

# Frame Problem

- In the previous slide, we cannot deduce if the following can be proven ( $G_1$  represents a particular lump of gold):  
*At( $G_1$ , [1, 1]), Result([Go([1, 1], [1, 2])), Grab( $G_1$ ), Go([1, 2], [1, 3]))*
  - It is because the effect axioms say only *what should change*, but not *what does not change when actions are taken*.

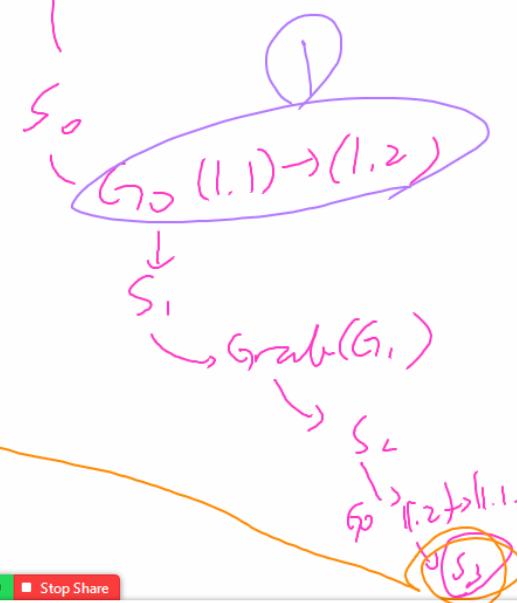
- Initial solution: *Frame axioms*

$$\begin{aligned} & At(o, x, s) \wedge (o \neq Agent) \wedge \neg Holding(o, s) \\ & \rightarrow At(o, x, Result(Do(y, z), s)). \end{aligned}$$

This says moving does not affect the gold when it is not held.

Problem is that you need  $O(AF)$  such axioms for all

*(action, fluent)* pair ( $A$ : num of actions,  $F$ : num of fluent predicates).





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$At(G_1, [1, 1]), Result([Go([1, 1], [1, 2])), Grab(G_1), Go([1, 2], [1, 1]), S_0)$

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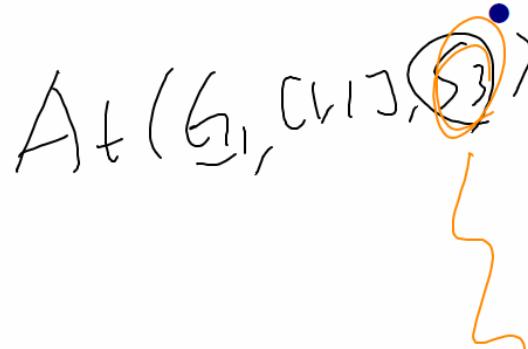
- Initial solution: *Frame axioms*

$$At(o, x, s) \wedge (o \neq Agent) \wedge \neg Holding(o, s)$$

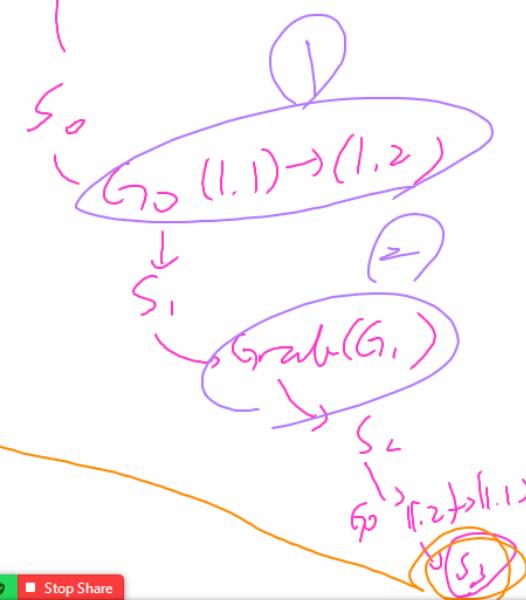
$$\rightarrow At(o, x, Result(Go(y, z), s)).$$

This says moving does not affect the gold when it is not held.

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$At(G_1, [1, 1], S_3)$





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*↑  
Agent*
- It is because the effect axioms say only *what should change*, but not *what does not change when actions are taken*.

- Initial solution: *Frame axioms*

$$At(o, x, s) \wedge (o \neq Agent) \wedge \neg Holding(o, s) \\ \rightarrow At(o, x, Result(Go(y, z), s)).$$

This says moving does not affect the gold when it is not held.

Problem is that you need  $O(AF)$  such axioms for all *(action, fluent)* pair ( $A$ : num of actions,  $F$ : num of fluent predicates).

To ensure that you have to actually add more description of these effects of moving around this stuff that you're holding



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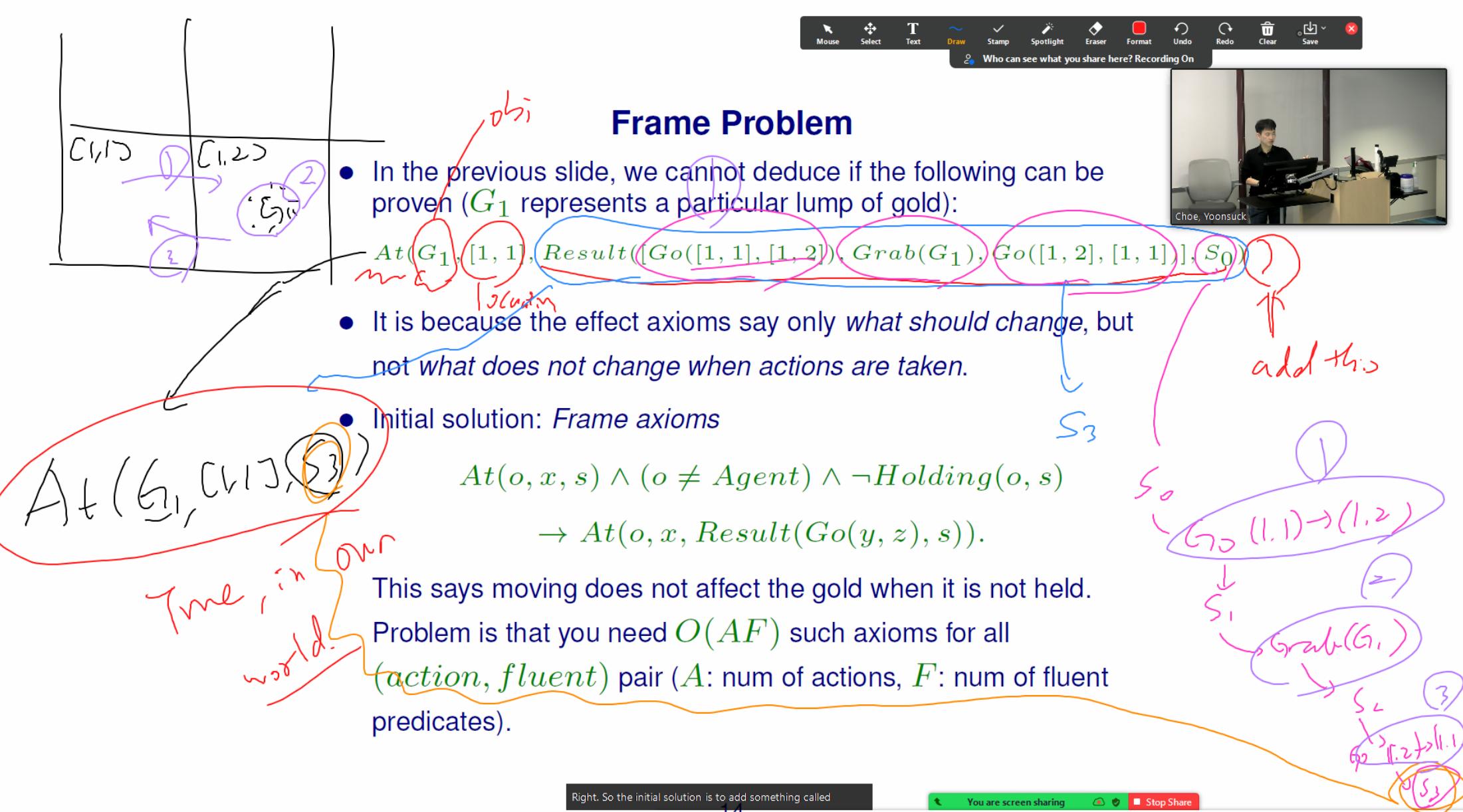
*↑(gold)*
- It is because the effect axioms say only *what should change*, but not *what does not change when actions are taken*.

- Initial solution: *Frame axioms*

$$At(o, x, s) \wedge (o \neq Agent) \wedge \neg Holding(o, s) \\ \rightarrow At(o, x, Result(Go(y, z), s)).$$

This says moving does not affect the gold when it is not held.

Problem is that you need  $O(AF)$  such axioms for all *(action, fluent)* pair ( $A$ : num of actions,  $F$ : num of fluent predicates).





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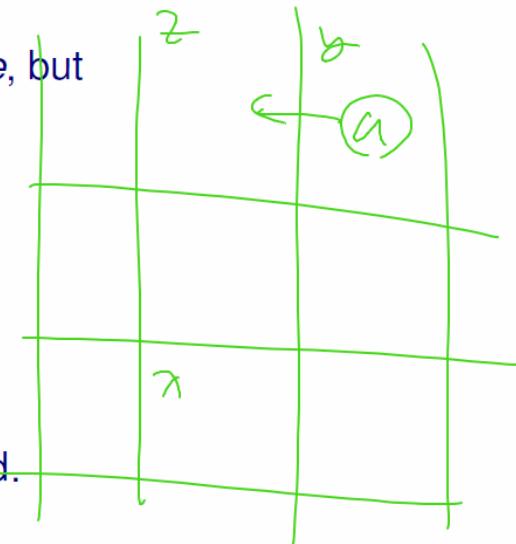
$\text{At}(G_1, [1, 1], \text{Result}([\text{Go}([1, 1], [1, 2]), \text{Grab}(G_1), \text{Go}([1, 2], [1, 1])]), S_0)$

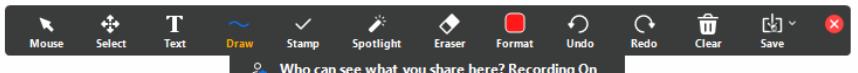
- It is because the effect axioms say only *what should change*, but not *what does not change when actions are taken*.
- Initial solution: Frame axioms

$$\begin{aligned} & \text{At}(o, x, s) \wedge (o \neq \text{Agent}) \wedge \neg \text{Holding}(o, s) \\ & \quad \xrightarrow{\text{obj loc situation}} \text{At}(o, x, \text{Result}(\text{Go}(y, z), s)). \end{aligned}$$

This says moving does not affect the gold when it is not held.

Problem is that you need  $O(AF)$  such axioms for all  $(\text{action}, \text{fluent})$  pair ( $A$ : num of actions,  $F$ : num of fluent predicates).





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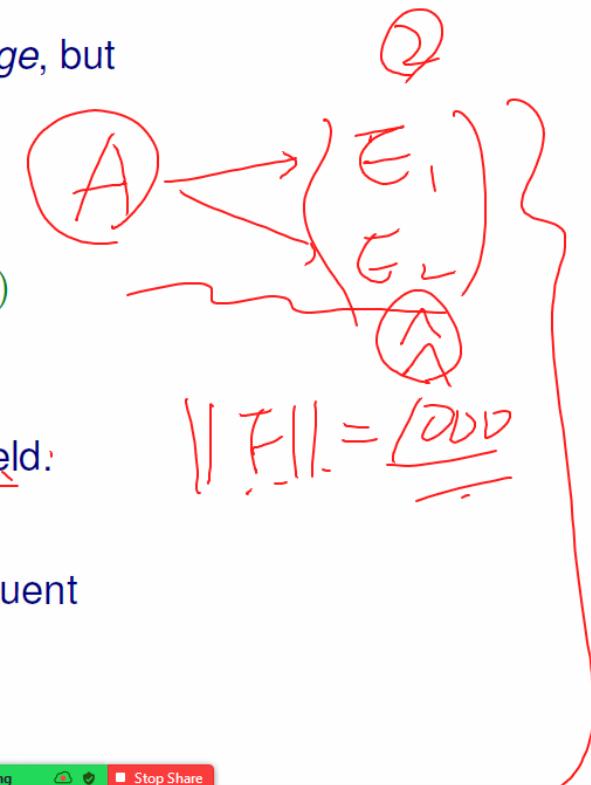
$$At(G_1, [1, 1], Result([Go([1, 1], [1, 2]), Grab(G_1), Go([1, 2], [1, 1])], S_0))$$

- It is because the effect axioms say only *what should change*, but not *what does not change when actions are taken*.
- Initial solution: *Frame axioms*

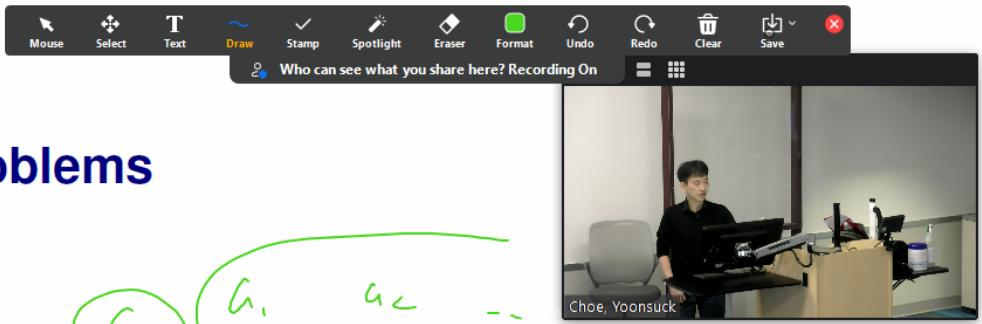
$$\left. \begin{array}{l} At(o, x, s) \wedge (o \neq Agent) \wedge \neg Holding(o, s) \\ \rightarrow At(o, x, Result(Go(y, z), s)). \end{array} \right\}$$

This says moving does not affect the gold when it is not held.

Problem is that you need  $O(AF)$  such axioms for all  $(action, fluent)$  pair ( $A$ : num of actions,  $F$ : num of fluent predicates).

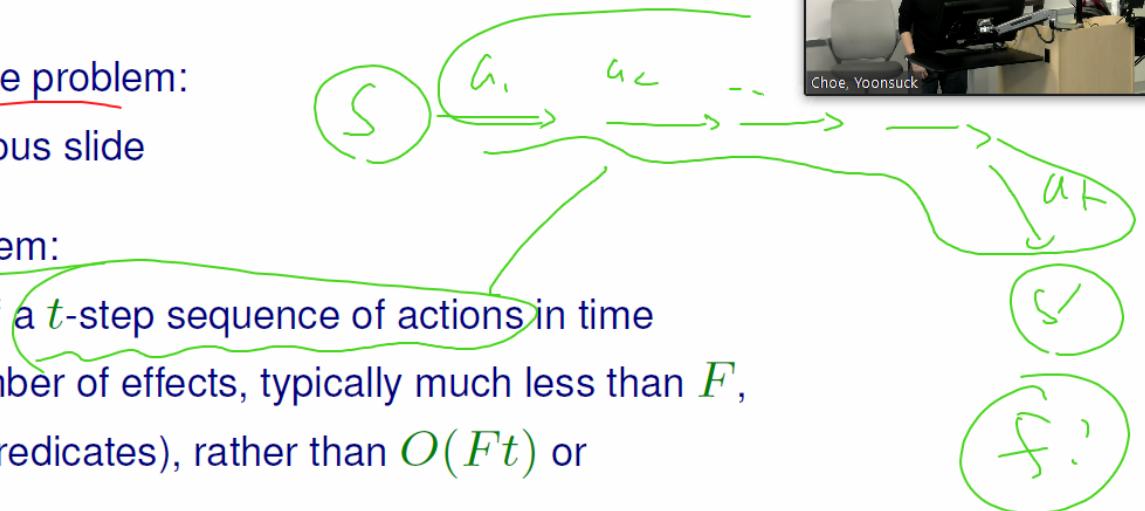


And the number of pretty kids. So if you have to actually have frame actions for the number of actions times this, then it gets pretty anything



## Two Frame Problems

- Representational frame problem:  
Explained in the previous slide
- Inferential frame problem:  
Projection of results of a  $t$ -step sequence of actions in time  
 $O(Et)$  ( $E$  is the number of effects, typically much less than  $F$ ,  
the number of fluent predicates), rather than  $O(Ft)$  or  
 $O(AEt)$ .

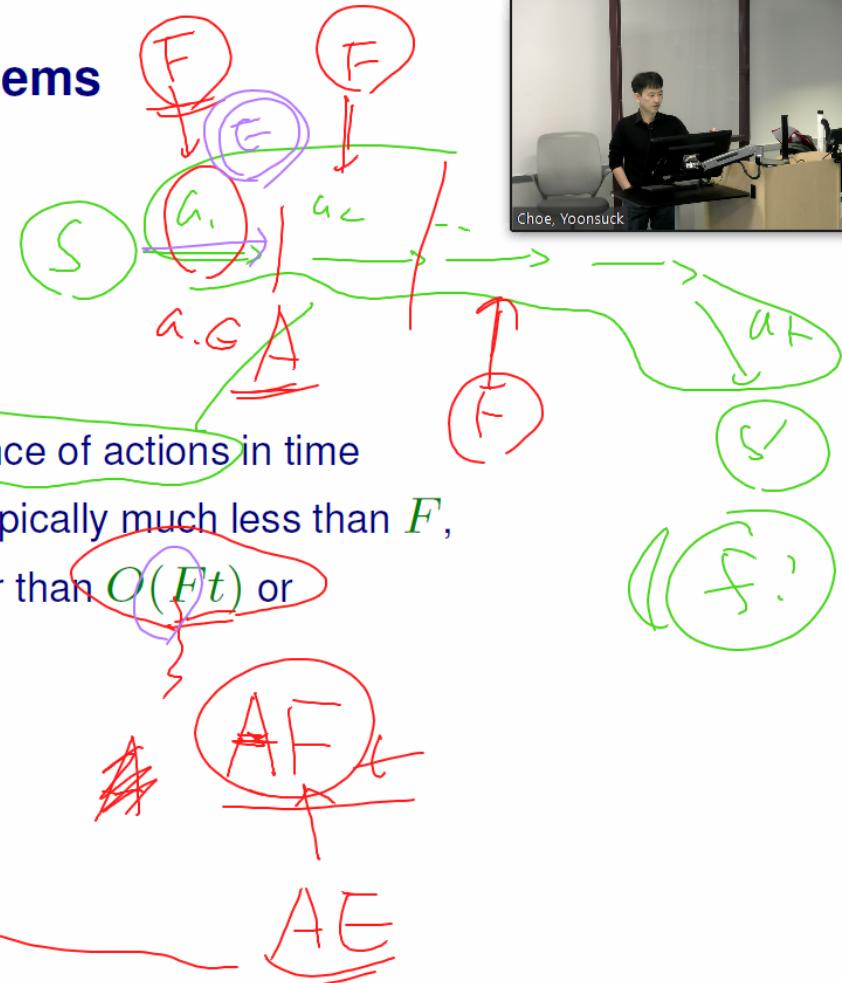


After the the sequence of actions. So you take a T-step sequence of actions which is this



## Two Frame Problems

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 $O(Et)$  ( $E$  is the number of effects, typically much less than  $F$ ,  
the number of fluent predicates), rather than  $O(Ft)$  or  
 $O(AEt)$ .





## Solving the Representational Frame Problem

- Consider how each fluent predicate evolves over time:

Successor-state axioms Action is possible →

Fluent is true in result state ↔ Action's effect made it true

$F_1 = T \rightarrow F_2 = T$

It was true before and action left it alone

- Example:

$Poss(a, s) \rightarrow$

$(At(Agent, y, Result(a, s)) \leftrightarrow a = Go(x, y))$

$\vee (At(Agent, y, s) \wedge a \neq Go(y, z))).$

- Remaining issues: implicit effect (moving while holding something moves that something as well) – ramification problem. Can solve by using a more general successor-state axiom.

So that's condition. one in condition 2 actions if it made it true, or it was be true already, and it wasn't touched



## Solving the Representational Frame Problem

- Consider how each fluent predicate evolves over time:

Successor-state axioms **Action is possible** →

(Fluent is true in result state  $\leftrightarrow$  Action's effect made it true)

$At(At(Agent, \gamma, S)) \vee$   
 $At(At(Agent, \gamma, S)) \wedge$   
 It was true before and action left it alone).

- Example:

$Poss(a, s) \rightarrow$

$(At(Agent, y), Result(a, s)) \leftrightarrow a = Go(x, y)$

$\vee (At(Agent, y, s) \wedge a \neq Go(y, z))).$

- Remaining issues: implicit effect (moving while holding something moves that something as well) – ramification problem. Can solve by using a more general successor-state axiom.

## 1.2 Substitution and Unification

**Problem 4 (9 pts):** Apply the following substitutions to the expressions (3 points)

1. Apply  $\{x/f(A)\}$  to  $P(x, y) \vee Q(x)$ .
2. Apply  $\{x/A, y/f(z)\}$  to  $P(x, y) \vee Q(x)$ .
3. Apply  $\{x/f(y), y/B\}$  to  $P(x, y) \vee Q(x)$ .

$(P(A, f(B))$

**Problem 5 (12 pts):** For each of the following example, given  $P(A)$  and  $P(x)$ , the unifier would be  $\{A/x\}$ . If the substitution of the expressions is not unifiable, indicate so. (3 points) Set  $D_k$  for each iteration, and the  $\sigma_k$ .

- 1  $P(x, f(B))$  and  $P(A, f(y))$
- 2  $P(y, y)$  and  $P(x, f(A))$
- 3  $P(f(y), x, y)$  and  $P(f(g(w)), w, g(A))$
- 4  $P(A, f(y), y, A)$  and  $P(x, f(g(x)), g(B))$

prob:  
P(x,f(y))  
var.  
upper  
lower

## 1.3 Proof by resolution

**Problem 6 (16 pts):** (1) Translate the following into a canonical form, and (3) prove the theorem

Given:

1. If a child is young, then he/she is adored.
2. Every child who is adored and fed well is happy.
3. Every child is fed well.

You get p. of A. F. of B. a single expression. So you got the unified expression, but it only shows you she's just the answer. So you have to

Show that the following is a logical consequence of the above:



linux2.cse.tamu.edu - PuTTY

```
If you get the error message: Failed to create [redacted]
Then you will need to first create your home directory. Directions are available in your browser by visiting the following web page: http://bit.ly/linuxhome
> medoc

COMPUTER NAME: linux2.cs.tamu.edu

End of banner message from server
choe@sun.cs.tamu.edu's password:
linux2:/home/faculty/c/choe>
linux2:/home/faculty/c/choe>
linux2:/home/faculty/c/choe> gprolog
GNU Prolog 1.4.4 (64 bits)
Compiled Jan 15 2014, 20:38:19 with gcc
By Daniel Diaz
Copyright (C) 1999-2013 Daniel Diaz
| ?- p(X, f(b)) = p(a, f(Y)).
```

X = a  
Y = b

yes | ?- □

$\therefore \Gamma = \{x/A, y/B\}$

You are screen sharing Stop Share



## Solving the Representational Frame Problem

- Consider how each fluent predicate evolves over time:

Successor-state axioms **Action is possible** →

(Fluent is true in result state  $\leftrightarrow$  Action's effect made it true)

$\vee$

(It was true before and action left it alone).

- Example:

$Poss(a, s) \rightarrow$

$(At(Agent, y), Result(a, s)) \leftrightarrow a = Go(x, y)$

$\vee (At(Agent, y, s) \wedge a \neq Go(y, z))$ .

already there

didn't move

- Remaining issues: implicit effect (moving while holding something moves that something as well) – ramification problem. Can solve by using a more general successor-state axiom.



## Solving the Representational Frame Problem

- Consider how each fluent predicate evolves over time:

Successor-state axioms **Action is possible** →

(Fluent is true in result state  $\leftrightarrow$  Action's effect made it true)

$\vee$

$At(At(Agent, x, s), s')$

It was true before and action left it alone.

- Example:

$Poss(a, s) \rightarrow$

$(At(Agent, y, s), Result(a, s)) \leftrightarrow a = Go(x, y)$

$\vee (At(Agent, y, s) \wedge a \neq Go(y, z))$

already there

didn't move

- Remaining issues: implicit effect (moving while holding something moves that something as well) – ramification problem. Can solve by using a more general successor-state axiom.

Okay, school. Still, there are remaining issues, even if you have these things laid out their implicit effects like moving while holding on something



## Solving the Inferential Frame Problem

- Typical frame axiom:  $Poss(a, s) \rightarrow$

$$F_i(\text{Result}(a, s)) \leftrightarrow (a = A_1 \vee a = A_2 \dots) \\ \vee (F_i(s) \wedge (a \neq A_3) \wedge (a \neq A_4) \dots)$$

- Several actions that make the fluent true and several that make the fluent false: Formalize using the predicate

$PosEffect(a, F_i)$  and  $NegEffect(a, F_i)$ .

$Poss(a, s)$   $\rightarrow$

$$F_i(\text{Result}(a, s)) \leftrightarrow PosEffect(a, F_i) \\ \vee [F_i(s) \wedge \neg NegEffect(a, F_i)]$$

$PosEffect(A_1, F_i), PosEffect(A_1, F_i)$

$NegEffect(A_3, F_i), NegEffect(A_4, F_i)$

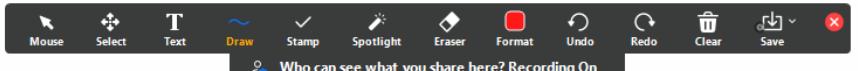
\* This can be done efficiently: get current action, and fetch its effects, then update those fluents  $O(Et)$ .

You introduce these things? So



## Solving the Inferential Frame Problem

- $S_0 \xrightarrow{a_1} S_1 \xrightarrow{a_2} S_2$
- Given a  $t$ -step plan  $p$  ( $S_t = \text{Result}(p, S_0)$ ), decide which fluents are true in  $S_t$ .
  - We need to consider each of the  $F$  frame axiom of each time step  $t$ .
  - Axioms have an average size of  $\underline{AE/F}$ , we have an  $\underline{O(AEt)}$  inferential work. Most of the work is done copying unchanged fluents from time step to time step.
  - Solutions: use fluent calculus rather than situation calculus, or make the process more efficient.



## Solving the Inferential Frame Problem

- Typical frame axiom:  $Poss(a, s) \rightarrow$

$$F_i(\text{Result}(a, s)) \leftrightarrow (a = A_1 \vee a = A_2 \dots) \quad \text{made it } \gg$$

$$\vee (F_i(s) \wedge (a \neq A_3) \wedge (a \neq A_4) \dots) \quad \text{exclude}.$$

- Several actions that make the fluent true and several that make the fluent false: Formalize using the predicate

$PosEffect(a, F_i)$  and  $NegEffect(a, F_i)$ .

$Poss(a, s) \rightarrow$

$$F_i(\text{Result}(a, s)) \leftrightarrow PosEffect(a, F_i)$$

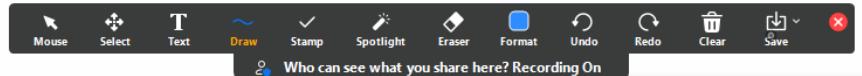
$$\vee [F_i(s) \wedge \neg NegEffect(a, F_i)]$$

$PosEffect(A_1, F_i), PosEffect(A_1, F_i)$

$NegEffect(A_3, F_i), NegEffect(A_4, F_i)$

\* This can be done efficiently: get current action, and fetch its effects, then update those fluents  $O(Et)$ .

So you want to exclude them



## Solving the Inferential Frame Problem

- Typical frame axiom:  $Poss(a, s) \rightarrow$

$$\underbrace{F_i(\text{Result}(a, s)) \leftrightarrow (\underbrace{a = A_1 \vee a = A_2 \dots}_{\text{True}})}_{\text{True}} \vee (F_i(s) \wedge (a \neq A_3) \wedge (a \neq A_4) \dots)$$

- Several actions that make the fluent true and several that make the fluent false: Formalize using the predicate

$PosEffect(a, F_i)$  and  $NegEffect(a, F_i)$ .

$Poss(a, s) \rightarrow$

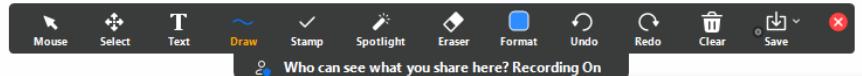
$$F_i(\text{Result}(a, s)) \leftrightarrow \underbrace{PosEffect(a, F_i)}_{\text{True}} \vee [F_i(s) \wedge \neg NegEffect(a, F_i)]$$

$PosEffect(A_1, F_i), PosEffect(A_1, F_i)$

$NegEffect(A_3, F_i), NegEffect(A_4, F_i)$

\* This can be done efficiently: get current action, and fetch its effects, then update those fluents  $O(Et)$ .

So that corresponds to this



## Solving the Inferential Frame Problem

- Typical frame axiom:  $Poss(a, s) \rightarrow$

$$F_i(\text{Result}(a, s)) \leftrightarrow (a = A_1 \vee a = A_2 \dots) \\ \vee (F_i(s) \wedge (a \neq A_3) \wedge (a \neq A_4) \dots)$$

- Several actions that make the fluent true and several that make the fluent false: Formalize using the predicate

$PosEffect(a, F_i)$  and  $NegEffect(a, F_i)$ .

$Poss(a, s) \rightarrow$

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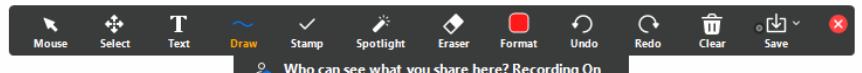
$PosEffect(A_1, F_i), PosEffect(A_1, F_i)$

$NegEffect(A_3, F_i), NegEffect(A_4, F_i)$  already true

\* This can be done efficiently: get current action, and fetch its effects, then update the fluent  $O(1)$ .

Do you want to exclude them? Well, making sure that this flew on was already true.

You are screen sharing Stop Share



## Solving the Inferential Frame Problem

- Typical frame axiom:  $Poss(a, s) \rightarrow$

$$F_i(\text{Result}(a, s)) \leftrightarrow (a = A_1 \vee a = A_2 \dots) \\ \vee (F_i(s) \wedge (a \neq A_3) \wedge (a \neq A_4) \dots)$$

- Several actions that make the fluent true and several that make the fluent false: Formalize using the predicate  $PosEffect(a, F_i)$  and  $NegEffect(a, F_i)$ .

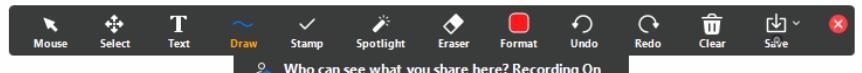
$$Poss(a, s) \rightarrow$$

$$F_i(\text{Result}(a, s)) \leftrightarrow PosEffect(a, F_i) \\ \vee [F_i(s) \wedge \neg NegEffect(a, F_i)]$$

PosEffect(A<sub>1</sub>, F<sub>i</sub>), PosEffect(A<sub>1</sub>, F<sub>i</sub>), NegEffect(A<sub>3</sub>, F<sub>i</sub>), NegEffect(A<sub>4</sub>, F<sub>i</sub>)

\* This can be done efficiently: get current action, and fetch its effects, then update the solution Q(Et).

A 2 is another action that would result in a positive effect for fi, and so on.

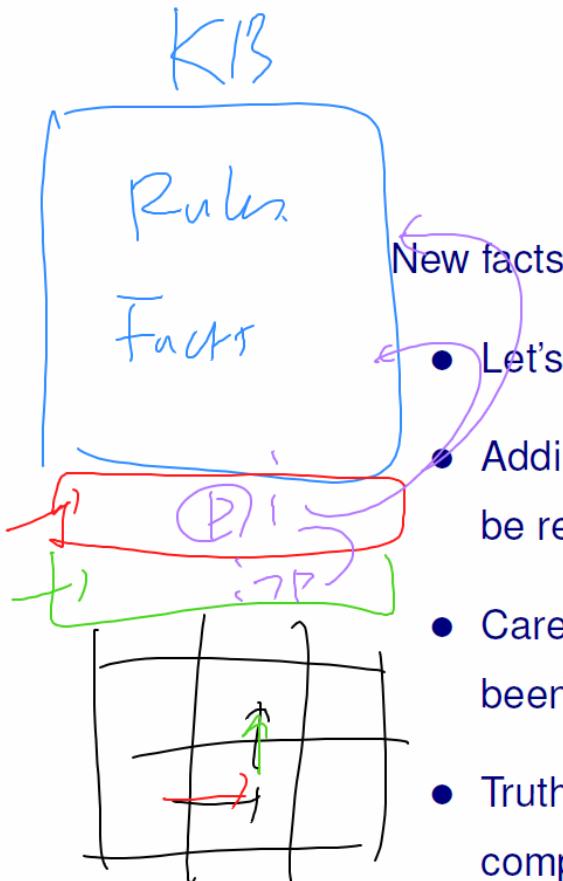
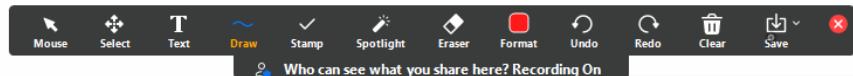


## Other Formalisms

- Event calculus: Fluents hold at different time points, not situations. Reasoning is done over time.
- Other constructs: generalized events (spatiotemporal), process, intervals, etc.
- Formal theory of belief: propositional attitude, reification, etc.

SKIP

But well, these are just for your reference let's say just we skip the



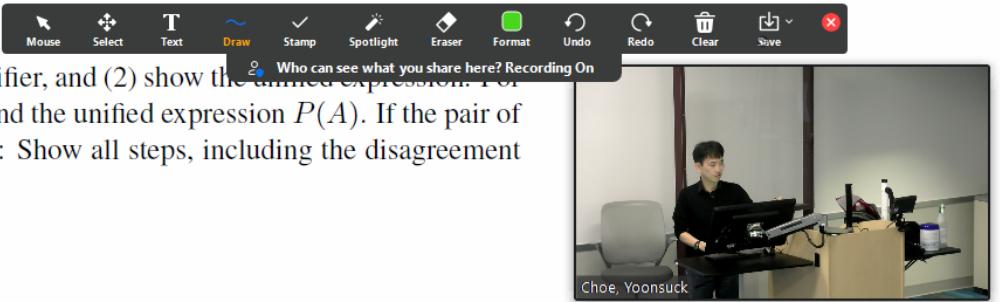
## Truth Maintenance Systems

New facts inferred from the KB can turn out to be incorrect.

- Let's say  $P$  was derived in the KB and later it was found that  $\neg P$ .
- Adding  $\neg P$  to the KB will invalidate the entire KB, so  $P$  should be removed ( $\text{Retract}(KB, P)$ ). *victims of predicate*
- Care needs to be taken since other facts in the KB may have been derived from  $P$ , etc.
- Truth maintenance systems are designed to handle these complications.

Wait a minute in knowledge based systems. This is a key functionality which is called truth, maintenance system.

3. Apply  $\{x/f(y), y/B\}$  to  $P(x, y) \vee Q(x)$ .



**Problem 5 (12 pts):** For each of the following, (1) find the unifier, and (2) show the unified expression. For example, given  $P(A)$  and  $P(x)$ , the unifier would be  $\{x/A\}$ , and the unified expression  $P(A)$ . If the pair of expressions is not unifiable, indicate so. (3 points each). Note: Show all steps, including the disagreement set  $D_k$  for each iteration, and the  $\sigma_k$ .

1.  $P(x, f(B))$  and  $P(A, f(y))$
2.  $P(y, y)$  and  $P(x, f(A))$
3.  $P(f(y), x, y)$  and  $P(f(g(w)), w, g(A))$
4.  $P(A, f(y), y, A)$  and  $P(x, f(g(x)), g(B), w)$

### 1.3 Proof by resolution

**Problem 6 (16 pts):** (1) Translate the following into first-order logic, (2) convert the resulting formulas into a canonical form, and (3) prove the theorem using resolution.

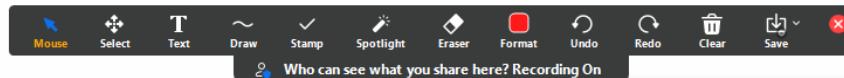
Given:

1. If a child is young, then he/she is adored.
2. Every child who is adored and fed well is happy.
3. Every child is fed well.

~~child (<)~~

Show that the following is a logical consequence of the above:

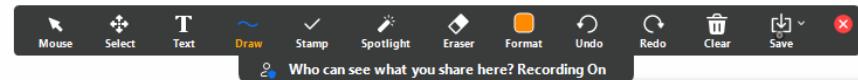
4. (Conclusion) Every young child is happy.



## Planning Approaches

- State-space search: forward or backward.
- Heuristic search: subgoal independence assumption.
- Partial-order planning: utilize problem decomposition. Can place two actions into a plan without specifying the order. Several different total order plans can be constructed from partial order plans.

Using this kind of partial between



## Acquisition of New Information and Probability

- The degree of belief changes as an agent perceives or acquires new information from the world: we call this the **evidence**.
- This is analogous to saying whether or not a given logical sentence is entailed by (i.e. is a logical consequence of) the knowledge base, because the truth value can change when new facts are added to the KB.

$P(\text{Rain}) = 0.5$

↓

*Wet Umbrella.*

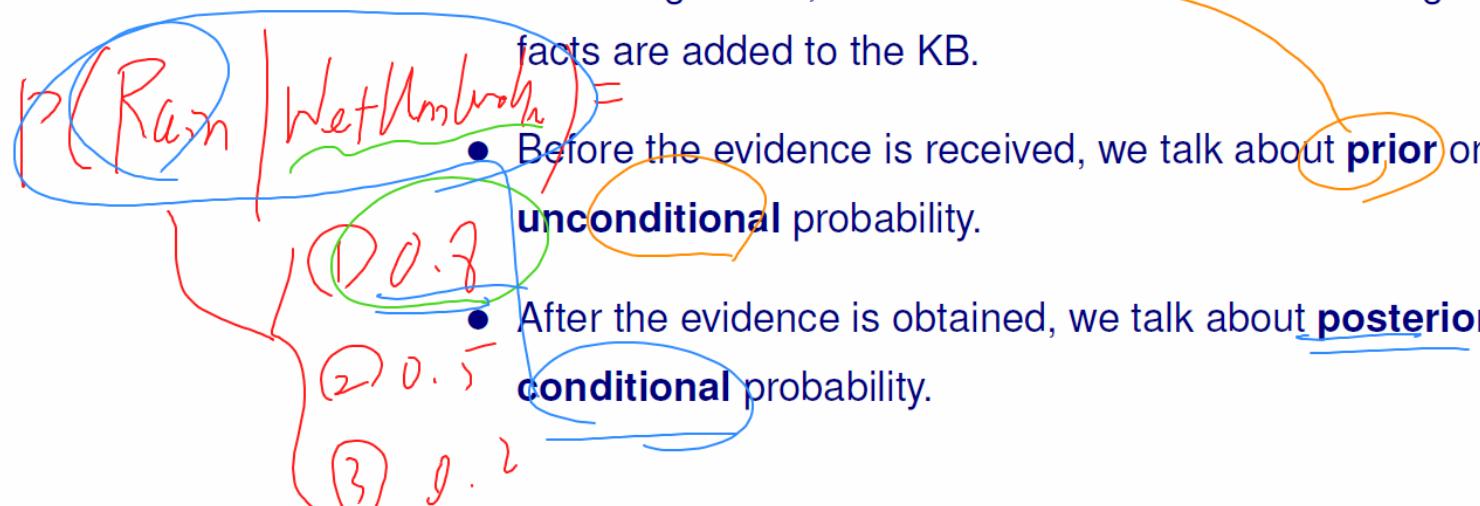
- Before the evidence is received, we talk about **prior** or **unconditional** probability.
  - After the evidence is obtained, we talk about **posterior** or **conditional** probability.
- (1) 0.7  
 (2) 0.5  
 (3) 0.2

Well, Uncle

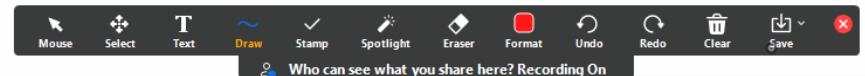


## Acquisition of New Information and Probability

- The degree of belief changes as an agent perceives or acquires new information from the world: we call this the **evidence**.
- This is analogous to saying whether or not a given logical sentence is entailed by (i.e. is a logical consequence of) the knowledge base, because the truth value can change when new facts are added to the KB.



So this is either called conditional, or the poststerior prime p

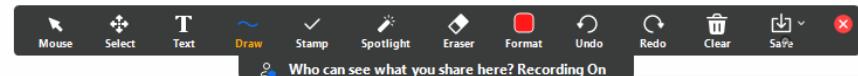


## Acquisition of New Information and Probability

$$\begin{aligned} & P(Rain) \\ & \quad \swarrow \\ P(Rain | \text{Wet Umbrella}) \\ & \quad \swarrow \\ P(Rain | \text{Wet Umbrella, Thunder}) \end{aligned}$$

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- Before the evidence is received, we talk about **prior** or **unconditional** probability.
- After the evidence is obtained, we talk about **posterior** or **conditional** probability.

Okay, then, this would be greater than that, and this would be greater than that.

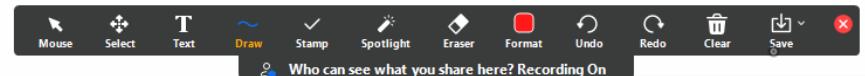


## Acquisition of New Information and Probability

$$\begin{aligned} & P(Rain) \\ & \quad \text{↑} \\ & P(Rain | Wet Umbrella) \\ & \quad \text{↑} \\ & P(Rain | Wet Umbrella, Thunder) \end{aligned}$$

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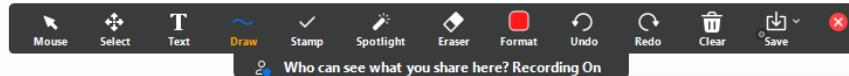
So you can keep on adding, and more



## Rational Decisions Under Uncertainty: Decision Theory

- There are trade-offs, and an agent must first have **preferences** between different results when a certain plan was executed.
- **Utility theory** deals with such preferences: how useful is such and such result to the agent?
- **Decision theory** is a general theory of rational decision under uncertainty, combining **probability theory** and **utility theory**.

Theory and utility Theory to come up with, like a rational way to make decisions, to pick which action in a certain given



## Decision Theory

- An agent is rational iff it chooses the action that yields the highest expected utility, averaged over all possible outcomes of the action:  
**Principle of Maximum Expected Utility**
- Example: backgammon (discussed earlier) – min-max trees with probabilistic levels.

What we want to do is to use the principle of Mac maximum expected utility



## Decision Theoretic Agent

*state*

**function** DT-Agent (*percept*) **returns** *action*

**static:** a set probabilistic *belief* about the state of the world

calculate updated probabilities for current state based on *percept*  
and past actions

calculate outcome probabilities for actions, given action  
descriptions and prob of current states.

$a_1 \rightarrow$  out<sub>1</sub>  
 $a_1 \rightarrow$  out<sub>2</sub>  
 $a_2 \rightarrow$  out<sub>3</sub>  
 $a_2 \rightarrow$  out<sub>4</sub>  
 $a_3 \rightarrow$  out<sub>5</sub>

select *action* with highest expected utility given prob of outcomes  
and utility information.

**return** *action*

And so on



## Decision Theoretic Agent

*state*

**function** DT-Agent (*percept*) **returns** *action*

**static:** a set probabilistic *belief* about the state of the world

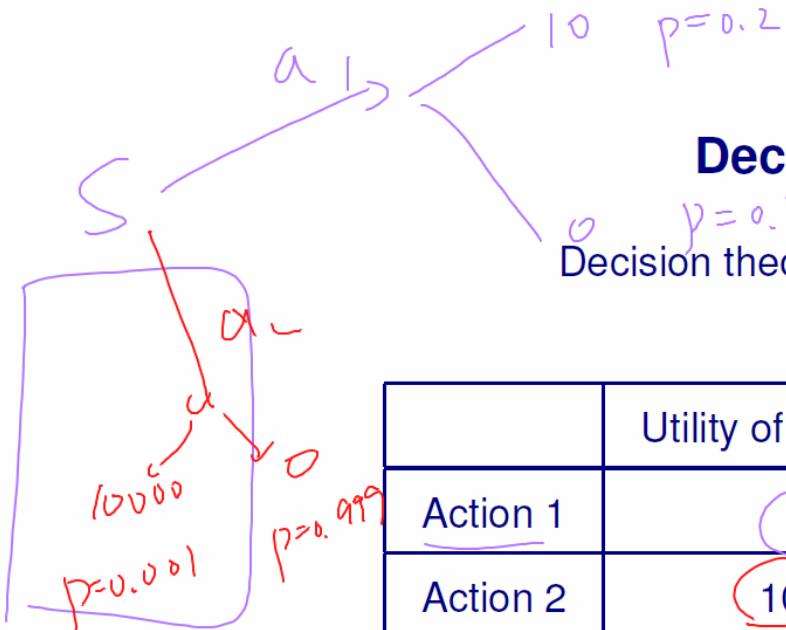
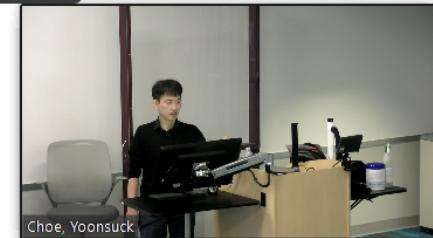
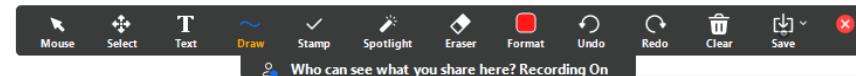
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select *action* with highest expected utility given prob of outcomes  
and utility information.

**return** *action*

So this is



## Decision Theory: Example

Decision theory = Probability theory + Utility theory

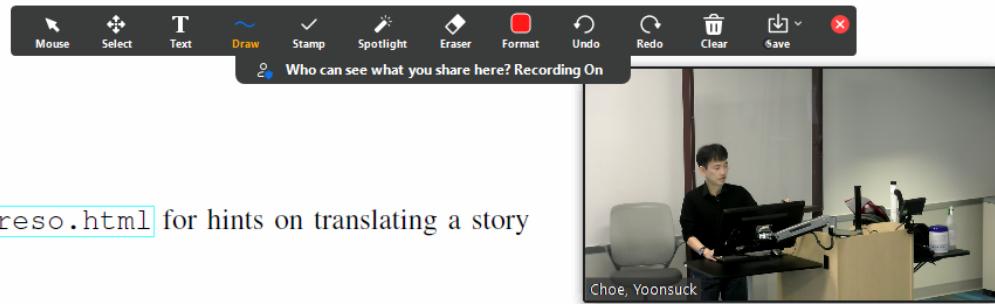
	Utility of Resulting State	Probability
Action 1	10 or 0	0.2, 0.8, respectively
Action 2	10000 or 0	0.001, 0.999, respectively
Action 3	5 or 0	0.799, 0.201, respectively

Which action would an optimal Decision Theoretic Agent take?

Of 0, then this has a probability of 0 point 0 0 one, and probably t of your point 9, 9, 9, and so on, and same fractio

- $Adored(x)$  : child  $x$  is adored.
- $Fed(x)$  : child  $x$  is fed well.
- $Happy(x)$  : child  $x$  is happy.

See <https://www.cs.utexas.edu/users/novak/reso.html> for hints on translating a story into FOL and proving it using resolution.



## 1.4 Programming

**Problem 7 (25 pts):** ~~Unification algorithm in Python.~~

For this programming component, you will be implementing a simple resolution-based theorem prover in Python.

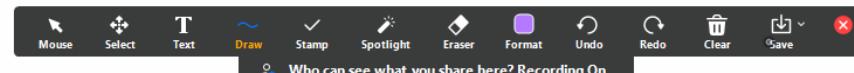
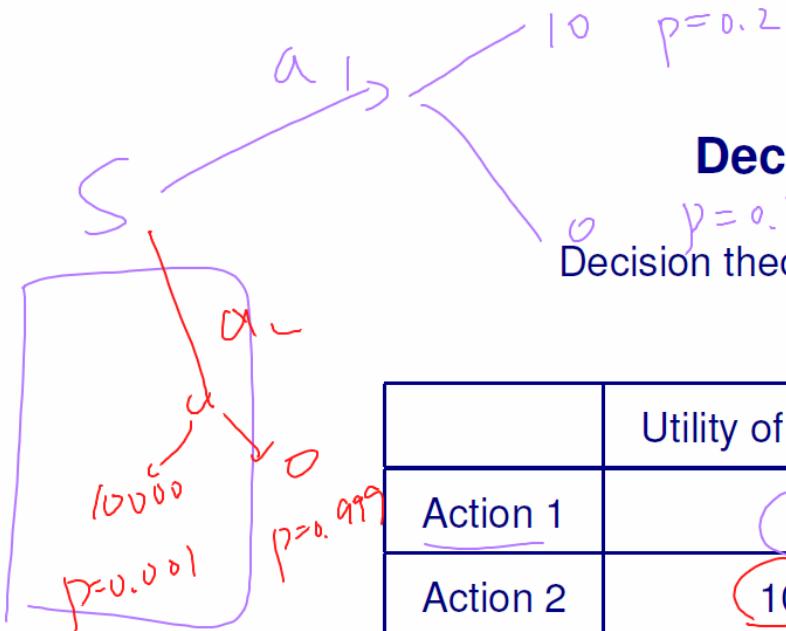
- Download the `resolution.ipynb` file from Canvas→Files→Assignment.
- Then upload to <https://research.colab.google.com> (use your TAMU NetID to login), and run it.
- Look at the test code to get yourself familiarized with the provided facilities, such as `resolve()`.
- You can create new code cells to experiment.

The only part you need to implement is the `prover()` function. You will be implementing the *two-pointer method* (same as level saturation), using the *set-of-support strategy*.  
for propositional logic

Here's a description of the algorithm<sup>1</sup>:

1. Initialize the two pointers (simply, the clause index) so that you will be using the set-of-support strategy. This can be done in the following way.
  - Set the "inner loop" pointer to the front of the list of clauses.
  - Set the "outer loop" By the way, this is for approval. for for position. to the first clause resulting from the negated conclusion.
  - Go to Step 2.

You are screen sharing



## Decision Theory: Example

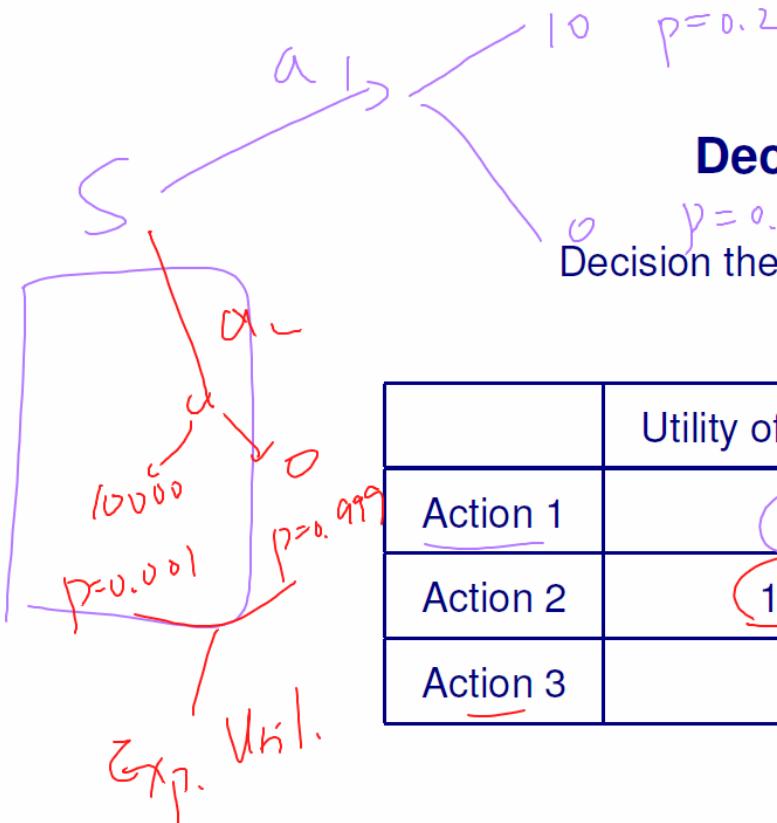
Decision theory = Probability theory + Utility theory



	Utility of Resulting State	Probability
Action 1	10 or 0	0.2, 0.8, respectively
Action 2	10000 or 0	0.001, 0.999, respectively
Action 3	5 or 0	0.799, 0.201, respectively

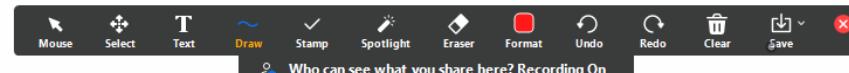
Which action would an optimal Decision Theoretic Agent take?

Then what is the expected Tuesday for this? and



## Decision Theory: Example

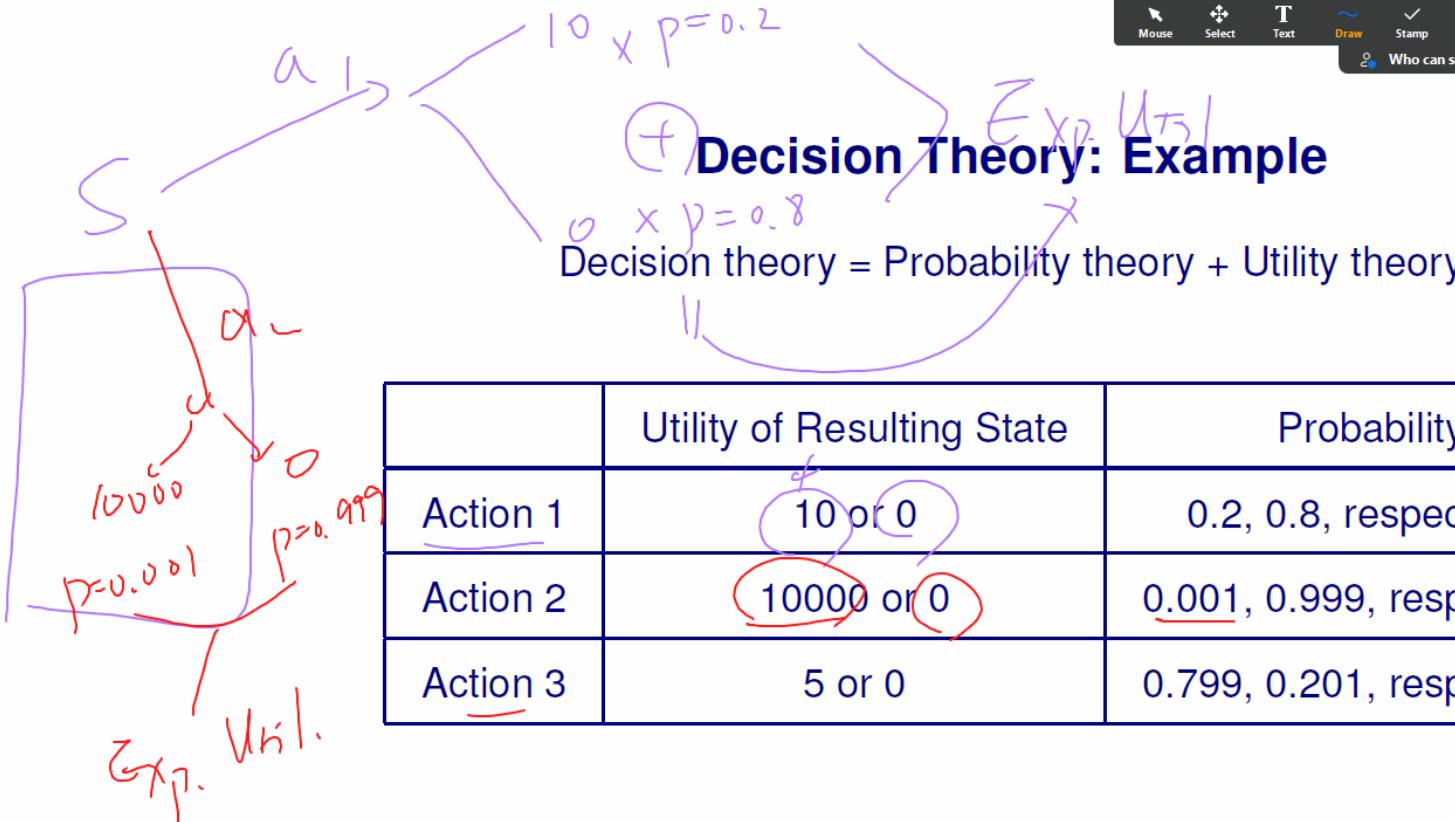
Decision theory = Probability theory + Utility theory



	Utility of Resulting State	Probability
Action 1	10 or 0	0.2, 0.8, respectively
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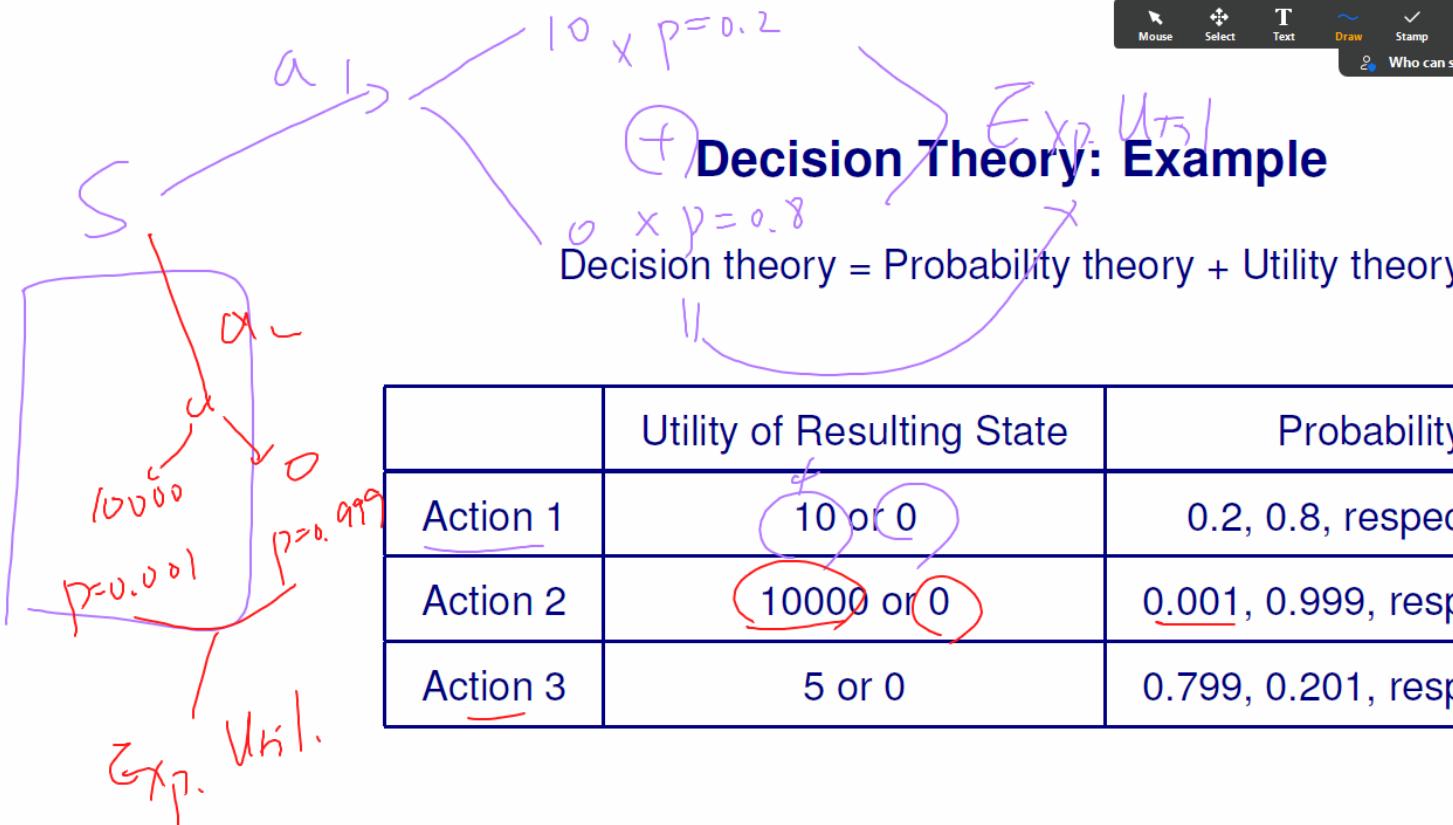
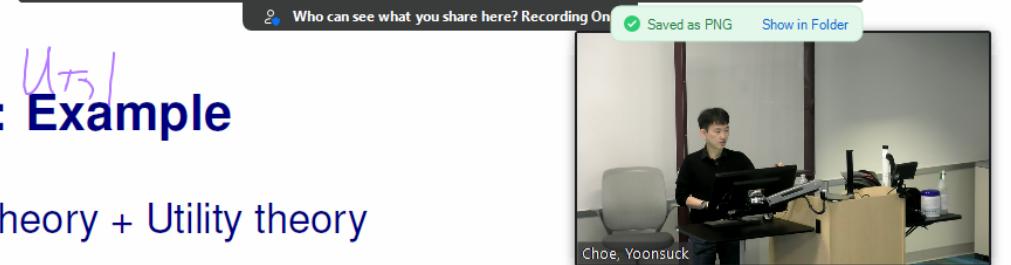
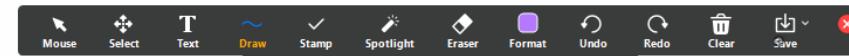
Which action would an optimal Decision Theoretic Agent take?

And what is the expected utility for that? So basically



Which action would an optimal Decision Theoretic Agent take?

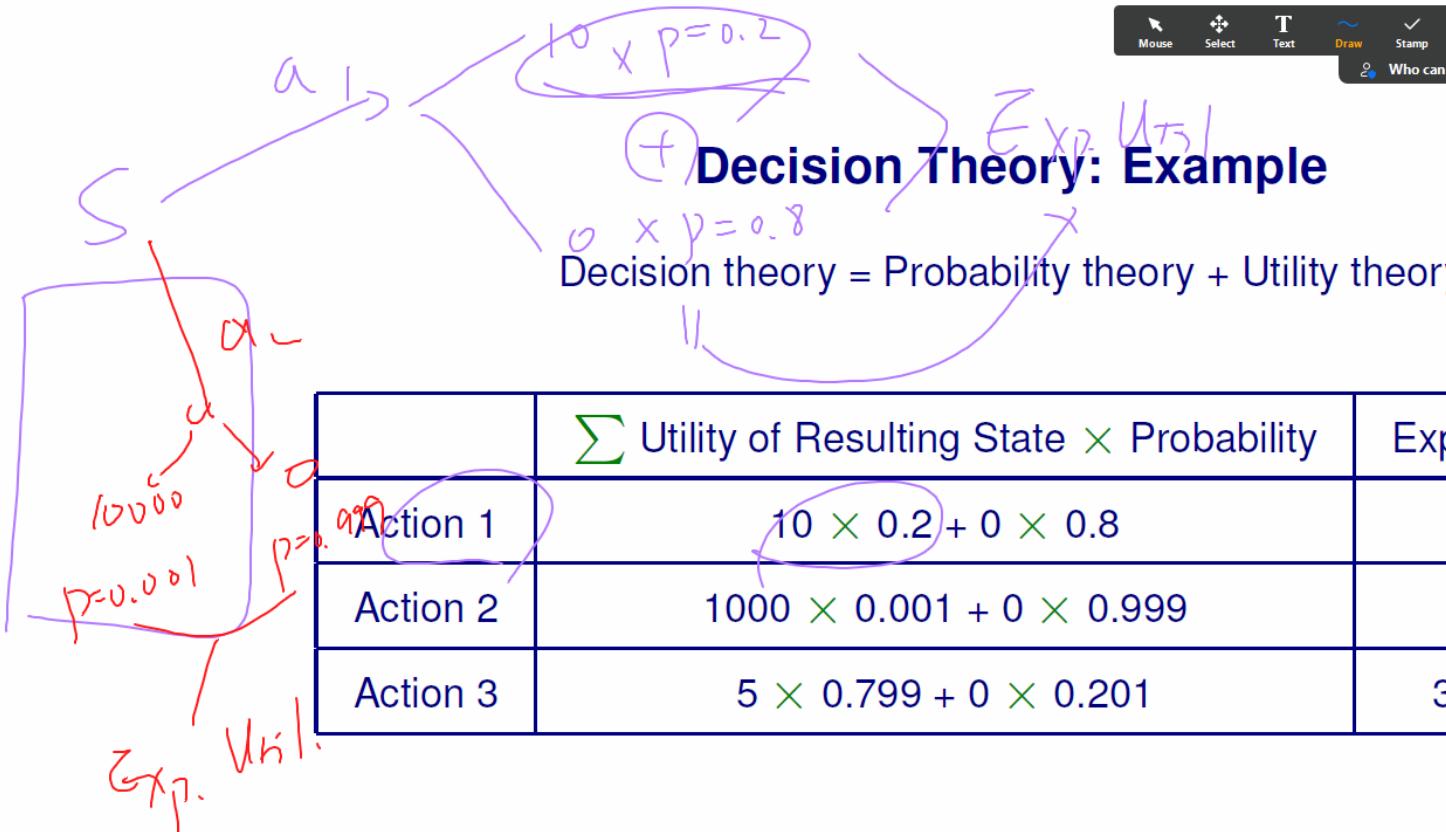
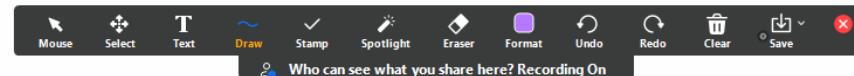
So basically it'd be this times that plus this time is that  
that'd be the expected utility



	Utility of Resulting State	Probability
Action 1	10 or 0	0.2, 0.8, respectively
Action 2	10000 or 0	0.001, 0.999, respectively
Action 3	5 or 0	0.799, 0.201, respectively

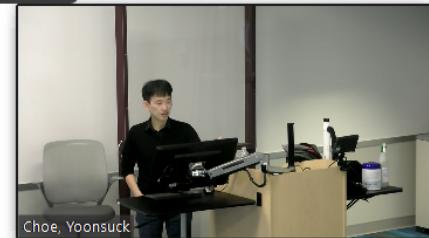
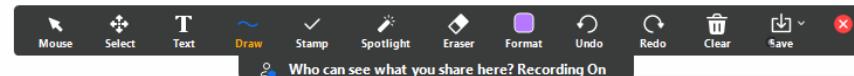
Which action would an optimal Decision Theoretic Agent take?

So basically it'd be this times that plus this time is that  
that'd be the speed utility and same for the action to any



Action 3 has the maximum expected utility, thus action 3 will be carried out.

So what we have here is the first one action, one yeah, 10 times point 2, and then



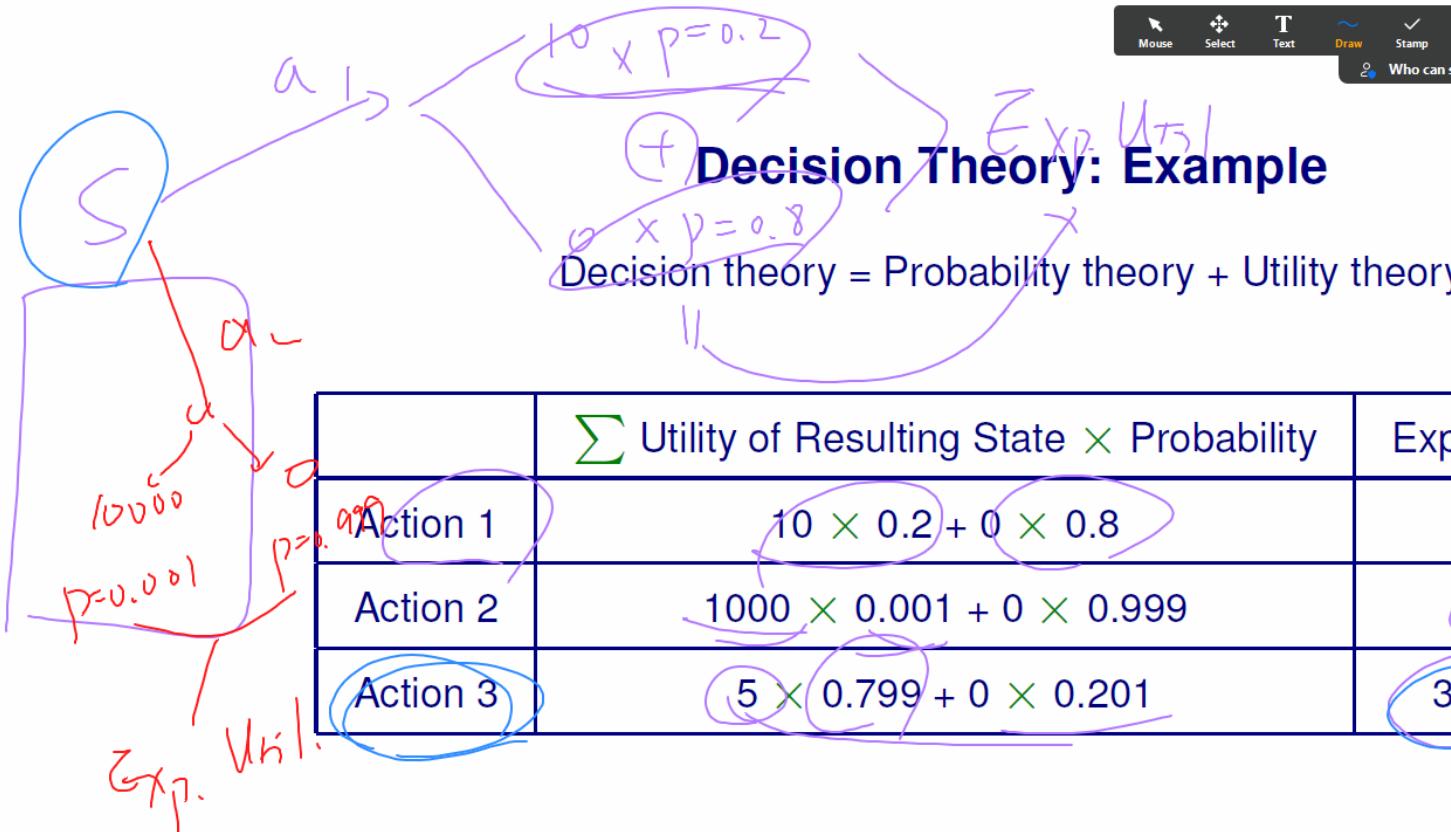
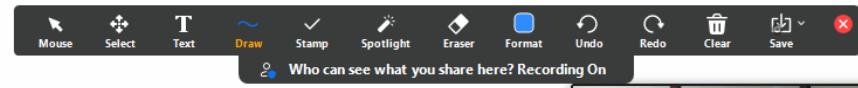
## Decision Theory: Example

Decision theory = Probability theory + Utility theory

	$\sum$ Utility of Resulting State $\times$ Probability	Expected Utility
Action 1	$10 \times 0.2 + 0 \times 0.8$	2
Action 2	$1000 \times 0.001 + 0 \times 0.999$	1
Action 3	$5 \times 0.799 + 0 \times 0.201$	3.995

Action 3 has the maximum expected utility, thus action 3 will be carried out.

And so in that case you get 3.9, 9, 5, as they expect you to



Action 3 has the maximum expected utility, thus action 3 will be carried out.

Okay, so that's it for today so 0 and start working on your

Homework 3 resolution.ipynb

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Code Text

clause representation:

```
[<positive-proposition-list>, <negative-proposition-list>]
```

proposition-list representation:

```
[ 'p', 'q', 'r' ]
```

Note: 'p', 'q', 'r', 's' are propositions : CASE SENSITIVE!

Example clause:

```
[[['p', 'q'], ['r']]] : This is clause P ∨ Q ∨ ~R
```

...  
DEBUG=True  
pos neg

```
#-----  
def rm_item(lst, item):  
#-----  
    ...  
    function: rm_pred()
```

They put all the narrative it was in the second list list, and that's the close

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Choe, Yoonsuck

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print("null? "+str(null\_p(test5)))

test1  
resolving: [['p', 'q'], ['r']] and [[], ['p']]  
resolvent = [['q'], ['r']]  
null? False

test2  
resolving: [['p'], []] and [[], ['p']]  
resolvent = [[], []]  
null? True

test3  
resolving: [['p', 'q'], ['r']] and [[['r']], ['p']]  
resolvent = False  
null? False

test4  
resolving: [['p', 'q'], ['r']] and [[['r']], []]  
resolvent = [['p', 'q'], []]  
null? False

test5  
resolving: [['p', 'q'], ['r']] and [[['r'], 'p'], []]

Test 1

$P \vee Q \vee \neg R \rightarrow Q \vee \neg R$

$\neg P$

$[['q'], ['r']]$



Choe, Yoonsuck

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```
theorem2 = [ ] # enter the example theorem in the homework

theorem3 = [ ] # enter your own example for testing

#-----
# prover() function : you must implement this function
#-----
def prover(thm, goal):
#-----
    ...
    function prover: implement this

    two-pointer method, with set of support
    - arguments:
        thm : theorem
        goal : integer index (clause number where the negated conclusion starts)
    - show resolution steps
    - if null_p checks, return True (theorem proven)
    - otherwise return False
    ...

    print('\nprover():\n\nTheorem: ')
```

Choe, Yoonsuck

resolution.ipynb hw3-22fall.pdf slide05-prob.pdf

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Close right to use the set of support, approach

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- Move the "inner loop" pointer forward one clause.
- If the "outer loop" pointer goes beyond the last clause in the list, stop; the theorem cannot be proved. Return "failure".
- If the "inner loop" pointer has not reached the "outer loop" pointer, go to the Resolve step (Step 2).
- Otherwise, reset the "inner loop" pointer to the front of the list of clauses and move the "outer loop" pointer forward one clause, then go to the Resolve step (Step 2).

Testing requirement:

1. Test the `prover()` function on the default theorem in the skeleton code.
2. Enter the Unicorn theorem in slide03-logic.pdf page 41 into your code as a new theorem. Test all three possible outcomes ( $M$  or  $G$  or  $H$ : try one conclusion at a time), given the premises (under "Given"). Don't forget to negate the conclusion.
3. In all example cases, report how many clauses were generated before deriving False (empty clause), or failing.



Include the following in one zip file:

1. `resolution.ipynb`; this should include all your code and test runs.

**Problem 8 (10 pts):** Simple knowledge base in Prolog.

Consider the following family tree (British royal family).





## Frame Problem

- In the previous slide, we cannot deduce if the following can be proven ( $G_1$  represents a particular lump of gold):

$At(G_1, [1, 1]), Result([Go([1, 1], [1, 2]), Grab(G_1), Go([1, 2], [1, 1])], S_0)$

- It is because the effect axioms say only *what should change*, but not *what does not change when actions are taken*.
- Initial solution: *Frame axioms*

$$At(o, x, s) \wedge (o \neq Agent) \wedge \neg Holding(o, s)$$

$$\rightarrow At(o, x, Result(Do(y, z), s)).$$

This says moving does not affect the gold when it is not held.

Problem is that you need  $O(AF)$  such axioms for all *(action, fluent)* pair ( $A$ : num of actions,  $F$ : num of fluent predicates).



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- It is because the effect axioms say only *what should change*, but not *what does not change when actions are taken*.

- Initial solution: *Frame axioms*

$At(G_1, [1, 1], S_3)$

$At(o, x, s) \wedge (o \neq Agent) \wedge \neg Holding(o, s)$

$\rightarrow At(o, x, Result(Go(y, z), s)).$

This says moving does not affect the gold when it is not held.

Problem is that you need  $O(AF)$  such axioms for all *(action, fluent)* pair ( $A$ : num of actions,  $F$ : num of fluent predicates).

One. The location of  $G_1$  one is 1 one in situation 3, whereas the situation 3 is basically this situation