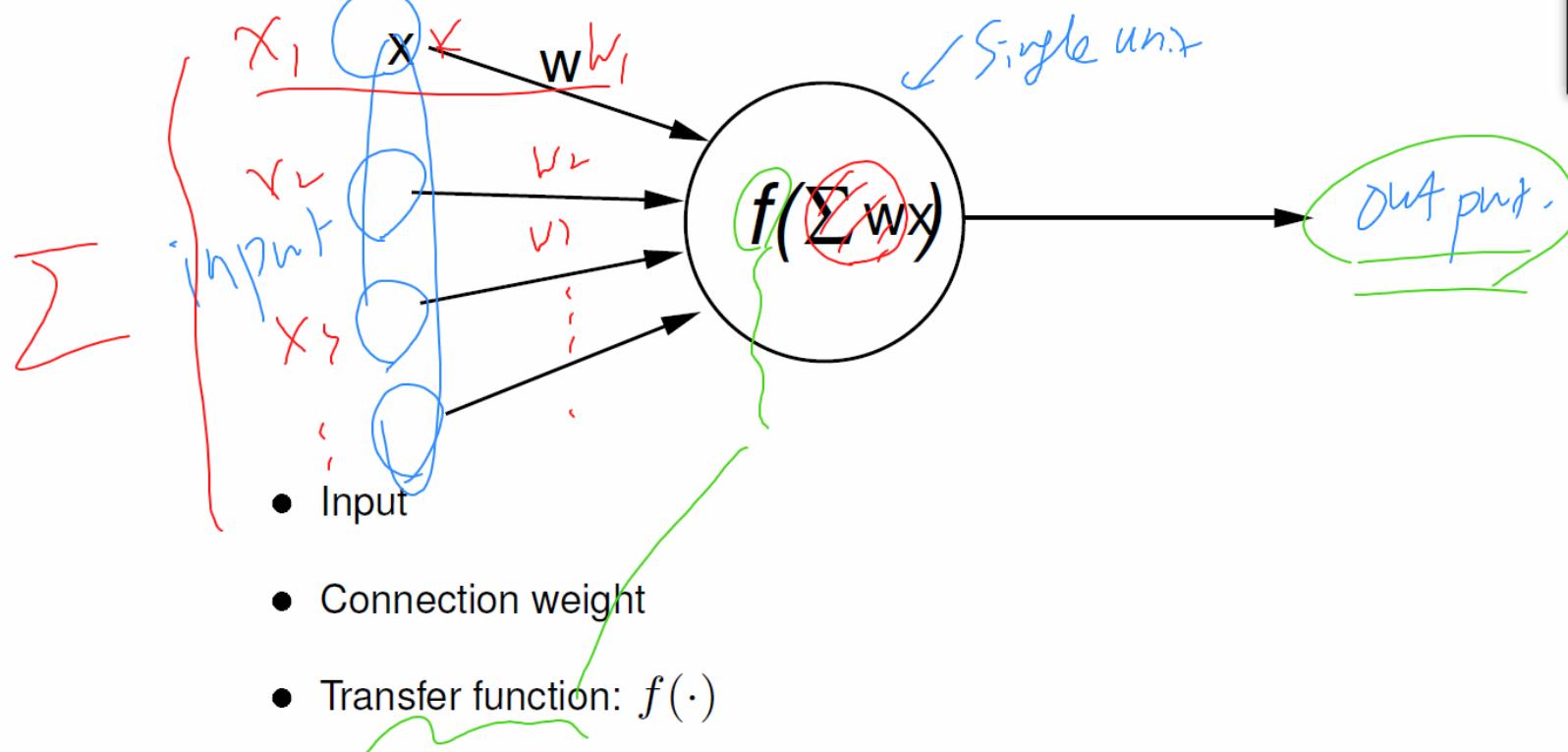


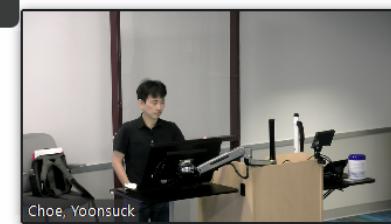


Abstraction of the Neuron in Neural Networks

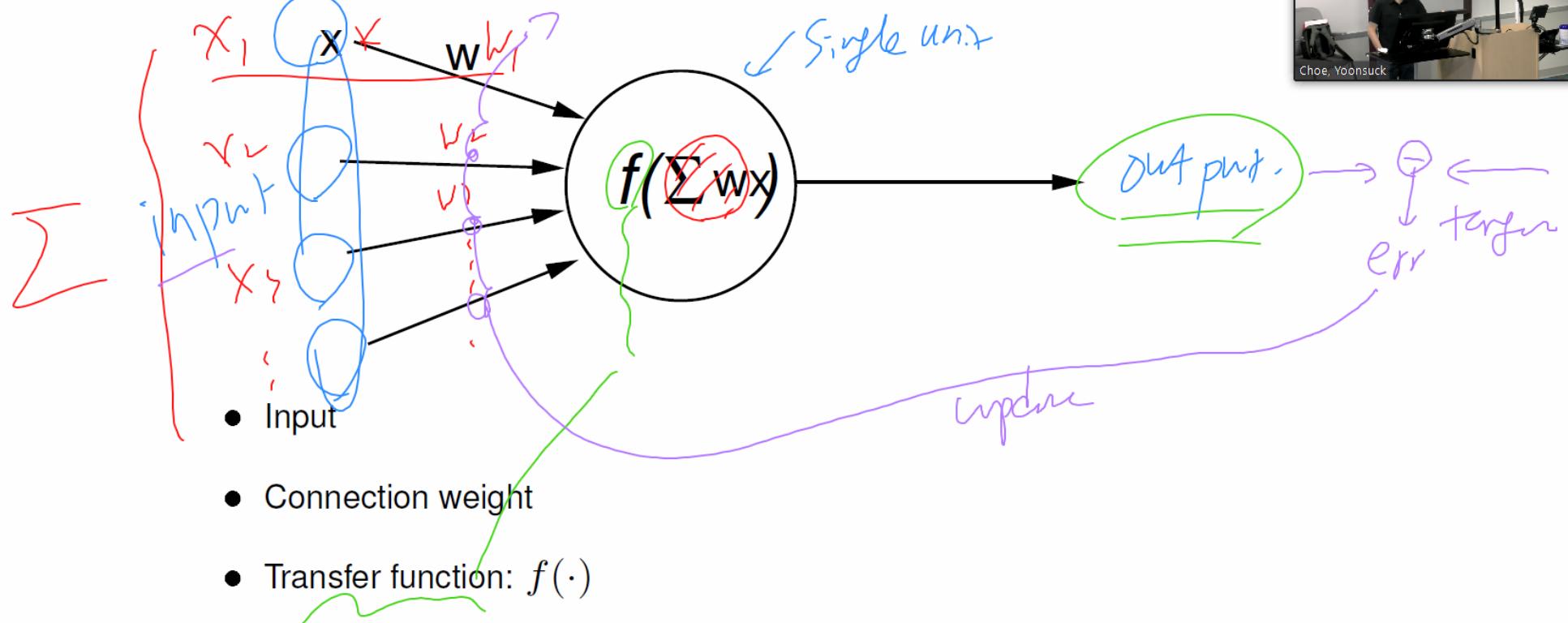


Typical transfer functions: step-function or sigmoid.

Then you get the output, so that's very simple and there could be many different forms of transfer functions will look

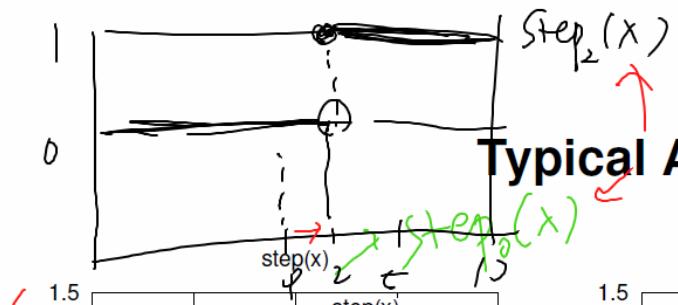


Abstraction of the Neuron in Neural Networks

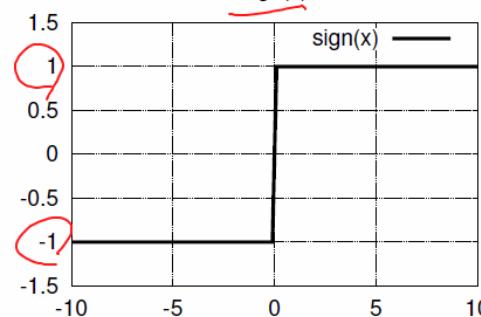


Typical transfer functions: step-function or sigmoid.

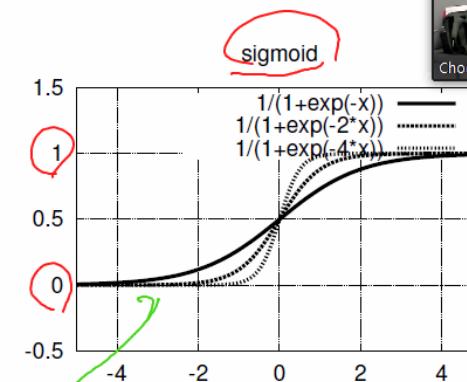
this arrow to update these question links so that the error
is reduced when you present the same input with the



Typical Activation Functions



Signum

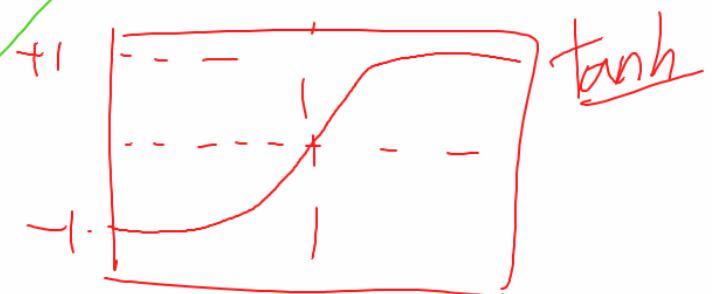


Sigmoid

- $\text{Step}_t(x) = 1 \text{ if } x \geq t, 0 \text{ if } x < t$
- $\text{Sign}(x) = +1 \text{ if } x \geq 0, -1 \text{ if } x < 0$

$$\bullet \text{Sigmoid}(x) = \frac{1}{1+e^{-x}}$$

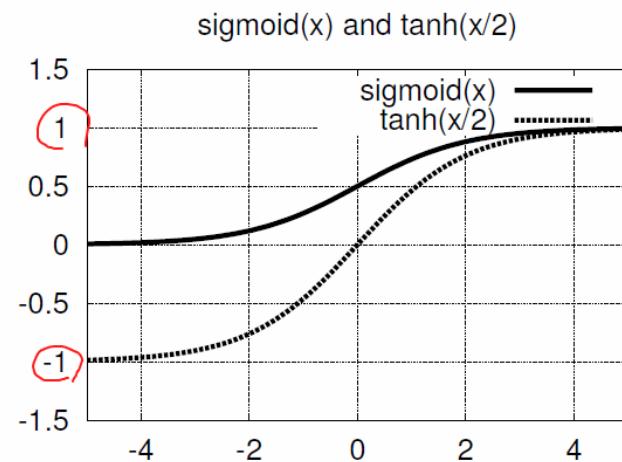
Note that $\text{Step}_t(x) = \text{Step}_0(x-t)$, which we will simply call $\text{Step}(x-t)$.



Then these 2 are the same

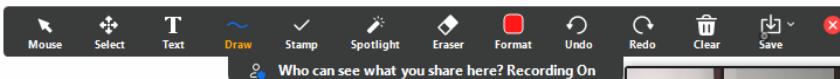


More Activation Functions: $\tanh(\frac{x}{2})$



- $Sigmoid(x) = \frac{1}{1+e^{-x}}$
- $\tanh(\frac{x}{2}) = \frac{1-e^{-x}}{1+e^{-x}}$))

And the functional form is this one over one minus the exponential of minus 6, divided by one plus exponential of minus X



Classification of Neural Networks

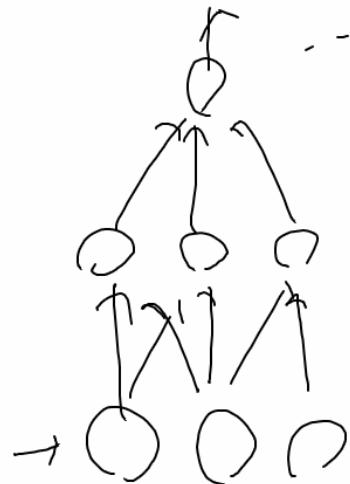
Teacher exists?

- Supervised (with teacher): perceptrons, backpropagation network, etc.
- Unsupervised (no teacher): self-organizing maps, etc.

multilayer perceptrons
neural networks

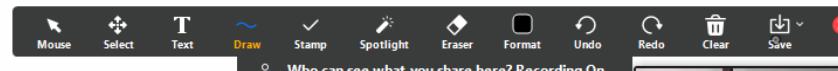
Recurrent connections?

- Feed-forward: perceptrons, backpropagation network, etc.
- Recurrent: Hopfield network, Boltzmann machines, SRN (simple recurrent network), LSTM, GRU, etc.



Feed forward

Classification of Neural Networks



Teacher exists?

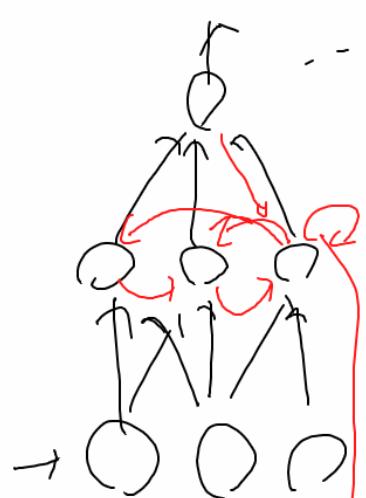
- Supervised (with teacher): perceptrons, backpropagation network, etc.
- Unsupervised (no teacher): self-organizing maps, etc.

multilayer perceptron
neural networks

Recurrent connections?

- Feed-forward: perceptrons, backpropagation network, etc.
- Recurrent: Hopfield network, Boltzmann machines, SRN (simple recurrent network), LSTM, GRU, etc.

So if there's no loop this is called the feed forward you know



Feed forward

Classification of Neural Networks



Choe, Yoonsuck

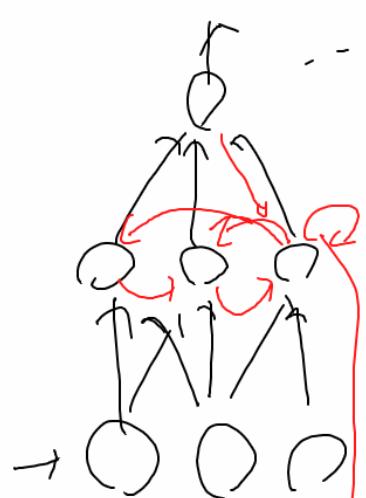
Teacher exists?

- Supervised (with teacher): perceptrons, backpropagation network, etc.
- Unsupervised (no teacher): self-organizing maps, etc.

multilayer perceptron
neural networks

Recurrent connections?

- Feed-forward: perceptrons, backpropagation network, etc.
- Recurrent: Hopfield network, Boltzmann machines, SRN (simple recurrent network), LSTM, GRU, etc.



Feed forward

Classification of Neural Networks



Teacher exists?

- Supervised (with teacher): perceptrons, backpropagation network, etc.
- Unsupervised (no teacher): self-organizing maps, etc.

*multilayer perceptron
neural networks*

Recurrent connections?

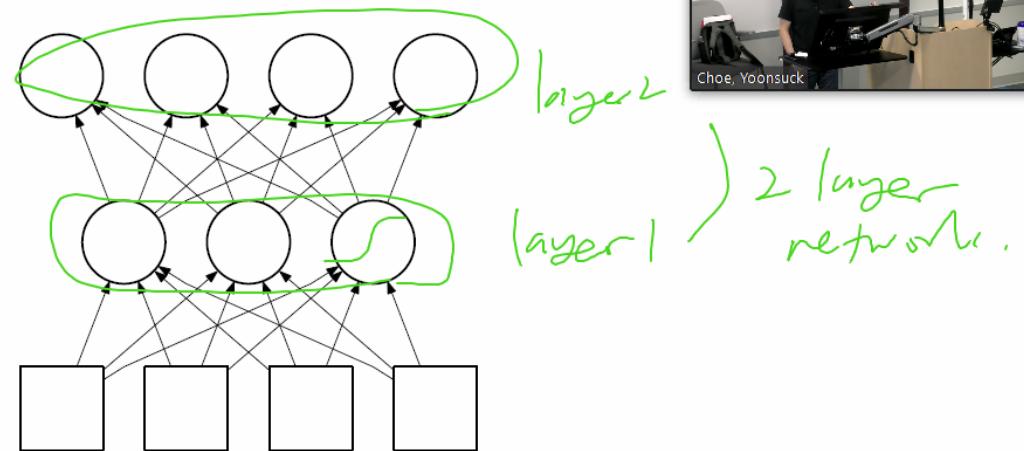
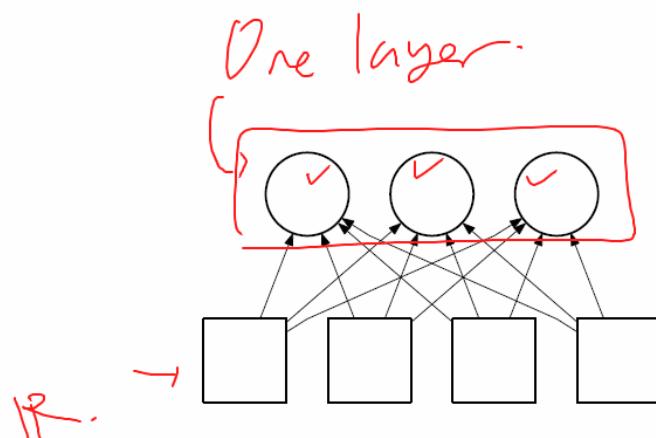
- Feed-forward: perceptrons, backpropagation network, etc.
- Recurrent: Hopfield network, Boltzmann machines, SRN (simple recurrent network), LSTM, GRU, etc.

Deep Learning

Okay, and there are several different instances of this and we'll probably go through some of these when we look into deep learning



Feedforward Networks

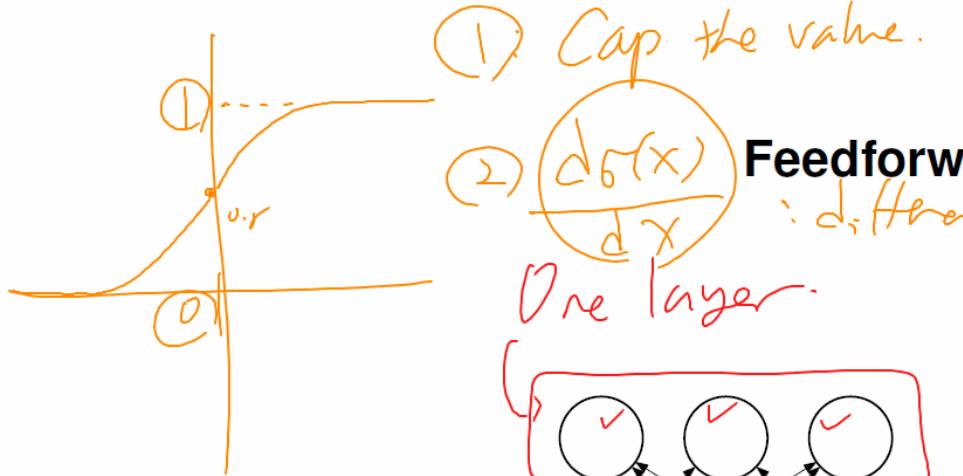


IP.

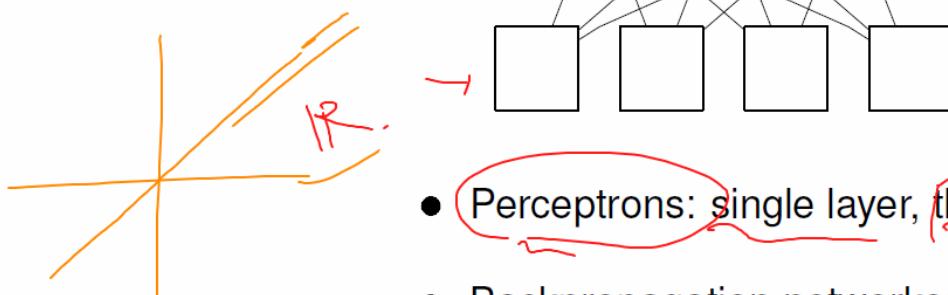
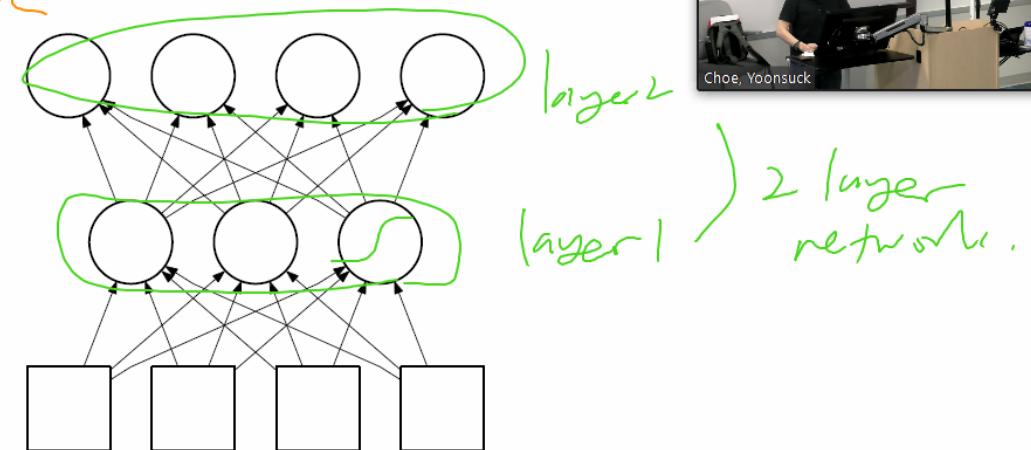
- Perceptrons: single layer, threshold-gated
- Backpropagation networks: multiple layers, sigmoid (or tanh) activation function.

ReLU \rightarrow Deep learning-

And again, these appear in deep learning, so we will only consider Sigmoid or hyperbolic tangent



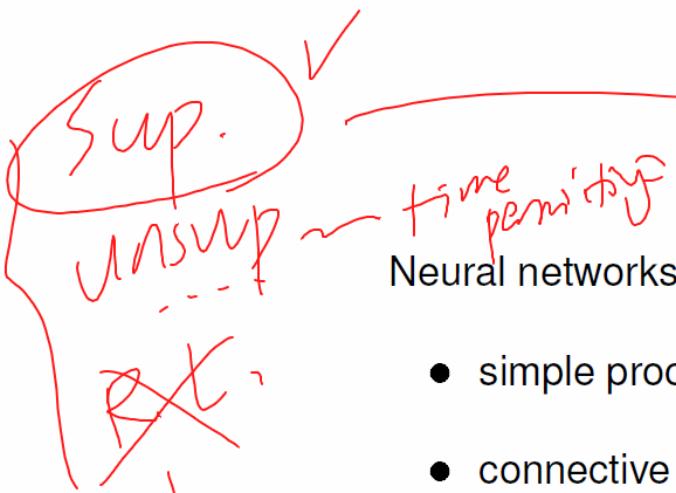
Feedforward Networks



- Perceptrons: single layer, threshold-gated.
- Backpropagation networks: multiple layers, sigmoid (or tanh) activation function.

$\text{ReLU} = \begin{cases} x & \text{if } x > 0 \\ 0 & \text{otherwise} \end{cases}$

Deep learning-



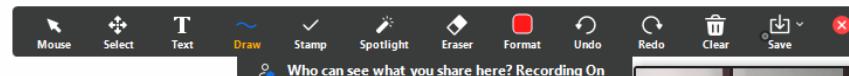
Neural Networks

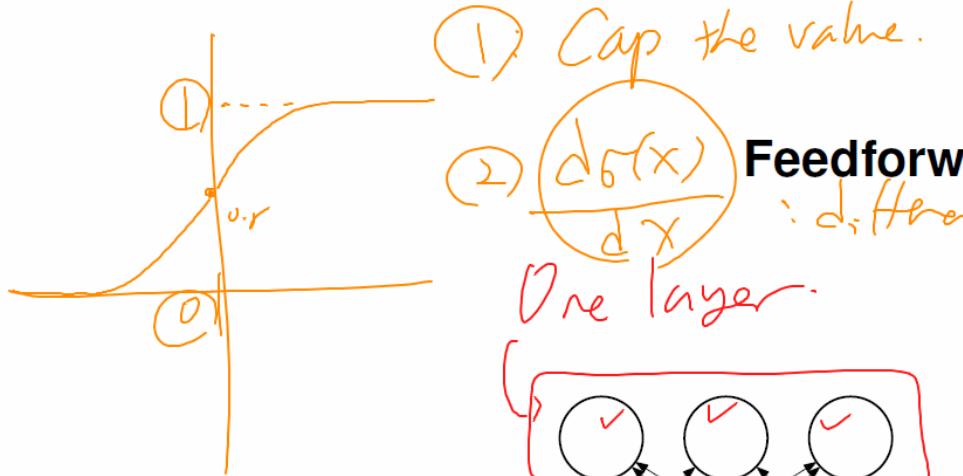
Neural networks is one particular form of learning from data.

- simple processing elements: called “units”, or “neurons”
- connective structure and associated connection weights
- learning: adaptation of connection weights

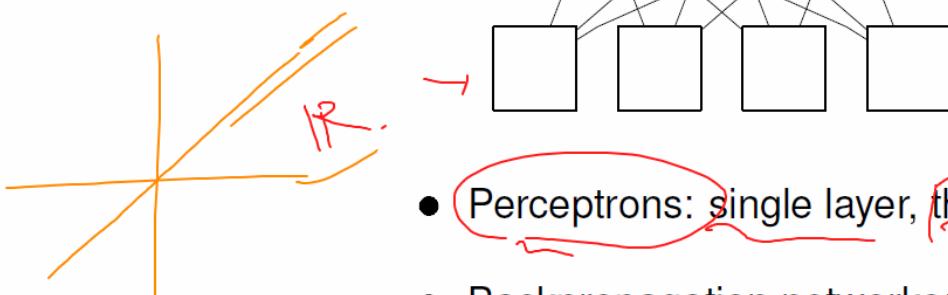
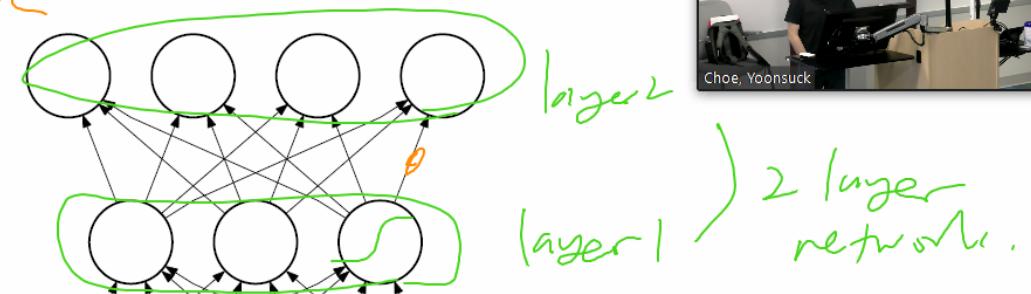
Neural networks mimic the human (or animal) nervous system.

D. Lemmij



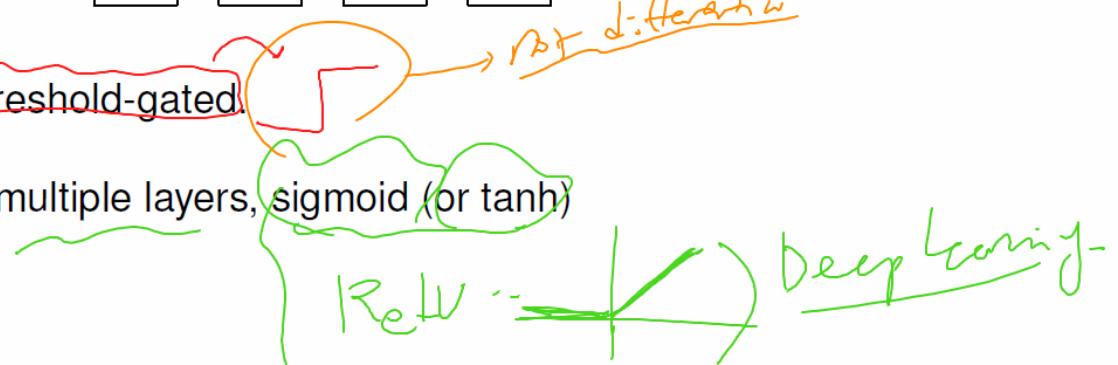


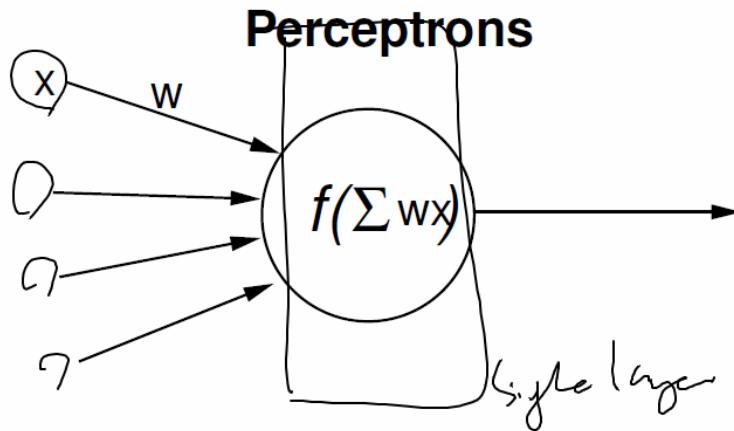
Feedforward Networks



- Perceptrons: single layer, threshold-gated.

- Backpropagation networks: multiple layers, sigmoid (or tanh) activation function.

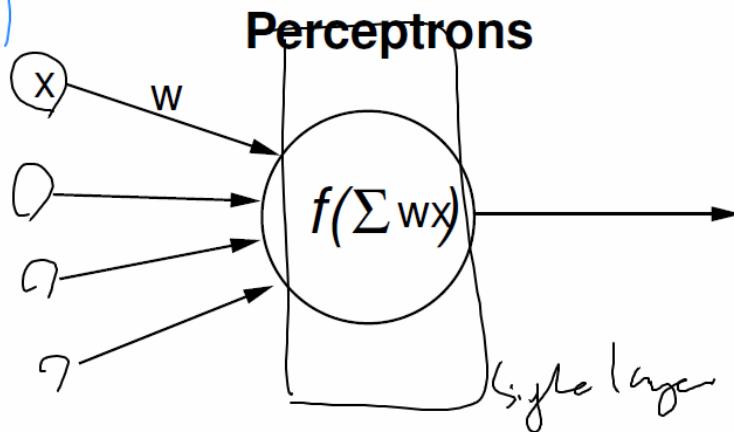
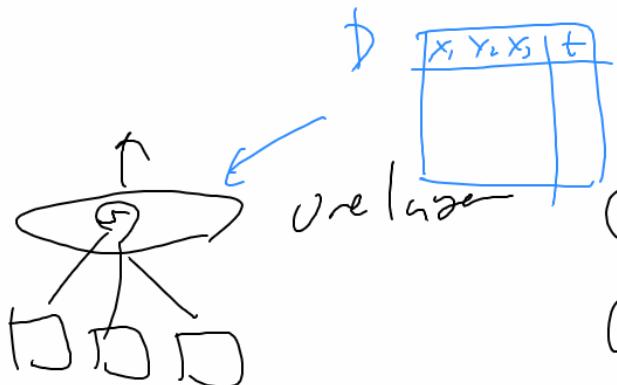




$$\begin{aligned}
 a_i &= \text{step}_t \left(\sum_{j=1}^n W_{ij} a_j \right) \\
 &= \text{step}_0 \left(\sum_{j=1}^n W_{ij} a_j - t \right) \\
 &= \text{step}_0 \left(t \times (-1) + \sum_{j=1}^n W_{ij} a_j \right) \\
 &= \text{step}_0 \left(\sum_{j=0}^n W_{ij} a_j \right), \text{ where } W_{i0} = t \text{ and } a_0 = -1 \quad (1)
 \end{aligned}$$

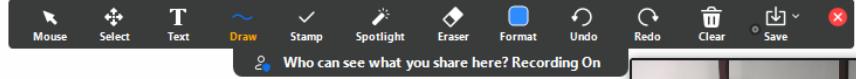
And then activation function is this step function



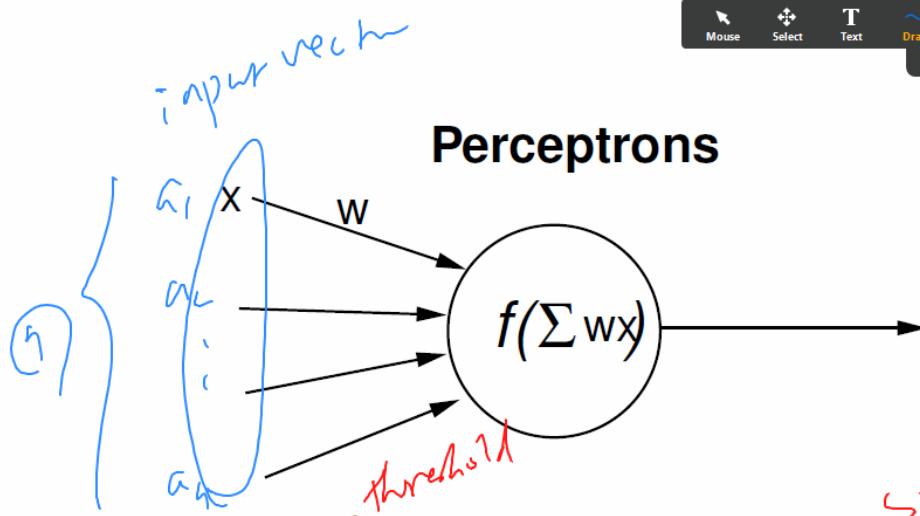
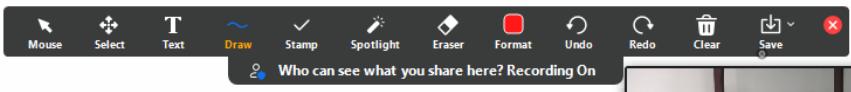


$$\begin{aligned}
 a_i &= \text{step}_t \left(\sum_{j=1}^n W_{ij} a_j \right) \\
 &= \text{step}_0 \left(\sum_{j=1}^n W_{ij} a_j - t \right) \\
 &= \text{step}_0 \left(t \times (-1) + \sum_{j=1}^n W_{ij} a_j \right) \\
 &= \text{step}_0 \left(\sum_{j=1}^n W_{ij} a_j \right), \text{ where } W_{i0} = t \text{ and } a_0 = -1 \quad (1)
 \end{aligned}$$

Let's say t one t right because you have 2 output values.
Alright.



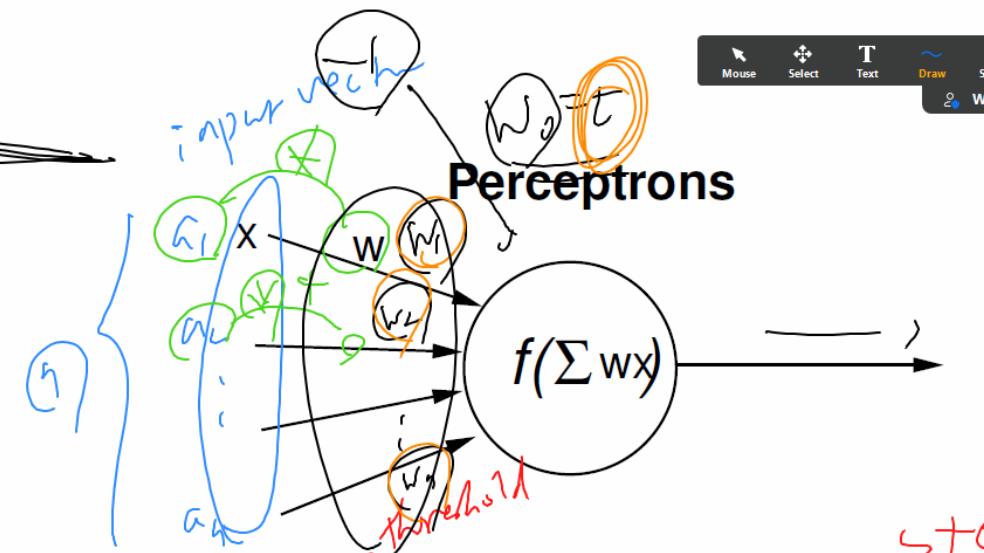
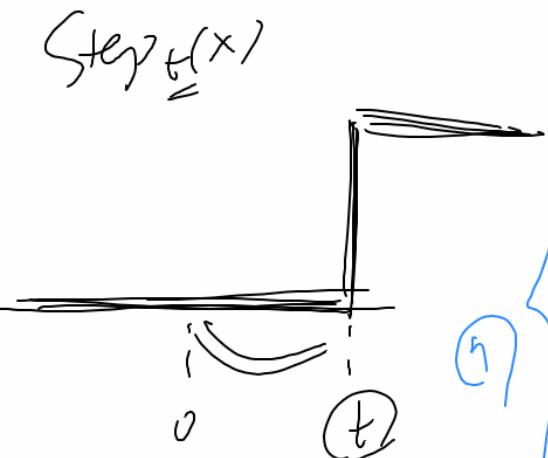
x_1	x_2	x_3	t_1	t_2



$$step_t(x) = step_0(x - t)$$

$$\begin{aligned}
 a_i &= step_t \left(\sum_{j=1}^n W_{ij} a_j \right) \\
 &= step_0 \left(\sum_{j=1}^n W_{ij} a_j - t \right) \\
 &= step_0 \left(t \times (-1) + \sum_{j=1}^n W_{ij} a_j \right) \\
 &= step_0 \left(\sum_{j=1}^n W_{ij} a_j \right), \text{ where } W_{i0} = t \text{ and } a_0 = -1 \quad (1)
 \end{aligned}$$

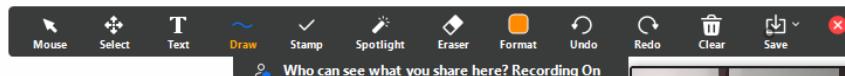
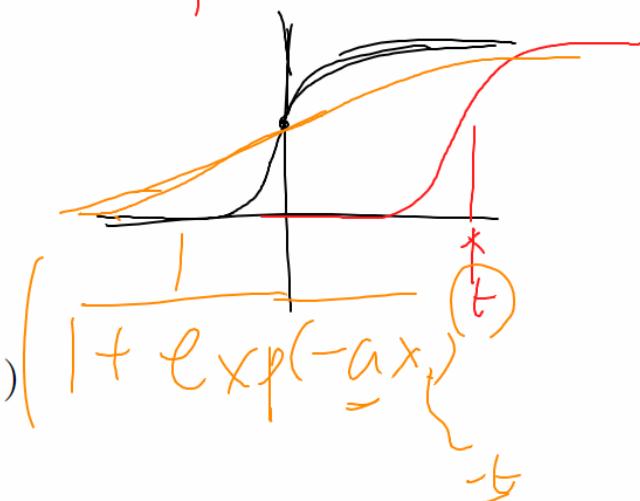
We saw that step T of X equals step 0 x minus t so that's how this becomes that



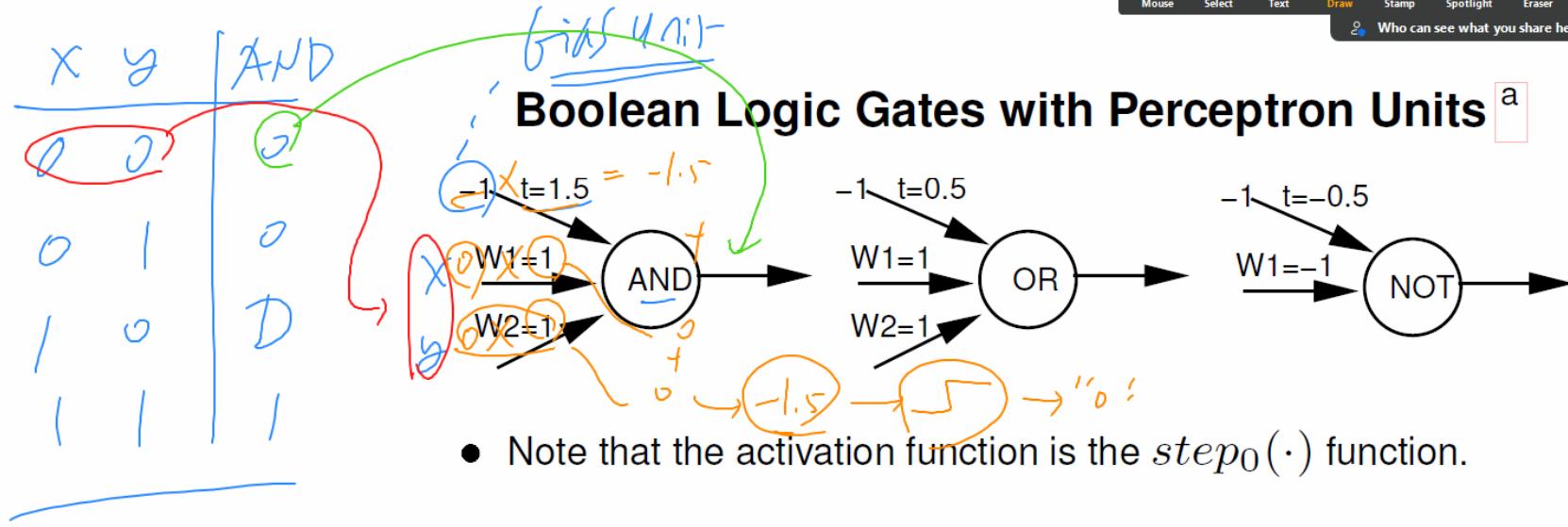
$$\begin{aligned}
 a_i &= \text{step}_t \left(\sum_{j=1}^n W_{ij} a_j \right) \\
 &= \text{step}_0 \left(\sum_{j=1}^n W_{ij} a_j - t \right) \\
 &= \text{step}_0 \left(t \times (-1) + \sum_{j=1}^n W_{ij} a_j \right) \\
 &= \text{step}_0 \left(\sum_{j=1}^n W_{ij} a_j \right), \text{ where } W_{i0} = t \text{ and } a_0 = -1 \quad (1)
 \end{aligned}$$

I guess you're already training that way, like Why, do you need a personal value and not Oh, yeah, so you see why this is very, very important.

$$\text{step}_t(x) = \text{step}_0(x-t)$$



You are screen sharing Stop Share

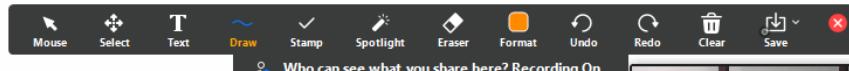


Boolean Logic Gates with Perceptron Units ^a

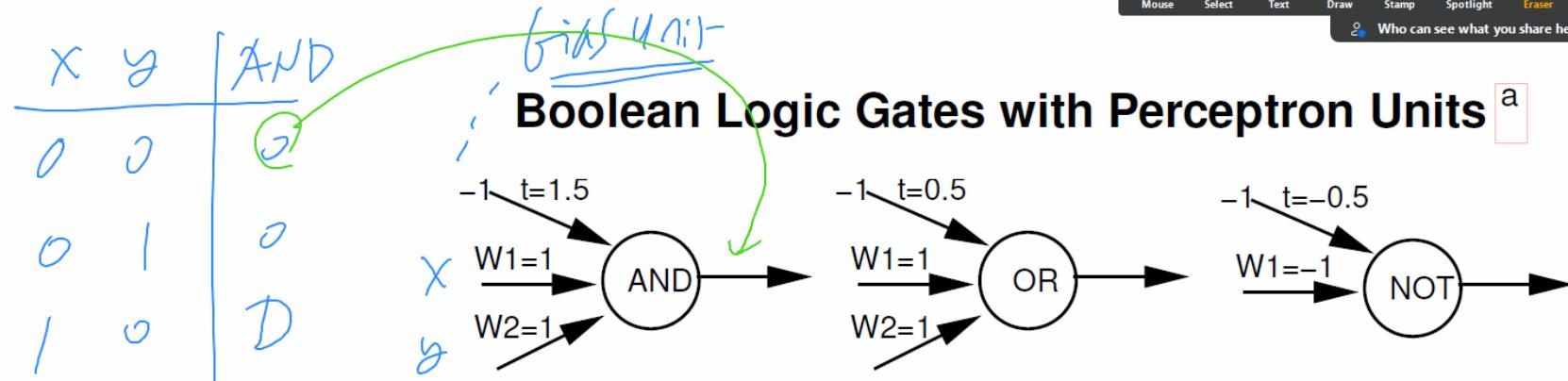
- Note that the activation function is the $\text{step}_0(\cdot)$ function.
- Perceptrons can represent basic boolean functions.
- Thus, a network of perceptron units can compute any Boolean function.

What about XOR or EQUIV?

^aSame as Russel & Norvig p.570, figure 19.6



x	y	AND
0	0	0
0	1	0
1	0	0
1	1	1



- Note that the activation function is the $\text{step}_0(\cdot)$ function.
- Perceptrons can represent basic boolean functions.
- Thus, a network of perceptron units can compute any Boolean function.

What about XOR or EQUIV?

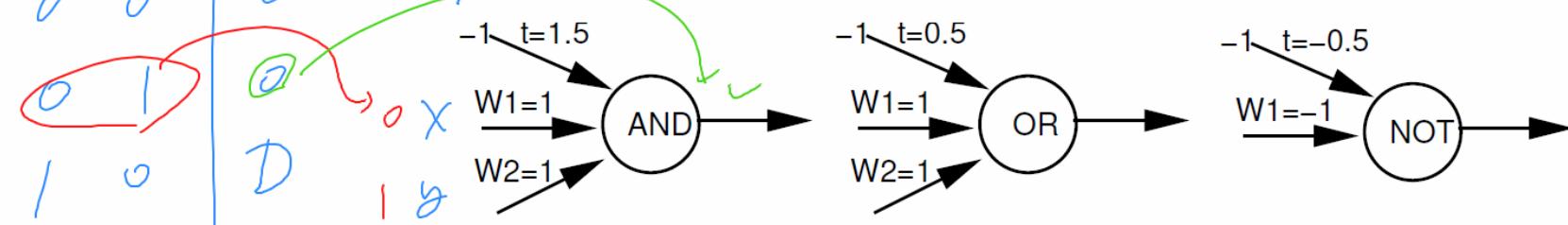
^aSame as Russel & Norvig p.570, figure 19.6



X	Y	AND
0	0	0
0	1	0
1	0	0
1	1	1

bias unit

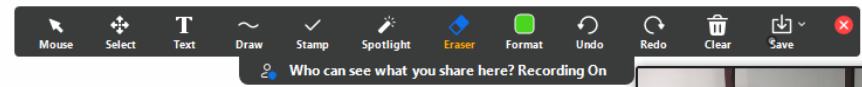
Boolean Logic Gates with Perceptron Units^a



- Note that the activation function is the $\text{step}_0(\cdot)$ function.
- Perceptrons can represent basic boolean functions.
- Thus, a network of perceptron units can compute any Boolean function.

What about XOR or EQUIV?

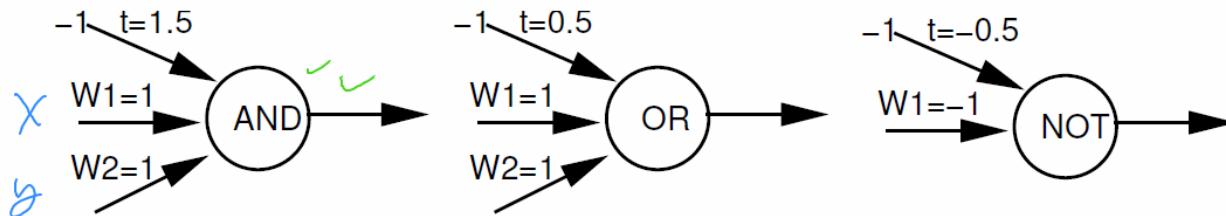
^aSame as Russel & Norvig p.570, figure 19.6



x	y	AND
0	0	0
0	1	0
1	0	0
1	1	1

bias unit

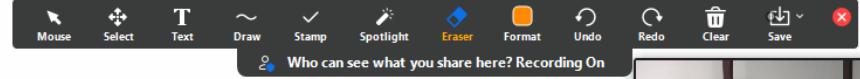
Boolean Logic Gates with Perceptron Units^a



- Note that the activation function is the $\text{step}_0(\cdot)$ function.
- Perceptrons can represent basic boolean functions.
- Thus, a network of perceptron units can compute any Boolean function.

What about XOR or EQUIV?

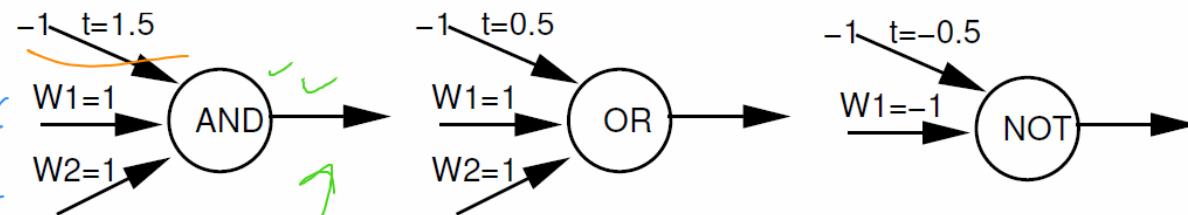
^aSame as Russel & Norvig p.570, figure 19.6



		AND
x	y	
0	0	0
0	1	0
1	0	0
1	1	1

bias unit

Boolean Logic Gates with Perceptron Units ^a

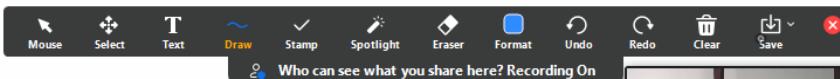


- Note that the activation function is the $\text{step}_0(\cdot)$ function.
- Perceptrons can represent basic boolean functions.
- Thus, a network of perceptron units can compute any Boolean function.

What about XOR or EQUIV?

^aSame as Russel & Norvig p.570, figure 19.6



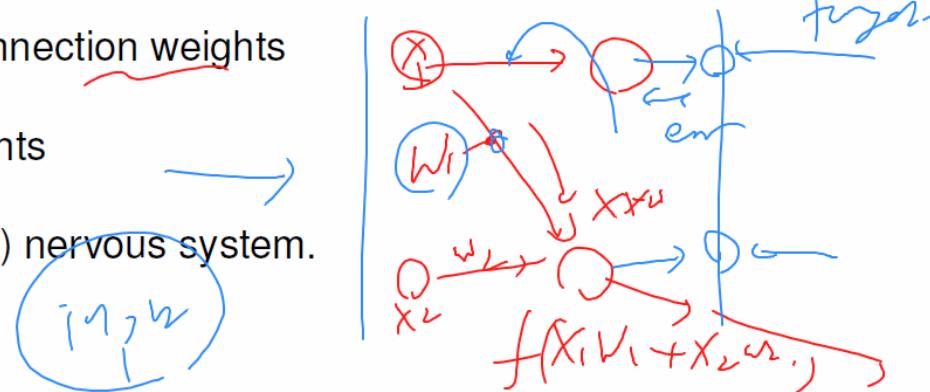


Neural Networks

Neural networks is one particular form of learning from data.

- simple processing elements: called “units”, or “neurons”
- connective structure and associated connection weights
- learning: adaptation of connection weights

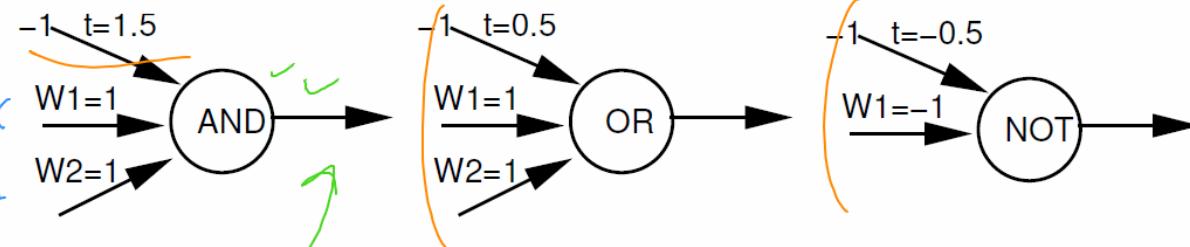
Neural networks mimic the human (or animal) nervous system.



X	Y	AND
0	0	0
0	1	0
1	0	0
1	1	1

bias unit

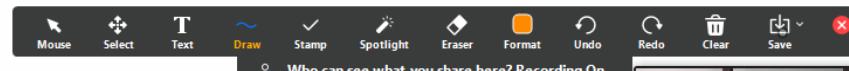
Boolean Logic Gates with Perceptron Units^a



- Note that the activation function is the $\text{step}_0(\cdot)$ function.
- Perceptrons can represent basic boolean functions.
- Thus, a network of perceptron units can compute any Boolean function.

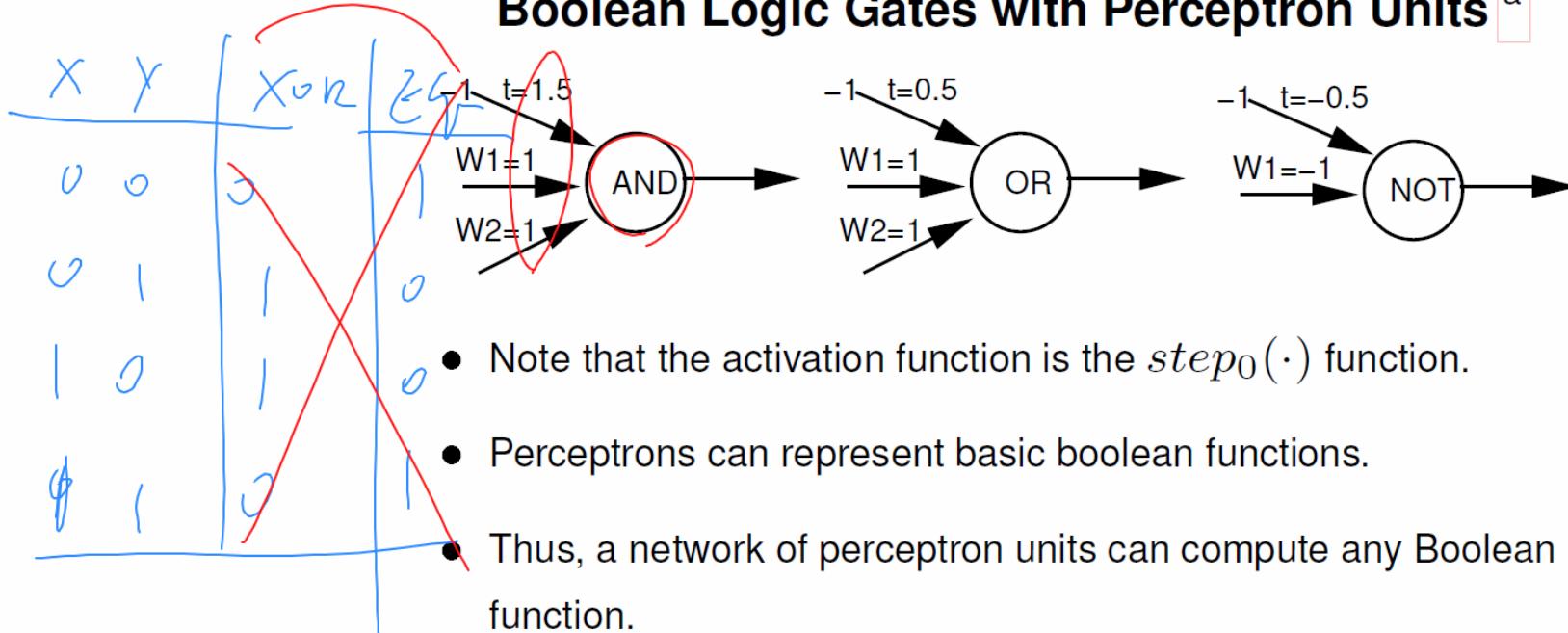
What about XOR or EQUIV?

^aSame as Russel & Norvig p.570, figure 19.6





Boolean Logic Gates with Perceptron Units ^a



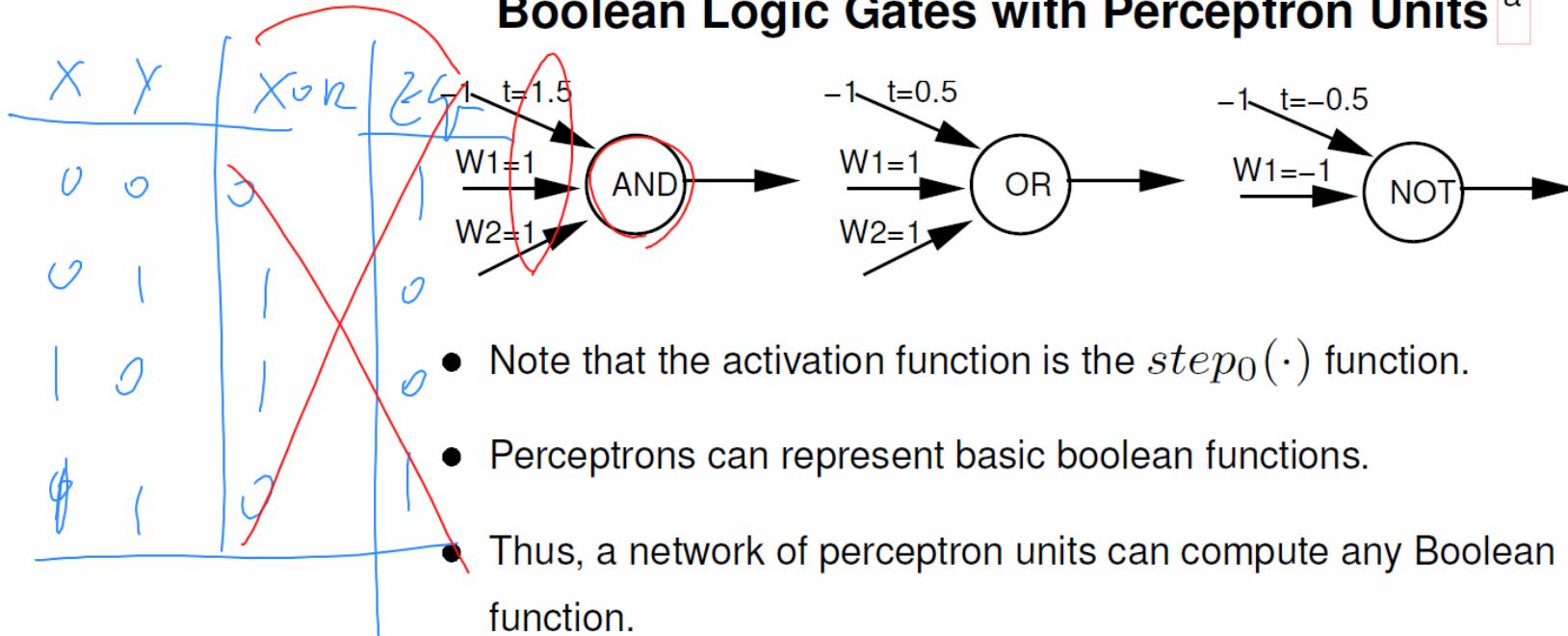
What about XOR or EQUIV?

^aSame as Russel & Norvig p.570, figure 19.6

realize only on is that this particular kind of sitting,
regardless of what connection rate you said, You cannot
learn these functions



Boolean Logic Gates with Perceptron Units^a



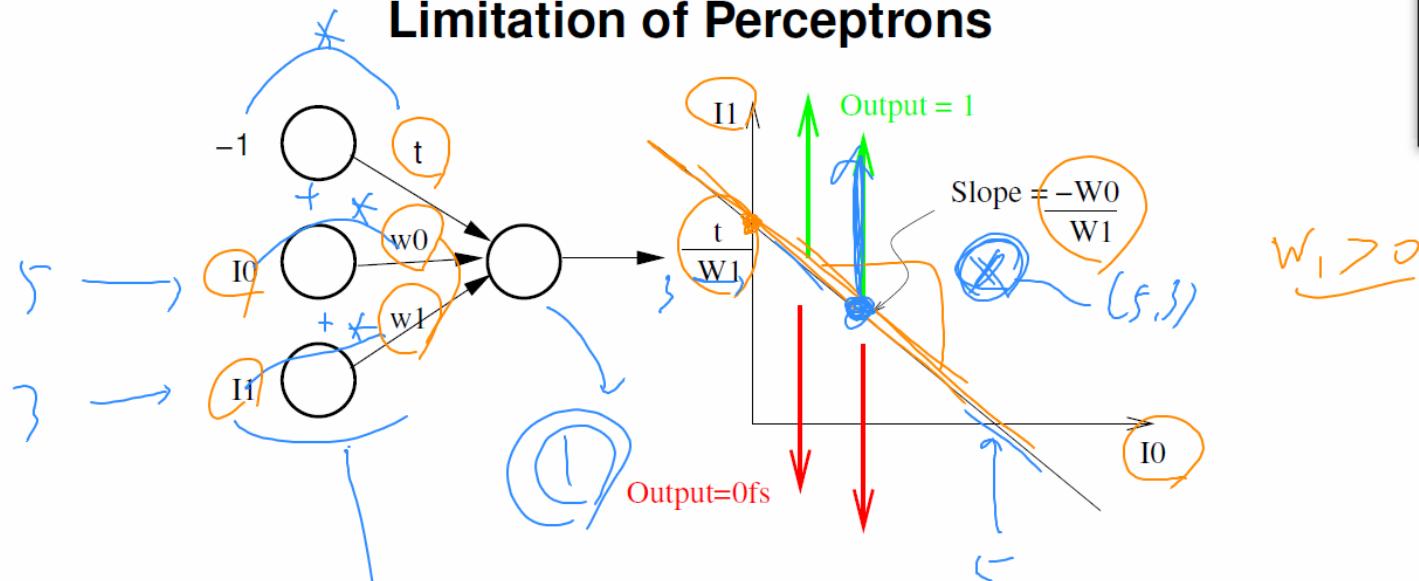
1985

What about XOR or EQUIV?

^aSame as Russel & Norvig p.570, figure 19.6



Limitation of Perceptrons



Perceptrons can only represent **linearly-separable** functions.

- Output of the perceptron:

$$W_0 \times I_0 + W_1 \times I_1 - t \geq 0, \text{ then output is } 1$$

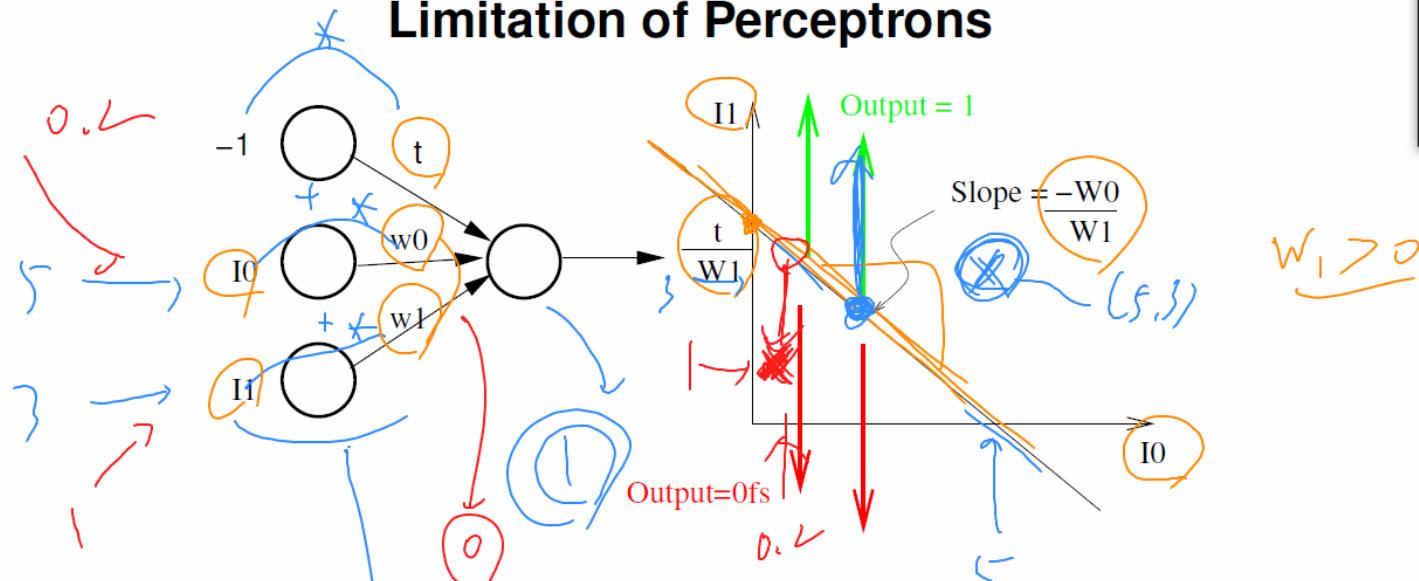
$$W_0 \times I_0 + W_1 \times I_1 - t < 0, \text{ then output is } 0$$

Input, this is input, 5, 3. And if it is all, or above this decision boundary, then this would give you the output of one

You are screen sharing Stop Share



Limitation of Perceptrons



- Output of the perceptron:

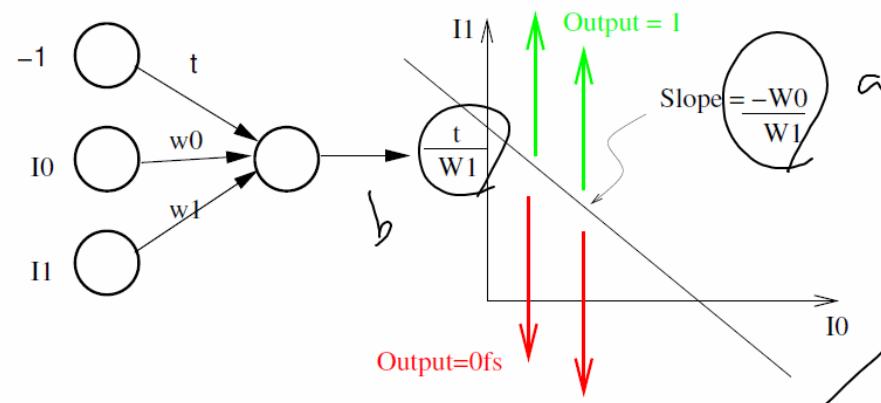
$$W_0 \times I_0 + W_1 \times I_1 - t \geq 0, \text{ then output is } 1$$

$$W_0 \times I_0 + W_1 \times I_1 - t < 0, \text{ then output is } 0$$

2, and then let's say the input was here and one so if you plug in point 2 and one then because it's below that line the output would be 0



Limitation of Perceptrons (cont'd)



$$w_0 I_0 + w_1 I_1 - t = 0$$

$$w_1 I_1 = -w_0 I_0 + t$$

- A geometrical interpretation of this is:

$$I_1 = \frac{-W_0}{W_1} \times I_0 + \frac{t}{W_1},$$

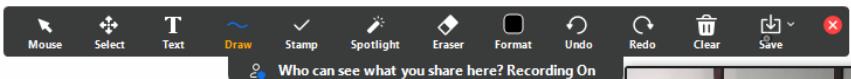
$$I_1 = \frac{-w_0}{w_1} I_0 + \frac{t}{w_1}$$

where points on or above the line, the output is 1, and 0 for those below the line (when W_1 is positive). Compare with

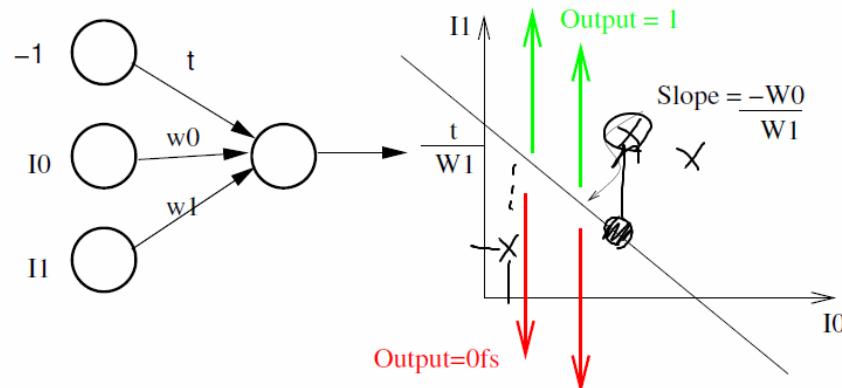
$$\underline{y} = \frac{-W_0}{W_1} \times \underline{x} + \frac{t}{W_1}.$$

$$\underline{y} = a \underline{x} + b$$

Note: When dividing both sides by W_1 , depending on the sign, the inequality can flip its direction (see previous page).



Limitation of Perceptrons (cont'd)



- A geometrical interpretation of this is:

$$I_1 = \frac{-W_0}{W_1} \times I_0 + \frac{t}{W_1}, \quad \geq 0$$

where points on or above the line, the output is 1, and 0 for those below the line (when W_1 is positive). Compare with

$$y = \frac{-W_0}{W_1} \times x + \frac{t}{W_1}.$$

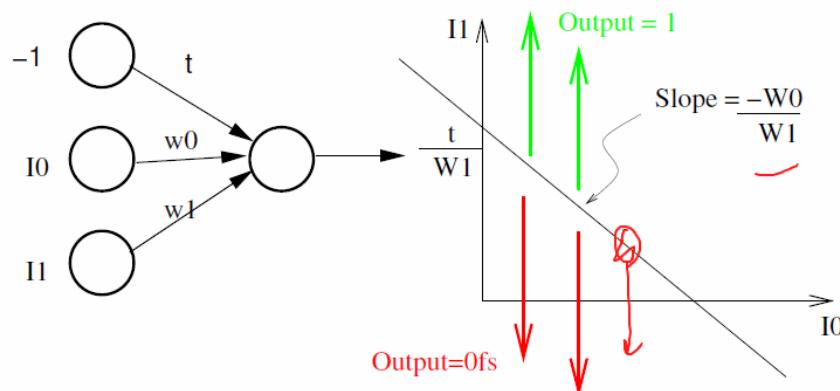
So now, if it is on or above, then it becomes 1'll put this one.
 If this particular look input is on our above that this
 decision boundary is one otherwise, if it is below did the

Note: When dividing both sides with $-W_1$, depending on the sign, the inequality

can flip its direction (see previous page).



Limitation of Perceptrons (cont'd)



- A geometrical interpretation of this is:

$$I_1 = \frac{-W_0}{W_1} \times I_0 + \frac{t}{W_1},$$

where points on or above the line, the output is 1, and 0 for those below the line (when W_1 is positive). Compare with

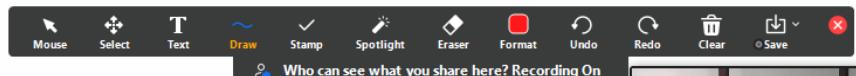
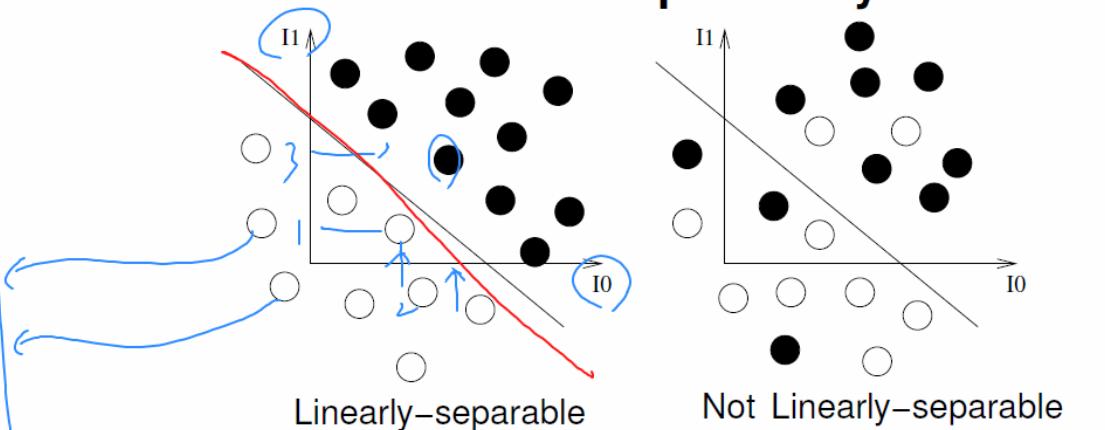
$$y = \frac{-W_0}{W_1} \times x + \frac{t}{W_1}.$$

One is positive, because it divided it by W_1 , one. If this was negative, then now everything below, on or below that line is positive, otherwise

Note: When dividing both sides with W_1 , depending on the sign, the inequality

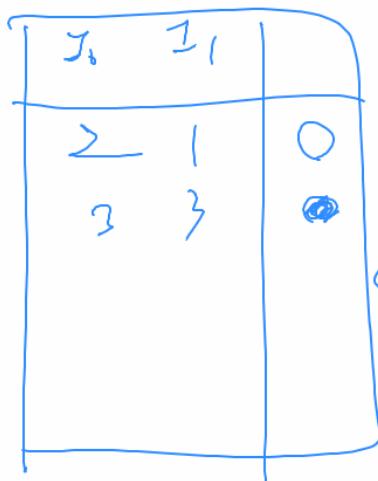
can flip its direction (see previous page).⁵⁵

I_1	I_1
2	1
3	3

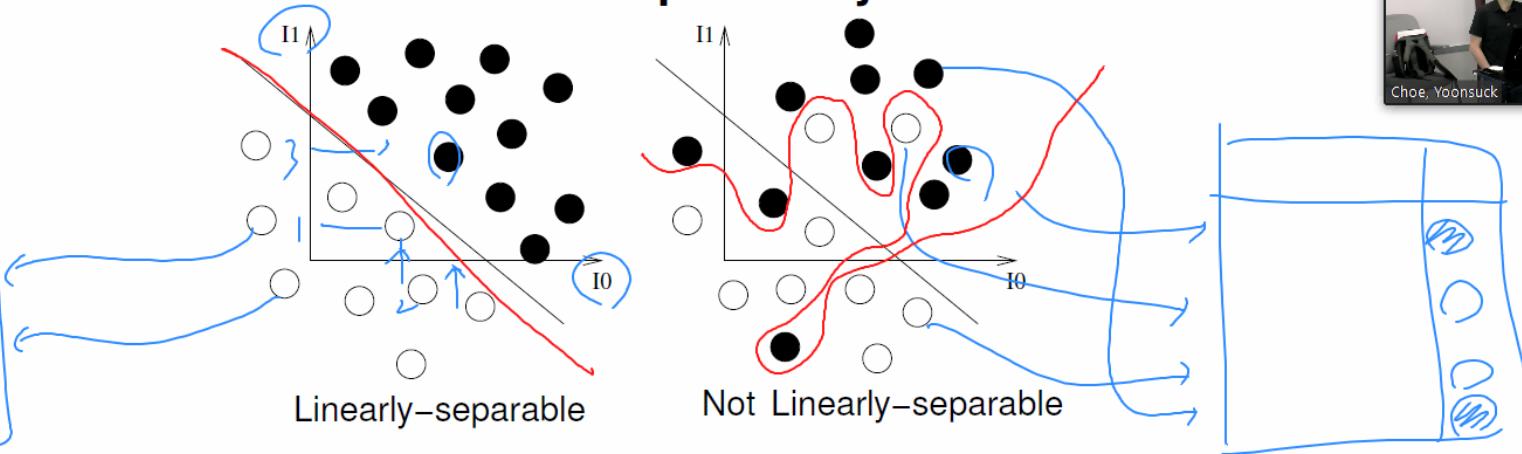


- For functions that take integer or real values as arguments and output either 0 or 1.
- Left: linearly-separable (i.e., can draw a straight line between the classes).
- Right: not linearly-separable (i.e., perceptrons cannot represent such a function)

Okay, then, this is called a linear it's a probable data sets.
Well,



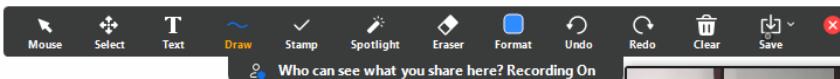
Linear Separability



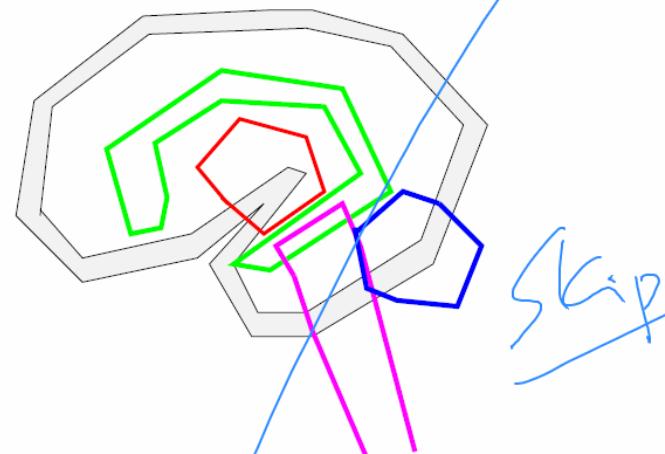
- For functions that take integer or real values as arguments and output either 0 or 1.
- Left: linearly-separable (i.e., can draw a straight line between the classes).
- Right: not linearly-separable (i.e., perceptrons cannot represent such a function)

To separate, clean separate between the the filled discs.
and then, yeah, blank discs

You are screen sharing Stop Share



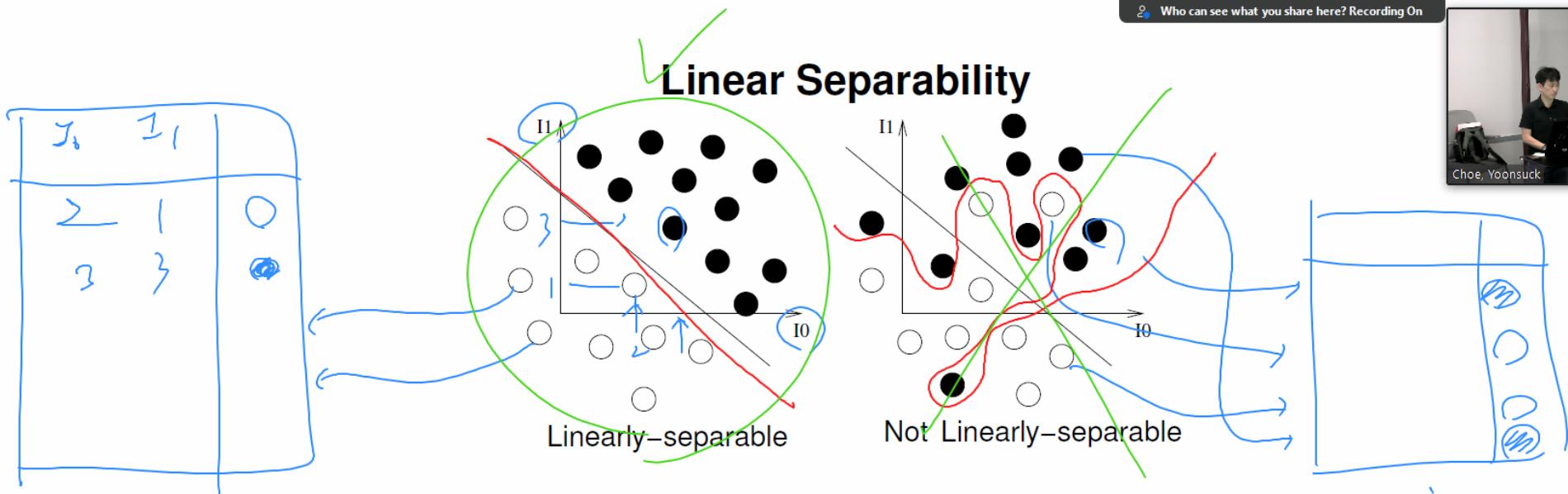
The Central Nervous System



- Cortex: thin outer sheet where most of the neurons are.
- Sub-cortical nuclei: thalamus, hippocampus, basal ganglia, etc.
- Midbrain, pons, and medulla, connects to the spinal cord.
- Cerebellum (hind brain, or small brain)

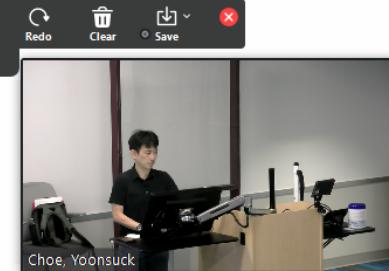
But i'm gonna gonna skip this because this is a little bit too detailed. I'm going to skip it. You can read it

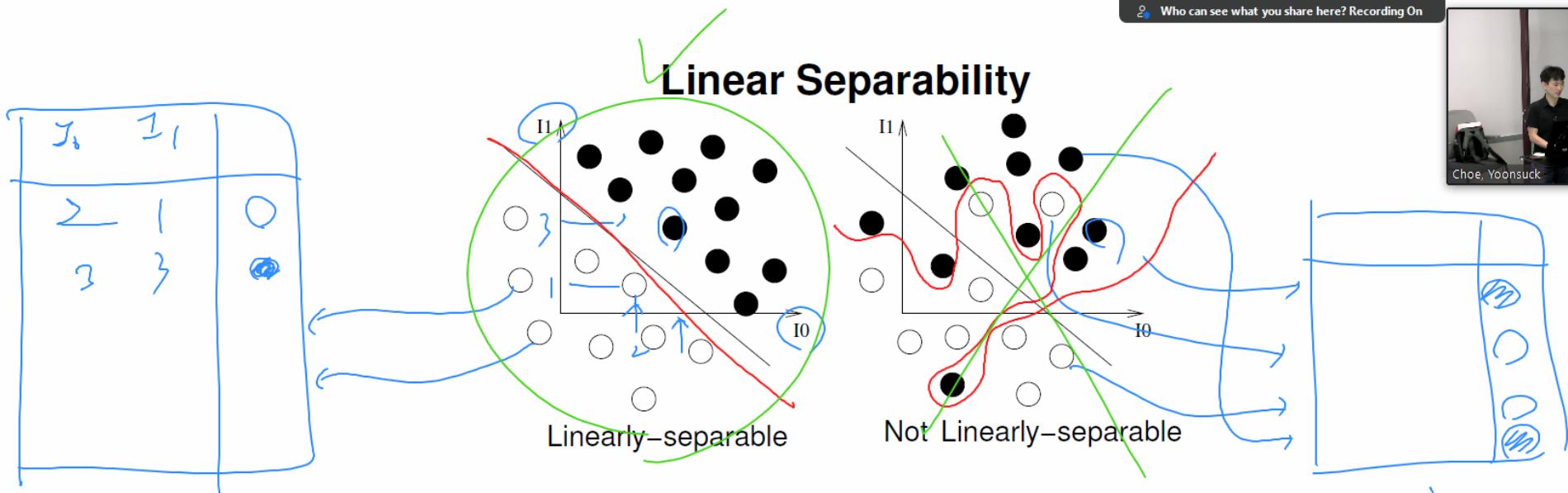
You are screen sharing Stop Share



- For functions that take integer or real values as arguments and output either 0 or 1.
- Left: linearly-separable (i.e., can draw a straight line between the classes).
- Right: not linearly-separable (i.e., perceptrons cannot represent such a function)

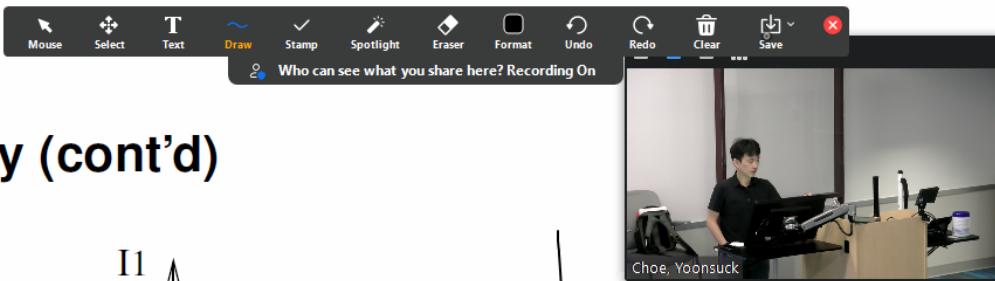
now know that it can only deal with the tests that have this kind of characteristic, so it cannot deal with any of these details that are not



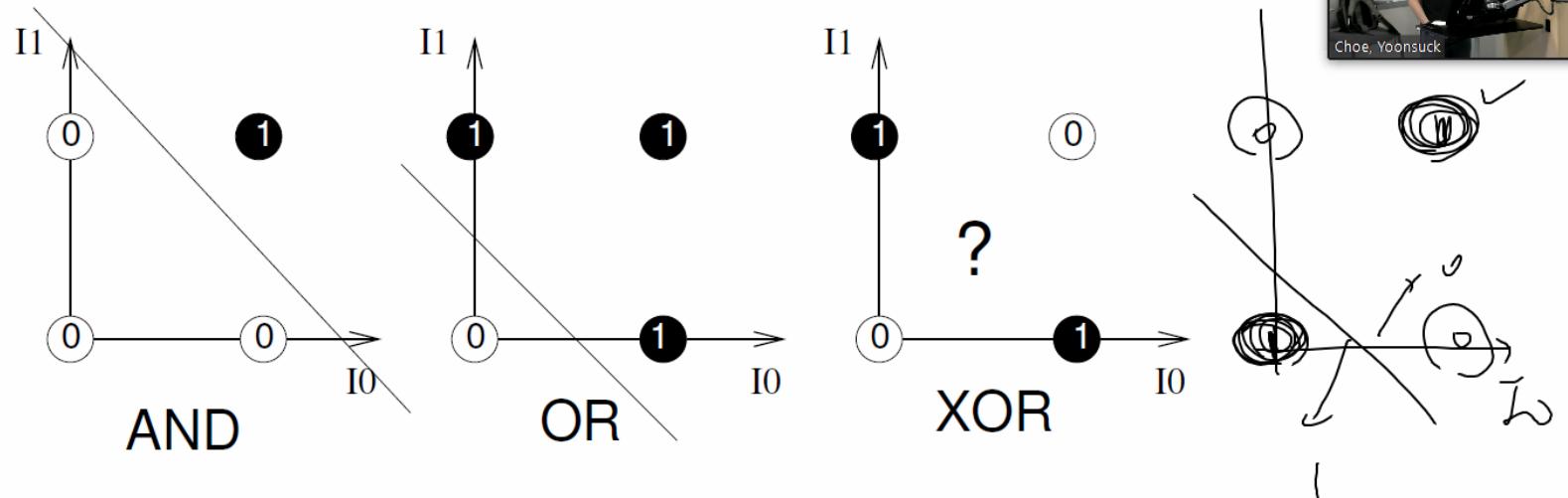


- For functions that take integer or real values as arguments and output either 0 or 1.
- Left: linearly-separable (i.e., can draw a straight line between the classes).
- Right: not linearly-separable (i.e., perceptrons cannot represent such a function)

now know that it can only deal with the tests that have this kind of characteristic. So it cannot deal with any of these details that are not linear is a probable



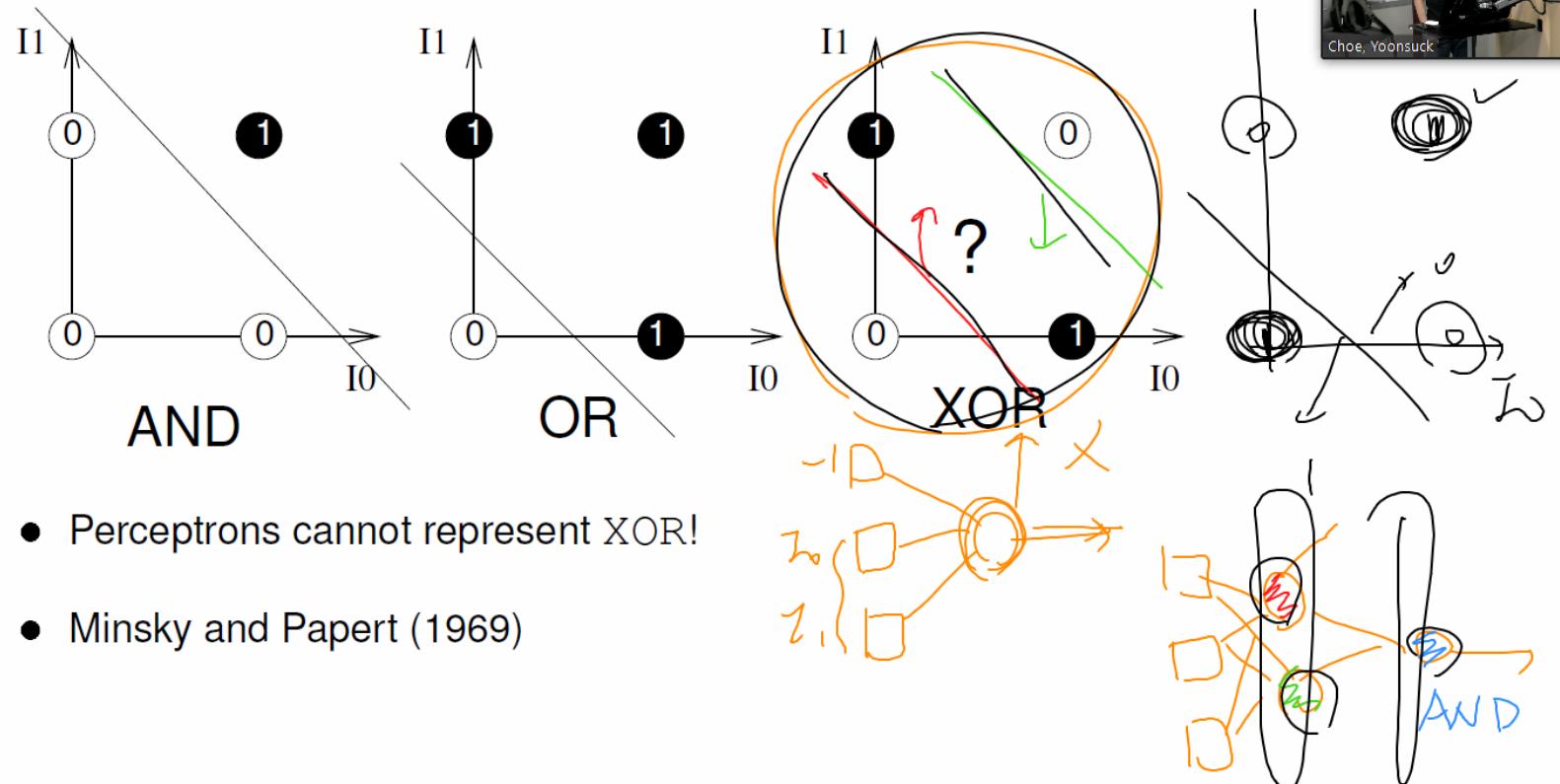
Linear Separability (cont'd)



- Perceptrons cannot represent XOR!
- Minsky and Papert (1969)



Linear Separability (cont'd)

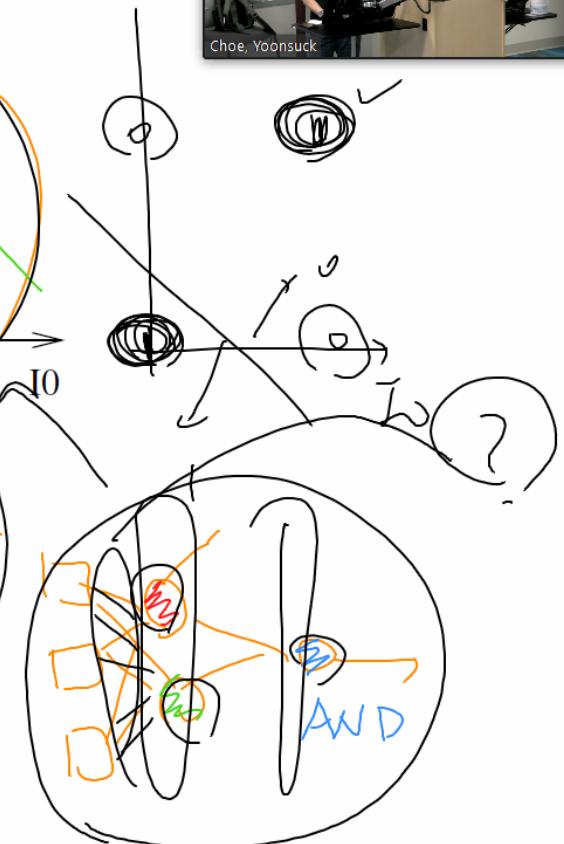
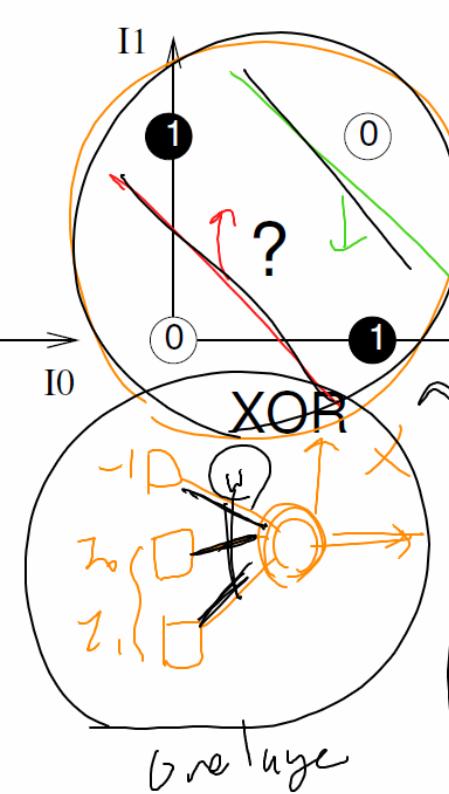
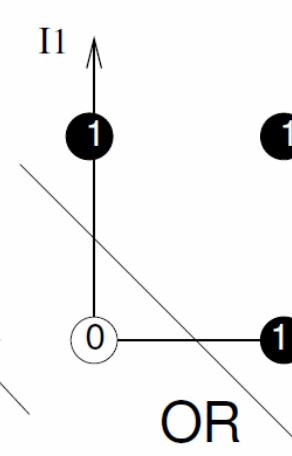
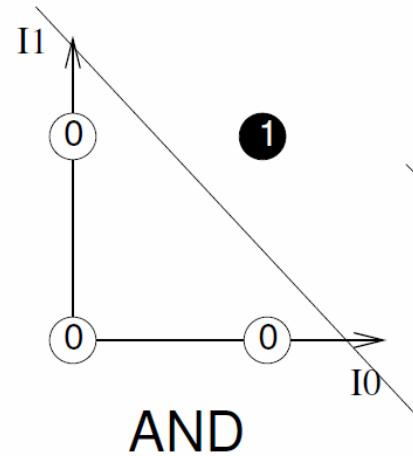


- Perceptrons cannot represent XOR!
- Minsky and Papert (1969)

Because it has 2 boundaries. Yeah, that is somehow combined

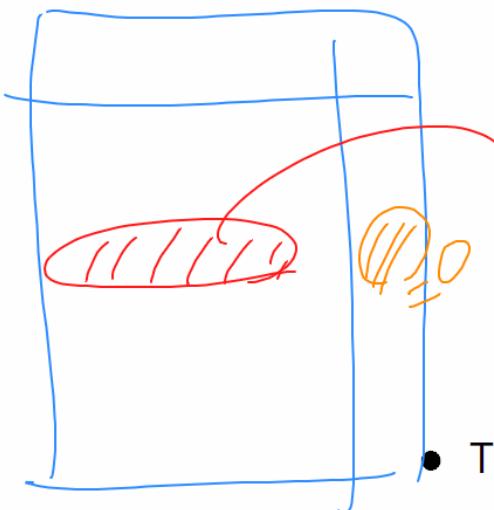


Linear Separability (cont'd)

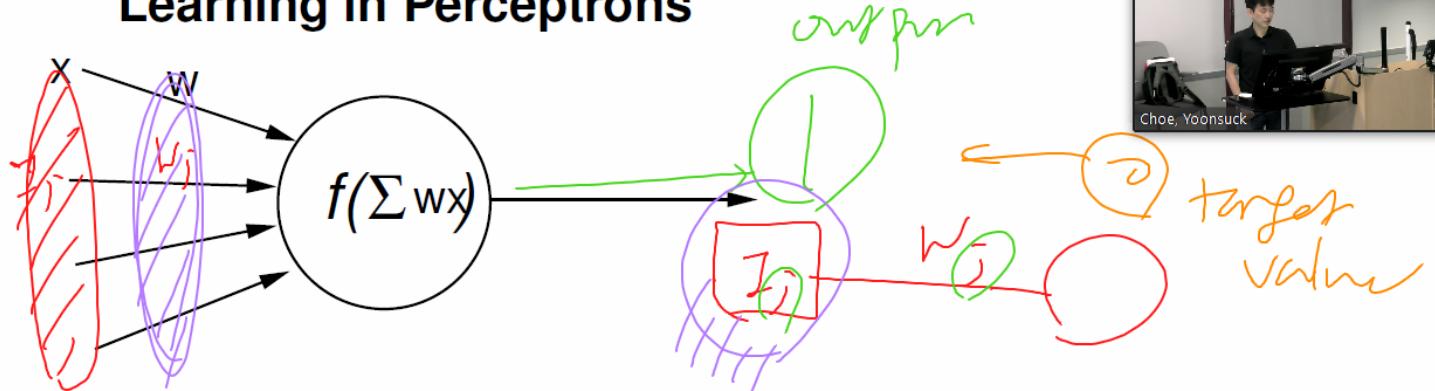


- Perceptrons cannot represent XOR!
- Minsky and Papert (1969)

But they did not know how to update these connection weights, so they kind of abandoned the support



Learning in Perceptrons



- The weights do not have to be calculated manually.
- We can train the network with (input,output) pair according to the following weight update rule:

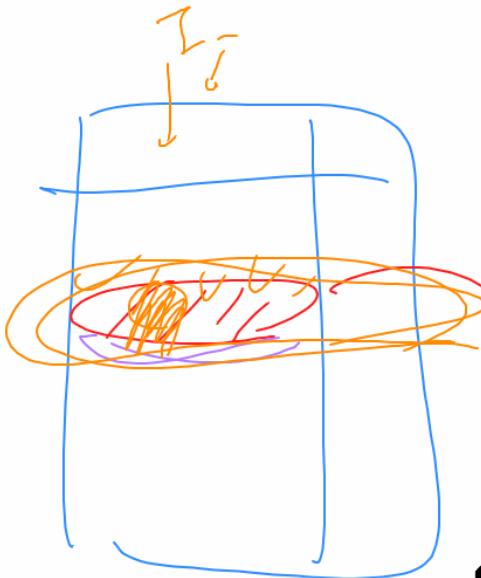
$$W_j \leftarrow W_j + \alpha \times I_j \times Err,$$

where α is the learning rate parameter, I_j is the input, and

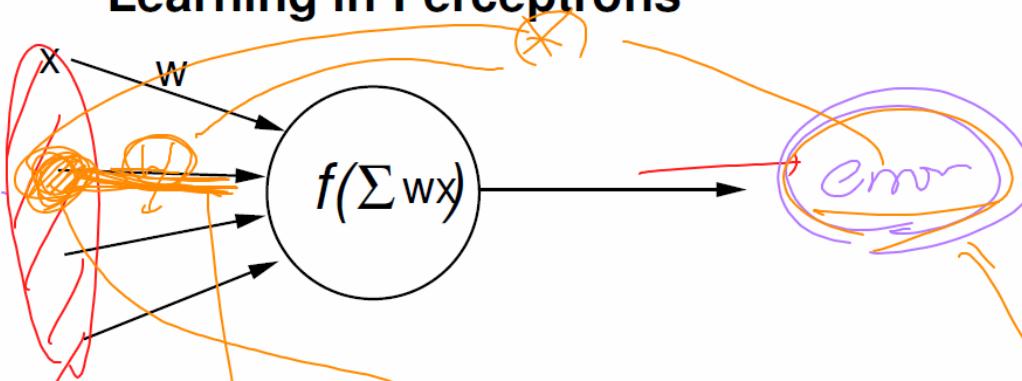
$Err = DesiredOutput - NetworkOutput.$

target

Yeah, well, it's applied by us



Learning in Perceptrons

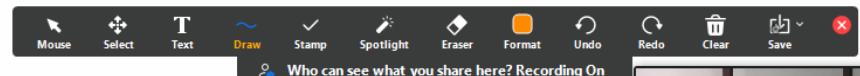


- The weights do not have to be calculated manually.
- We can train the network with (input, output) pair according to the following weight update rule:

$$W_j \leftarrow W_j + \alpha \times I_j \times Err,$$

same for all

where α is the learning rate parameter, I_j is the input, and $Err = DesiredOutput - NetworkOutput$.



22 FALL CSCE 420 501: ARTIFICIAL NEURAL NETWORKS

A Neural Network Playground

playground.tensorflow.org/#activation=tanh&batchSize=10&dataset=gauss®Dataset=reg-plane&learningRate=0.03®ularizationRate=0&noise=1

Who can see what you share here? Recording On

Epoch: 002,466 | Learning rate: 0.03 | Activation: Tanh | Regularization: None | Regularization rate: 0 | Problem type: Classification

DATA: Which dataset do you want to use? (Gauss, Reg-plane, Fire, Moons) | Ratio of training to test data: 50% | Noise: 0 | Batch size: 10 | REGENERATE

FEATURES: Which properties do you want to feed in? (X₁, X₂, X₁², X₂², X₁X₂, sin(X₁), sin(X₂))

OUTPUT: Test loss 0.001 | Training loss 0.000 | 0 HIDDEN LAYERS

Colors shows data, neuron and weight values.

Show test data | Discretize output

Um, What Is a Neural Network?

It's a technique for just maybe it's almost one right this is the it's a value those also. It is based very loosely on how we think the human brain works. First, a

You are screen sharing | Stop Share

Type here to search

12:02 PM
11/8/2022

A Neural Network Playground

Who can see what you share here? Recording On

Epoch: 002,353 | Learning rate: 0.03 | Activation: Tanh | Regularization: None | Regularization rate: 0 | Problem type: Classification

DATA
Which dataset do you want to use?

 Ratio of training to test data: 50%
 Noise: 0
 Batch size: 10

FEATURES
Which properties do you want to feed in?
 X_1
 X_2
 X_1^2
 X_2^2
 $X_1 X_2$
 $\sin(X_1)$
 $\sin(X_2)$

1 HIDDEN LAYER
 + - 2 neurons
 This is the output from one neuron. Hover to see it larger.

OUTPUT
 Test loss 0.219
 Training loss 0.166

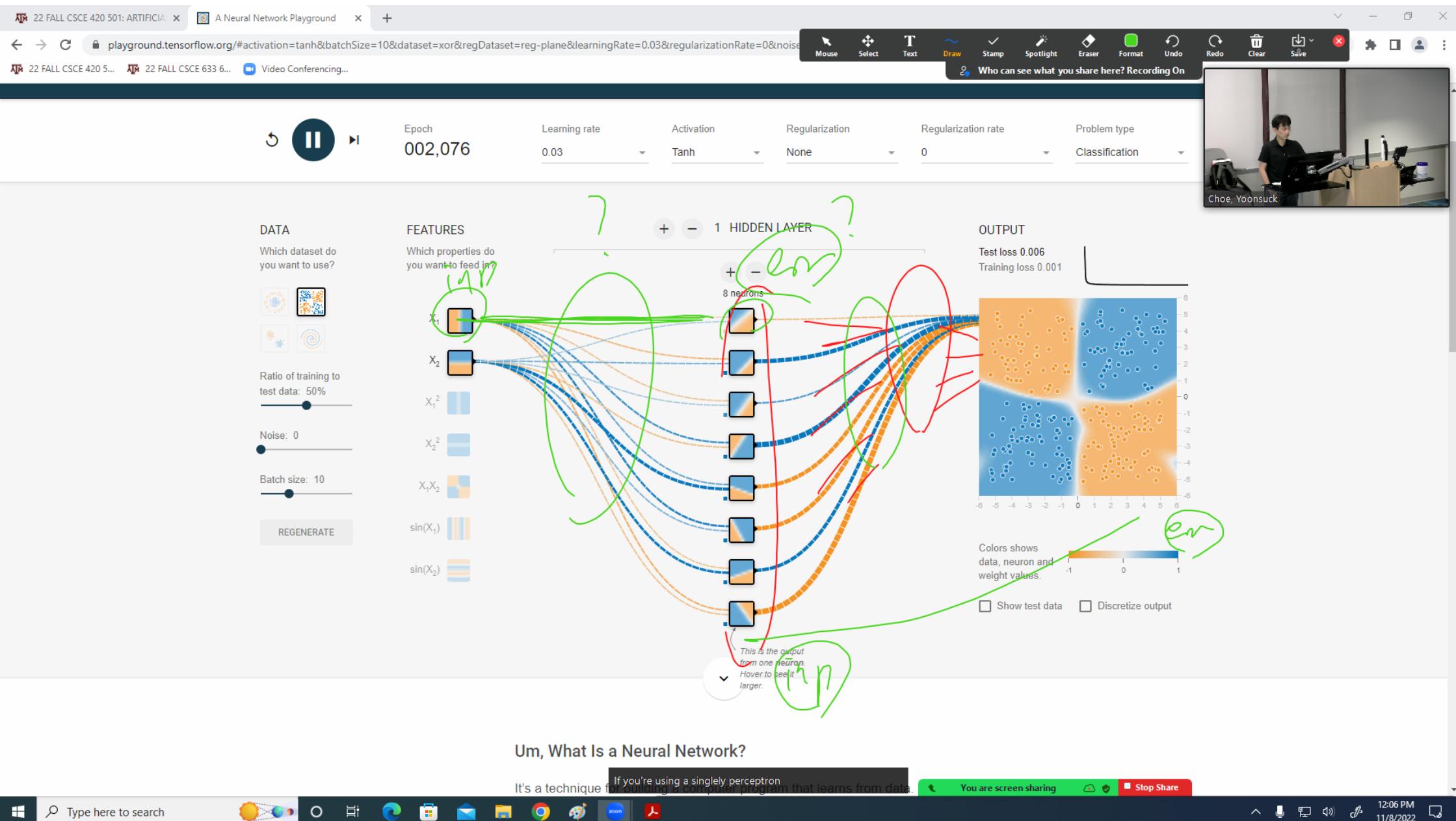
 Colors show data, neuron and weight values.
 Show test data Discretize output
 -1 +1
 +1 -1

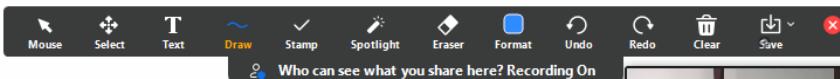
Um, What Is a Neural Network?

It's a technique for building a computer program that learns from data. It is based very loosely on how the human brain works. First, a right. So so to solve this, the human brain works. First, a

You are screen sharing

Type here to search 12:04 PM 11/8/2022





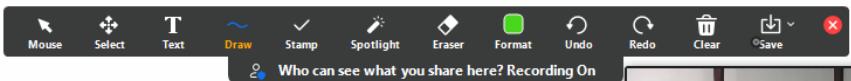
The Central Nervous System: Facts

Facts: human brain

- Neocortex Thickness: 1.6mm
- Neocortex Area: $2,500 \text{ cm}^2$ (about 2.5 ft^2 : Peters and Jones, 1984)
- Neurons: 86 billion (86×10^9 : Frederico Azevedo et al. 2009), 10 billion in the neocortex (Shepherd, 1998).
- Connections: 150 trillion (150^{12} : Pakkenberg et al. 1997, 2003). 60 trillion in the neocortex (Shepherd, 1998).
- Connections per neuron: $\sim 1,800$ (from above)
- Energy usage per operation: 10^{-16} J (compare to 10^{-6} J in modern computers)

Unless specified, the numbers are from

Where is the area of your cortex? If you spread it out on a flat sheet, and so on. *Neural networks: a comprehensive foundation* by Simon Haykin (1994)



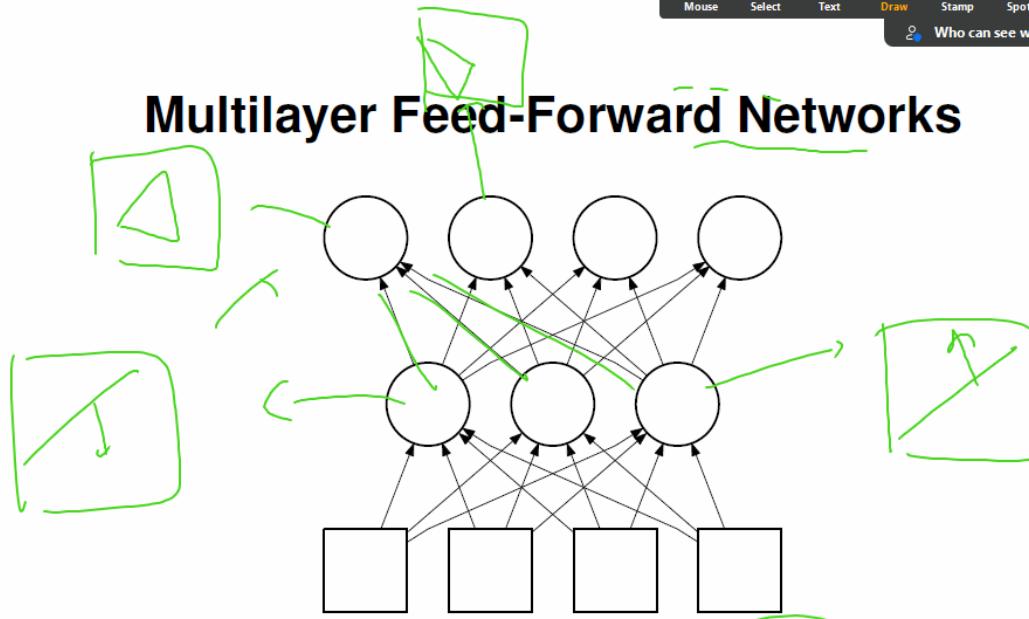
Overview

- Multilayer feed-forward networks
- Gradient descent search
- Backpropagation learning rule
- Evaluation of backpropagation
- Applications of backpropagation

gradient descent, which is the basis for the the main learning rule for these multilay annual networks, and then we look at some

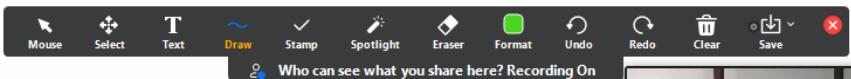


Multilayer Feed-Forward Networks

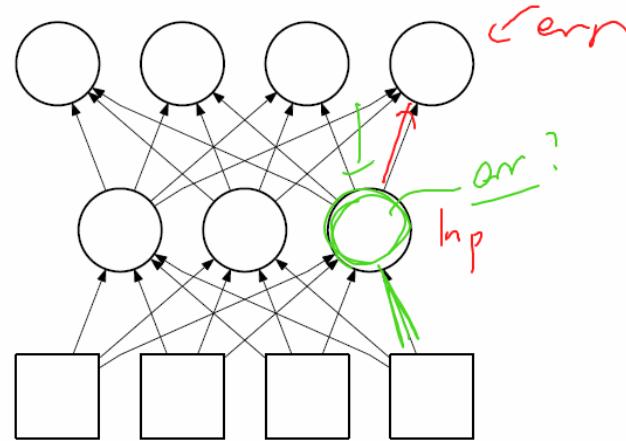


- Proposed in the 1950s
- Proper procedure for training the network came later (1969) and became popular in the 1980s; **back-propagation**

So they found a really cool technique, but it turns out that there were

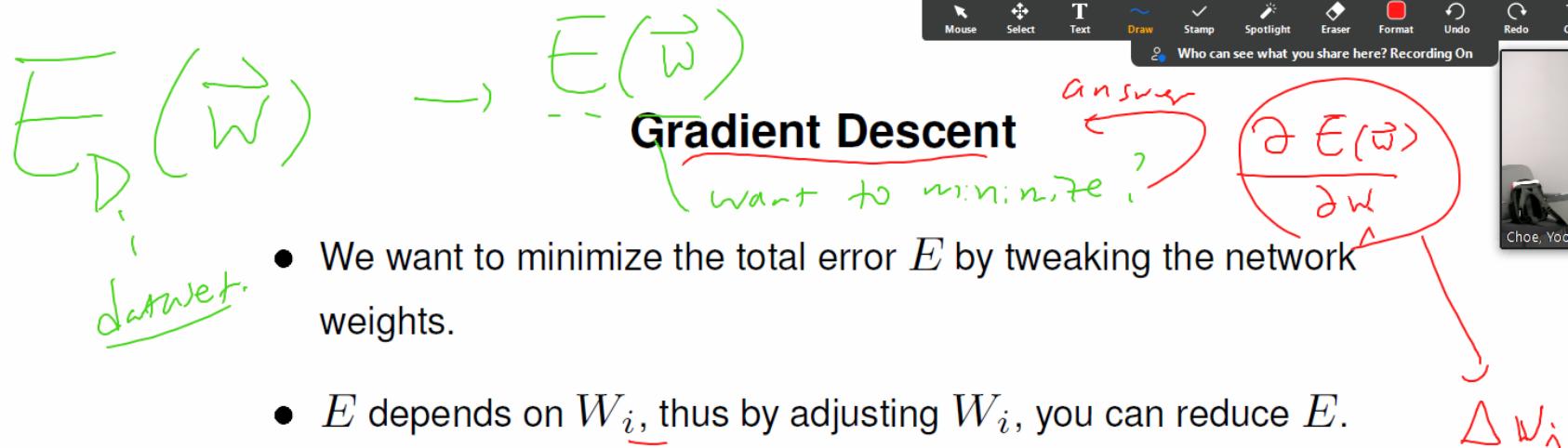


Back-Propagation Learning Rule



- Back-prop is basically a **gradient descent** algorithm.
- The tough problem: output layer has explicit error measure, so finding the error surface is trivial. However, for the hidden layers, how much error each connection eventually cause at the output nodes is hard to determine.
- Backpropagation determines how to distribute the **blame** to each connection.

Unit that is detached from the output side. So this was the tough part

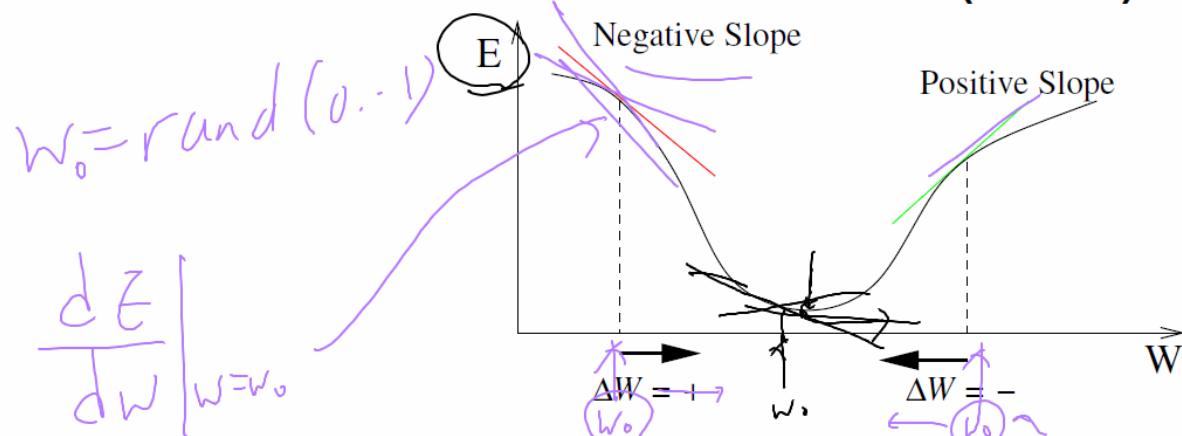


- We want to minimize the total error E by tweaking the network weights.
- E depends on W_i , thus by adjusting W_i , you can reduce E .
- Figuring out how to simultaneously adjust weights W_i for all i at once is practically impossible, so use an iterative approach.
- A sensible way is to reduce E with respect to one weight W_i at a time, proportional to the gradient (or slope) at that point.

And then the answer is gradient descent. The idea is to basically find this partial derivative for a particular connection, and then use that to update the question. Wait



Gradient Descent (cont'd)



- For weight W_i and error function E , to minimize E , W_i should be changed according to $W_i \leftarrow W_i + \Delta W_i$:

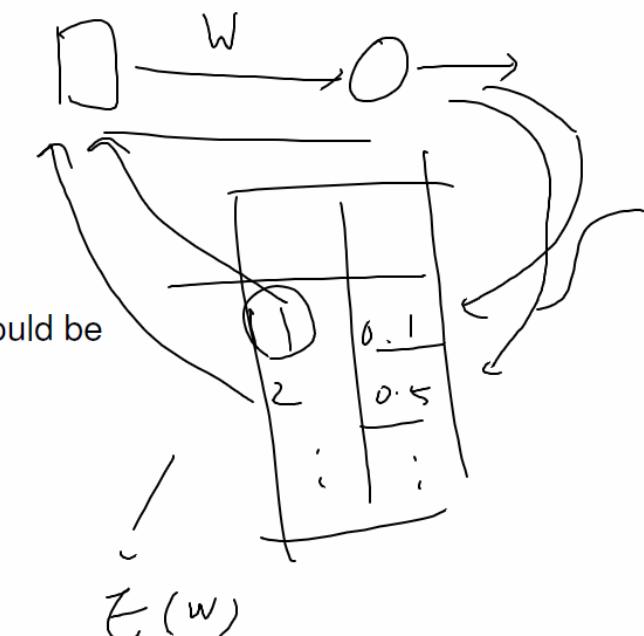
$$\Delta W_i = \alpha \times \left(-\frac{\partial E}{\partial W_i} \right),$$

where α is the learning rate parameter.

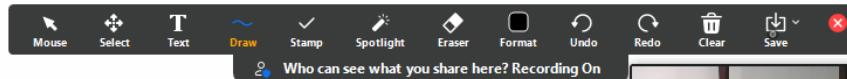
- E can be a function of many weights, thus the partial derivative is used in the above:

$$E(W_1, W_2, \dots, W_i, \dots, W_n, \dots)$$

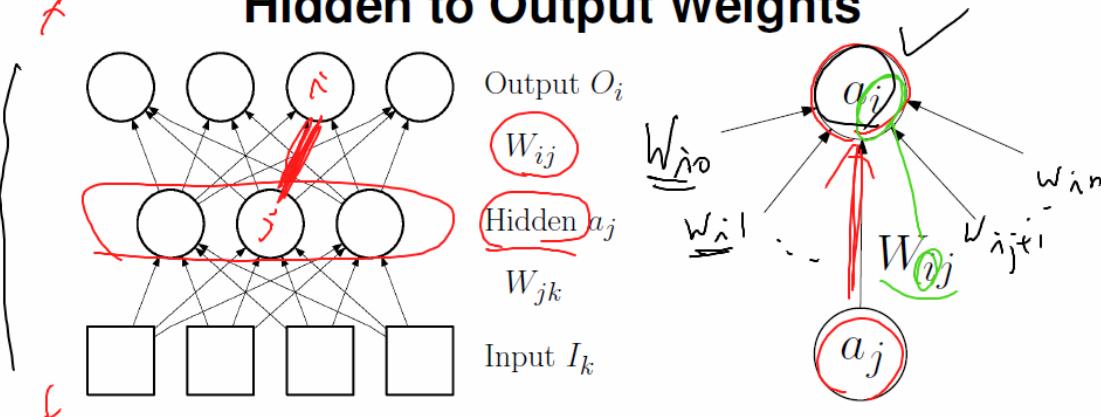
This will become 0 at that point, and your weight will remain unchanged.



$$E(\underline{w})$$



Hidden to Output Weights



- Error function

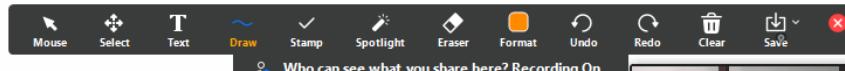
$$E = \frac{1}{2} \sum_i (E_i)^2$$

$$\begin{aligned} E_i &= T_i - O_i \\ &= T_i - g \left(\sum_j W_{ij} a_j \right), \end{aligned}$$

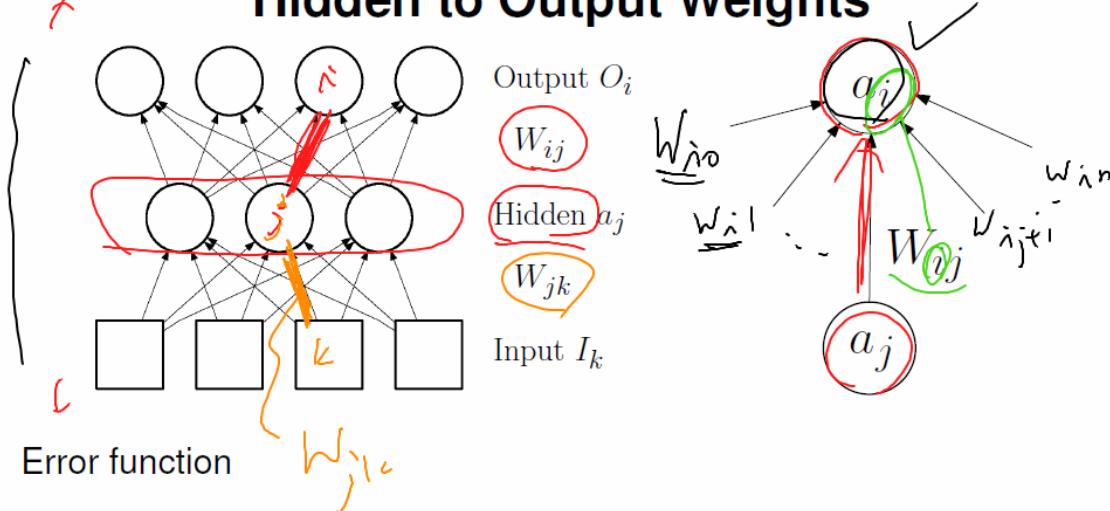
where $g(\cdot)$ is the sigmoid activation function, and T_i the target.

N Hi. So when you look at this first subscript it tells you that it's i the index i is for the output side of the connection

$$E(\underline{w})$$



Hidden to Output Weights



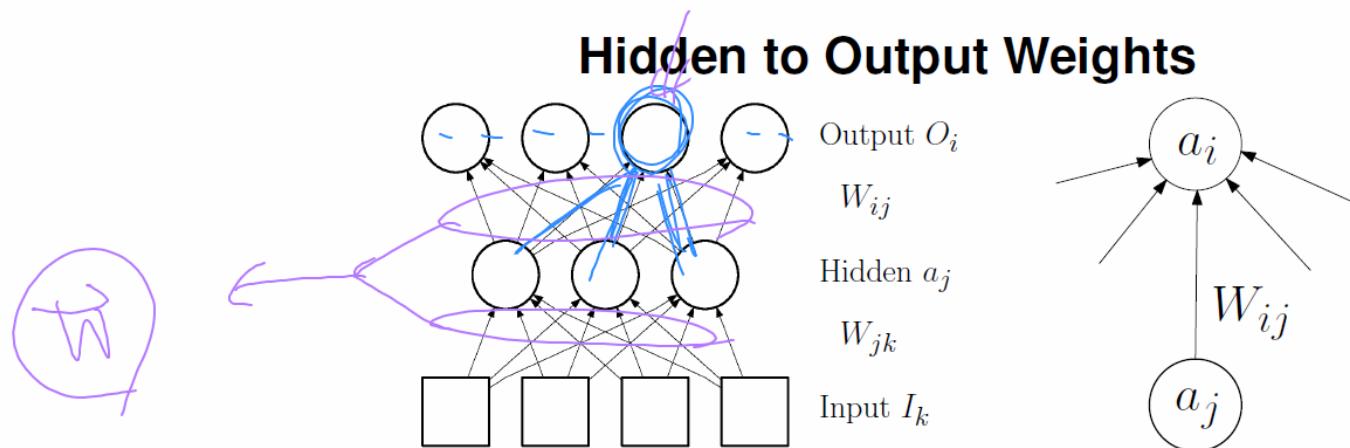
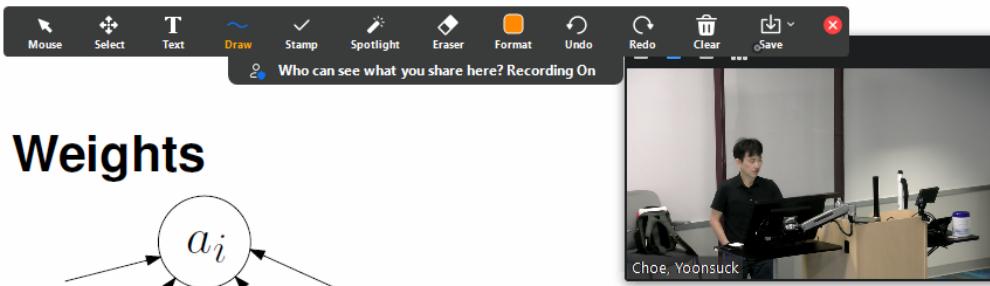
- Error function

$$E = \frac{1}{2} \sum_i (E_i)^2$$

$$\begin{aligned} E_i &= T_i - O_i \\ &= T_i - g \left(\sum_j W_{ij} a_j \right), \end{aligned}$$

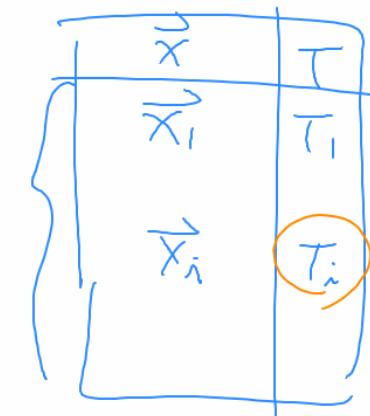
where $g(\cdot)$ is the sigmoid activation function, and T_i the target.

We just assume that there is this kind of nice shaped



- Error function

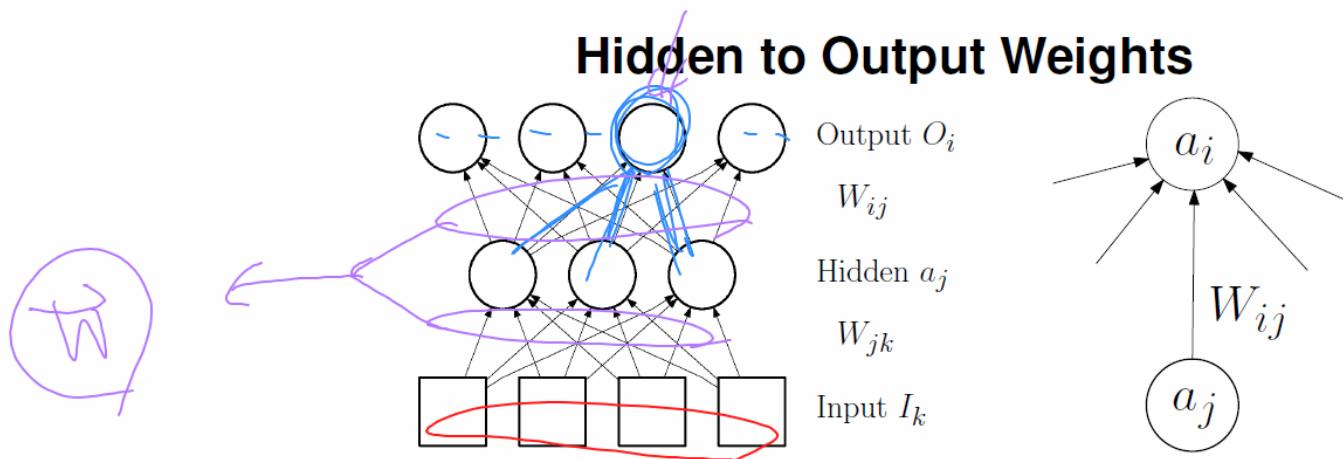
$$\begin{aligned}
 E &= \frac{1}{2} \sum_{i \in D} (E_i)^2 \\
 E_i &= T_i - O_i \\
 &= T_i - g \left(\sum_j W_{ij} a_j \right),
 \end{aligned}$$



where $g(\cdot)$ is the sigmoid activation function, and T_i the target.

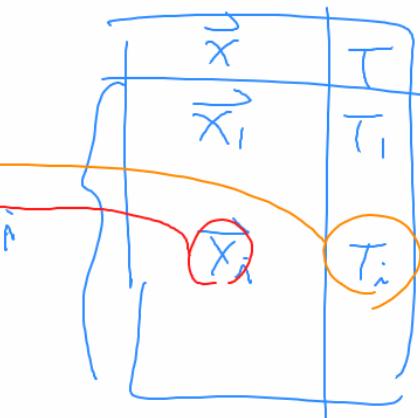


Hidden to Output Weights

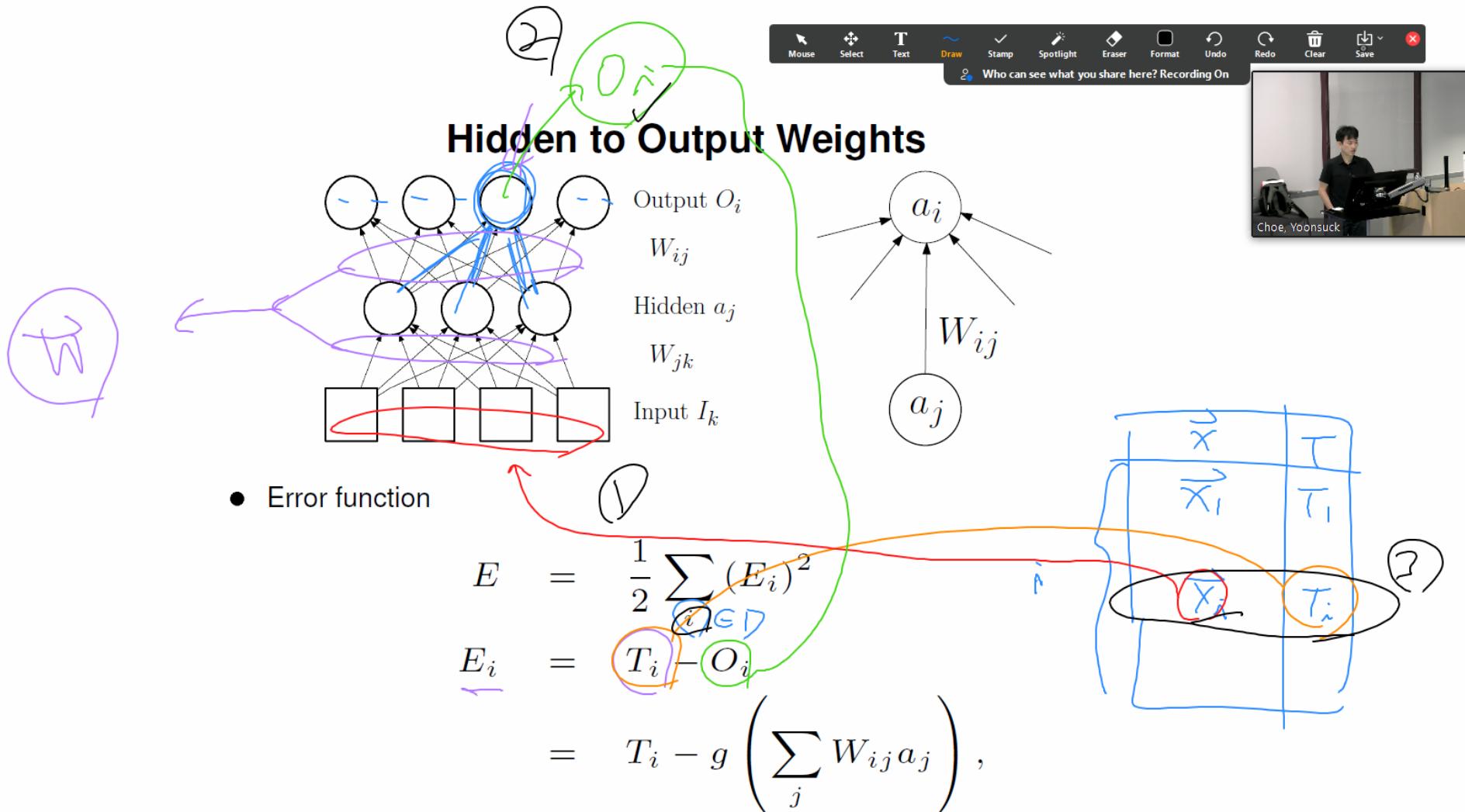


- Error function

$$\begin{aligned}
 E &= \frac{1}{2} \sum_{i \in D} (E_i)^2 \\
 E_i &= T_i - O_i \\
 &= T_i - g \left(\sum_j W_{ij} a_j \right),
 \end{aligned}$$

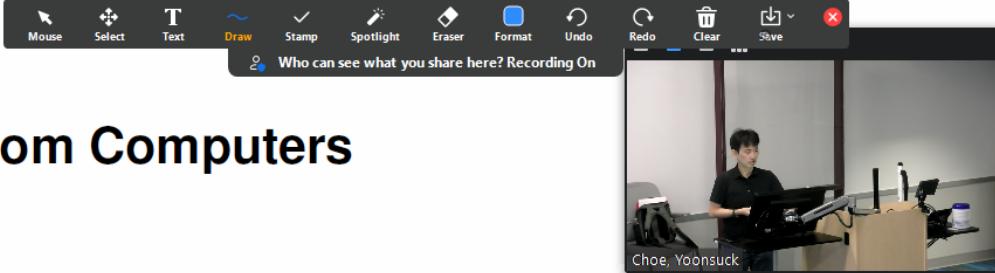


where $g(\cdot)$ is the sigmoid activation function, and T_i the target.



where $g(\cdot)$ is the sigmoid activation function, and T_i the target.

So this is plugging the input, Get output and then look up the target



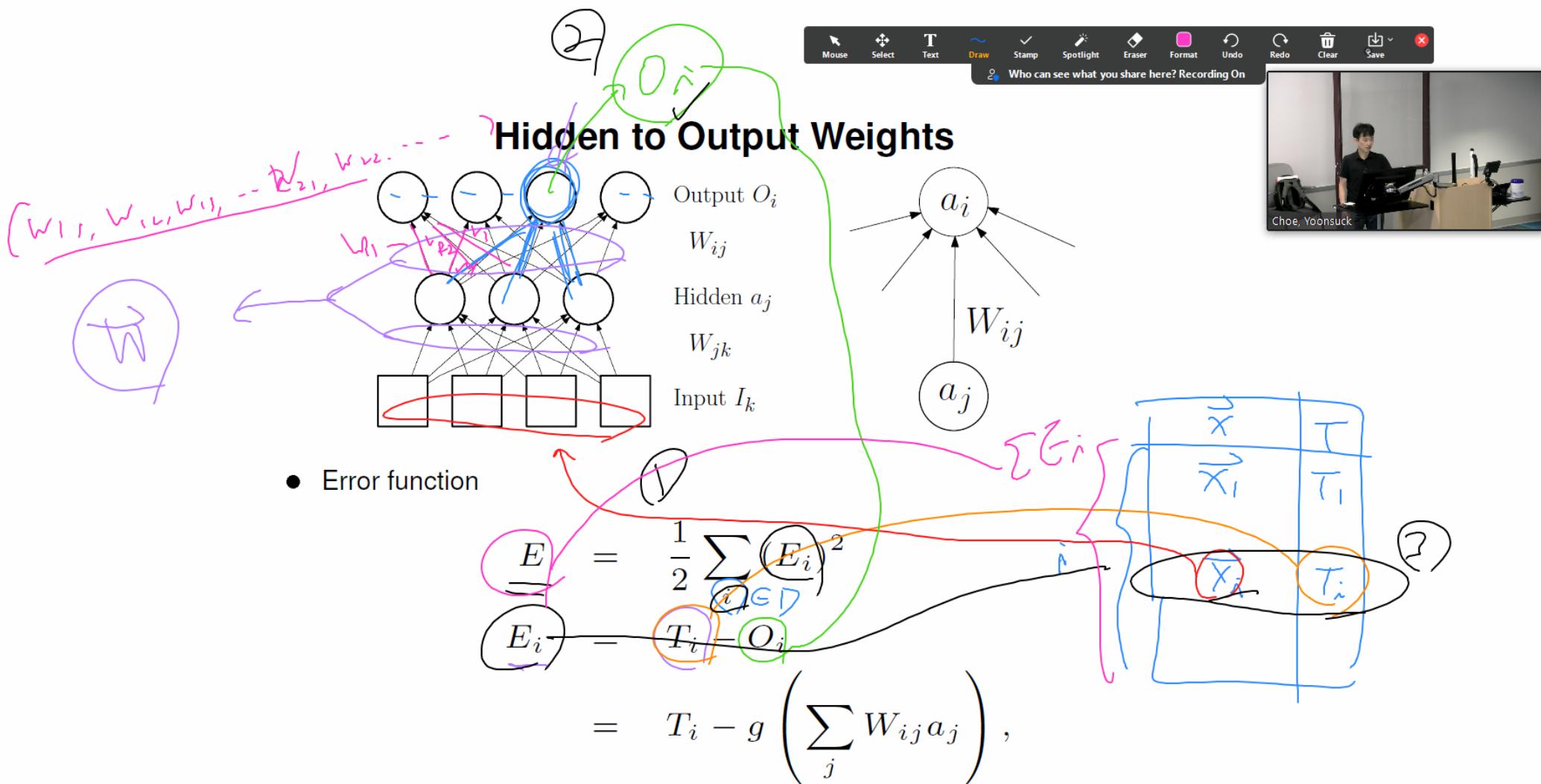
How the Brain Differs from Computers

- Densely connected.
- Massively parallel.
- Highly nonlinear.
- Asynchronous: no central clock.
- Fault tolerant.
- Highly adaptable.
- Creative.

skip

Why are these crucial?

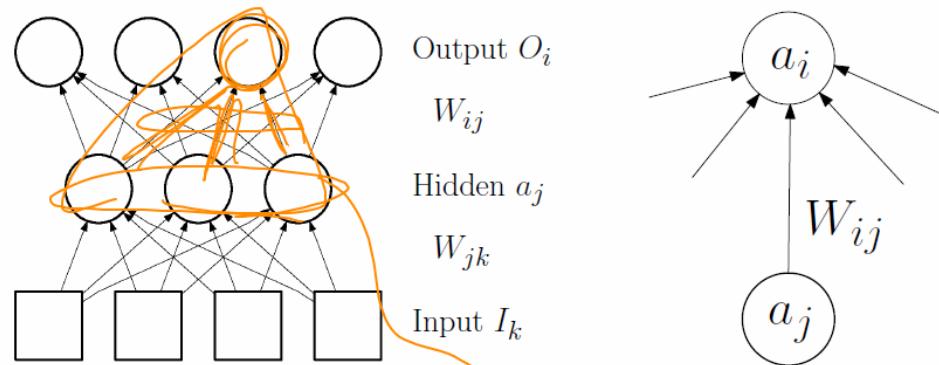
And here's how the brain differs from computers so again
I'm gonna just skip this



where $g(\cdot)$ is the sigmoid activation function, and T_i the target.



Hidden to Output Weights



- Error function

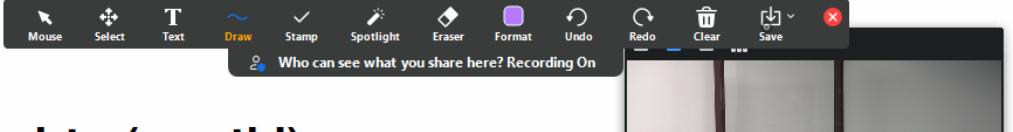
$$\begin{aligned}
 E &= \frac{1}{2} \sum_i (E_i)^2 \\
 E_i &= T_i - O_i \\
 &= T_i - g \left(\sum_j W_{ij} a_j \right),
 \end{aligned}$$

activation func ..

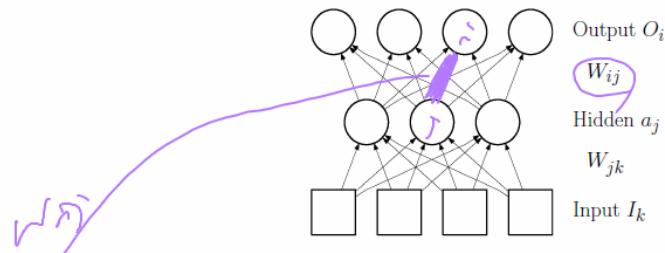
where $g(\cdot)$ is the sigmoid activation function, and T_i the target.

And then the input so here we're just looking at 1 one of these, then you pass it through the activation function

You are screen sharing Stop Share

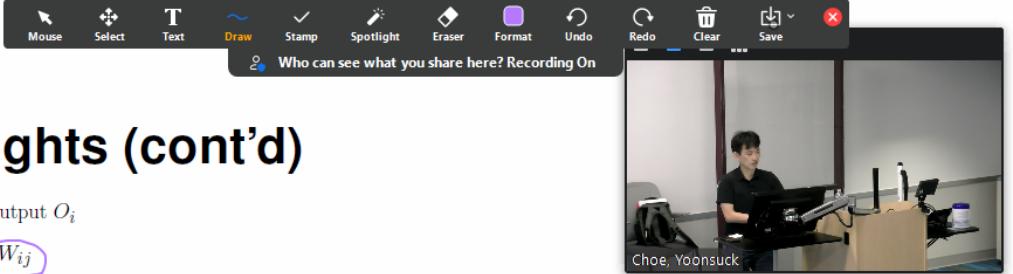


Hidden to Output Weights (cont'd)

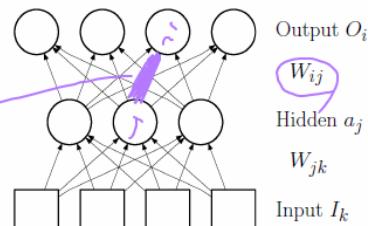


$$\begin{aligned}
 \frac{\partial E}{\partial W_{ij}} &= \frac{\partial \left(\frac{1}{2} \sum_i \left(T_i - g \left(\sum_j W_{ij} a_j \right) \right)^2 \right)}{\partial W_{ij}} \\
 &= \frac{\partial \left(\frac{1}{2} \left(T_i - g \left(\sum_j W_{ij} a_j \right) \right)^2 \right)}{\partial W_{ij}} \\
 &= (T_i - O_i) \times \left(-\frac{\partial g(\sum_j W_{ij} a_j)}{\partial W_{ij}} \right) \\
 &= -(T_i - O_i) \times g'(\sum_j W_{ij} a_j) \times a_j
 \end{aligned}$$

Then this would be w. l. J. So you find the partial derivative of the error function, and this is from the previous page



Hidden to Output Weights (cont'd)

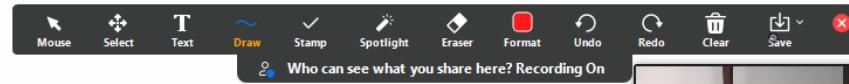
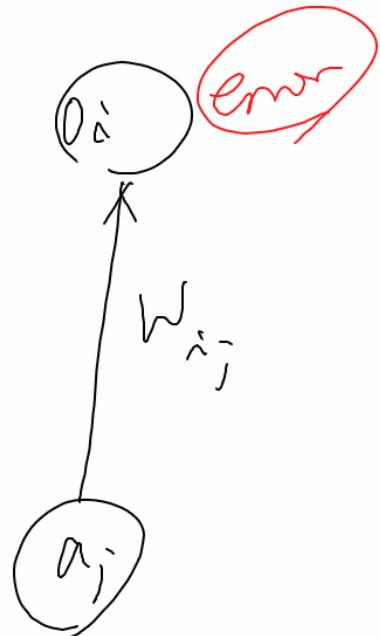


$$\begin{aligned}
 \frac{\partial E}{\partial W_{ij}} &= \frac{\partial \left(\frac{1}{2} \sum_i \left(T_i - g \left(\sum_j W_{ij} a_j \right) \right)^2 \right)}{\partial W_{ij}} \\
 &= \frac{\partial \left(\frac{1}{2} \left(T_i - g \left(\sum_j W_{ij} a_j \right) \right)^2 \right)}{\partial W_{ij}} \\
 &= (T_i - O_i) \times \left(-\frac{\partial g(\sum_j W_{ij} a_j)}{\partial W_{ij}} \right) \\
 &= -(T_i - O_i) \times g'(\sum_j W_{ij} a_j) \times a_j
 \end{aligned}$$

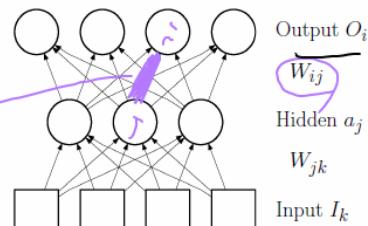
from the prev. page

derivation skipped.

So the derivation skipped



Hidden to Output Weights (cont'd)

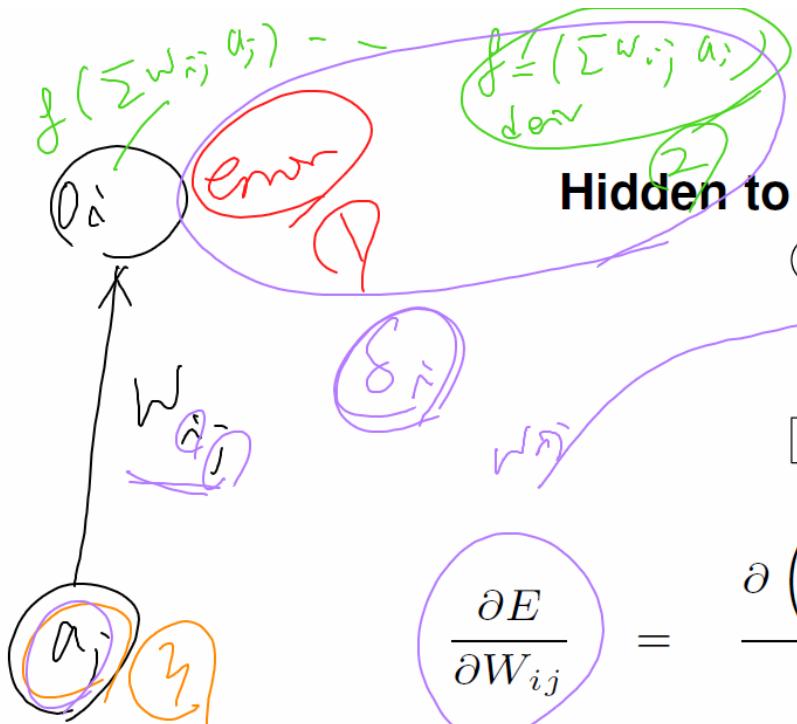


$$\begin{aligned}
 \frac{\partial E}{\partial W_{ij}} &= \frac{\partial \left(\frac{1}{2} \sum_i \left(T_i - g \left(\sum_j W_{ij} a_j \right) \right)^2 \right)}{\partial W_{ij}} \\
 &= \frac{\partial \left(\frac{1}{2} \left(T_i - g \left(\sum_j W_{ij} a_j \right) \right)^2 \right)}{\partial W_{ij}} \\
 &= (T_i - O_i) \times \left(-\frac{\partial g(\sum_j W_{ij} a_j)}{\partial W_{ij}} \right) \\
 &= -(T_i - O_i) \times g'(\sum_j W_{ij} a_j) \times a_j
 \end{aligned}$$

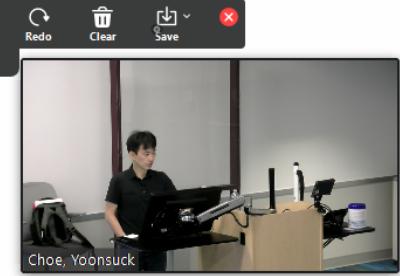
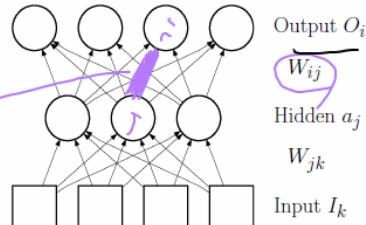
from the prev. page

derivation stopped!

That you want to update. So you compute the error so that's



Hidden to Output Weights (cont'd)



$$\frac{\partial E}{\partial W_{ij}} = \frac{\partial \left(\frac{1}{2} \sum_i (T_i - g(\sum_j W_{ij} a_j))^2 \right)}{\partial W_{ij}}$$

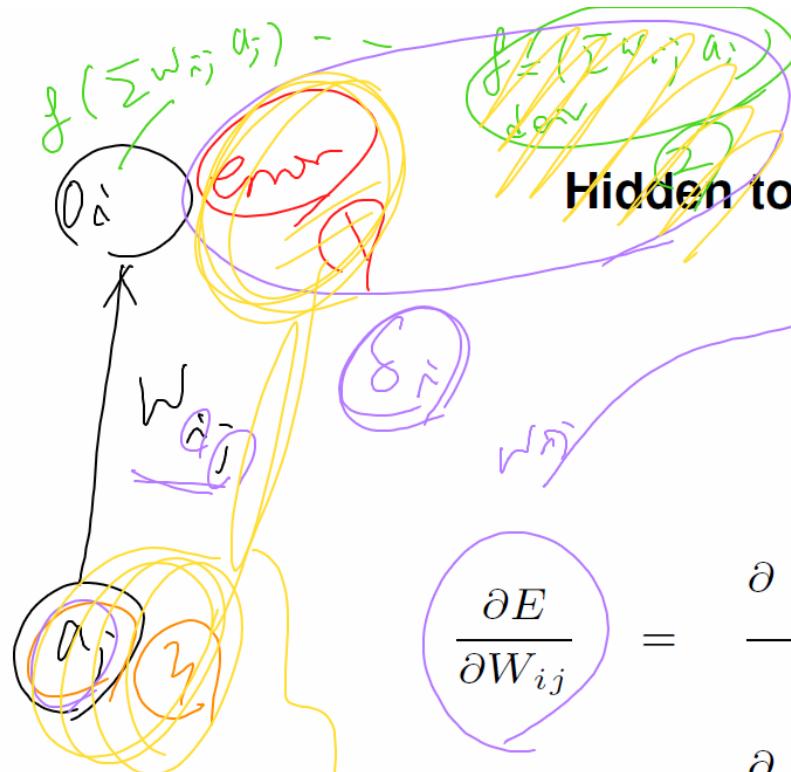
$$= \frac{\partial \left(\frac{1}{2} (T_i - g(\sum_j W_{ij} a_j))^2 \right)}{\partial W_{ij}}$$

$$= (T_i - O_i) \times \left(\frac{\partial g(\sum_j W_{ij} a_j)}{\partial W_{ij}} \right)$$

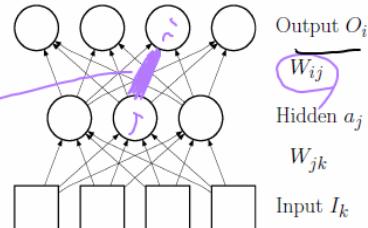
$$= -(T_i - O_i) \times g'(\sum_j W_{ij} a_j) \times a_j$$

from the prev. page
derivation stopped!

So the weight is updated based on delta of i, and then the input of j.



Hidden to Output Weights (cont'd)



from the prev. page

$$\frac{\partial E}{\partial W_{ij}} = \frac{\partial \left(\frac{1}{2} \sum_i (T_i - g \left(\sum_j W_{ij} a_j \right))^2 \right)}{\partial W_{ij}}$$

$$= \frac{\partial \left(\frac{1}{2} (T_i - g \left(\sum_j W_{ij} a_j \right))^2 \right)}{\partial W_{ij}}$$

just these
→ perf. func.

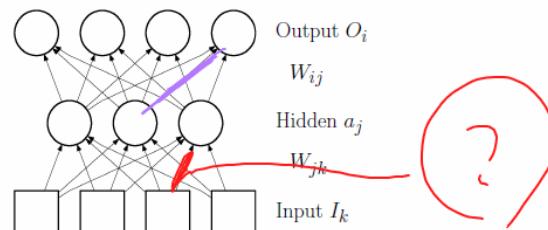
$$(T_i + O_i) \times \left(\frac{\partial g(\sum_j W_{ij} a_j)}{\partial W_{ij}} \right)$$

$$= -(T_i - O_i) \times g'(\sum_j W_{ij} a_j) \times a_j$$

derivation
skipped!

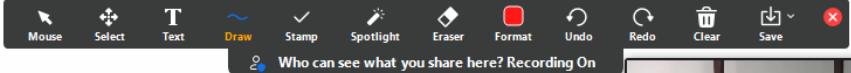


Hidden to Output Weights (cont'd)

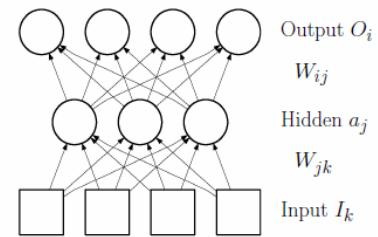


$$\begin{aligned}
 &= \frac{\partial E}{\partial W_{ij}} = \frac{\partial}{\partial W_{ij}} \left(\frac{1}{2} \sum_i \left(T_i - g \left(\sum_j W_{ij} a_j \right) \right)^2 \right) \\
 &= \frac{\partial}{\partial W_{ij}} \left(\frac{1}{2} \left(T_i - g \left(\sum_j W_{ij} a_j \right) \right)^2 \right) \\
 &= (T_i - O_i) \times \left(-\frac{\partial g(\sum_j W_{ij} a_j)}{\partial W_{ij}} \right) \\
 &= -(T_i - O_i) \times g'(\sum_j W_{ij} a_j) \times a_j
 \end{aligned}$$

But the real question is, what about these connections and we'll look at that in the next lecture right so

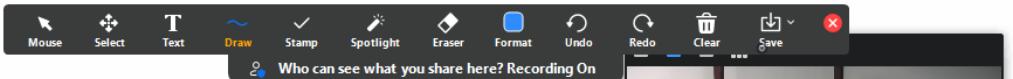


Hidden to Output Weights (cont'd)

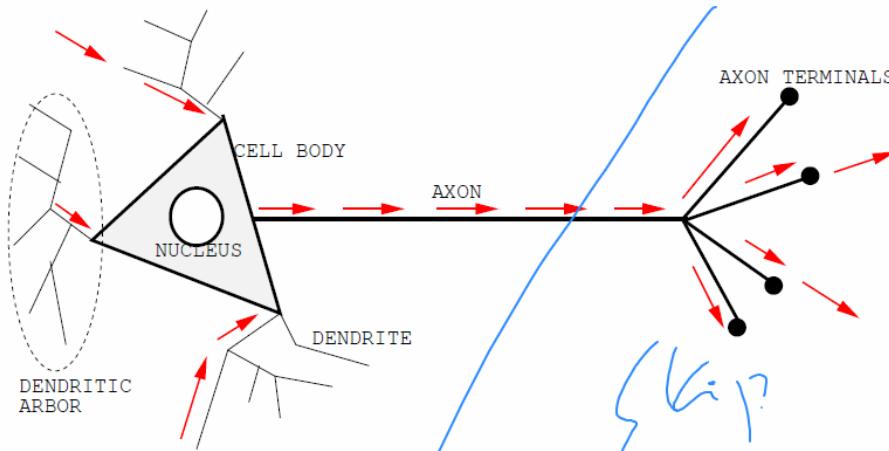


$$\begin{aligned}
 \frac{\partial E}{\partial W_{ij}} &= \frac{\partial \left(\frac{1}{2} \sum_i \left(T_i - g \left(\sum_j W_{ij} a_j \right) \right)^2 \right)}{\partial W_{ij}} \\
 &= \frac{\partial \left(\frac{1}{2} \left(T_i - g \left(\sum_j W_{ij} a_j \right) \right)^2 \right)}{\partial W_{ij}} \\
 &= (T_i - O_i) \times \left(-\frac{\partial g(\sum_j W_{ij} a_j)}{\partial W_{ij}} \right) \\
 &= -(T_i - O_i) \times g'(\sum_j W_{ij} a_j) \times a_j
 \end{aligned}$$

Please sign it and bring it to the podium. Please



Neurons: Basic Functional Unit of the Brain

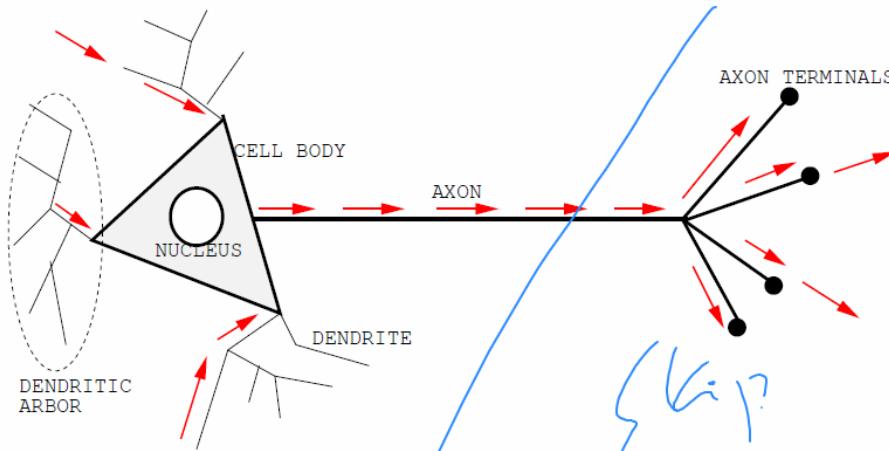


- Dendrites receive input from upstream neurons.
- Ions flow in to make the cell positively charged.
- Once a firing threshold is reached, a spike is generated and transmitted along the axon.
- Axon terminals release neurotransmitters to relay the signal to the downstream neurons.

So the next one is about how the neuron functions. So you can skip



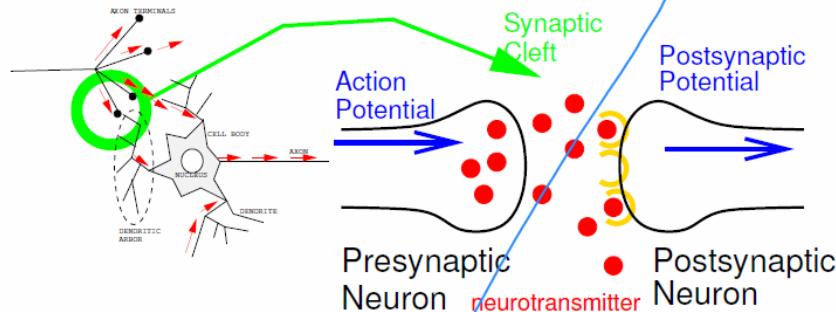
Neurons: Basic Functional Unit of the Brain



- Dendrites receive input from upstream neurons.
- Ions flow in to make the cell positively charged.
- Once a firing threshold is reached, a spike is generated and transmitted along the axon.
- Axon terminals release neurotransmitters to relay the signal to the downstream neurons.



Propagation of Activation Across the Synapse



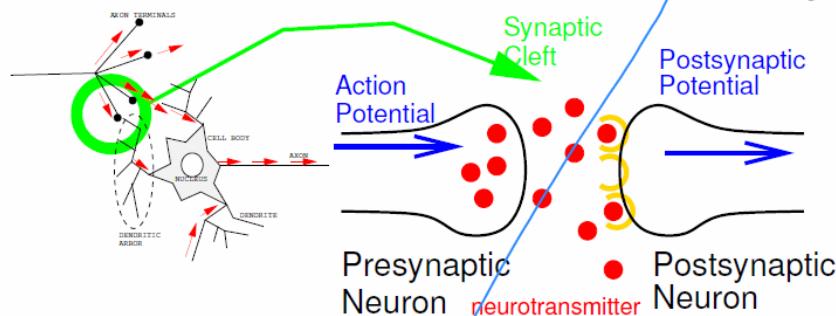
1. Action potential reaches axon terminal.
2. Neurotransmitters are released into synaptic cleft and bind to postsynaptic cell's receptors.
3. Binding allows ion channels to open (Na^+), and Na^+ ions flows in and makes the postsynaptic cell depolarize.
4. Once the membrane voltage reaches the threshold, an action potential is generated.

(Ski?)

Lesson: neural activity propagation has a very complex cellular/molecular mechanism.



Propagation of Activation Across the Synapse



1. Action potential reaches axon terminal.
 2. Neurotransmitters are released into synaptic cleft and bind to postsynaptic cell's receptors.
 3. Binding allows ion channels to open (Na^+), and Na^+ ions flows in and makes the postsynaptic cell depolarize.
 4. Once the membrane voltage reaches the threshold, an action potential is generated.
- (Ski?)*

Lesson: neural activity propagation has a very complex cellular/molecular mechanism.