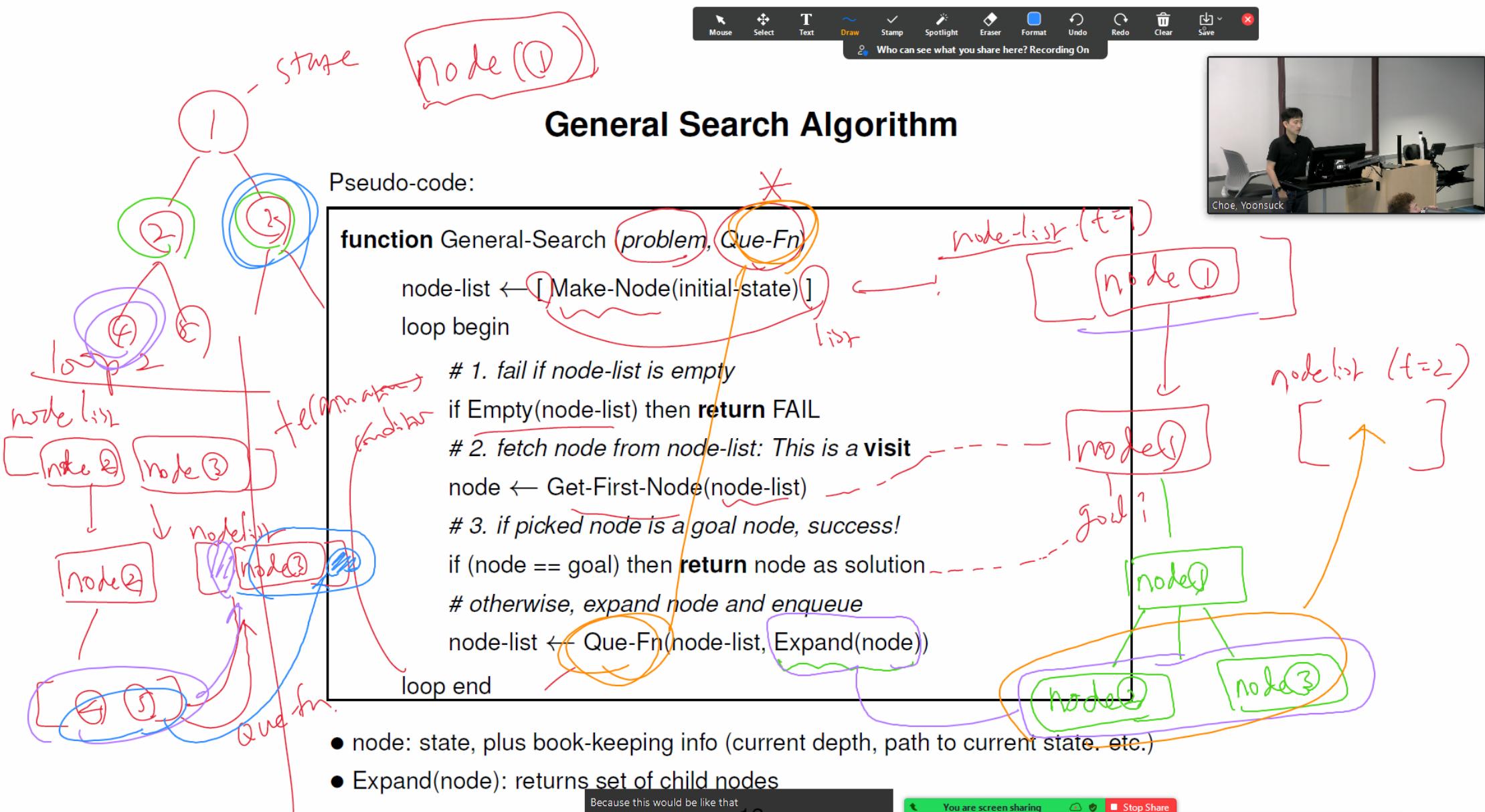
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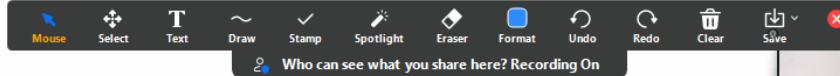
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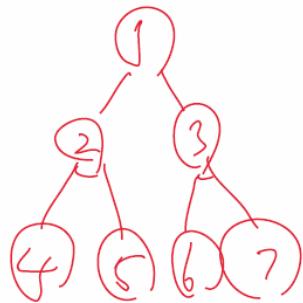
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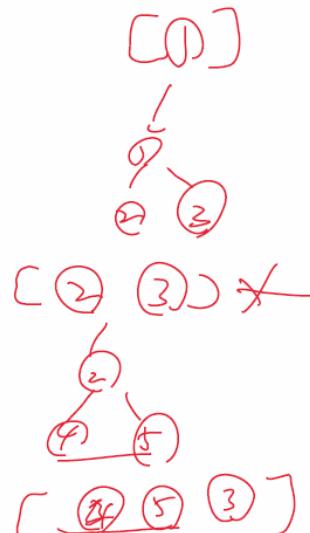
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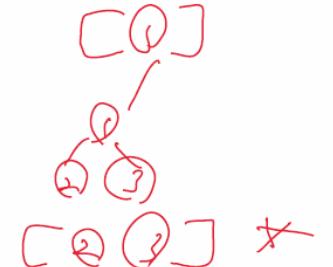
```



*Que-fn : push*



*Que-fn: enqueues as the end*

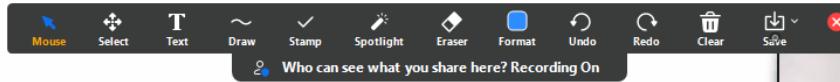


- node: state, plus book-keeping info (current depth, path to current state. etc.)
- Expand(node): returns set of child nodes

Is this empty? So these 2 are the same right

13

You are screen sharing Stop Share



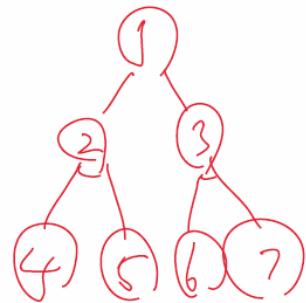
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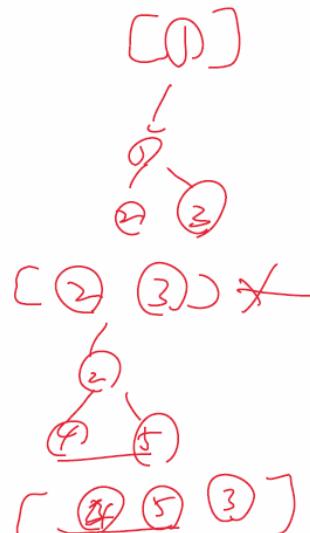
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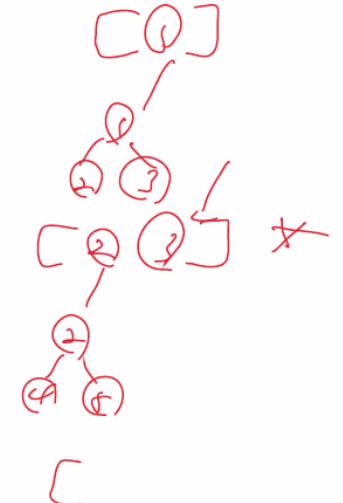
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*Que-fn : push*



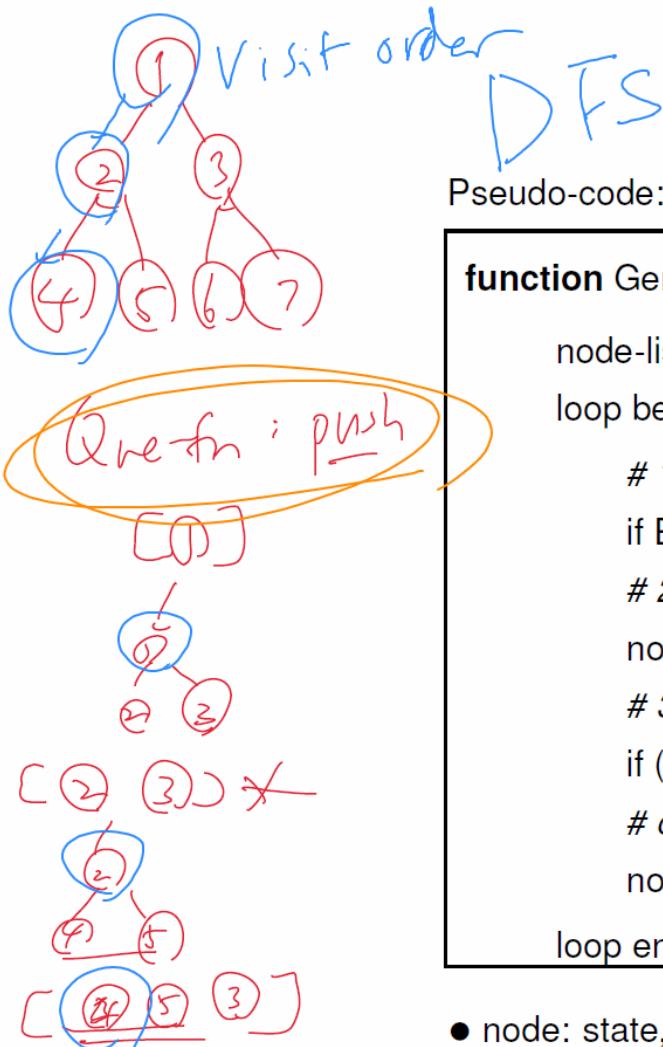
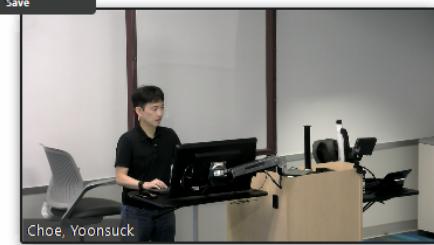
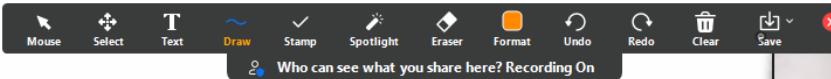
*Que-fn: enque as the end*



- node: state, plus book-keeping info (current depth, path to current state. etc.)
- Expand(node): returns set of child nodes

Then here, now you have to put it in the back

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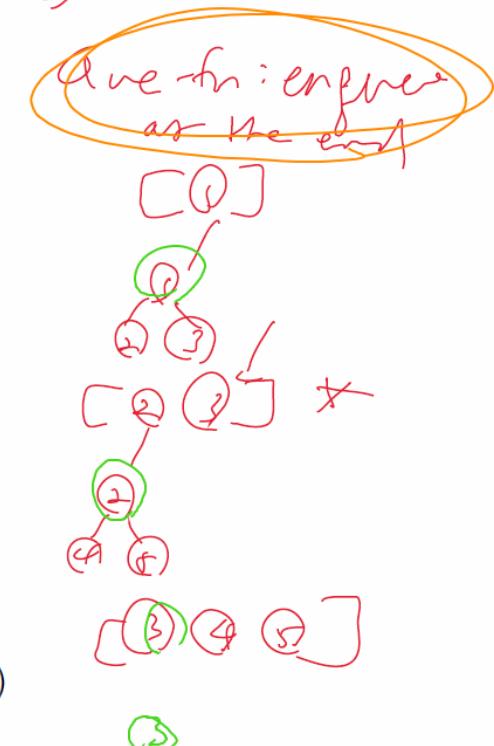
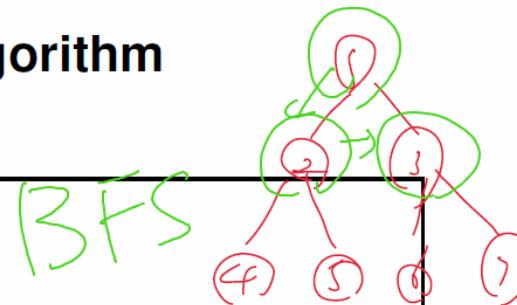


## General Search Algorithm

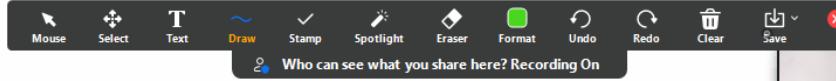
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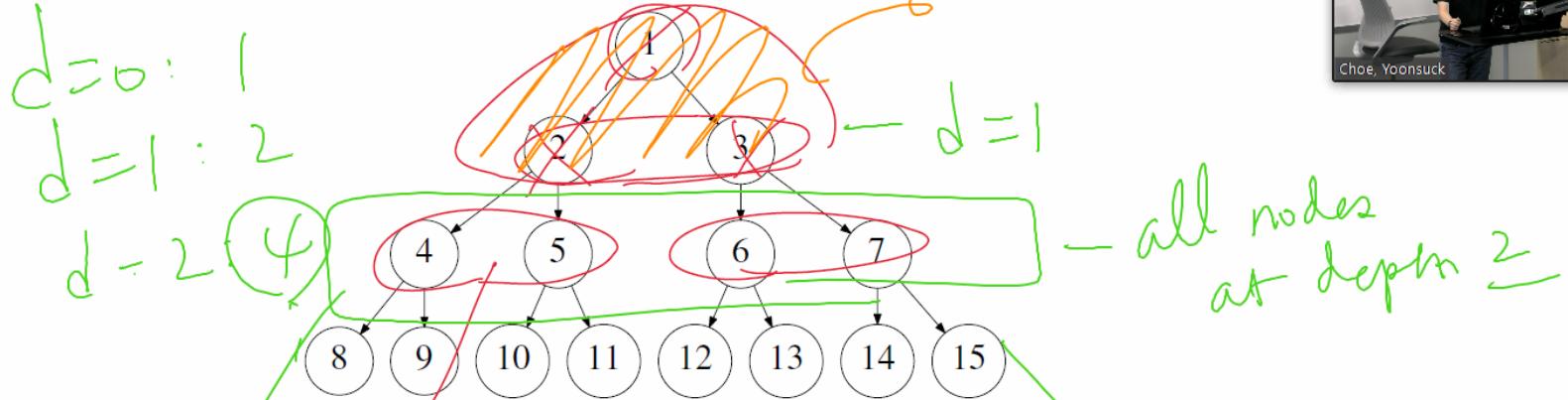
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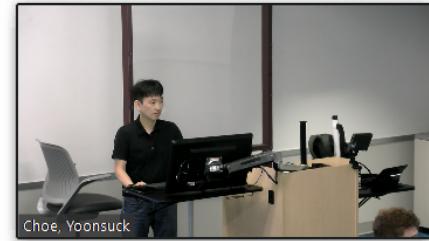
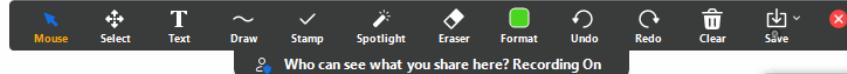


## BFS: Visit Order and Node List



Evolution of the queue (**bold**= expanded and added children):

1.  $[1]$  : initial node list contains the initial state
  2.  $[(2)(3)]$  : visit 1 (dequeued) and enqueue 2 and 3
  3.  $[[3] \mathbf{[4][5]}]$  : visit 2 (dequeued) and enqueue 4 and 5
  4.  $[[4] [5] \mathbf{[6][7]}]$  : visit 3 (dequeued) and enqueue 6 and 7. All depth 2 nodes are in the node list.
  - ...
  8.  $[[8] [9] [10]]$  : visit 7, ..., All depth 3 nodes are in the node list.
- So once you have gone through this steps, you have 2 to them plus one things in your node list. So that's a huge number

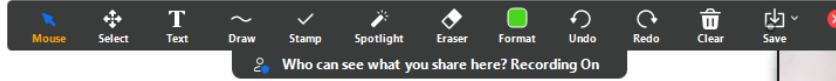


# Search and Game Playing

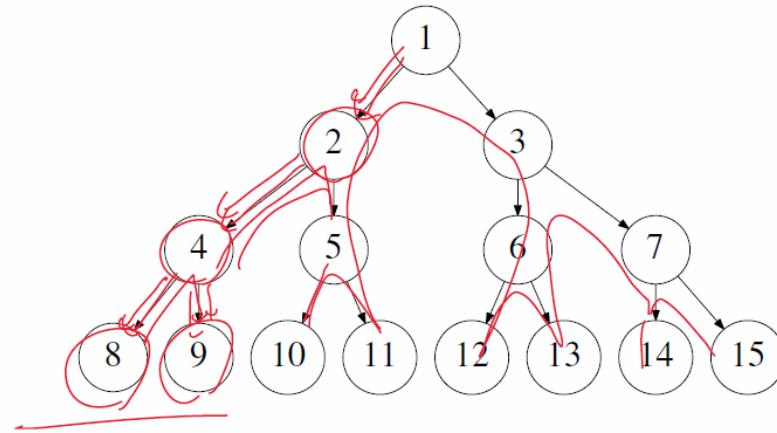
- Uninformed search
- Informed search *← where AI gets involved-*
- Iterative improvement, Constraint satisfaction
- Game playing

So again, this is where AI, hey? I gets involved

You are screen sharing Stop Share

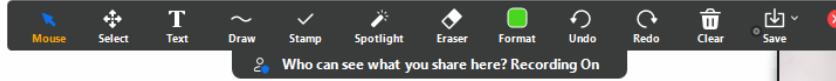


## Depth First Search

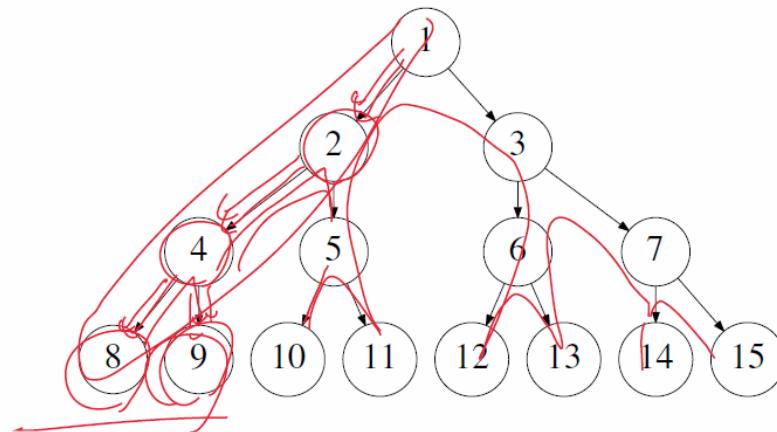


- node visit order (fetch/goal-test): 1 2 4 8 9 5 10 11 3 6 12 13 7 14  
15
- queuing function: enqueue at left (stack push; add expanded nodes at the beginning of the list)

And it will basically go like that



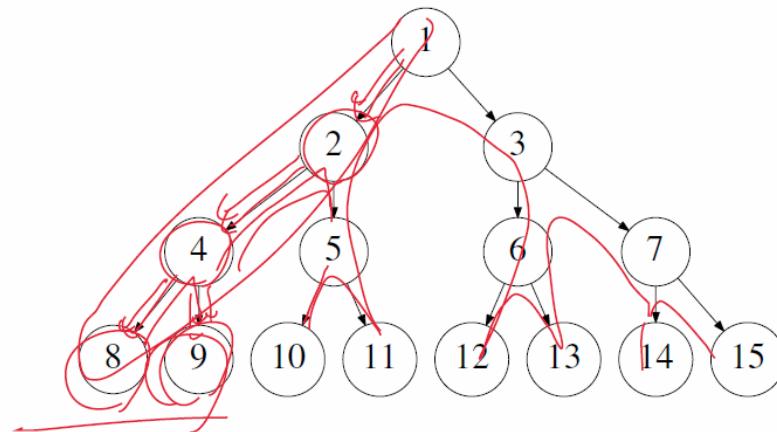
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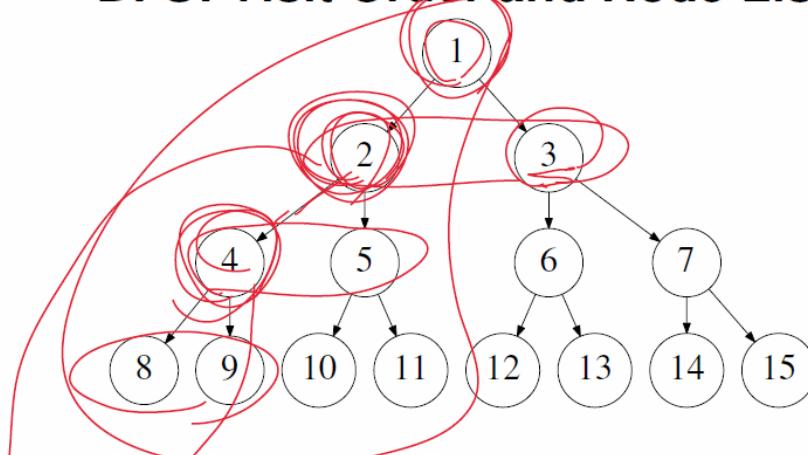
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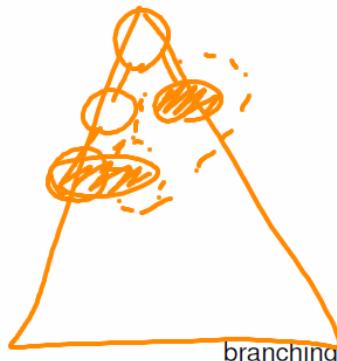
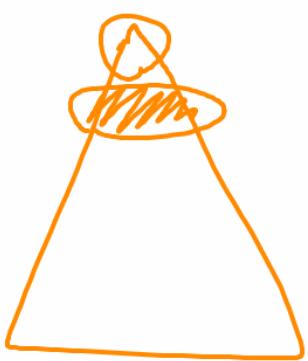
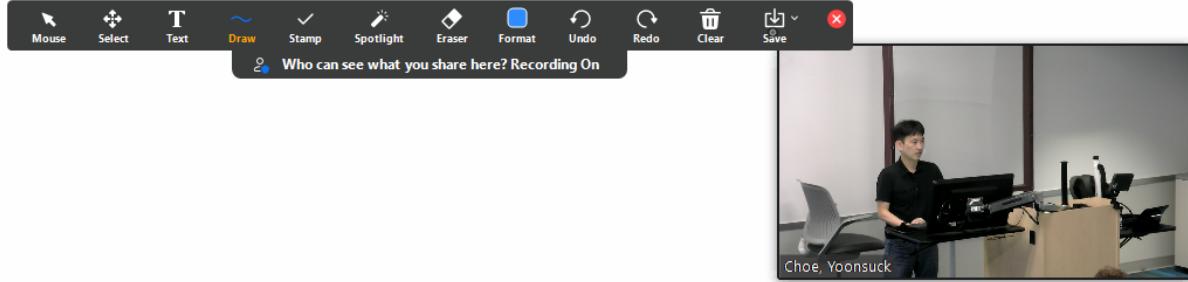
## DFS: Visit Order and Node List



Evolution of the queue (**bold**=expanded and added children):

1. **[1]** : initial node list contains the initial state
  2. **[2][3]** : visit (pop) 1 and push expanded nodes in the front
  3. **[4][5][3]** : visit (pop) 2 and push expanded nodes in the front
  4. **[8][9][5][3]** : visit (pop) 4 and push expanded nodes in the front
- ...

So this 3 that was pushed into the list pretty early on,  
would keep on remaining in it until all of the Friends here  
have been external

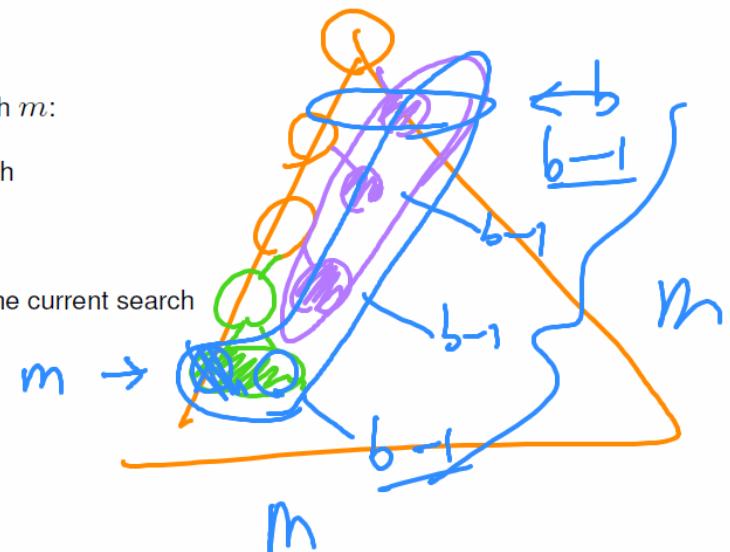
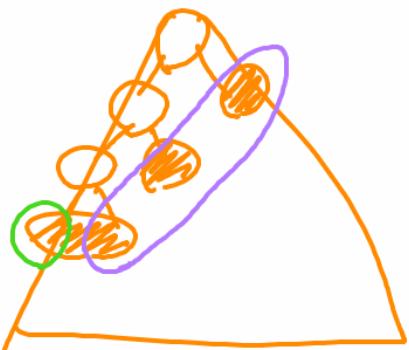


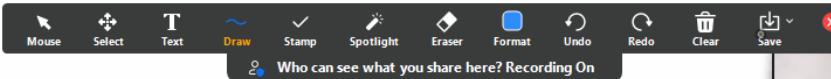
## DFS: Evaluation

branching factor  $b$ , depth of solutions  $d$ , max depth  $m$ :

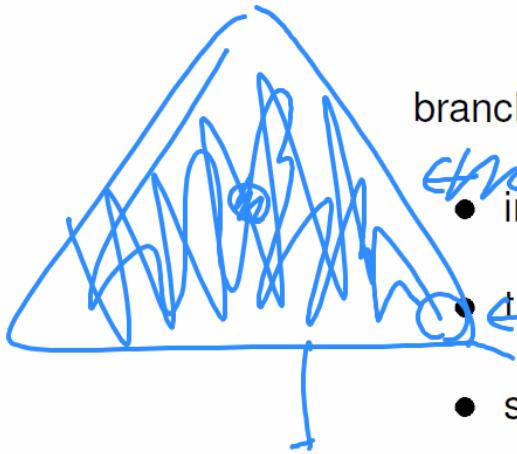
- incomplete: may wander down the wrong path
- time:  $O(b^m)$  nodes visited (worst case)
- space:  $O(bm)$  (dangling nodes just along the current search path)
- good when there are many shallow goals
- bad for deep or infinite depth state space

$$O(b^{d+1})$$





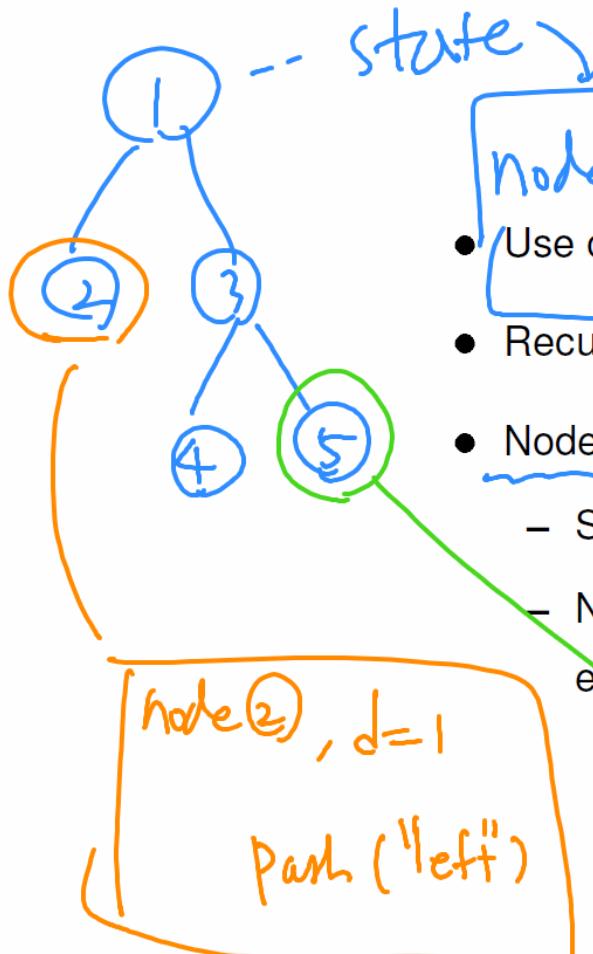
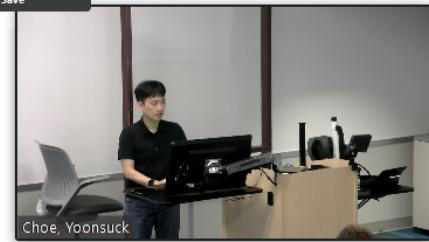
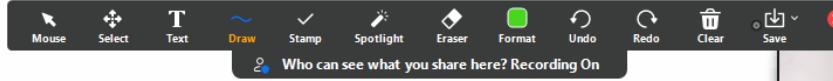
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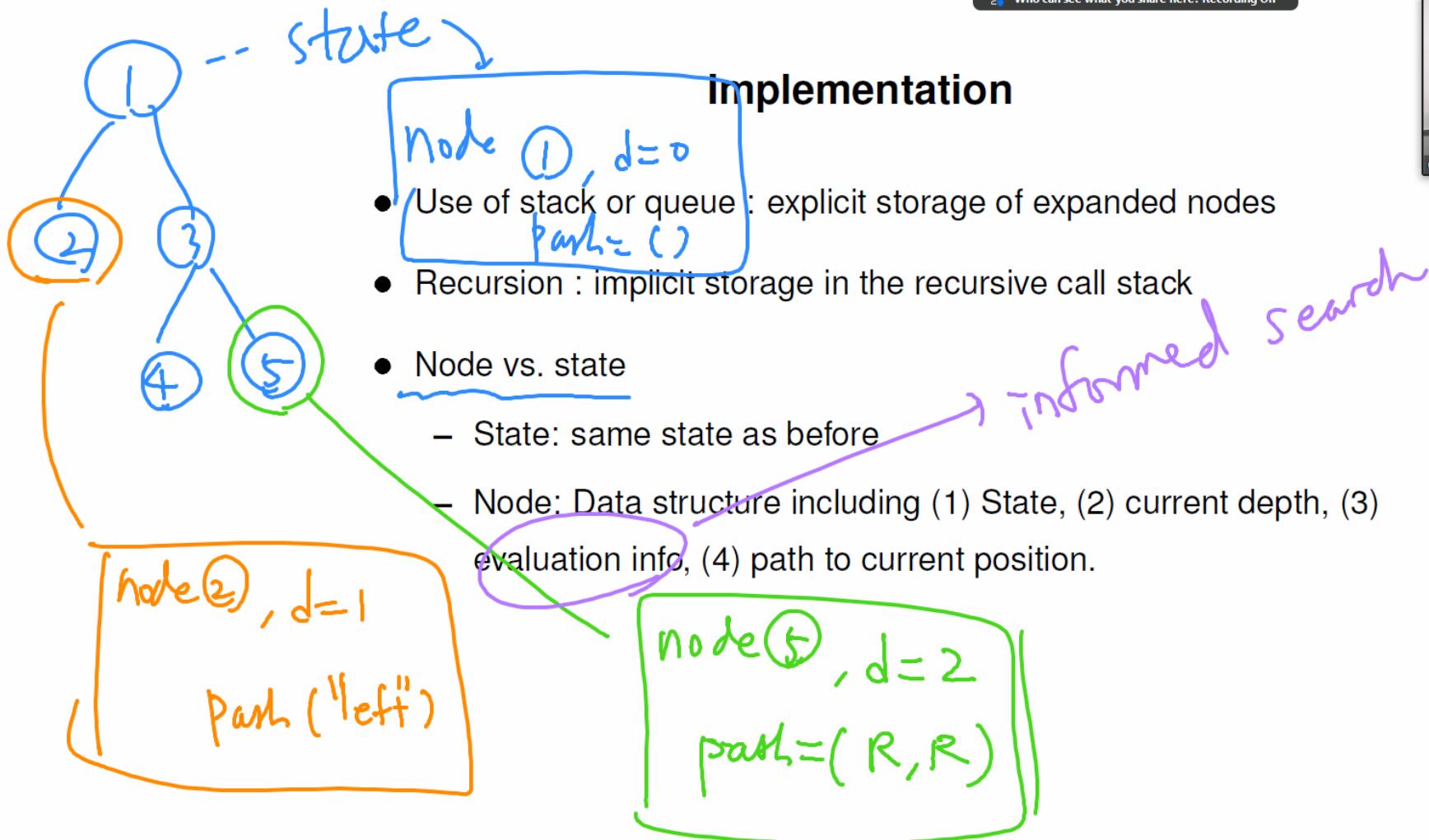
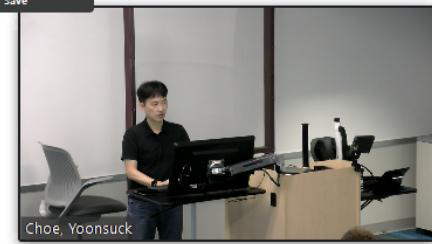
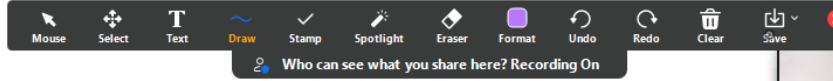
So it's good when there are many shallow goals but that  
for deep or very, very deep or infinite

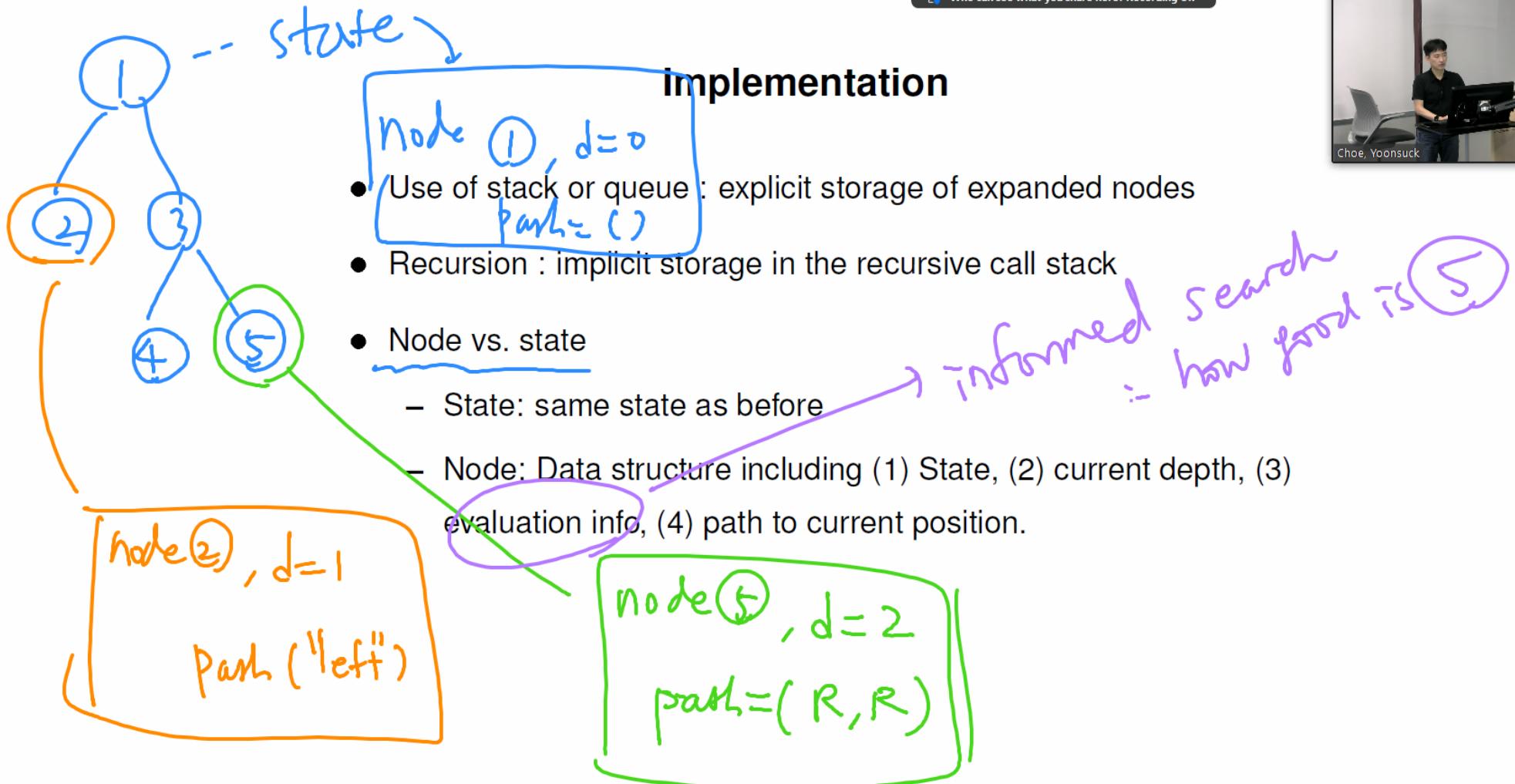
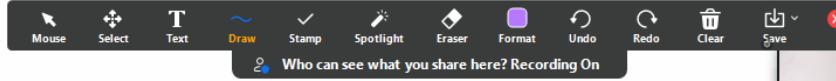


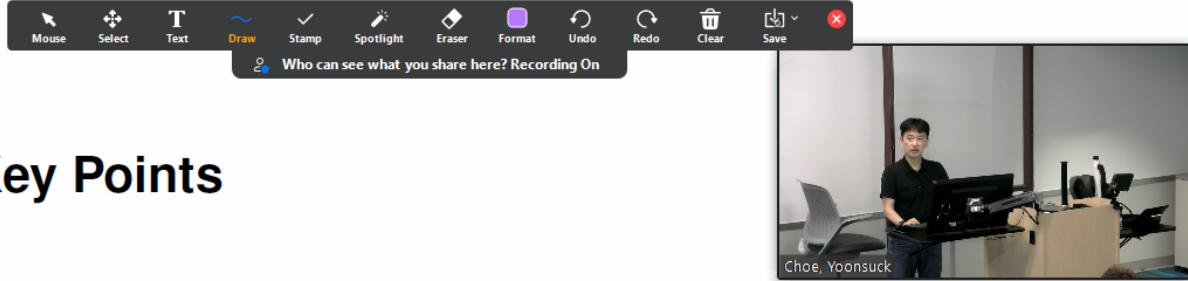
## implementation

- Node ①,  $d=0$   
path = ()
- Use of stack or queue : explicit storage of expanded nodes
- Recursion : implicit storage in the recursive call stack
- Node vs. state
  - State: same state as before
  - Node: Data structure including (1) State, (2) current depth, (3) evaluation info, (4) path to current position.

node ⑤,  $d=2$   
path = (R, R)



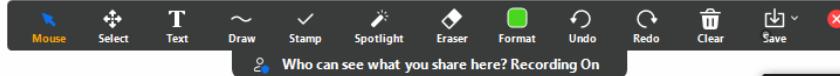




## Key Points

- Description of a search problem: initial state, goals, operators, etc.
- Considerations in designing a representation for a state
- Evaluation criteria — *Space, time, completeness, optimality*
- BFS, UCS, DFS: time and space complexity, completeness
- Differences and similarities between BFS and UCS
- When to use one vs. another
- Node visit orders for each strategy
- Tracking the stack or queue at any moment

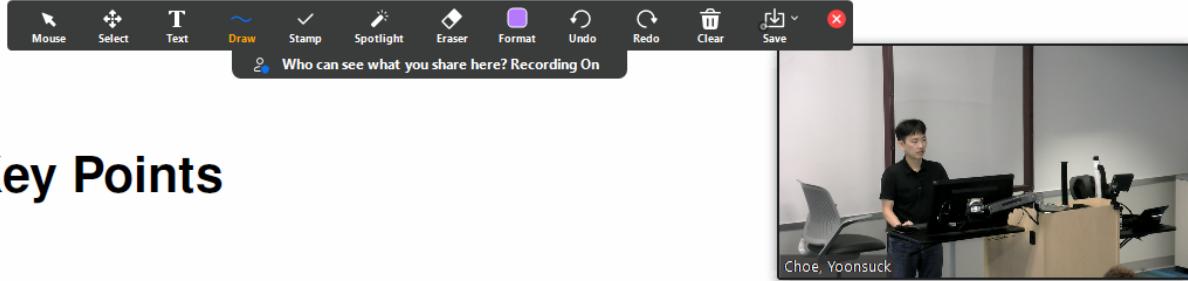
There is, and then optimality, would you find the shortest path to the



# Search and Game Playing

- Uninformed search
  - Informed search
  - Iterative improvement, Constraint satisfaction
  - Game playing
- where AI gets involved*

You can consider that as an extension of search so we'll look at that

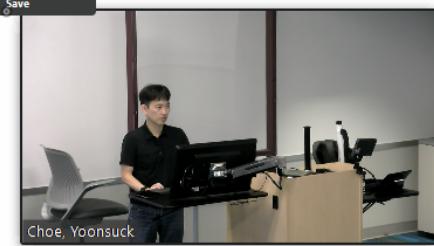


## Key Points

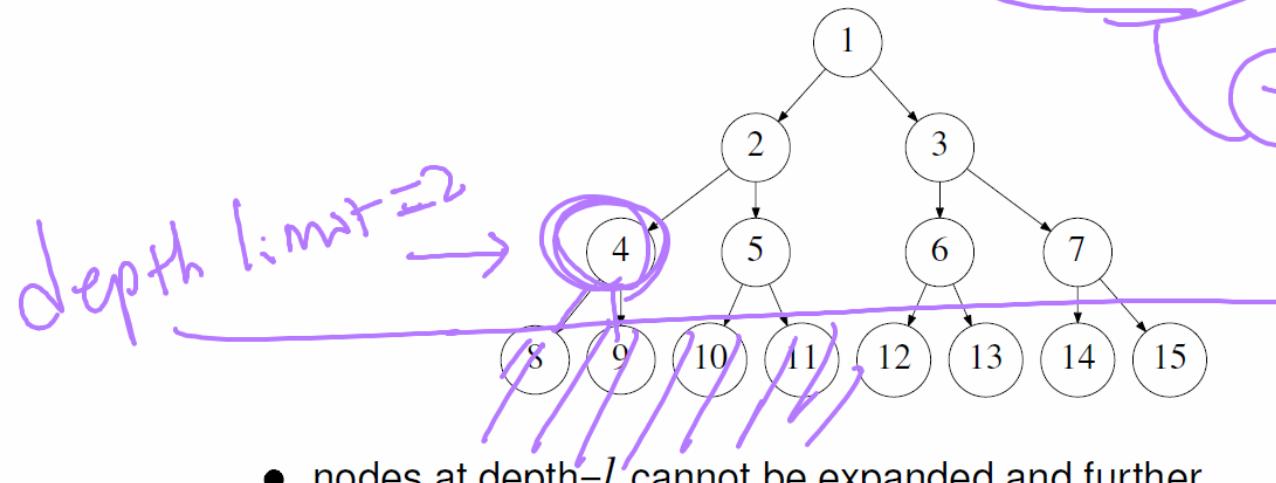
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- Differences and similarities ~~X~~ between BFS and UCS
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node list

I mean I went to use one versus the other and then the node visitor, and so on, cracking tracking the stack order queue at any moment that's the noodle

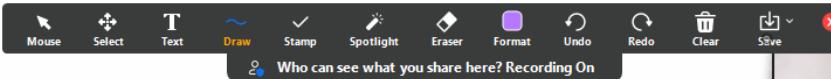


## Depth Limited Search (DLS): Limited Depth DFS

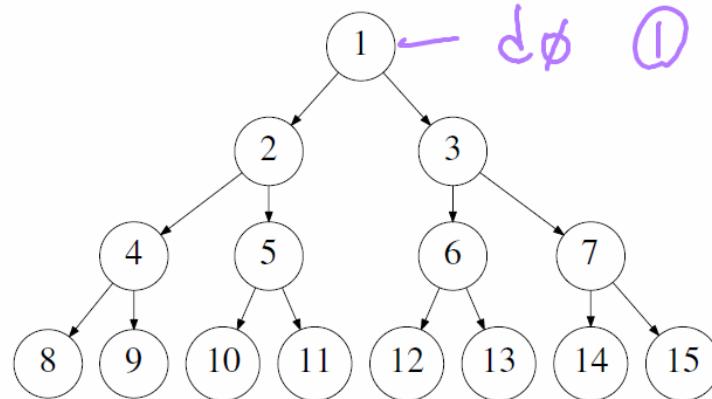


- nodes at depth =  $l$  cannot be expanded and further.
- node visit order for each depth limit  $l$ :  
1 ( $l = 0$ ); 1 2 3 ( $l = 1$ ); 1 2 4 5 3 6 7 ( $l = 2$ );
- queuing function: enqueue at front (i.e. stack push)
- **push the depth of the node as well:**  
( $<\text{depth}>$   $<\text{node}>$ )

Actually, this is a little bit redundant. So the node, and, as we have shown you, includes the the



## DLS: Visit Order and Node List



Evolution of the queue (**bold**=expanded and then added):

(<depth>, <node>) ); Depth limit = 2

1. [ [ **(d0, 1)** ] ] : initial state
2. [ [ **(d1,2)**] [**(d1,3)**] ] : pop 1 and push 2 and 3
3. [ [ **(d2,4)**] [**(d2,5)**] [ (d1, 3) ] ] : pop 2 and push 4 and 5
4. [ [ (d2, 5) ] [ (d1, 3) ] ] : pop 4, cannot expand it further
5. [ [ (d1, 3) ] ] : pop 5, cannot expand it further
6. [ [ **(d2,6)**] [**(d2,7)**] ] : pop 3, and push 6, 7

...

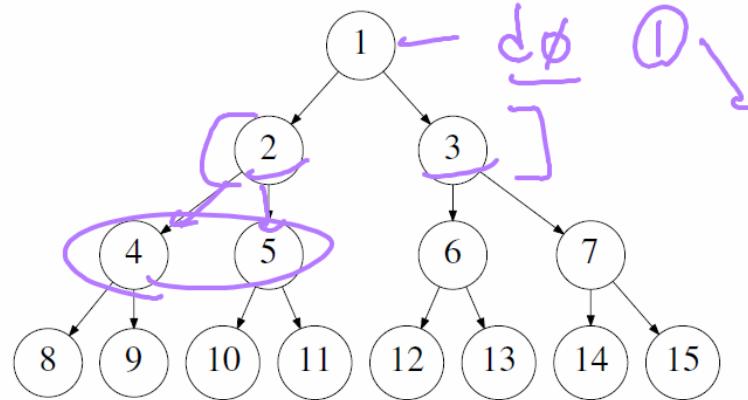
So you have a no one that looks like this. So this is

25

You are screen sharing Stop Share



## DLS: Visit Order and Node List



Evolution of the queue (**bold**=expanded and then added):

(<depth>, <node>) ); Depth limit = 2

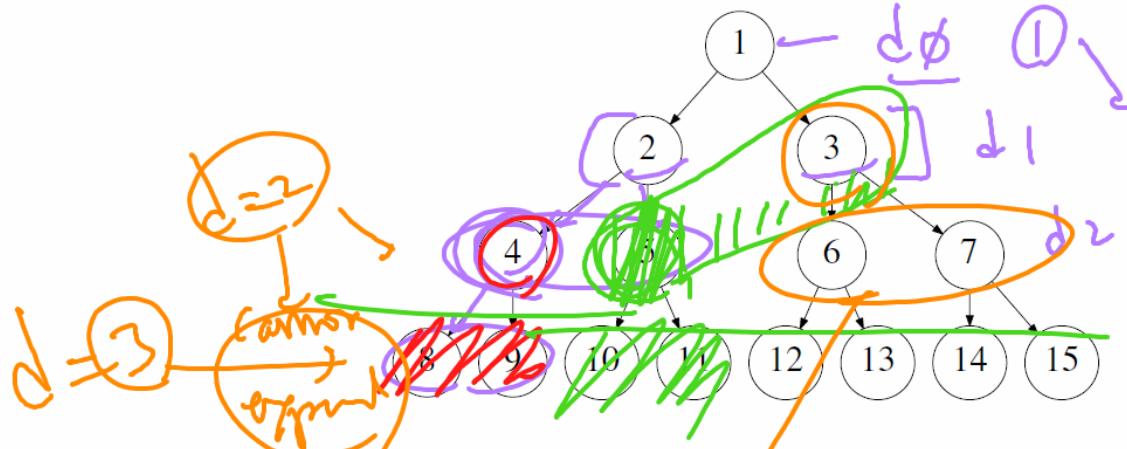
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4. [ [ (d2, 5) ] [ (d1, 3) ] ] : pop 4, cannot expand it further
5. [ [ (d1, 3) ] ] : pop 5, cannot expand it further
6. [ [ **(d2, 6)** ] [ **(d2, 7)** ] ] : pop 3 and push 6, 7

These are the walls, so you can expand 2 you're allowed to expand, too, because it's below the that's limit to expand them into 4 and 5

...



## DLS: Visit Order and Node List



Evolution of the queue (**bold**=expanded and then added):

(<depth>, <node>) ); Depth limit = 2

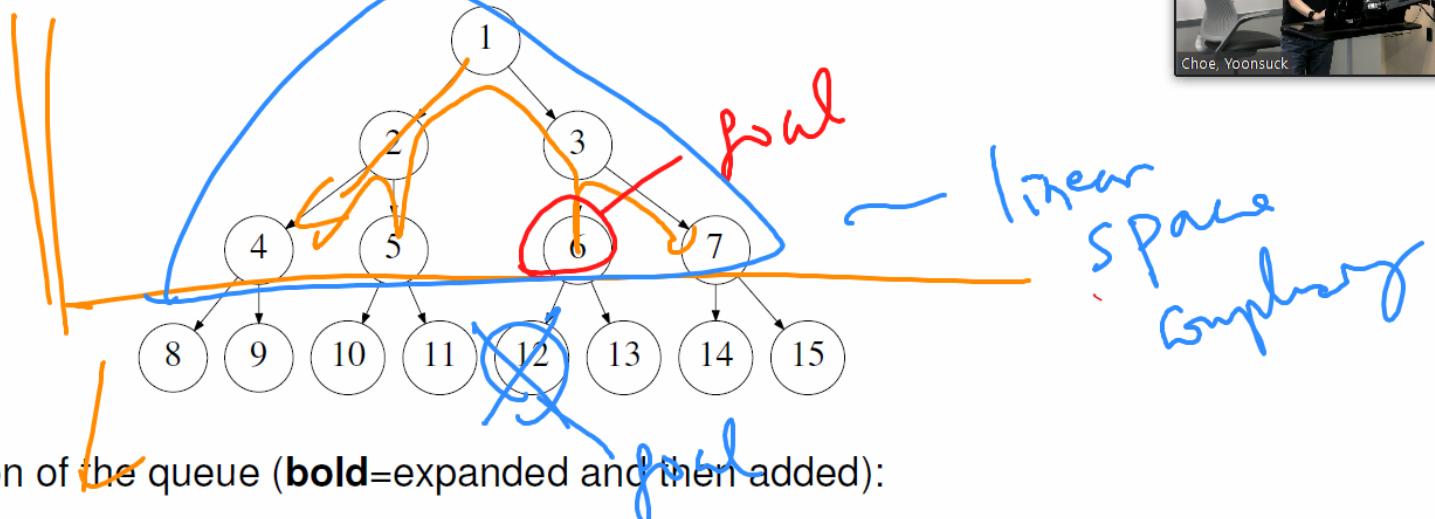
1. **[ [ (d0, 1) ] ]** : initial state
2. **[ [(d1,2)][(d1,3)] ]** : pop 1 and push 2 and 3
3. **[ [(d2,4)][(d2,5)] [ (d1,3) ] ]** : pop 2 and push 4 and 5
4. **[ [ (d2,5) ] [ (d1,3) ] ]** : pop 4, cannot expand it further
5. **[ [ (d1,3) ] ]** : pop 5, cannot expand it further
6. **[ [(d2,6)][(d2,7)] ]** : pop 3, and push 6, 7

We showed that that's goes 3 red this the nodes at depth equals 2 cannot expand right. So that's where this deaf limit

...



## DLS: Visit Order and Node List



(<depth>, <node>) ); Depth limit = 2

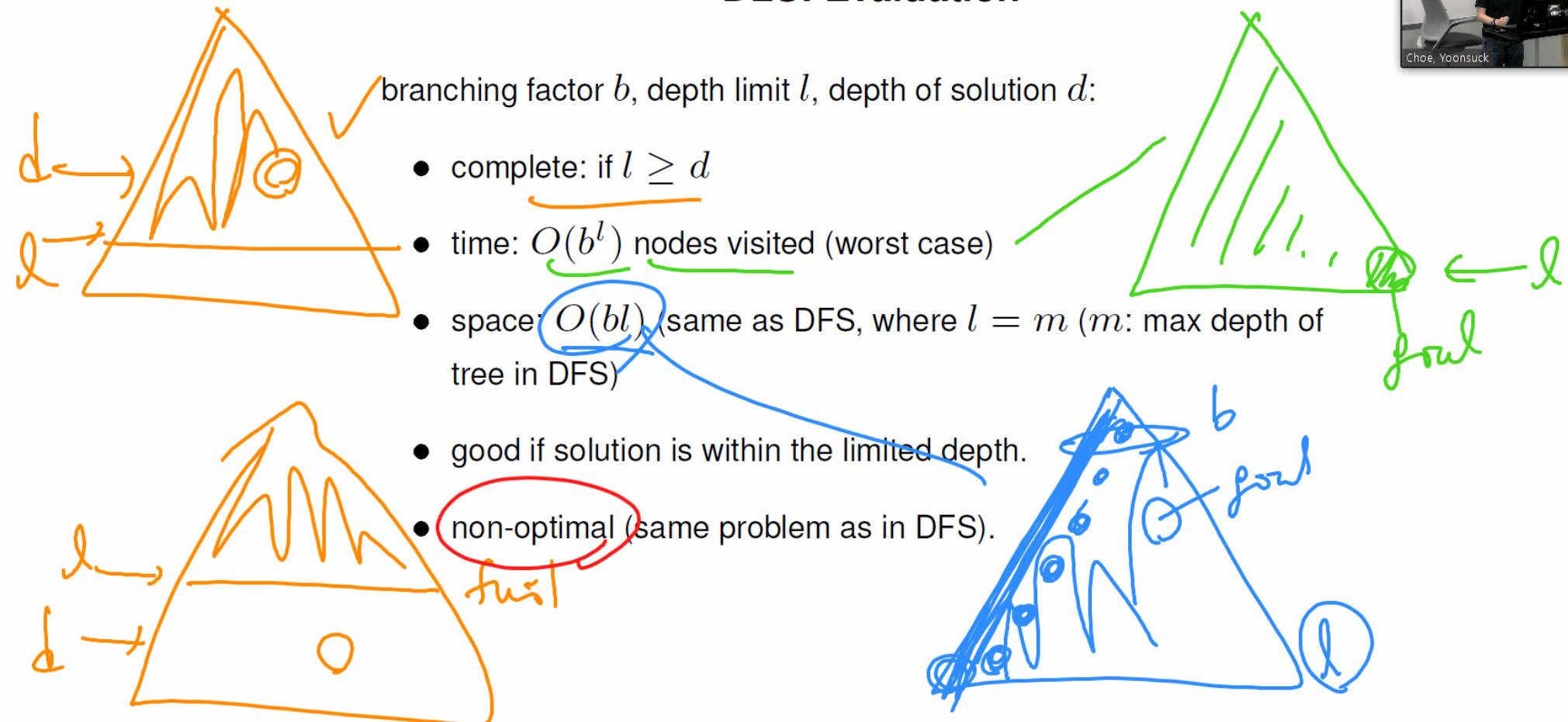
1. [ [ (d0, 1) ] ] : initial state
2. [[(d1,2)][(d1,3)]] : pop 1 and push 2 and 3
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4. [ [ (d2, 5) ] [ (d1, 3) ] ] : pop 4, cannot expand it further
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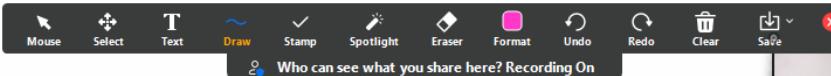
Then this won't be found right but as you're exploring this,  
you get the same benefit of linear space complexity

...

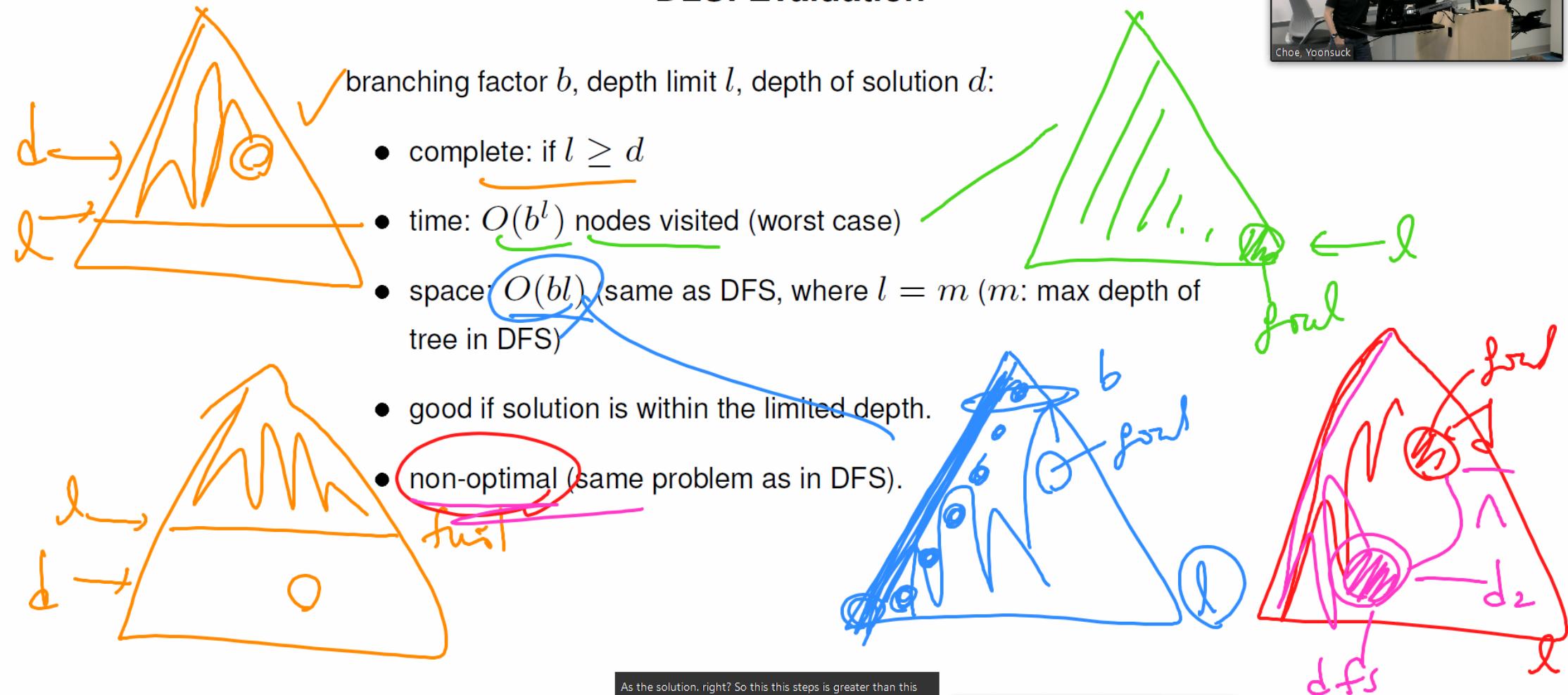


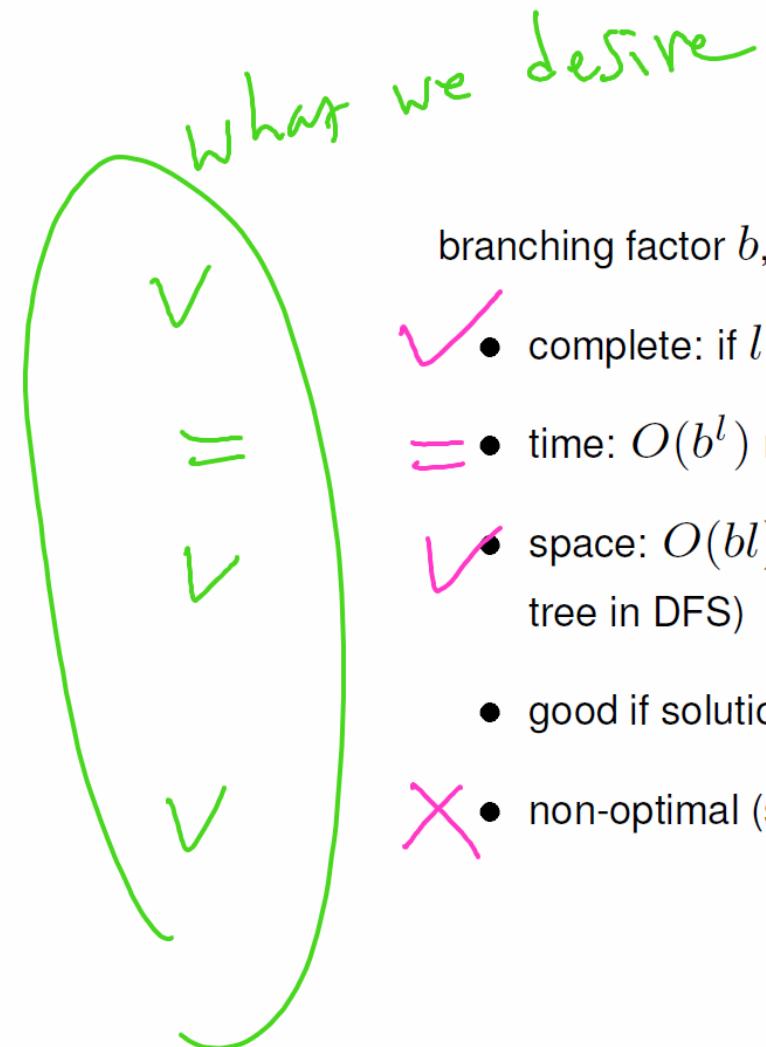
## DLS: Evaluation





## DLS: Evaluation





## DLS: Evaluation

branching factor  $b$ , depth limit  $l$ , depth of solution  $d$ :

- ✓ • complete: if  $l \geq d$  ← BFS
- = • time:  $O(b^l)$  nodes visited (worst case) ← same as others
- ✓ • space:  $O(bl)$  (same as DFS, where  $l = m$  ( $m$ : max depth of tree in DFS)) ← DFS
  - good if solution is within the limited depth.
- X • non-optimal (same problem as in DFS).

bad. ⇒ want to be like BFS

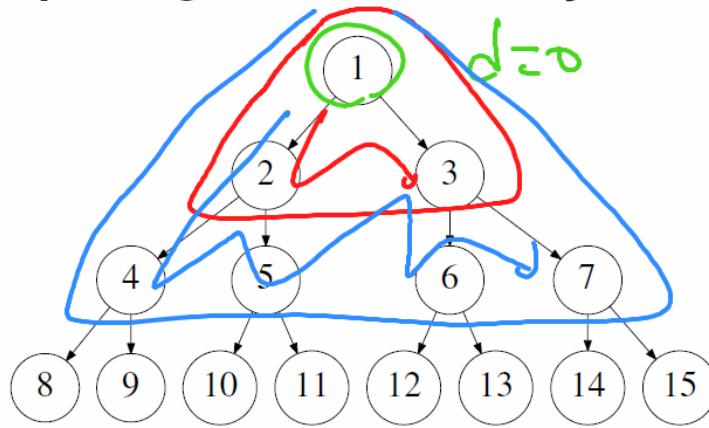


## Iterative Deepening Search: DLS by Increasing Limit

DLS with  $l=0$

DLS with  $l=1$

DLS w/  $l=2$



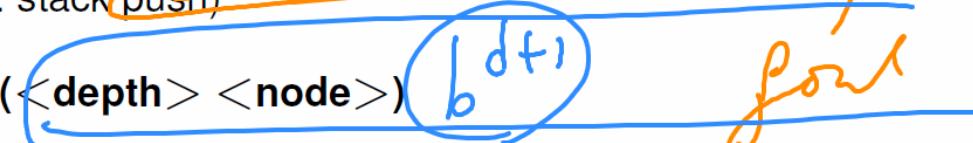
- node visit order:

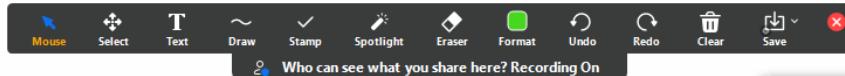
1 ; 1 2 3; 1 2 4 5 3 6 7; 1 2 4 8 9 5 10 11 3 6 12 13 7 14 15; ...

- revisits already explored nodes at successive depth limit

- queuing function: enqueue at front (i.e. stack push)

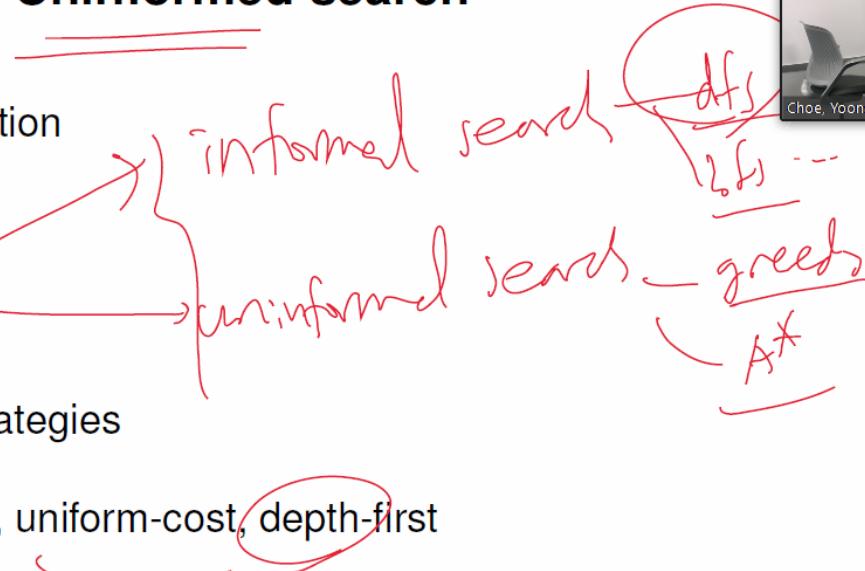
- **push the depth of the node as well:** ( $\langle \text{depth} \rangle \langle \text{node} \rangle$ )





## Overview: Uninformed search

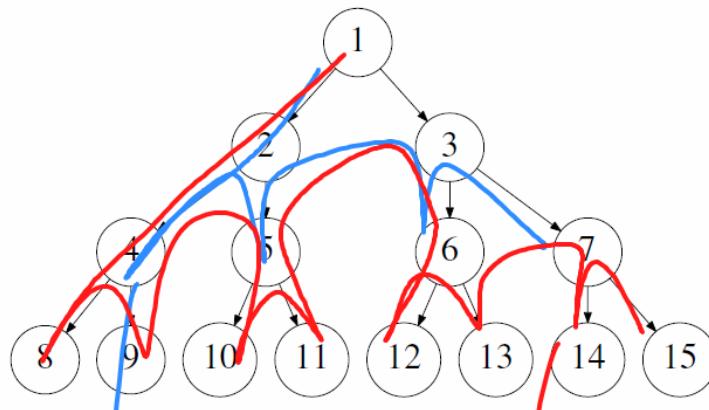
- Search problems: definition
- Example: 8-puzzle
- General search
- Evaluation of search strategies
- Strategies: breadth-first, uniform-cost, depth-first
- More uninformed search: depth-limited, iterative deepening, bidirectional search



First search, the first search, and also things like in from cool search, and so on, and then more advanced versions of it.



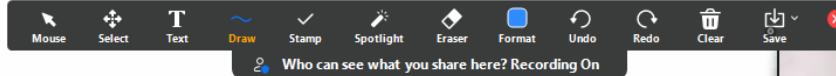
## Iterative Deepening Search: DLS by Increasing Limit



- node visit order:

1, 1, 2, 3, 1, 2, 4, 5, 3, 6, 7; 1, 2, 4, 8, 9, 5, 10, 11, 3, 6, 12, 13, 7, 14, 15, ...

- revisits already explored nodes at successive depth limit
- queuing function: enqueue at front (i.e. stack push)
- **push the depth of the node as well: (<depth> <node>)**



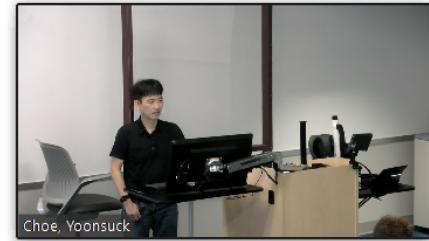
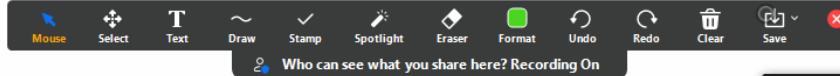
## IDS: Evaluation

branching factor  $b$ , depth of solution  $d$ :

- complete: cf. DLS, which is conditionally complete
- time:  $O(b^d)$  nodes visited (worst case)
- space:  $O(bd)$  (cf. DFS and DLS)
- **optimal!**: unlike DFS or DLS
- good when search space is huge and the depth of the solution is not known (\*)

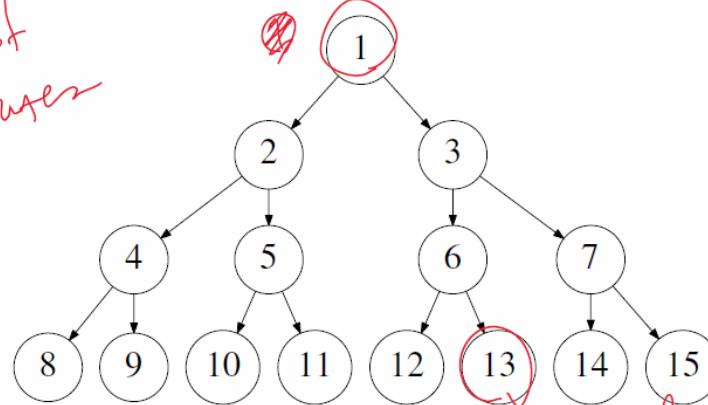
$$1 + (1+b) + (1+b+b^2)$$

+ ...



## Search Problems: Definition

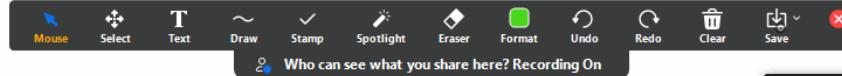
Op: State → Set of states



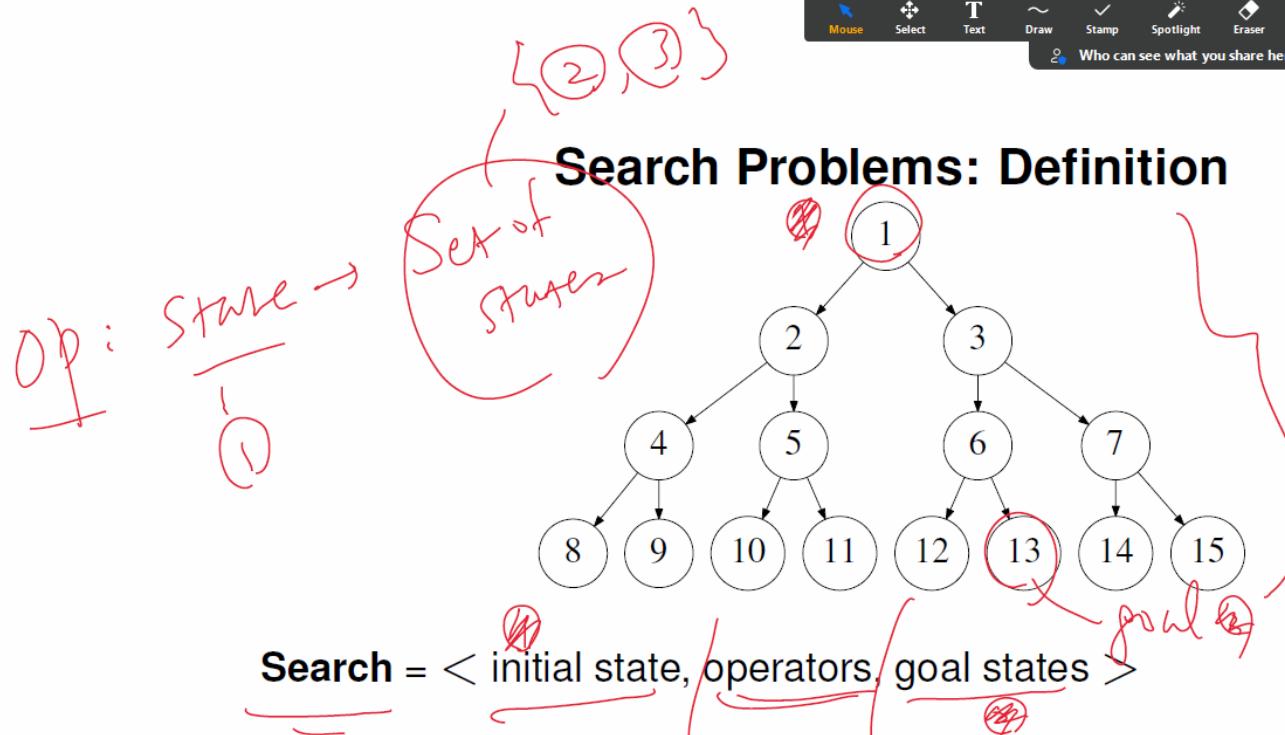
Search = < initial state, operators, goal states >

- Initial State: description of the current situation as given in a problem
- Operators: functions from any state to a set of successor (or neighbor) states
- Goal: subset of states, or test rule

So let me confuse me. K. I wrote this let's just ignore it, for now

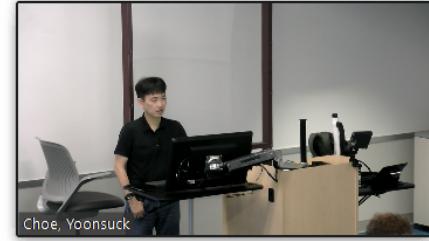
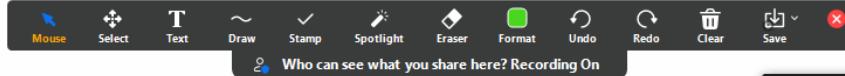


## Search Problems: Definition

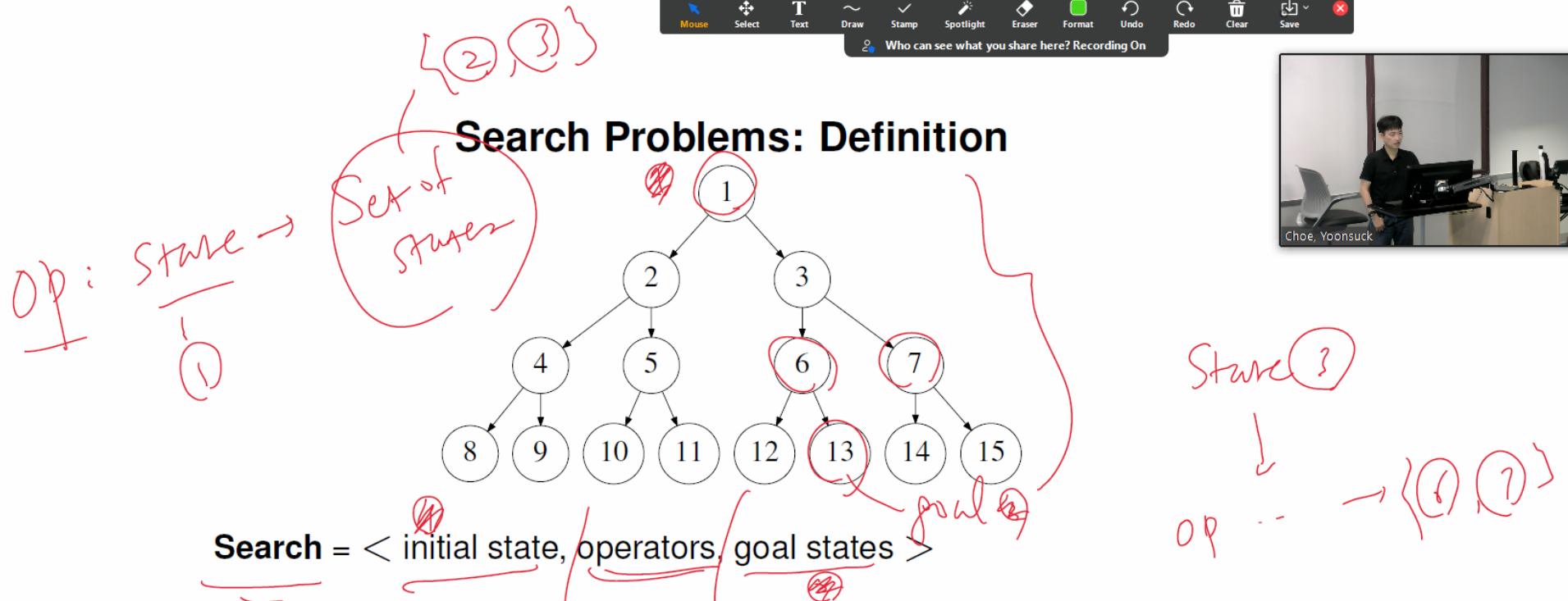


- Initial State: description of the current situation as given in a problem
- Operators: functions from any state to a set of successor (or neighbor) states
- Goal: subset of states, or test rule

Okay. Then, the set of States would include what for given this 3 so it's 3 actually be 2 and 3 right

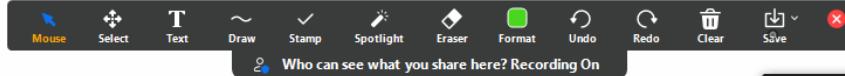


## Search Problems: Definition



- Initial State: description of the current situation as given in a problem
- Operators: functions from any state to a set of successor (or neighbor) states
- Goal: subset of states, or test rule

Then operator with operating on this day 3 would give you 6 and 7, as the out output



## Variants of Search Problems

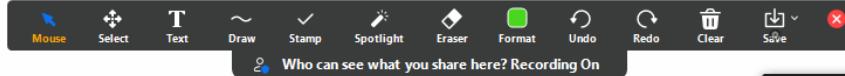
**Search** = < state space, initial state, operators, goal states >

- State space: set of all possible states reachable from the current initial state through repeated application of the operators (i.e. path).

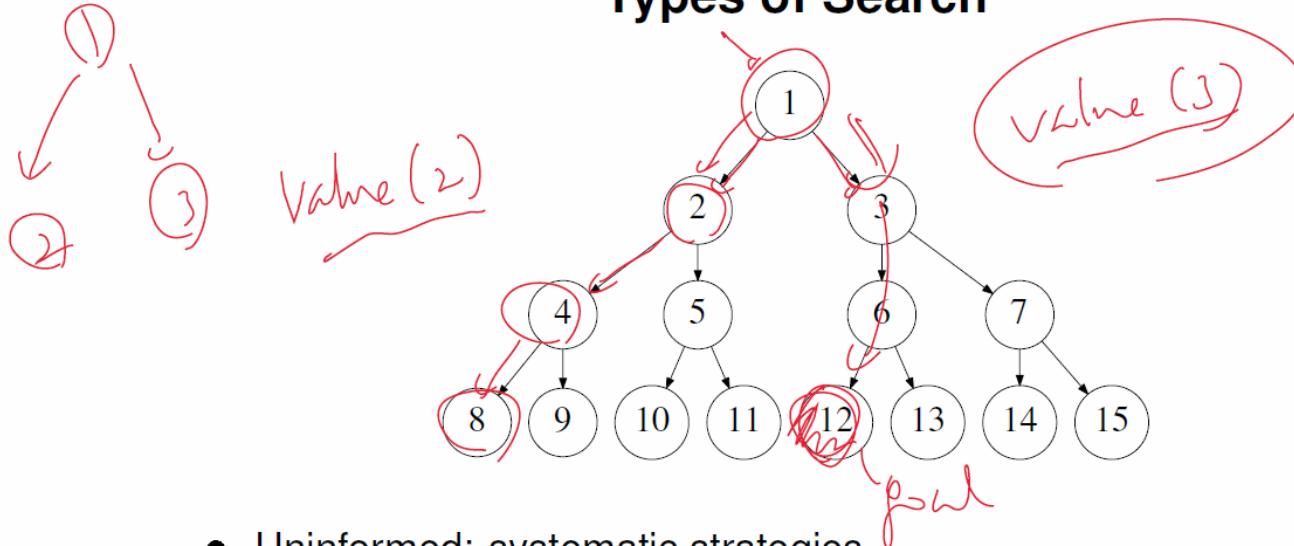
**Search** = < initial state, operators, goal states, path cost >

- Path cost: find **the best** solution, not just **a** solution. Cost can be many different things.

To reach your goal. But on top of that you want to ask what is how good it is, or how bad it is

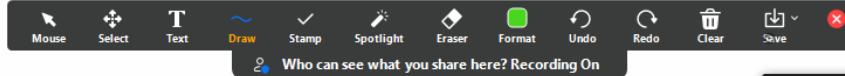


## Types of Search



- Uninformed: systematic strategies
- Informed: Use domain knowledge to narrow down scope of search
- Game playing as search: minimax, state pruning, probabilistic games

And suppose this was the actual goal, then you can just go



## Goal Test

Simply check if the current state is the same as the goal state.

Implementation may vary.



But if you do it like this, since they attend then use keep on repeating the State. Alright, so you'll never get to the ball