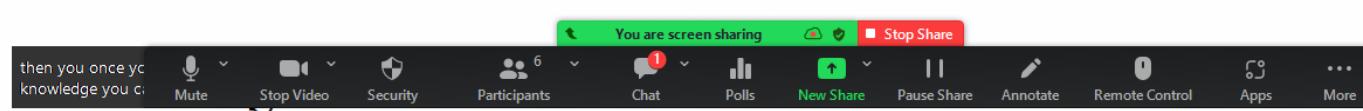


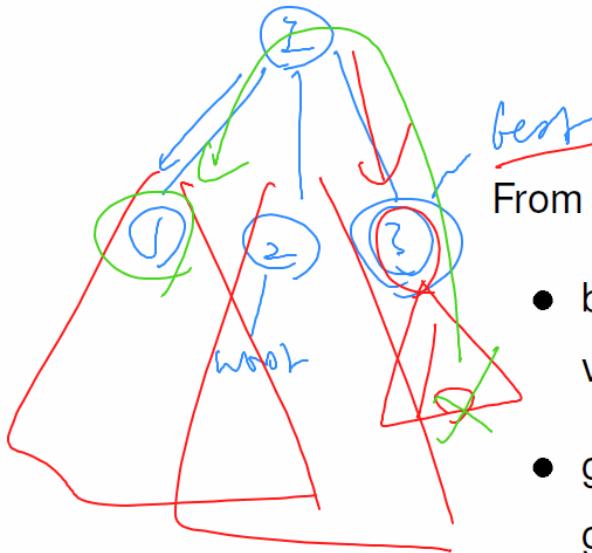
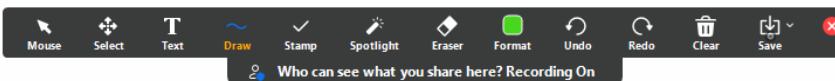
Informed Search

From domain knowledge, obtain an **evaluation function**.

how good
is a state

- best-first search: order nodes according to the evaluation function value
- greedy search: minimize estimated cost $h(n)$ for reaching the goal: this is fast, but incomplete and non-optimal.
- A*: minimize $f(n) = g(n) + h(n)$, where $g(n)$ is the current path cost from start to n , and $h(n)$ is the estimated cost from n to goal.





Informed Search

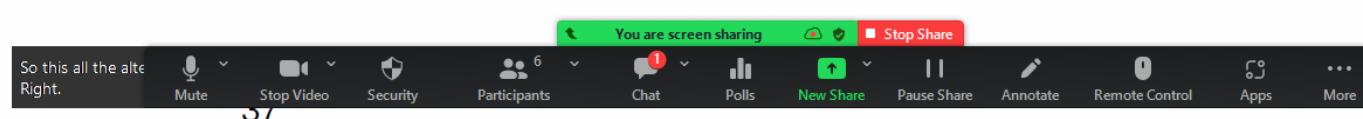
From domain knowledge, obtain an **evaluation function**.

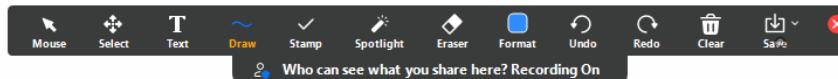
- best-first search: order nodes according to the evaluation function value
- greedy search: minimize estimated cost $h(n)$ for reaching the goal: this is fast, but incomplete and non-optimal.
- A*: minimize $f(n) = g(n) + h(n)$, where $g(n)$ is the current path cost from start to n , and $h(n)$ is the estimated cost from n to goal.

how good
is a state
~~approx.~~



Choe, Yoonsuck





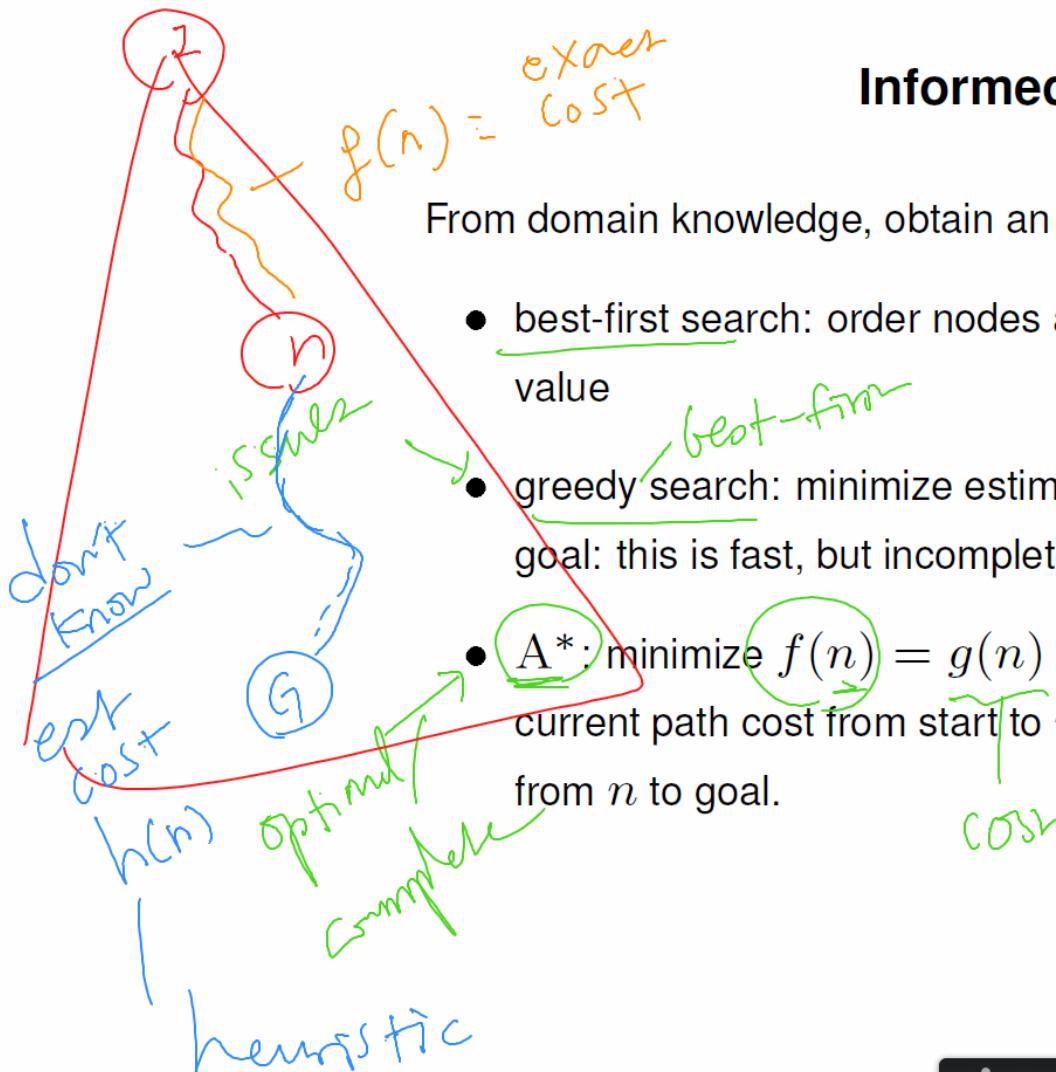
Informed Search

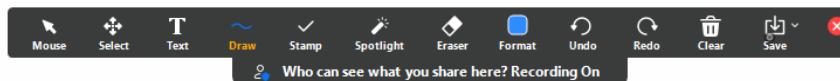


From domain knowledge, obtain an **evaluation function**.

- best-first search: order nodes according to the evaluation function value
 - greedy search: minimize estimated cost $h(n)$ for reaching the goal: this is fast, but incomplete and non-optimal.
 - A*: minimize $f(n) = g(n) + h(n)$, where $g(n)$ is the current path cost from start to n , and $h(n)$ is the estimated cost from n to goal.

$h(n)$ - est. dist to
goal



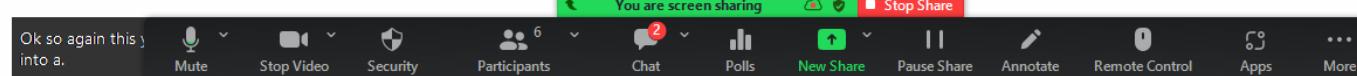
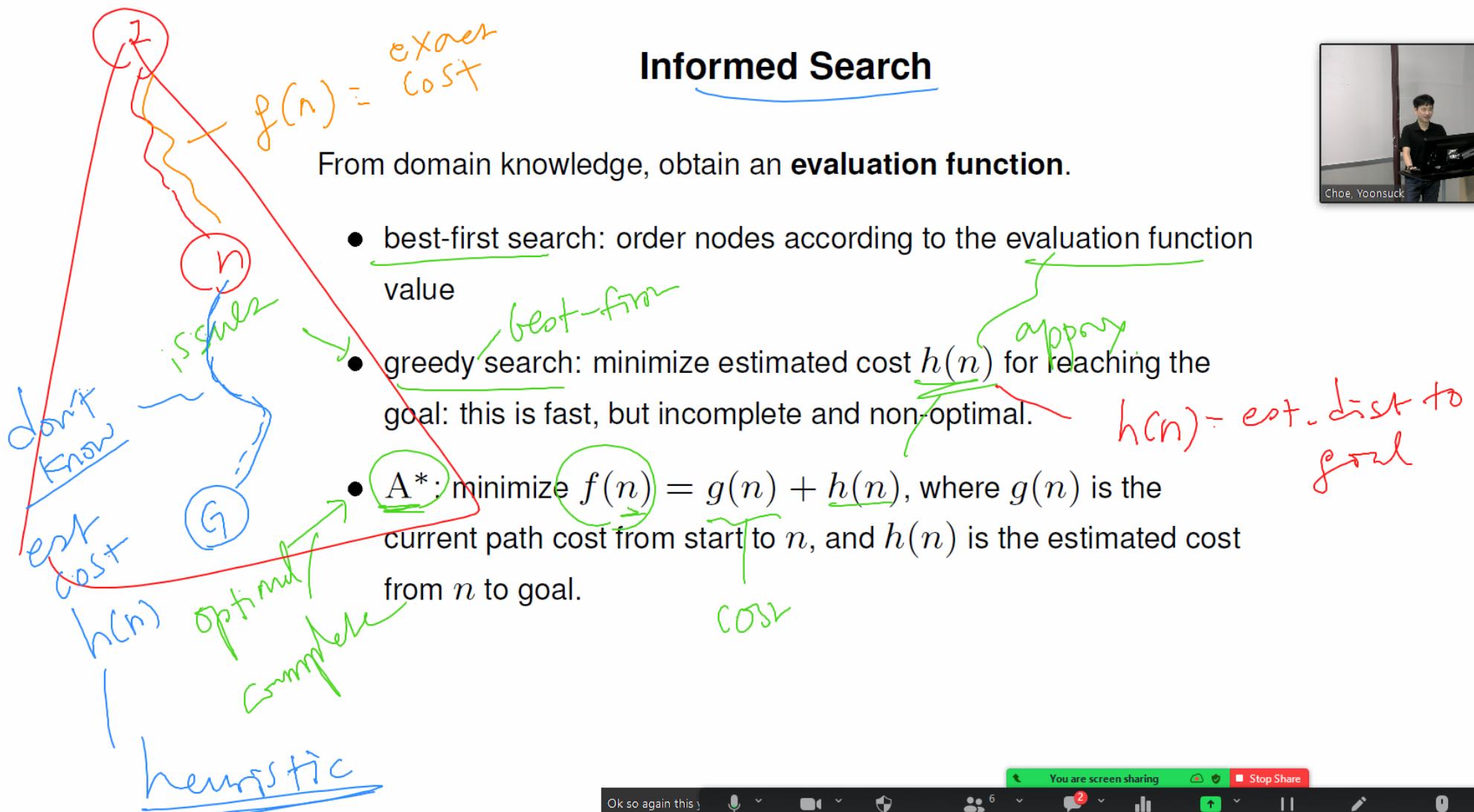


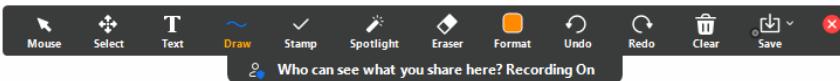
Informed Search



From domain knowledge, obtain an **evaluation function**.

- best-first search: order nodes according to the evaluation function value
- greedy search: minimize estimated cost $h(n)$ for reaching the goal: this is fast, but incomplete and non-optimal.
- A*: minimize $f(n) = g(n) + h(n)$, where $g(n)$ is the current path cost from start to n , and $h(n)$ is the estimated cost from n to goal.



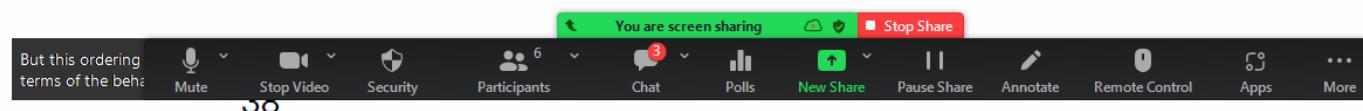


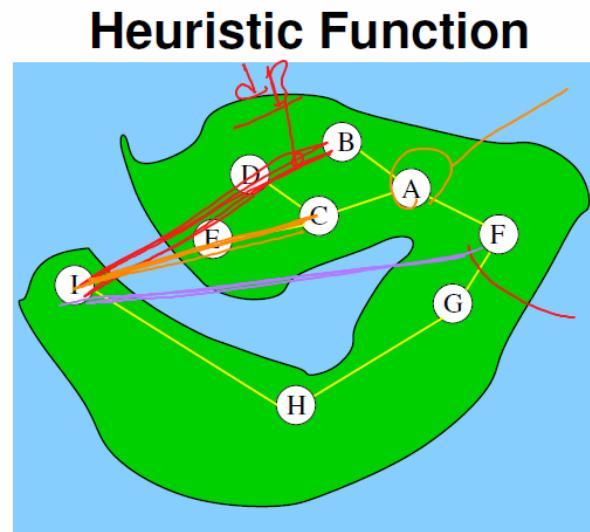
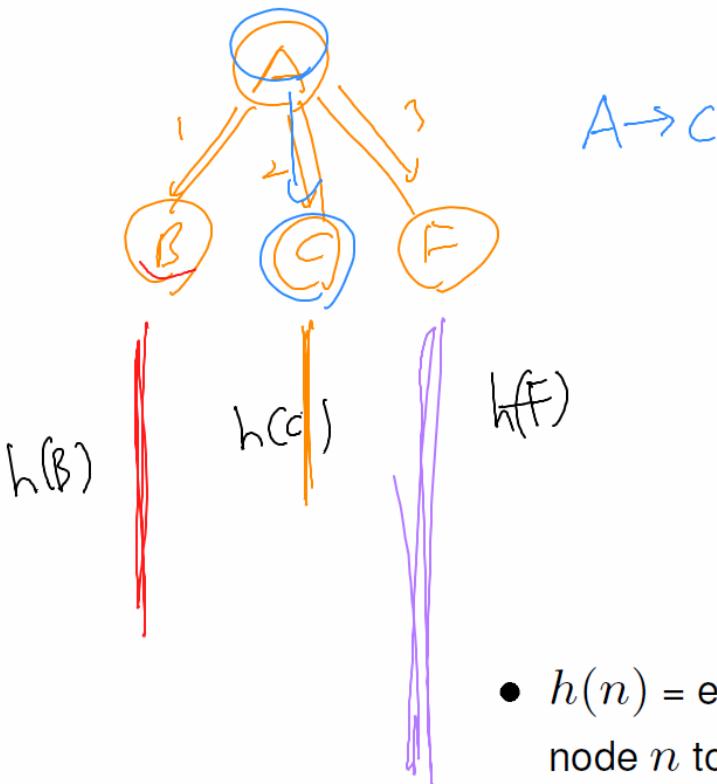
Best First Search

```
function Best-First-Search (problem, Eval-Fn)
    Queuing-Fn ← sorted list by Eval-Fn(node)
    return General-Search(problem, Queuing-Fn)
```



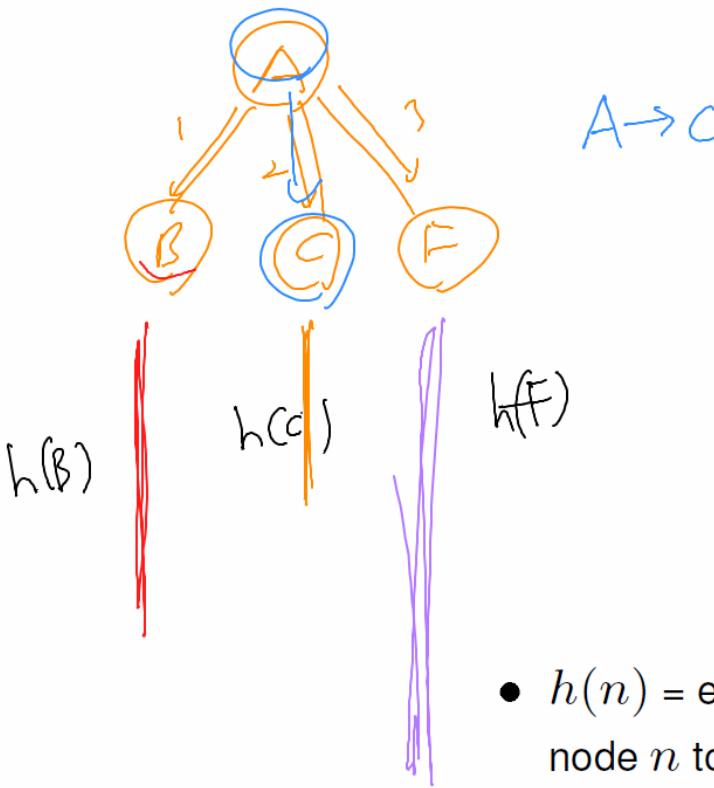
- The queuing function queues the expanded nodes, and sorts it every time by the *Eval-Fn* value of each node.
- One of the simplest Eval-Fn: **estimated cost** to reach the goal.



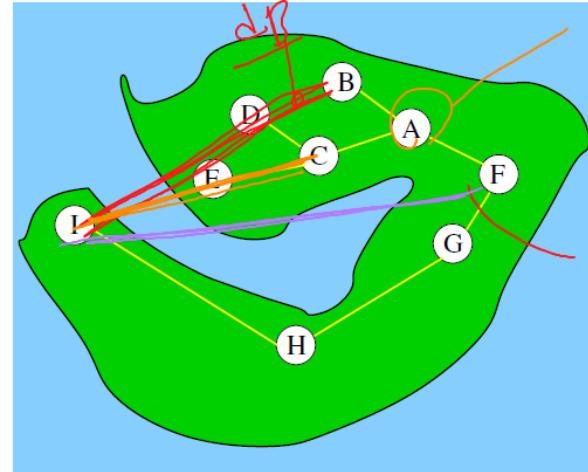


- $h(n)$ = estimated cost of the cheapest path from the state at node n to a goal state.
- The only requirement is the $h(n) = 0$ at the goal.
- **Heuristics** means “to find” or “to discover”, or more technically, “how to solve problems” (Polya, 1957).

Right, given just this information, see it looks the most promising. You don't know the exact map.



Heuristic Function

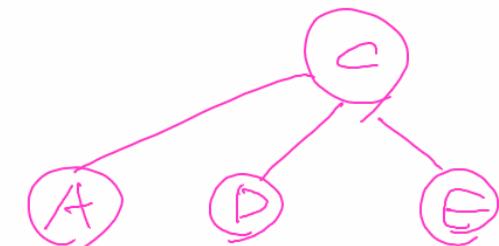


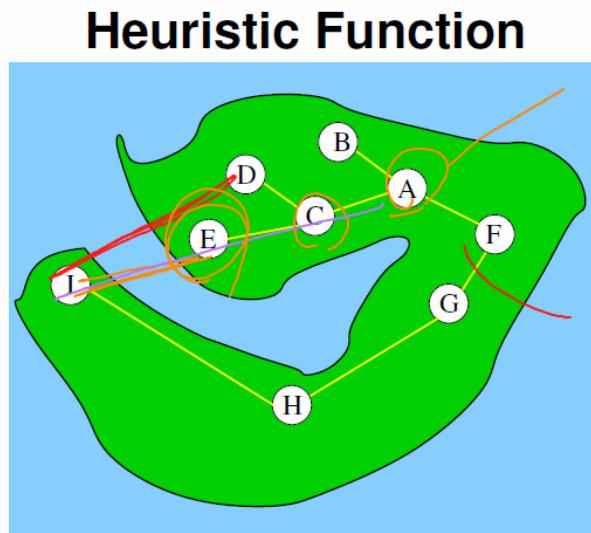
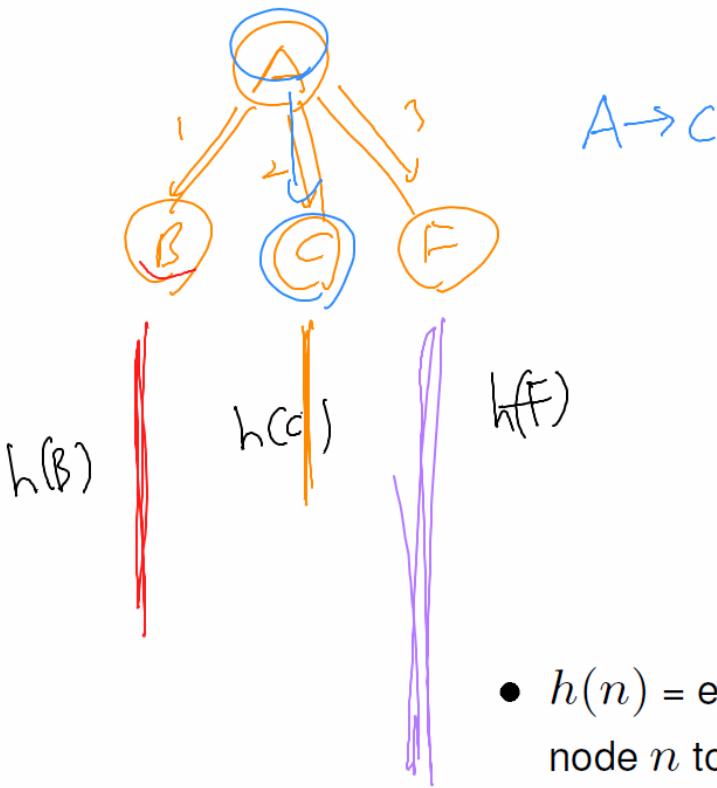
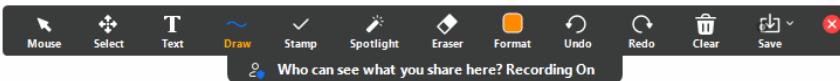
Init

straight line dist



- $h(n)$ = estimated cost of the cheapest path from the state at node n to a goal state.
- The only requirement is the $h(n) = 0$ at the goal.
- **Heuristics** means “to find” or “to discover”, or more technically, “how to solve problems” (Polya, 1957).



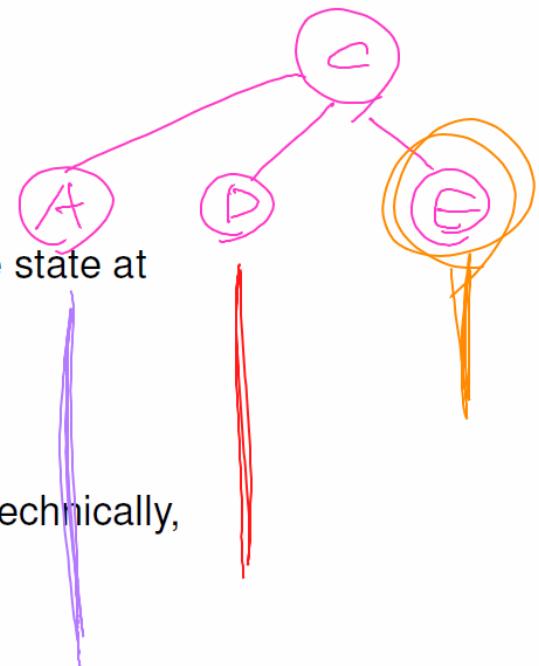


- $h(n)$ = estimated cost of the cheapest path from the state at node n to a goal state.
- The only requirement is the $h(n) = 0$ at the goal.
- **Heuristics** means “to find” or “to discover”, or more technically, “how to solve problems” (Polya, 1957).

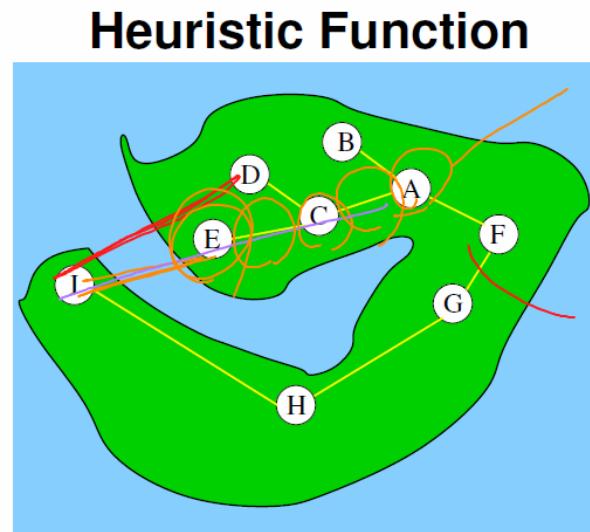
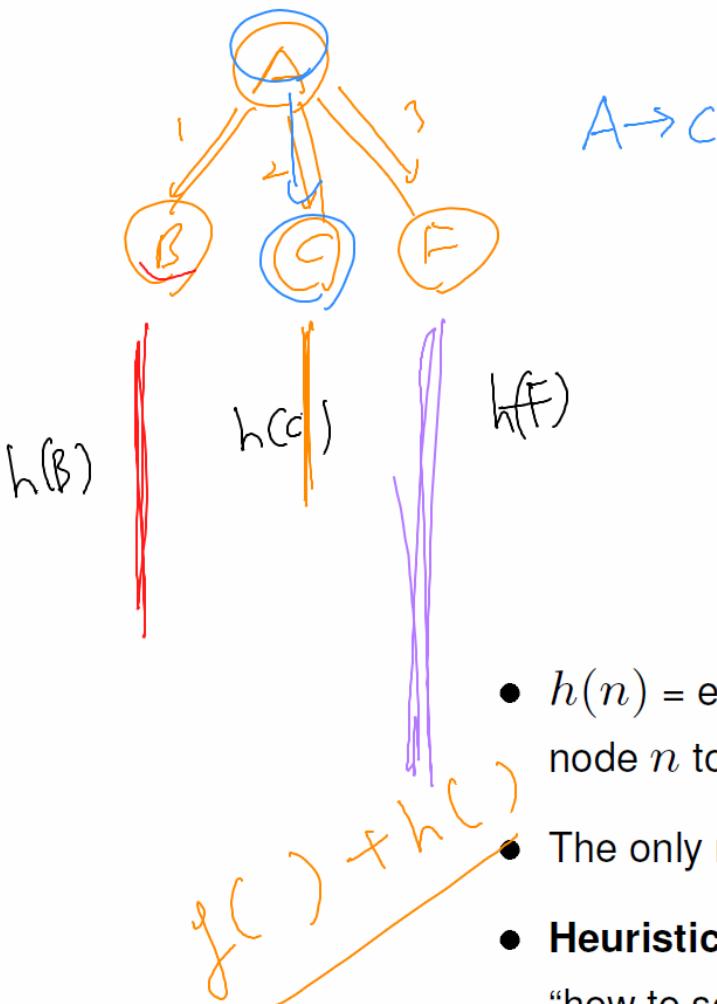
A → C → E
Init



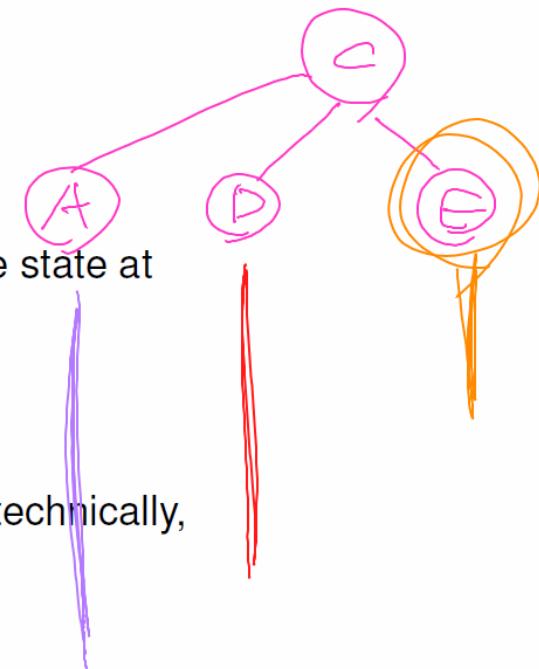
straight line dist



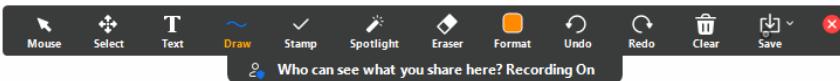
Right. And they have to go back. So, this case, there's use the function doesn't help you that much.



- $h(n)$ = estimated cost of the cheapest path from the state at node n to a goal state.
- The only requirement is the $h(n) = 0$ at the goal.
- **Heuristics** means “to find” or “to discover”, or more technically, “how to solve problems” (Polya, 1957).



So if you also consider G, as well as the shoe is the function, then this find you document.



Greedy Best-First Search



```
function Greedy-Best-First Search (problem)
```

$h(n)$: estimated cost from n to goal

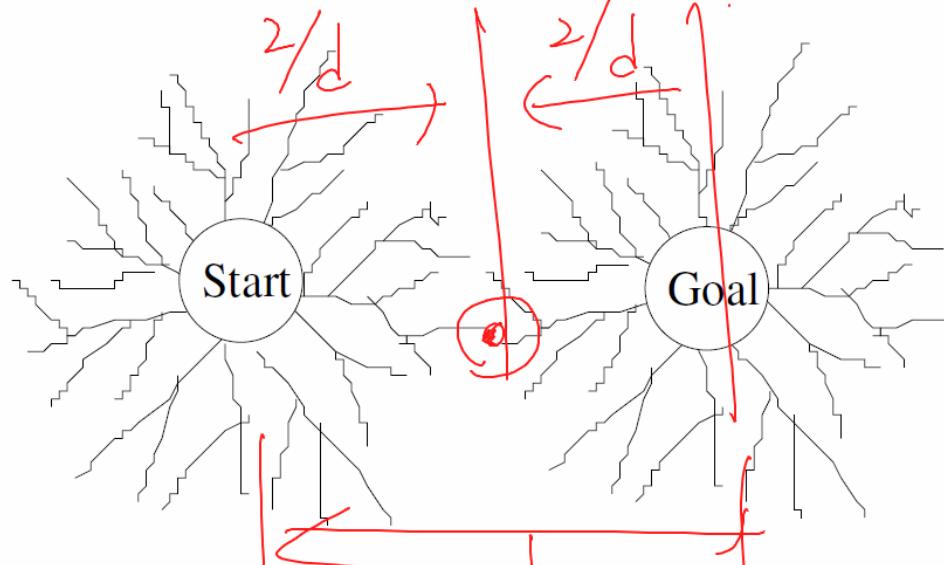
return Best-First-Search(problem, h)

eval-fn

- Best-first with heuristic function $h(n)$ as evaluation function.



Bidirectional Search (BDS)



- Search from both initial state and goal to reduce search depth.

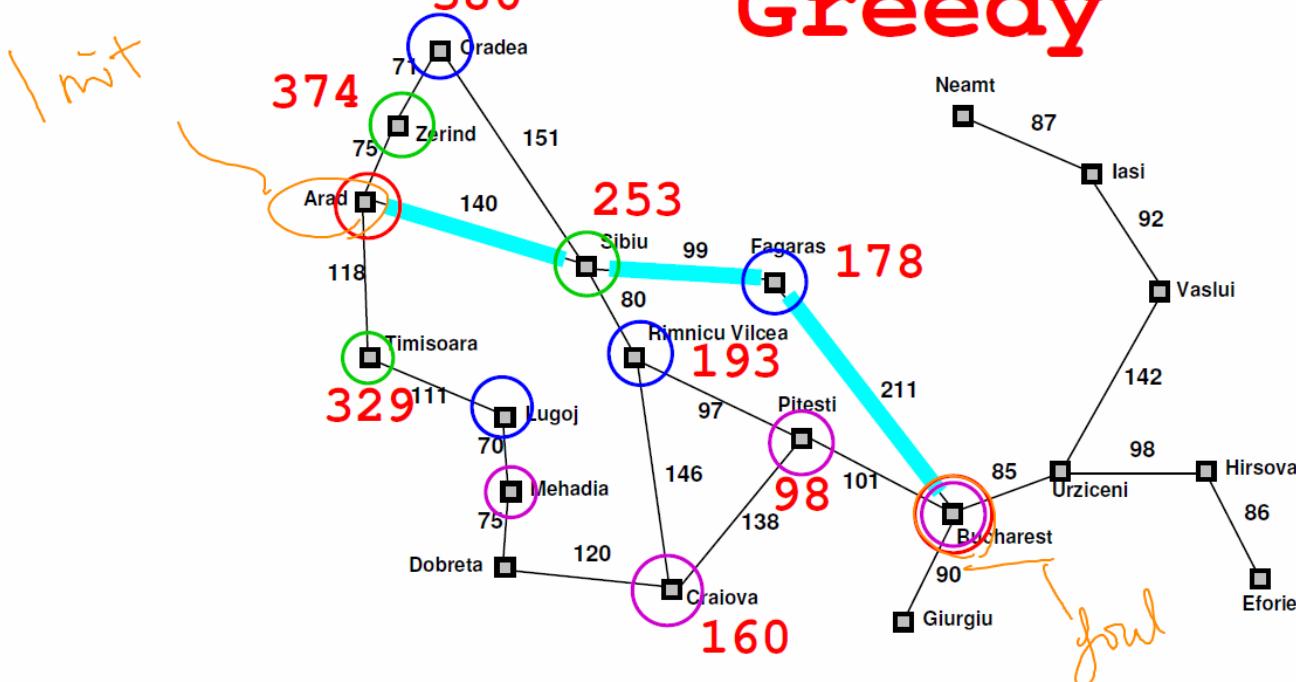
- $O(b^{d/2})$ of BDS vs. $O(b^{d+1})$ of BFS.





Romania with step costs in km

Greedy



Straight-line distance to Bucharest

<u>Arad</u>	366
<u>Bucharest</u>	0
Craiova	160
Dobreta	242
Eforie	161
Fagaras	178
Giurgiu	77
Hirsova	151
Iasi	226
Lugoj	244
Mehadia	241
Neamt	234
Oradea	380
Pitesti	98
Rimnicu Vilcea	193
Sibiu	253
Timisoara	329
Urziceni	80
Vaslui	199
Zerind	374

Total Path Cost = 450

This is the goal to all of these cities, so era, is the first city, that we can see this is supposed to be the initial state.

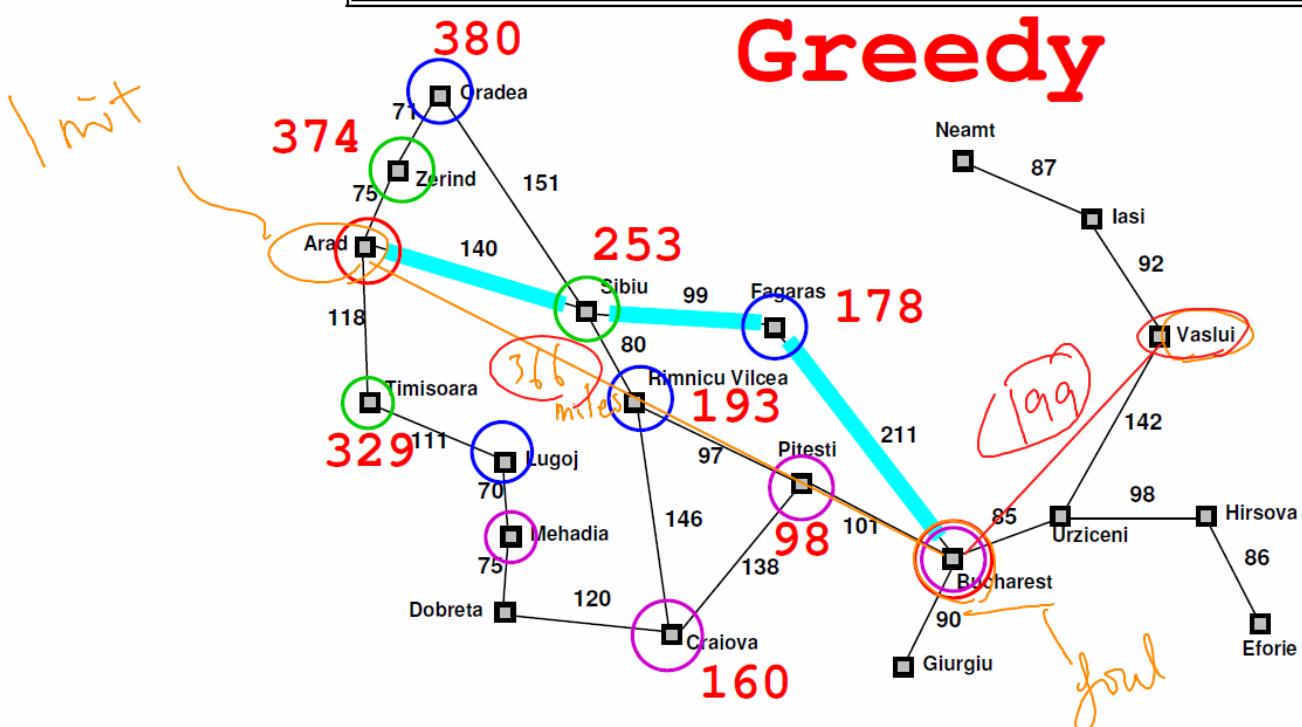
You are screen sharing Stop Share

$h_{SLD}(n)$



Romania with step costs in km

Greedy



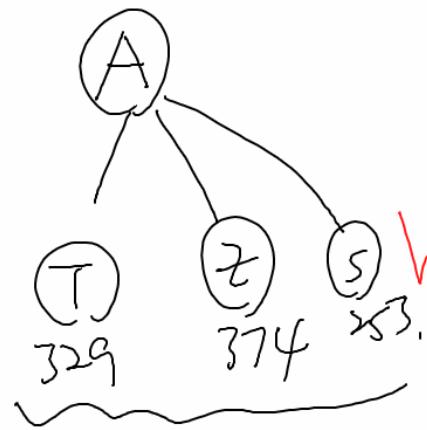
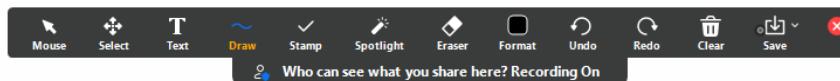
Straight-line distance to Bucharest	
Arad	366
Bucharest	0
Craiova	160
Dobreta	242
Eforie	161
Fagaras	178
Giurgiu	77
Hirsova	151
Iasi	226
Lugoj	244
Mehadia	241
Neamt	234
Oradea	380
Pitesti	98
Rimnicu Vilcea	193
Sibiu	253
Timisoara	329
Urziceni	80
Vaslui	199
Zerind	374

Total Path Cost = 450

So this is the HSLD of a particular.

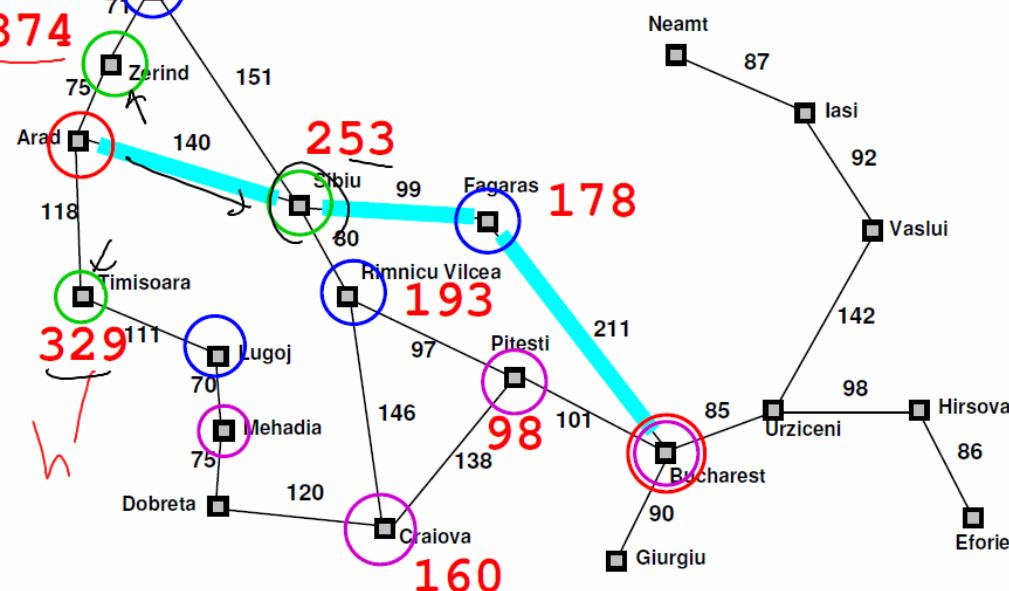
42

You are screen sharing Stop Share



Romania with step costs in km

Greedy



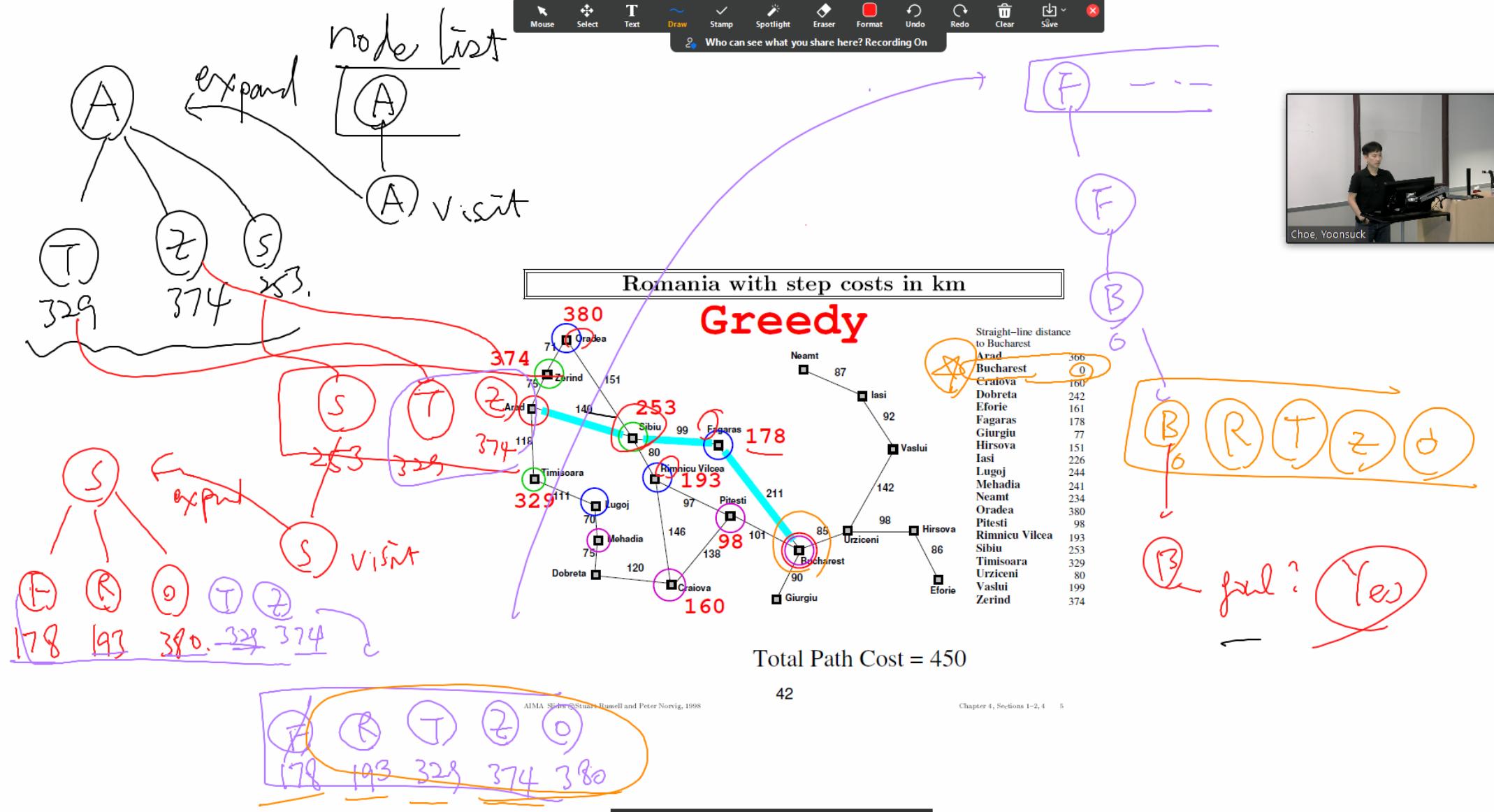
Straight-line distance to Bucharest	
Arad	366
Bucharest	0
Craiova	160
Dobreta	242
Eforie	161
Fagaras	178
Giurgiu	77
Hirsova	151
Iasi	226
Lugoj	244
Mehadia	241
Neamt	234
Oradea	380
Pitesti	98
Rimnicu Vilcea	193
Sibiu	253
Timisoara	329
Urziceni	80
Vaslui	199
Zerind	374

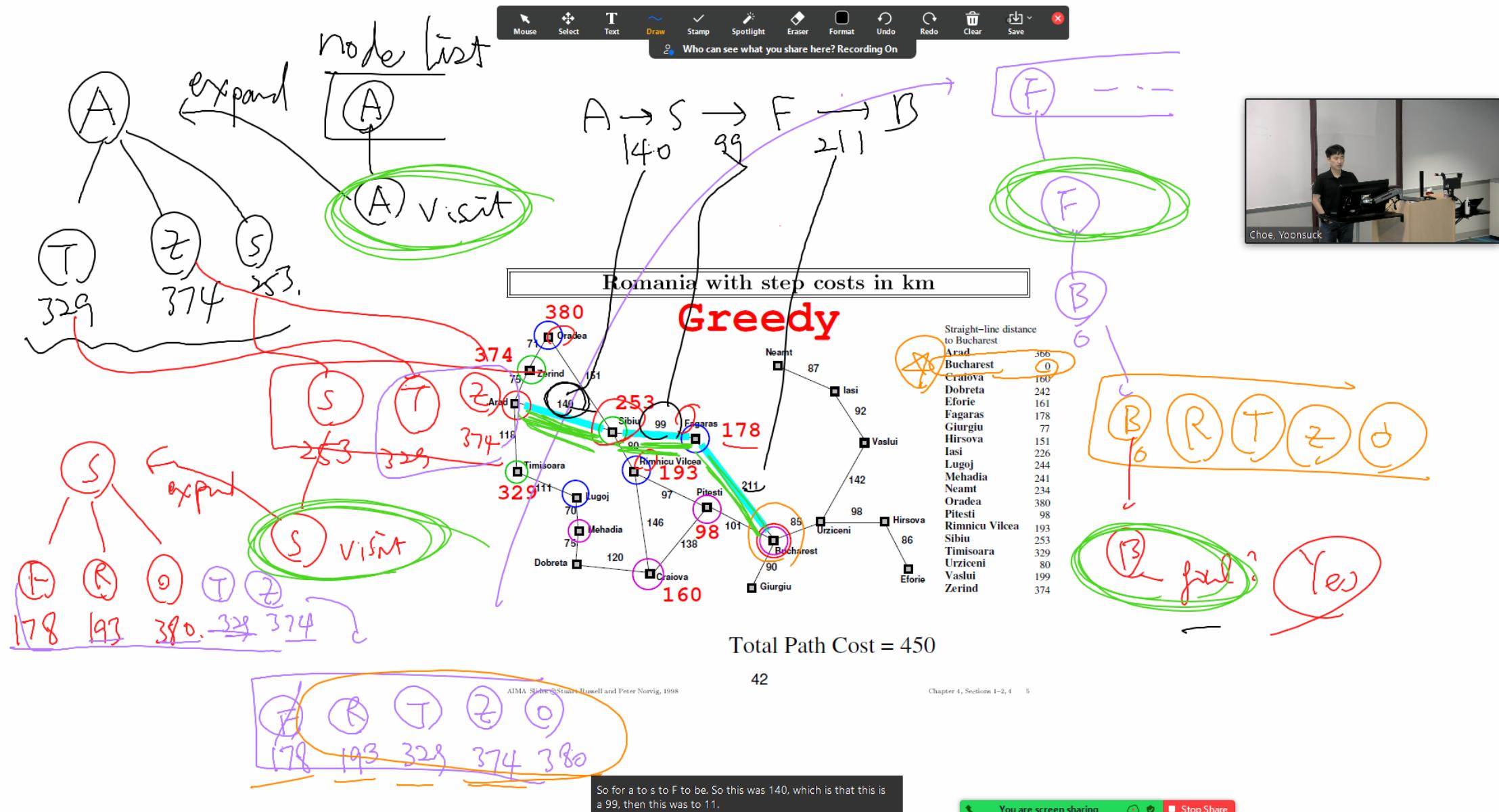
Total Path Cost = 450

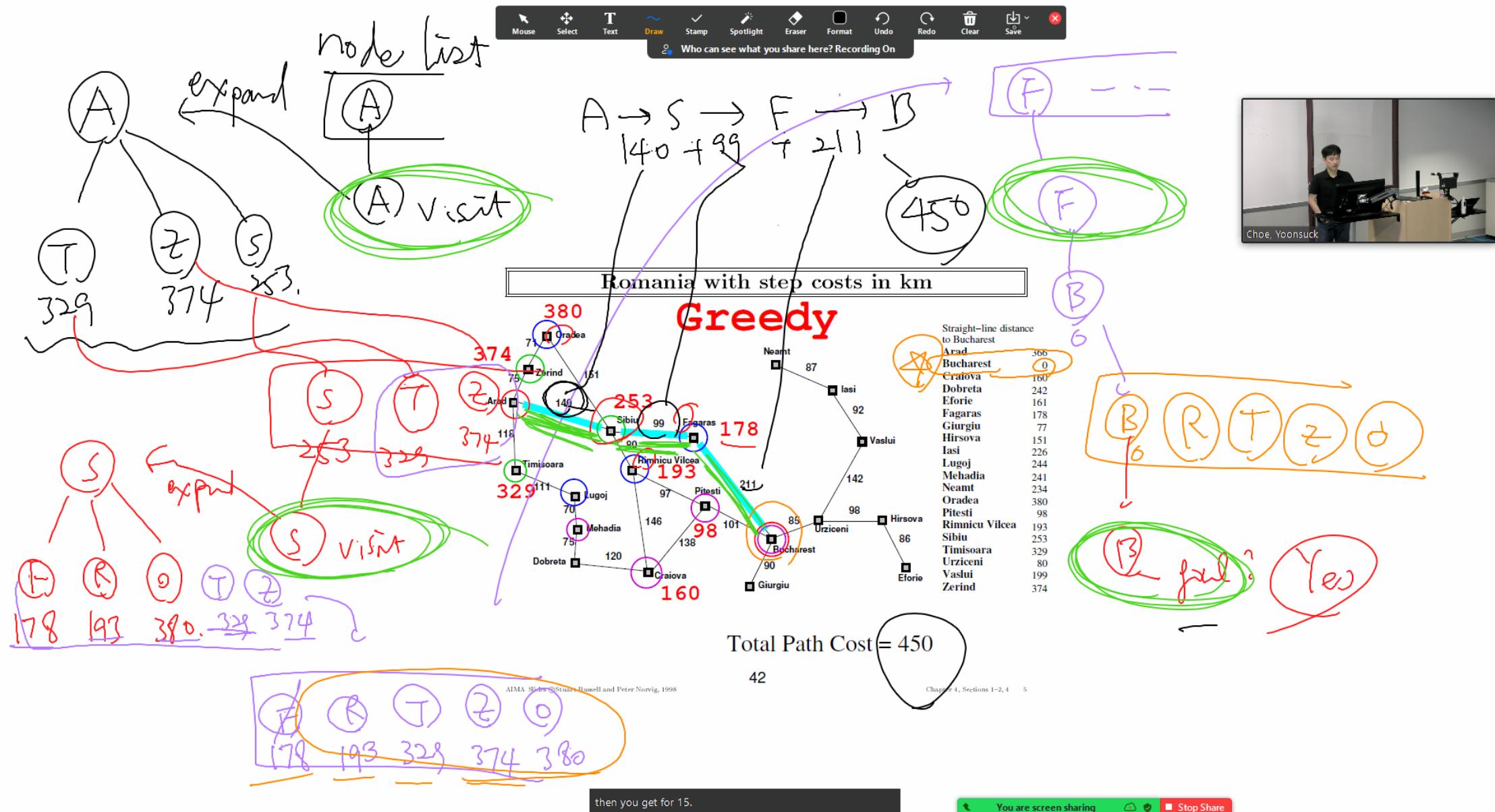
So this. So basically, these nodes, those would be separated so if you look at the

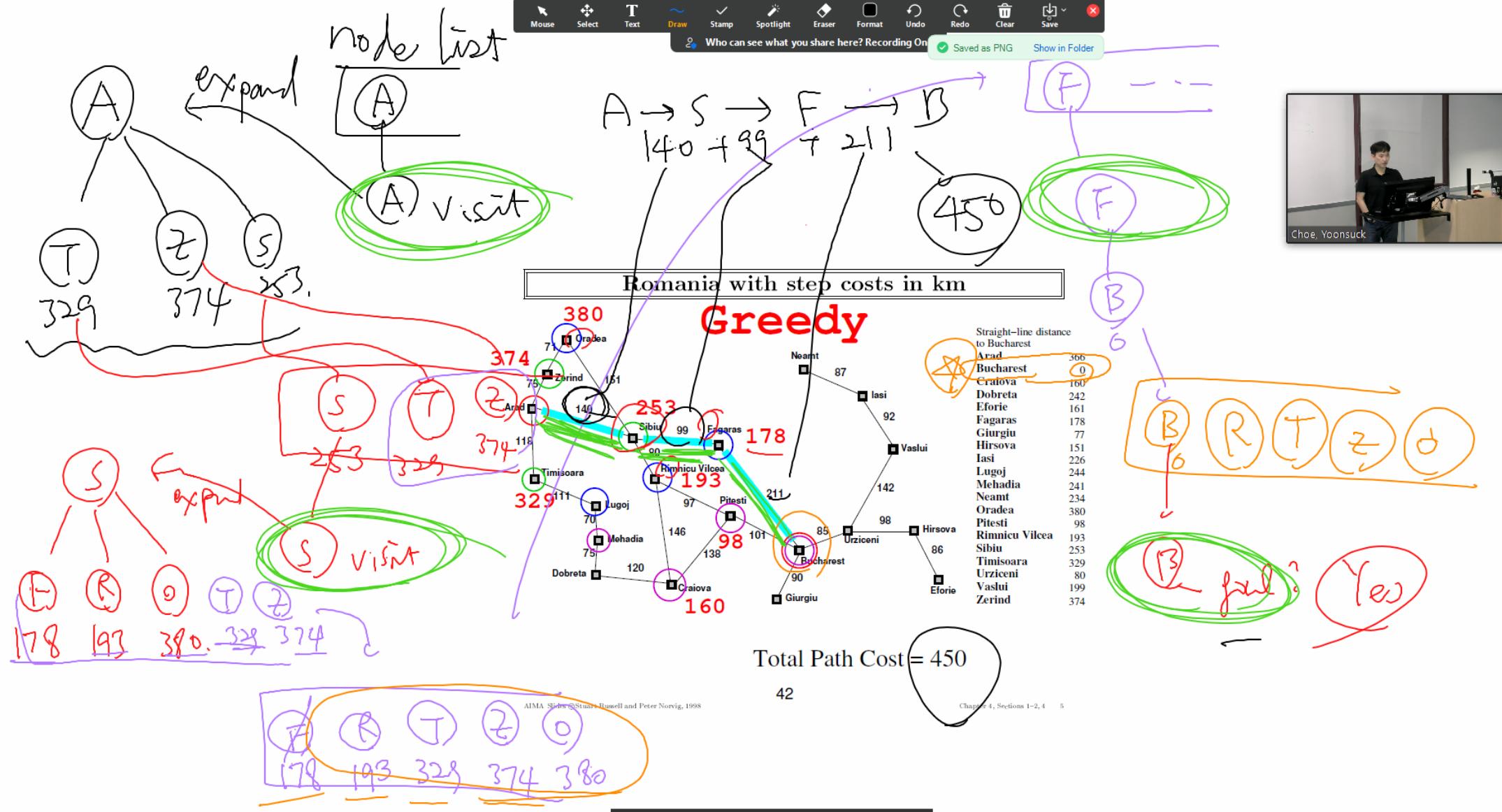
42

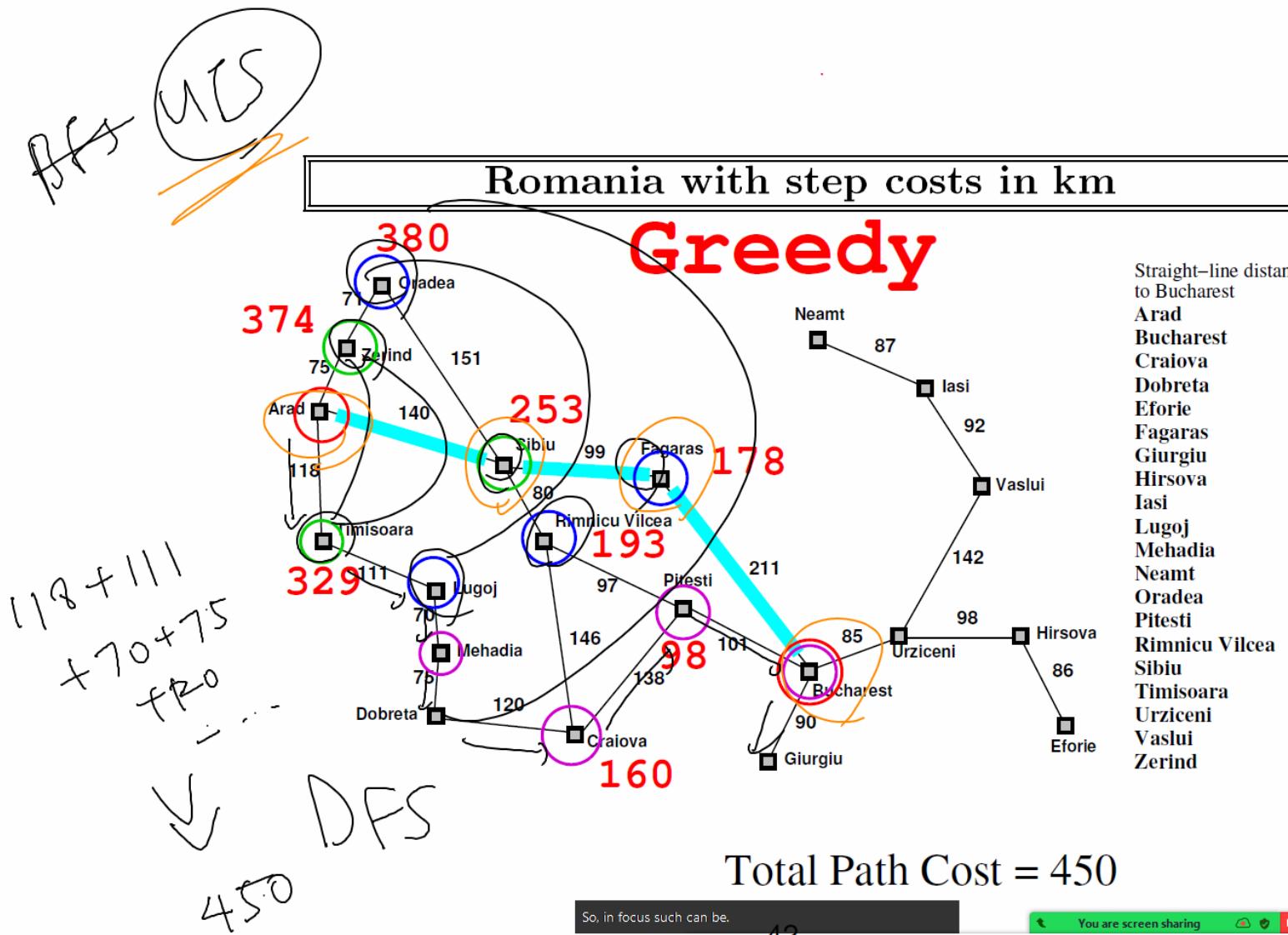
You are screen sharing



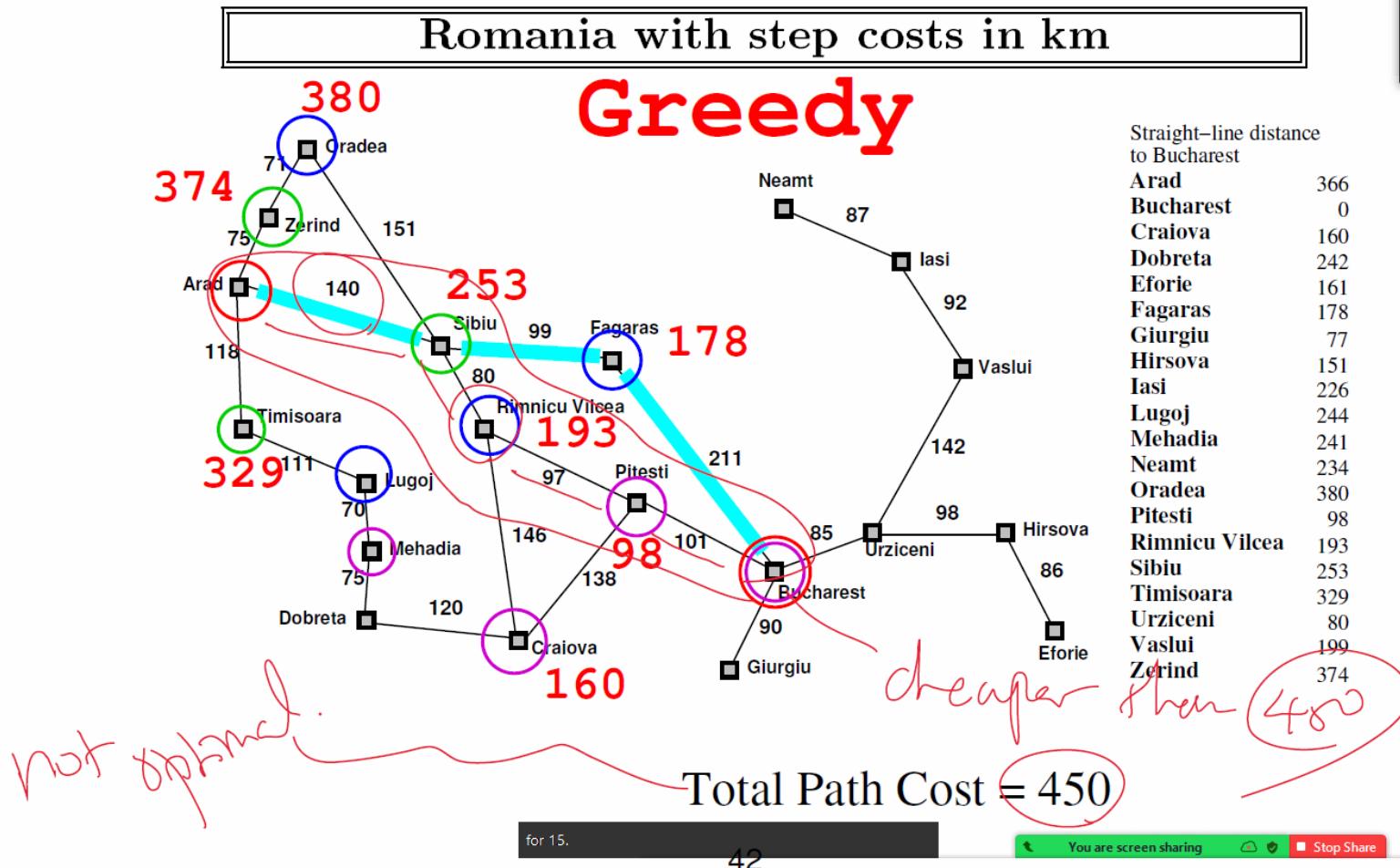
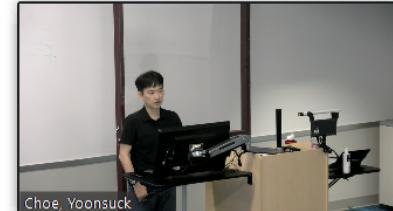








Straight-line distance to Bucharest	
Arad	366
Bucharest	0
Craiova	160
Dobreta	242
Eforie	161
Fagaras	178
Giurgiu	77
Hirsova	151
Iasi	226
Lugoj	244
Mehadia	241
Neamt	234
Oradea	380
Pitesti	98
Rimnicu Vilcea	193
Sibiu	253
Timisoara	329
Urziceni	80
Vaslui	199
Zerind	374





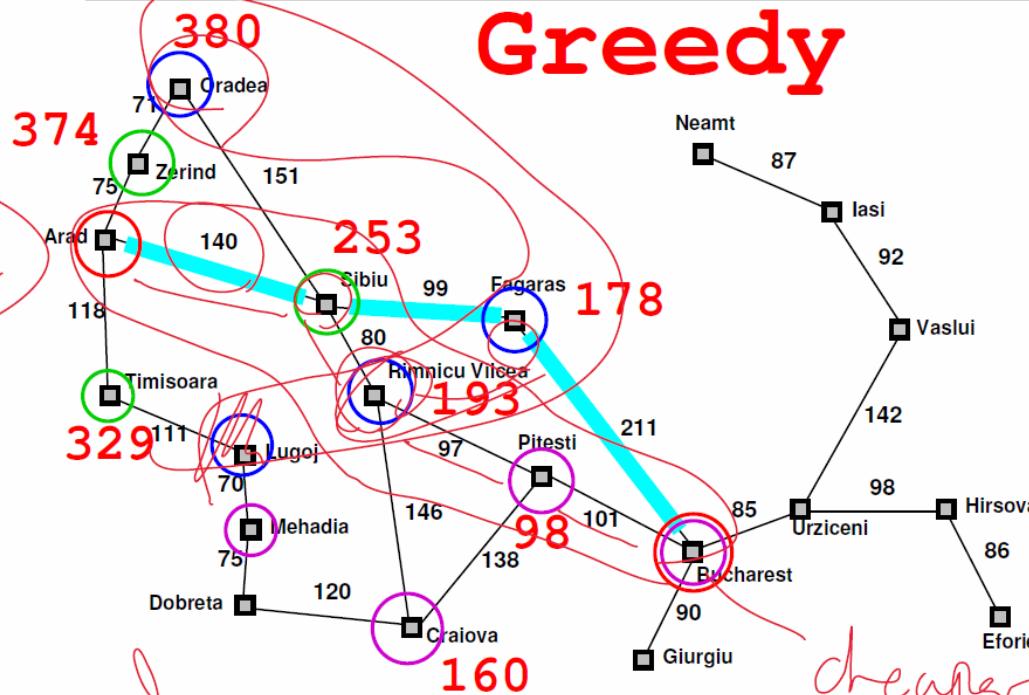
287

27

ORF 27

Romania with step costs in km

Greedy



Straight-line distance to Bucharest

Arad	366
Bucharest	0
Craiova	160
Dobreta	242
Eforie	161
Fagaras	178
Giurgiu	77
Hirsova	151
Iasi	226
Lugoj	244
Mehadia	241
Neamt	234
Oradea	380
Pitesti	98
Rimnicu Vilcea	193
Sibiu	253
Timisoara	329
Urziceni	80
Vaslui	199
Zerind	374

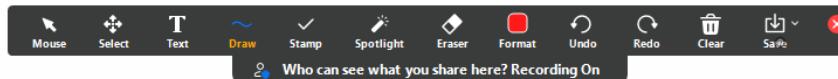
not optimal cheaper than 450

Total Path Cost = 450

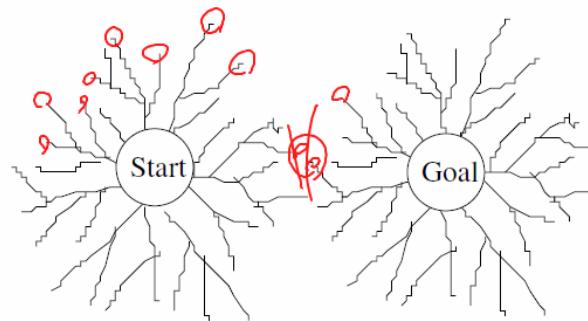
So, in the worst case this can also grow up explanation.

42

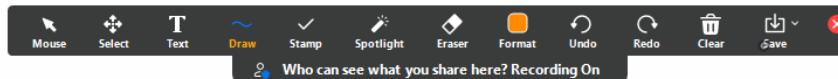
You are screen sharing Stop Share



BDS: Considerations



1. how to back trace from the goal?
2. successors and predecessors: are operations reversible?
3. are goals explicit?: need to know the goal to begin with
4. check overlap in two branches
5. BFS? DFS? which strategy to use? Same or different?



Greedy Best-First Search: Evaluation

Branching factor b and max depth m :



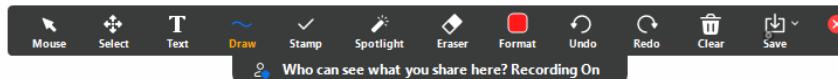
- Fast, just like Depth-First-Search: directed path toward the goal.
- Time: $O(b^m)$
- Space: same as time, in the worst case (bad heuristic function),
unlike DFS
- Incomplete, just like DFS
- Non-optimal, just like DFS

infinite depth

finite

even when

So if it is a finite then it will be complete, somehow.



$$h(G) = 0$$

A*: Uniform Cost + Heuristic Search

$$f(n)$$

$$h(n)$$

Avoid visiting paths that are already found to be expensive:

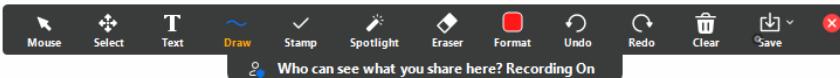
- $f(n) = g(n) + h(n)$
- $f(n)$: estimated cost to goal that goes through node n
- **provably complete and optimal!**
- **restrictions:** $h(n)$ should be an **admissible heuristic**
- admissible heuristic: one that **never overestimate** the actual cost of the best solution through n

$$h(n) \leq h^*(n)$$

true
cost



Choe, Yoonsuck



A* Search



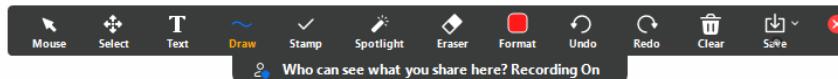
exair

```
function A*-Search (problem)
    g(n): current cost up till n
    h(n): estimated cost from n to goal
    return Best-First-Search(problem, g + h)
```

est.

eval-fn

- Condition: $h(n)$ must be an **admissible heuristic function!**
- A* is **complete and optimal!**



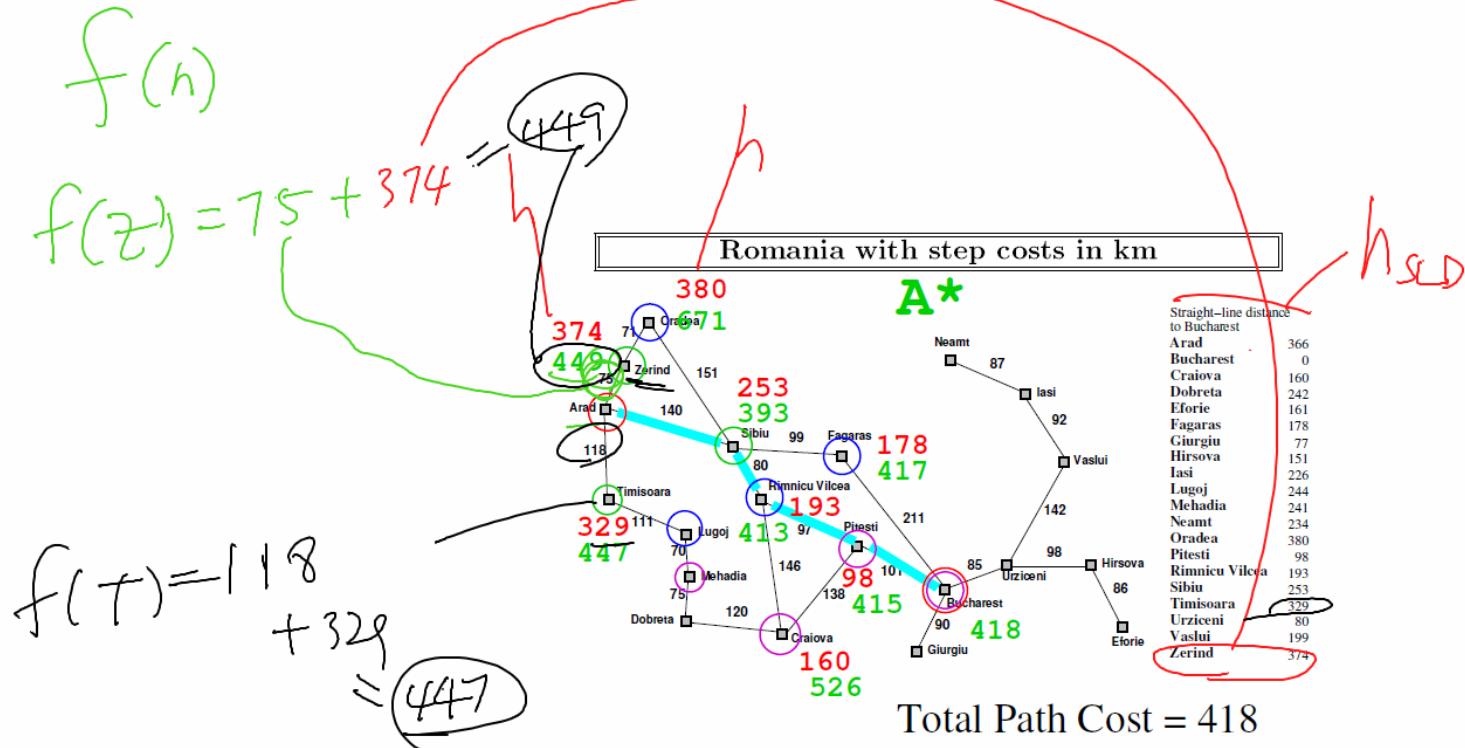
Behavior of A* Search



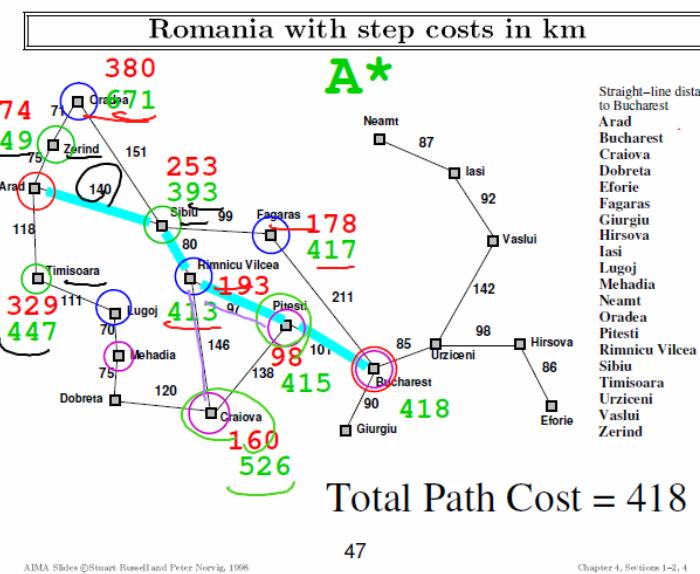
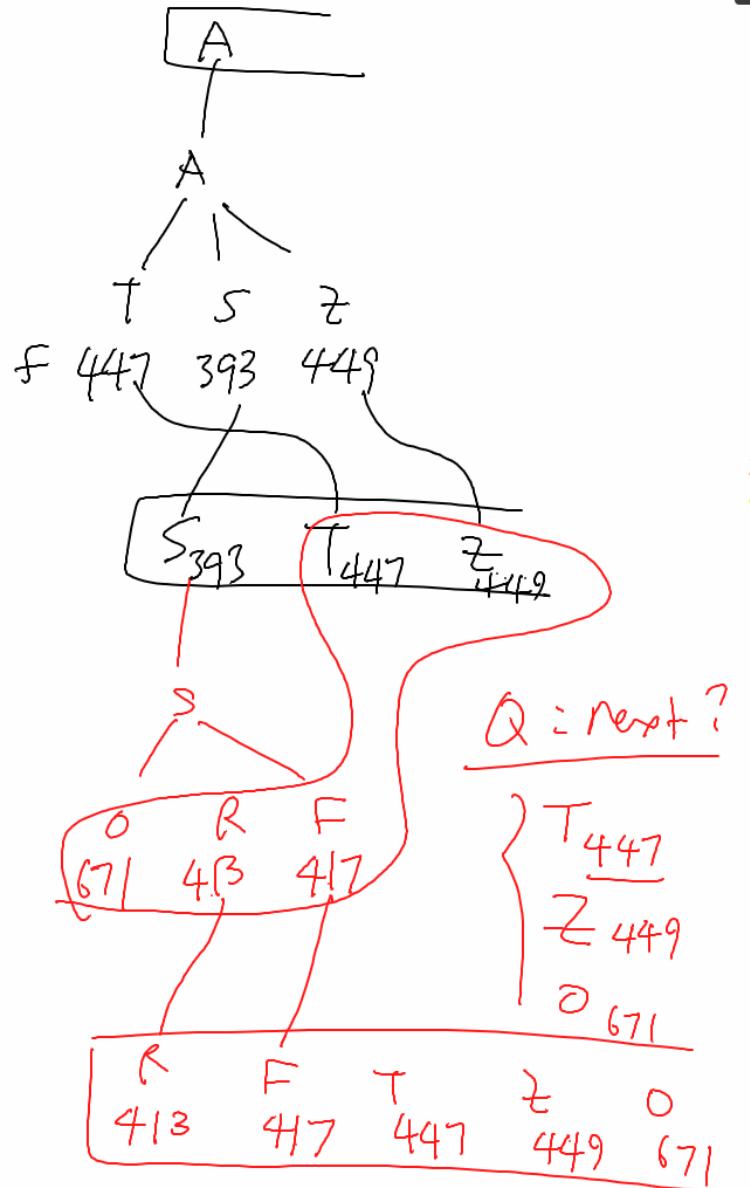
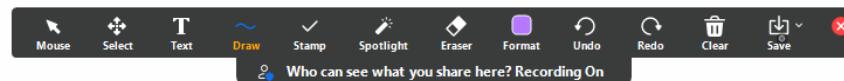
- usually, the f value never decreases along a given path:
monotonicity
- in case it is nonmonotonic, i.e. $f(\text{Child}) < f(\text{Parent})$,
make this adjustment:
$$f(\text{Child}) = \max(f(\text{Parent}), g(\text{Child}) + h(\text{Child})).$$
- this is called **pathmax**

And there are some ways of making sure that this properties mean.

You are screen sharing Stop Share



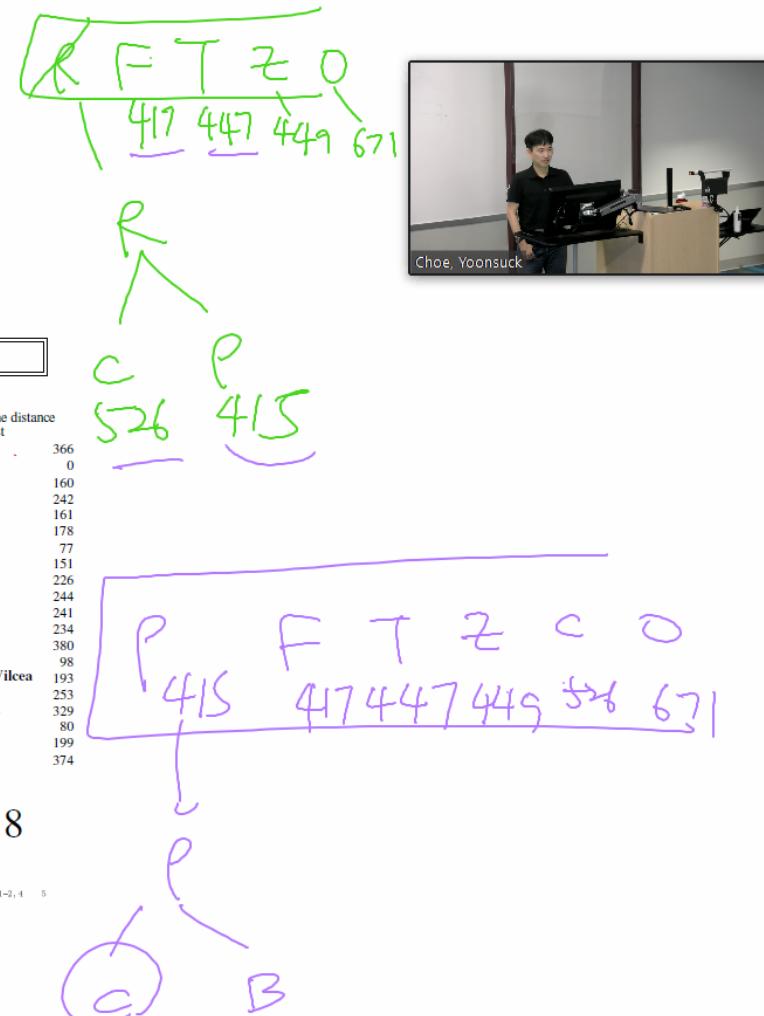
plus the uCLA function value of team, which is 329, which gives you, 447.

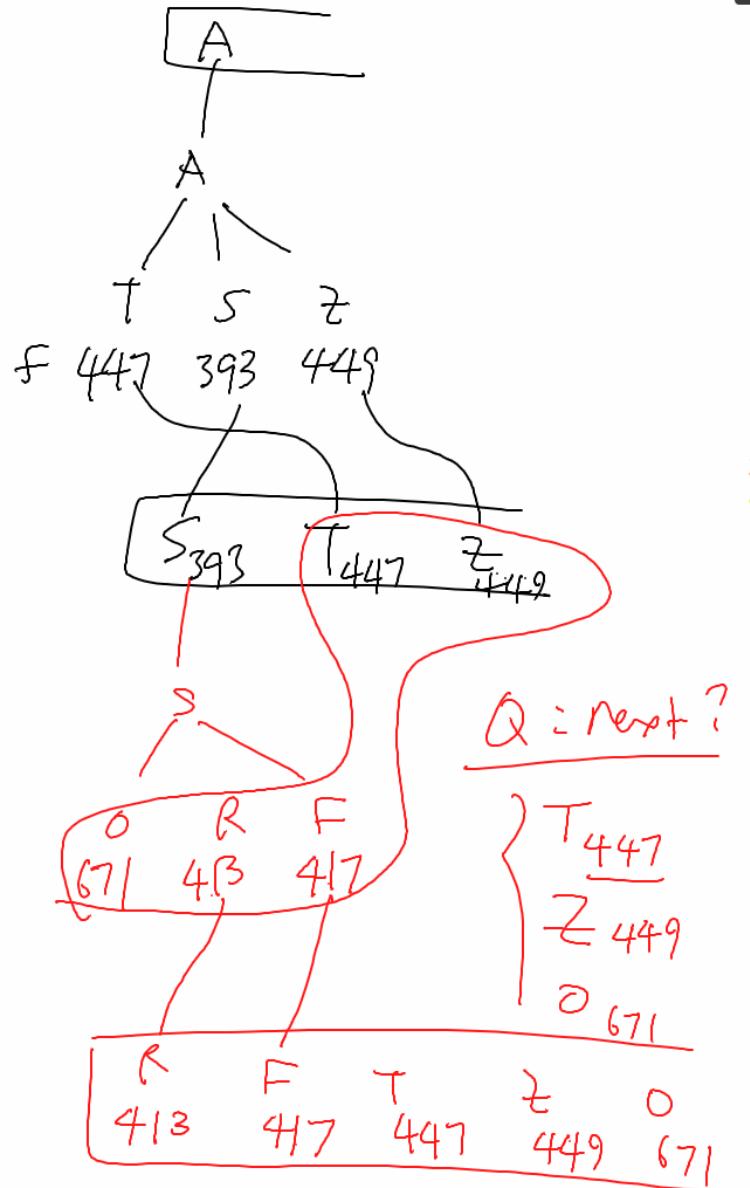
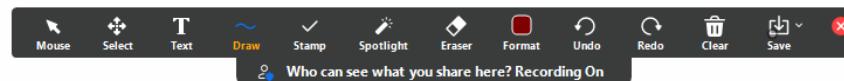


Actually this he has a different value.

You are screen sharing

Stop Share



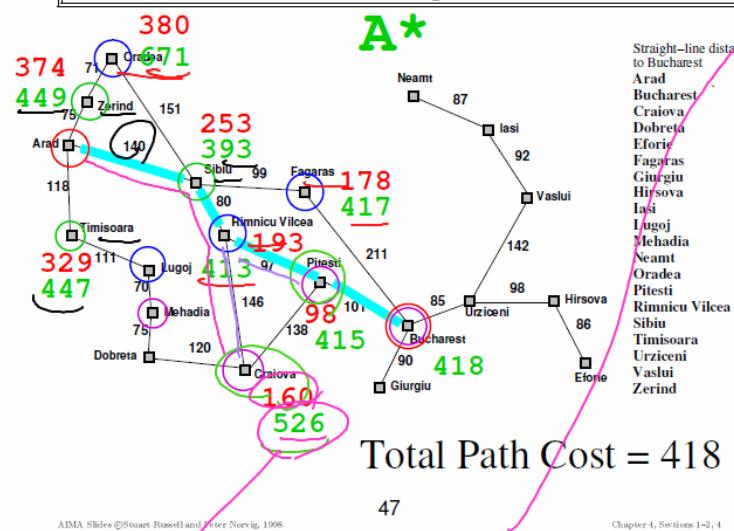


$A \rightarrow S$
140

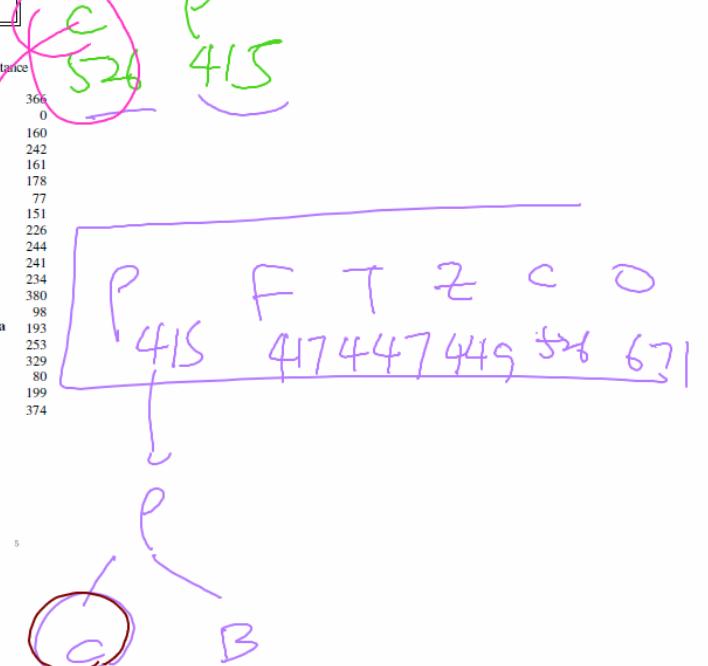
R F T Z O
417 447 449 671



Romania with step costs in km

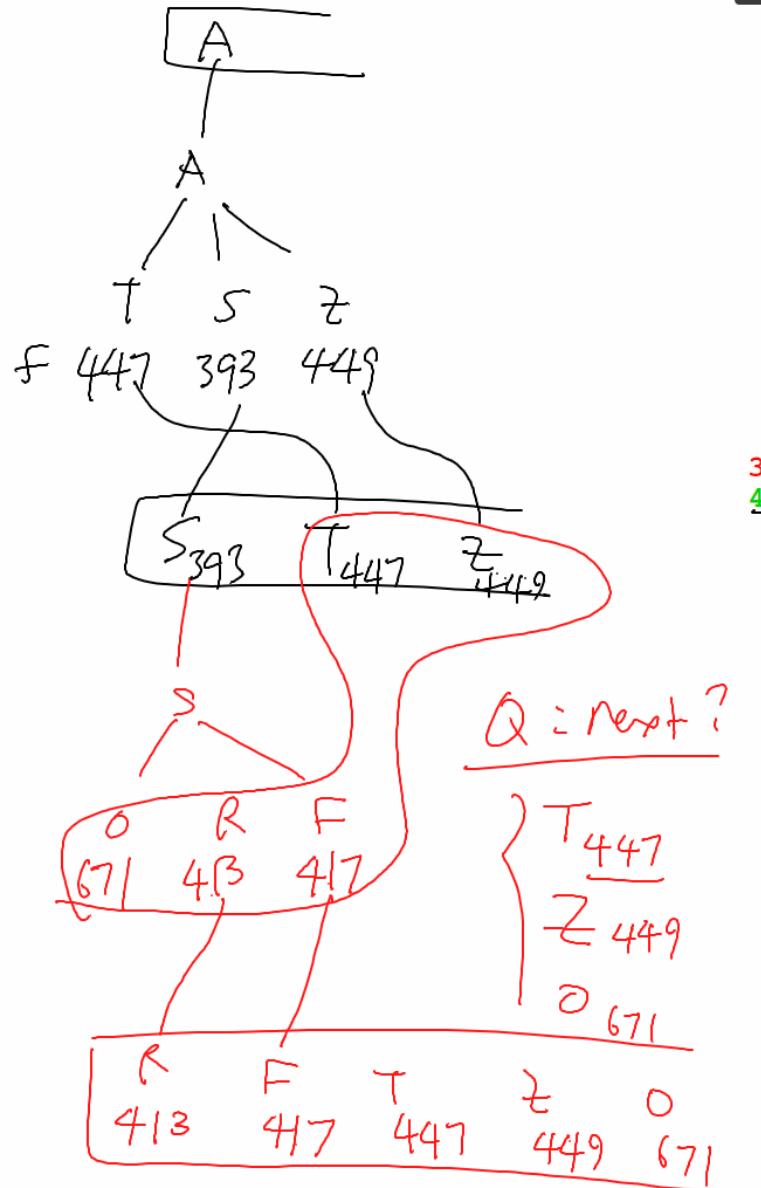
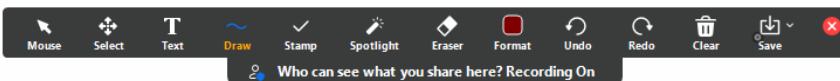


$$140 + 80 + 146 + 160$$



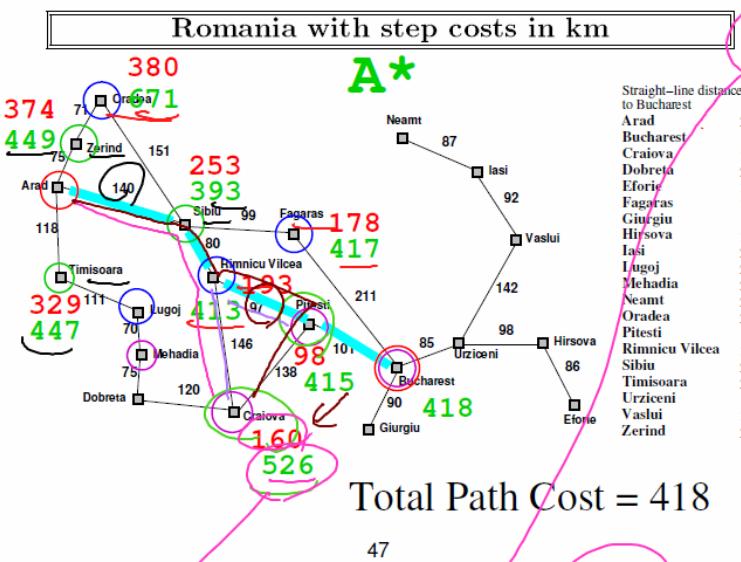
But we encounter see once again here.

You are screen sharing Stop Share



$A \rightarrow S$
140

R F T Z O
417 447 449 671

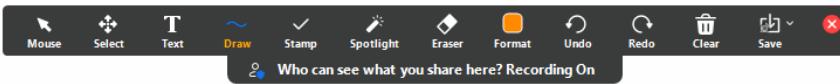


$$140 + 80 + 146 + 160 = 526$$

$$140 + 80 + 97 + 138 + 160 = 515$$

You are screen sharing

Stop Share



B_0 F T z C O
417 447 449 515 526 671

B_0

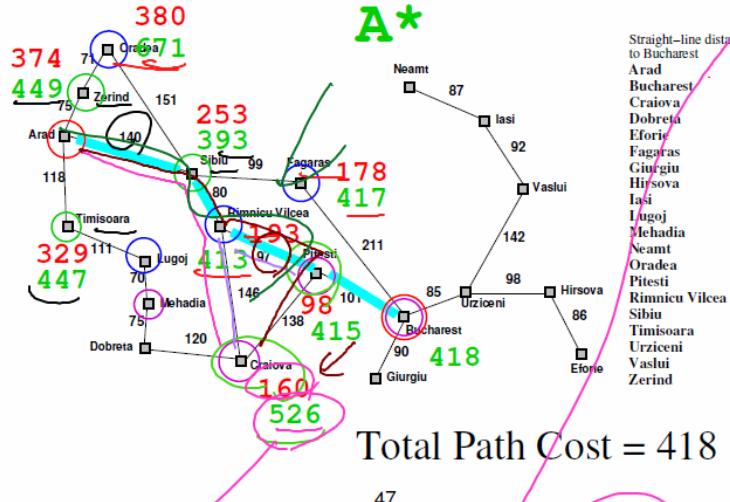
A-S-R-P-C

A \rightarrow S
140

R F T z O
417 447 449 671



Romania with step costs in km
A*



Total Path Cost = 418

$$140 + 80 + 146 + 160 + 526$$

You are screen sharing Stop Share

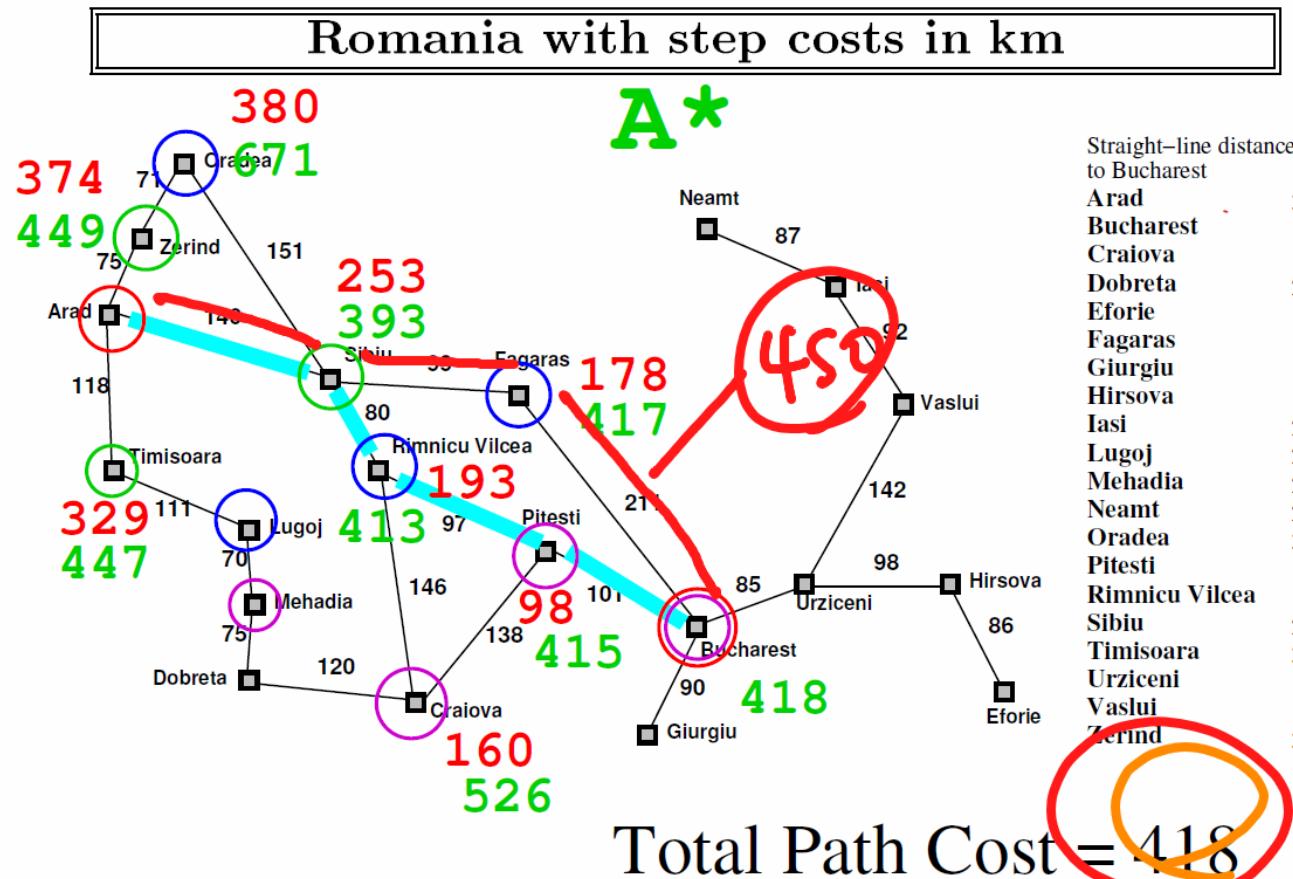
R F T z C O
413 417 447 449 526 671

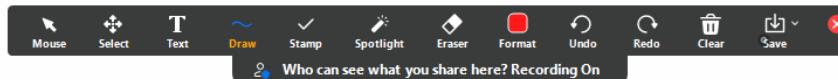
$(220 + 100) / 220 \times 3 - 2 \times STS$
 $+ (40) / 360 \times 2 = STS$

$140 + 80 + 197 + 138 + 160 = STS$

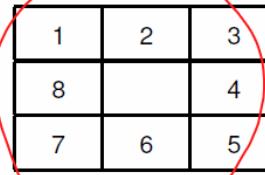
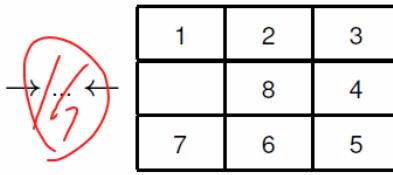
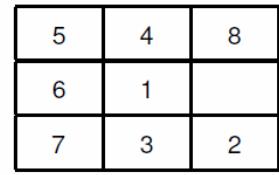
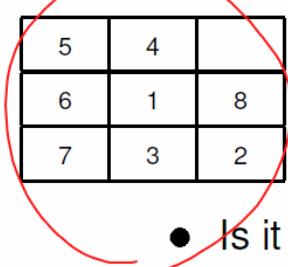
Right. So, the point is, I guess, conveyed.

$A \rightarrow S \rightarrow R \rightarrow P \rightarrow B$





BDS Example: 8-Puzzle

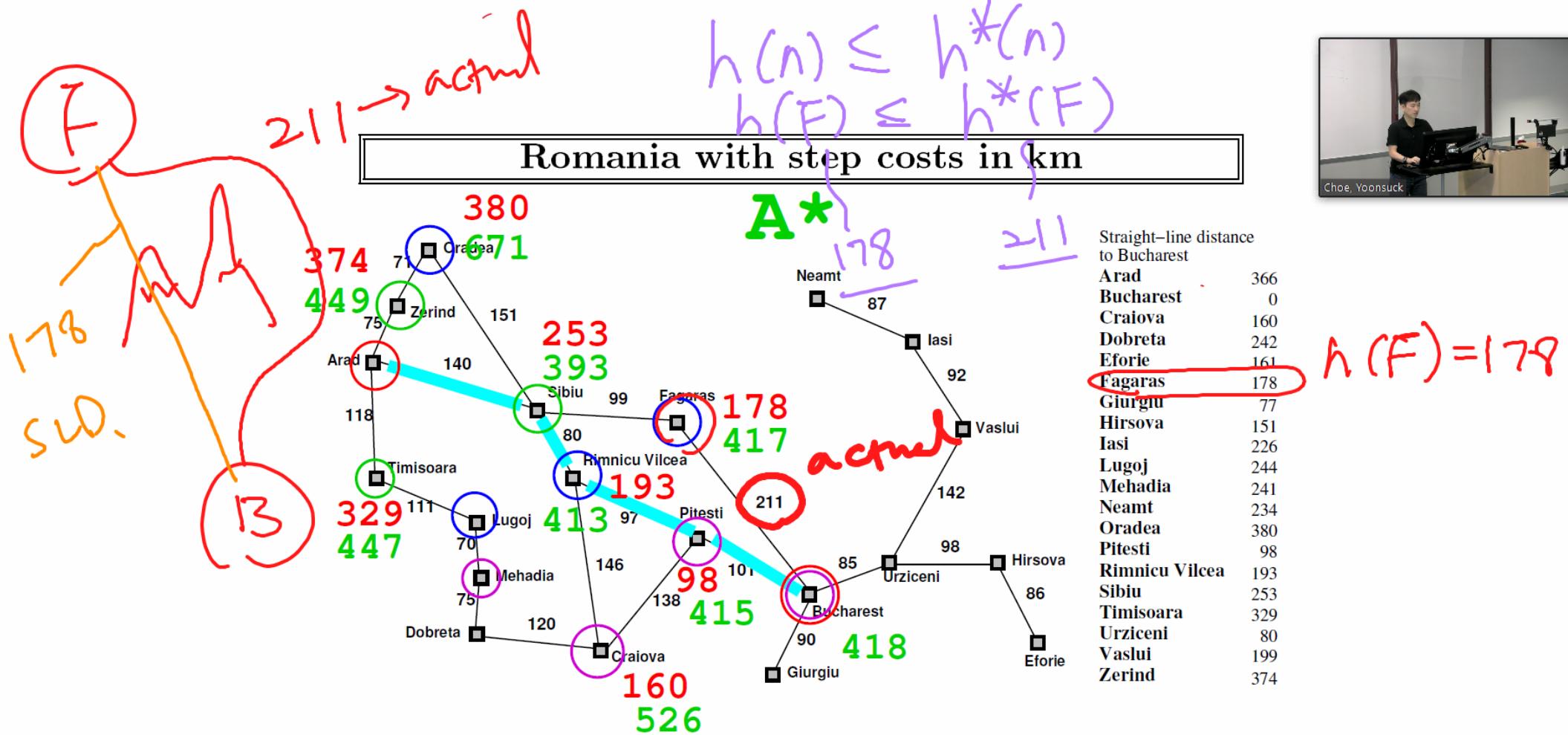


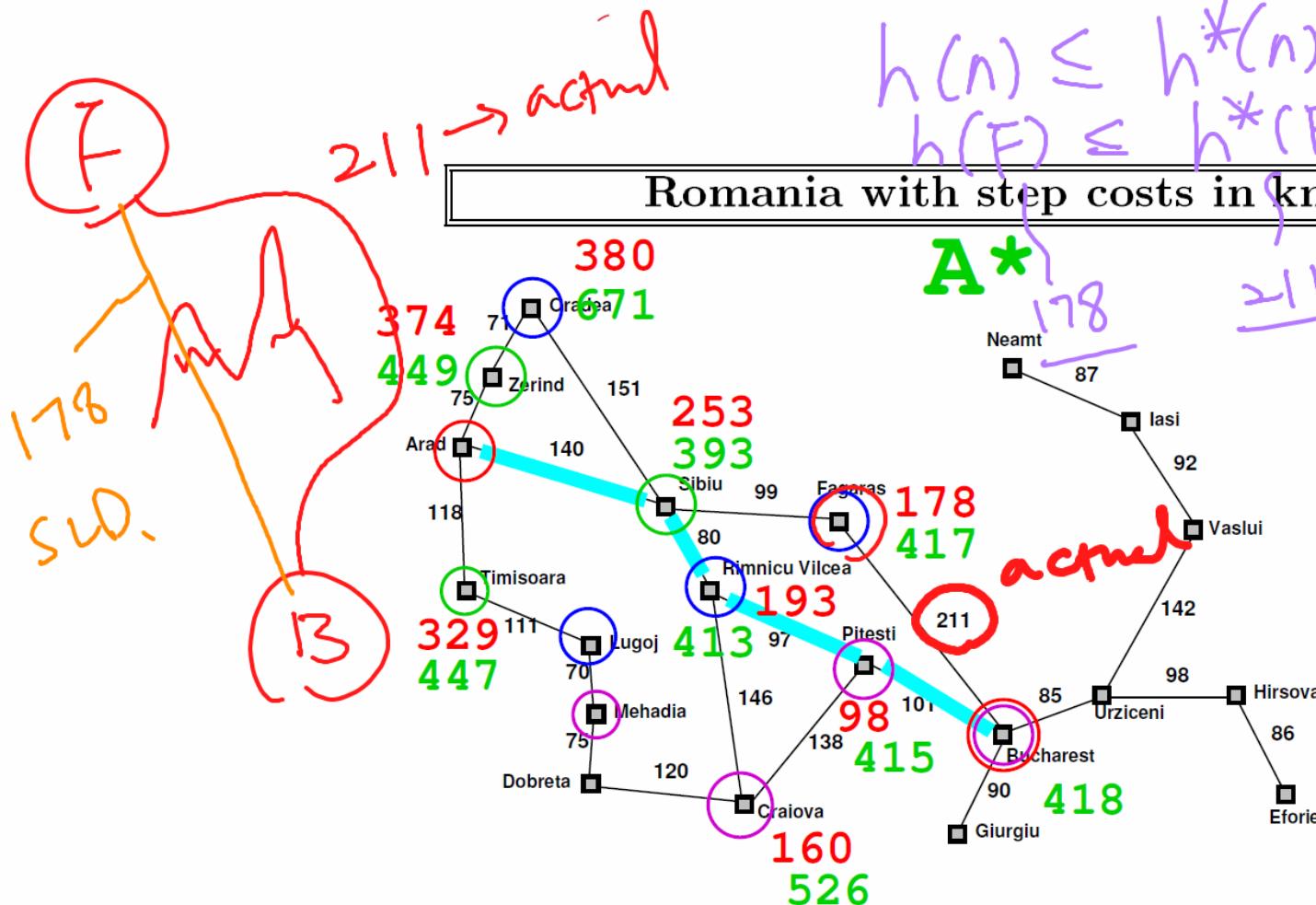
- Is it a good strategy?
- What about Chess? Would it be a good strategy?
- What kind of domains may be suitable for BDS?



And this is the goal state. So you start moving the tiles from the initial state, that way and then you start moving the tiles from the state backward and hope to meet some.

You are screen sharing Stop Share





Straight-line distance to Bucharest	
Arad	366
Bucharest	0
Craiova	160
Dobreta	242
Eforie	161
Fagaras	178
Giurgiu	77
Hirsova	151
Iasi	226
Lugoj	244
Mehadia	241
Neamt	234
Oradea	380
Pitesti	98
Rimnicu Vilcea	193
Sibiu	253
Timisoara	329
Urziceni	80
Vaslui	199
Zerind	374

$$h(p) = 98$$

$$h^*(p) = 101$$

$$h(R) = 193$$

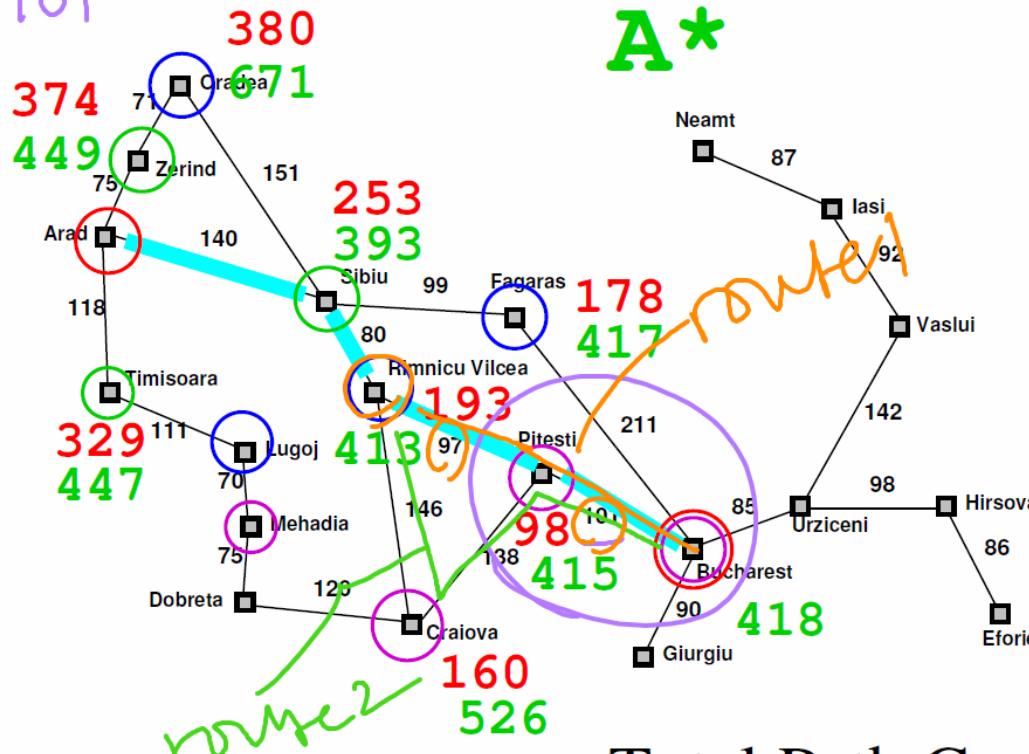
$$h^*(R)$$

route 1 = 97 + 101



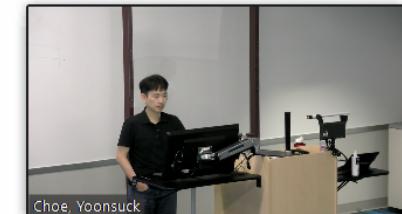
Romania with step costs in km

A*



Straight-line distance to Bucharest	
Arad	366
Bucharest	0
Craiova	160
Dobreta	242
Eforie	161
Fagaras	178
Giurgiu	77
Hirsova	151
Iasi	226
Lugoj	244
Mehadia	241
Neamt	234
Oradea	380
Pitesti	98
Rimnicu Vilcea	193
Sibiu	253
Timisoara	329
Urziceni	80
Vaslui	199
Zerind	374

Total Path Cost = 418



$$h(p) = 98$$

$$h^*(p) = 101$$

$$h(R) = 193$$

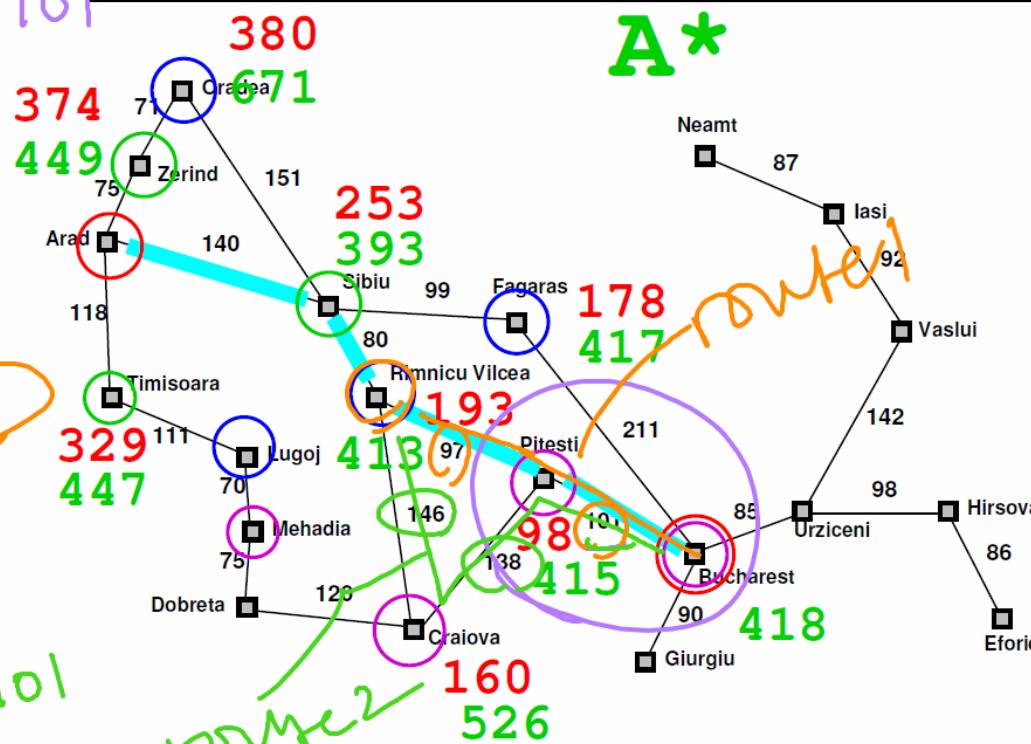
$$h^*(R) = 200$$

$$\begin{aligned} \text{route } 2: \\ 146 + 138 + 101 \\ 380 \end{aligned}$$

$$\text{route } 1 = \frac{97 + 101}{200}$$

Romania with step costs in km

A*



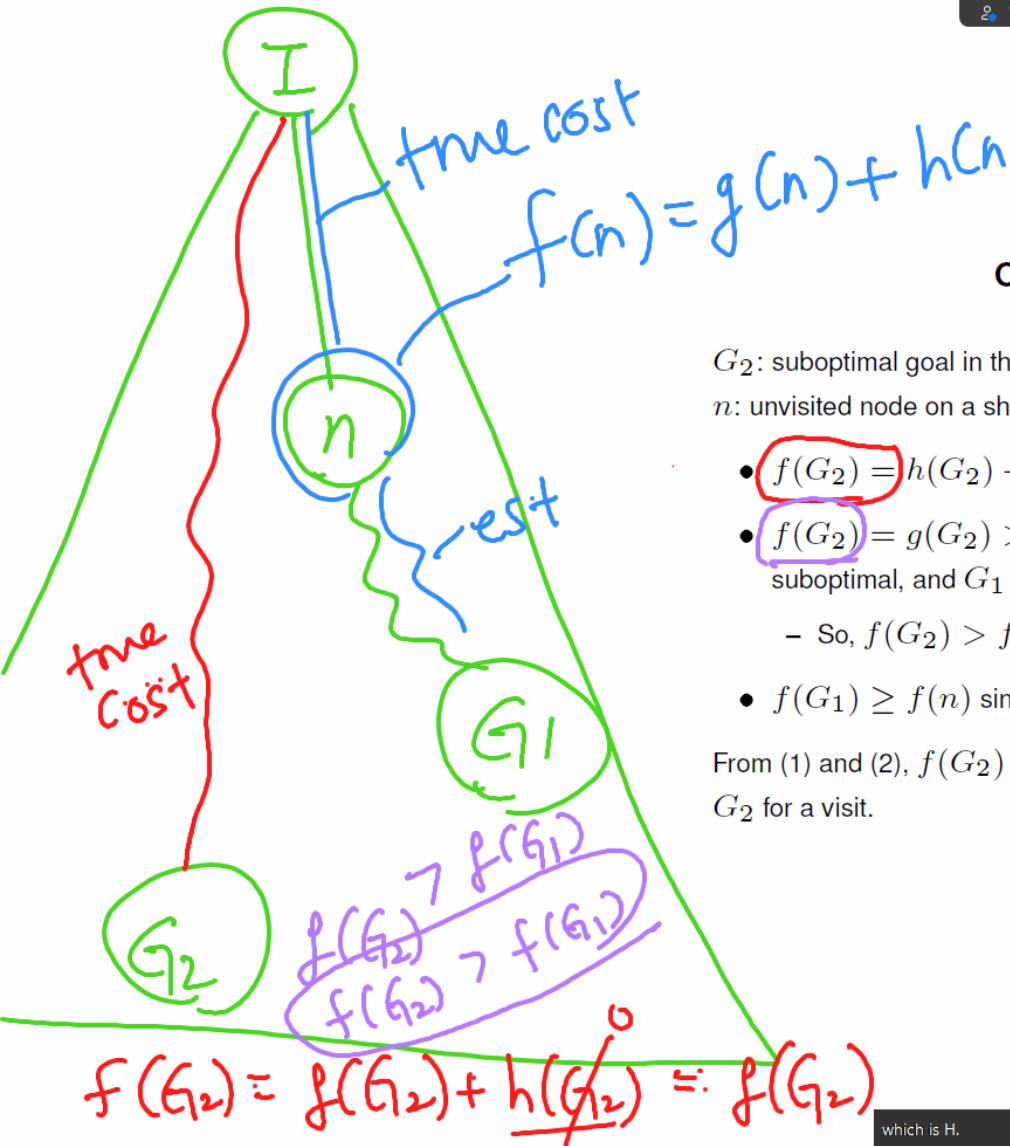
Straight-line distance to Bucharest

Arad	366
Bucharest	0
Craiova	160
Dobreta	242
Eforie	161
Fagaras	178
Giurgiu	77
Hirsova	151
Iasi	226
Lugoj	244
Mehadia	241
Neamt	234
Oradea	380
Pitesti	98
Rimnicu Vilcea	193
Sibiu	253
Timisoara	329
Urziceni	80
Vaslui	199
Zerind	374

Total Path Cost = 418

To find out the particular problem for that particular problem but here's the function values have this admissible property.

47



Optimality of A*

G_2 : suboptimal goal in the node-list.

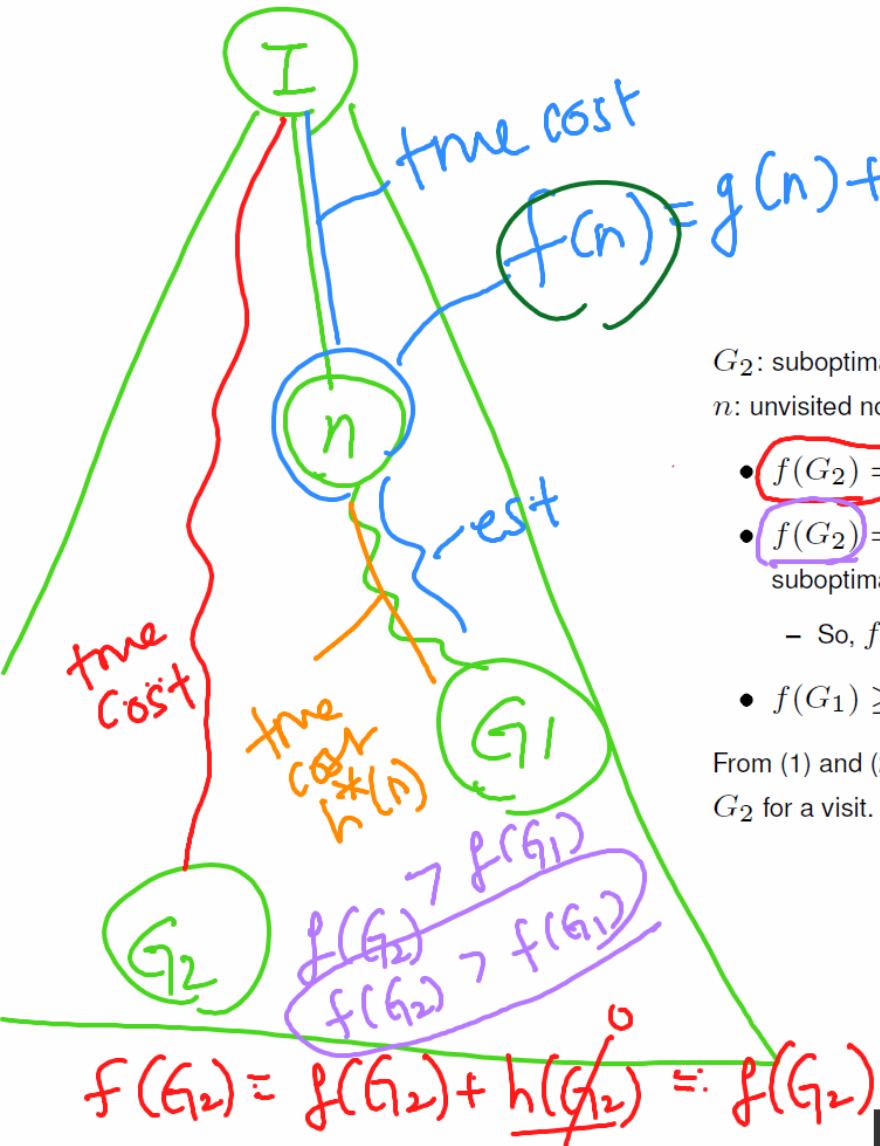
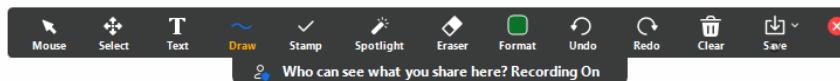
n : unvisited node on a shortest path to goal G_1

- $f(G_2) = h(G_2) + g(G_2) = g(G_2)$ since $h(G_2) = 0$
- $f(G_2) = g(G_2) > g(G_1) = f(G_1)$ since G_2 is suboptimal, and G_1 is a goal,
 - So, $f(G_2) > f(G_1)$: (1)
- $f(G_1) \geq f(n)$ since h is admissible : (2)

From (1) and (2), $f(G_2) > f(G_1) \geq f(n)$, so A* will never select G_2 for a visit.

48





$$= g(n) + h(n) \leq f(n) + h^*(n)$$

G_2 : suboptimal goal in the node-list.

n : unvisited node on a shortest path to goal G_1

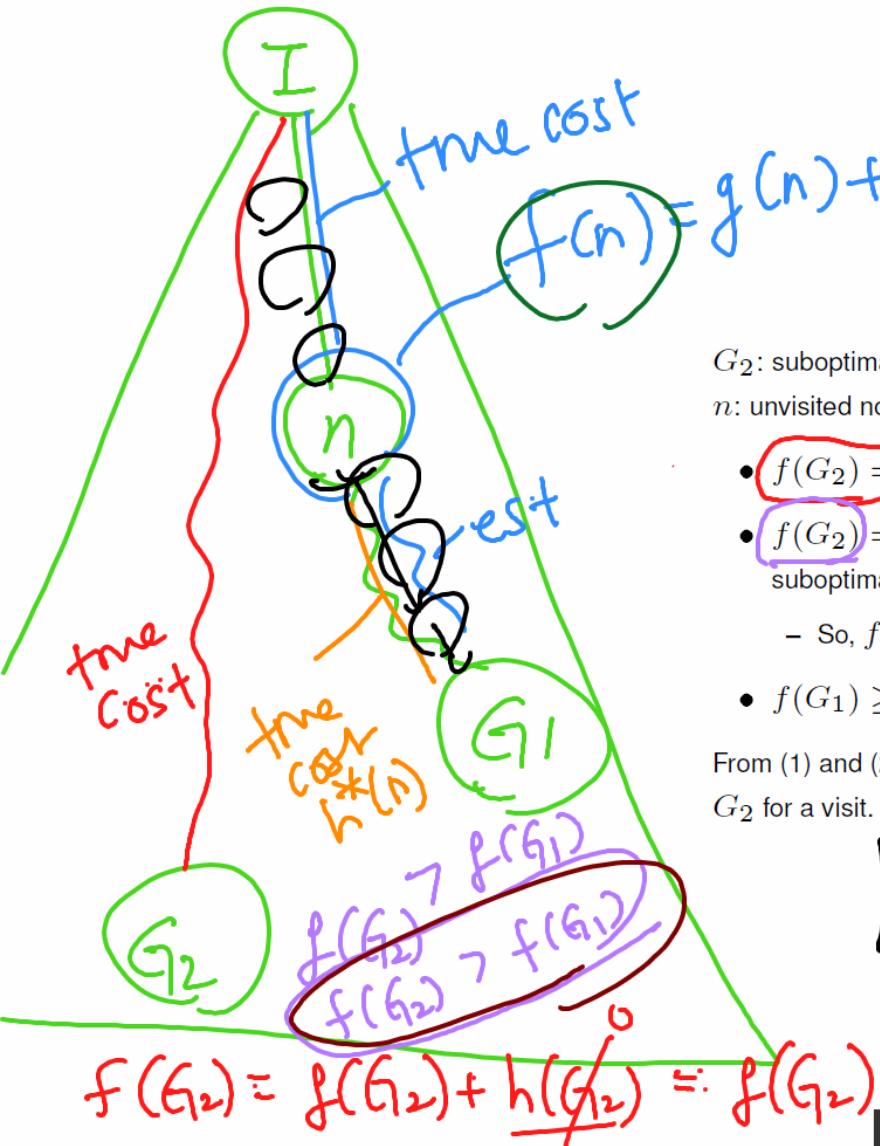
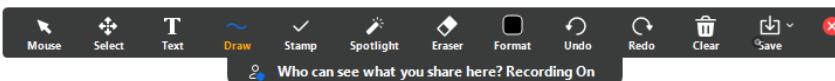
- $f(G_2) = h(G_2) + g(G_2) = g(G_2)$ since $h(G_2) = 0$
 - $f(G_2) = g(G_2) > g(G_1) = f(G_1)$ since G_2 is suboptimal, and G_1 is a goal,
 - So, $f(G_2) > f(G_1)$: (1)
 - $f(G_1) \geq f(n)$ since h is admissible : (2)

$h(n)$ is admissible



$$f(c_0) \leq f(G_1)$$

From (1) and (2), $f(G_2) > f(G_1) \geq f(n)$, so A* will never select G_2 for a visit.

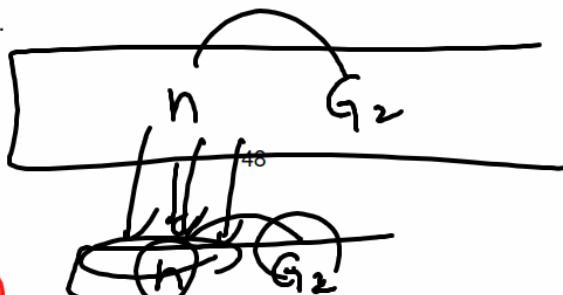


G_2 : suboptimal goal in the node-list.

n : unvisited node on a shortest path to goal G_1

- $f(G_2) = h(G_2) + g(G_2) = g(G_2)$ since $h(G_2) = 0$
- $f(G_2) = g(G_2) > g(G_1) = f(G_1)$ since G_2 is suboptimal, and G_1 is a goal,
 - So, $f(G_2) > f(G_1)$: (1)
- $f(G_1) \geq f(n)$ since h is admissible : (2)

From (1) and (2), $f(G_2) > f(G_1) \geq f(n)$, so A^* will never select G_2 for a visit.



Okay.

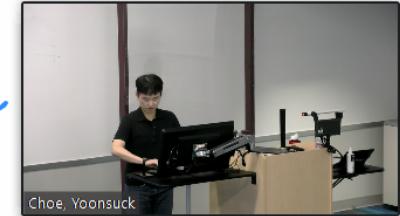
You are screen sharing Stop Share

Who can see what you share here? Recording On

$$Optimality\ of\ A^* \quad f(n) = g(n) + h(n) \leq f(G_1) \leq f(G_2)$$

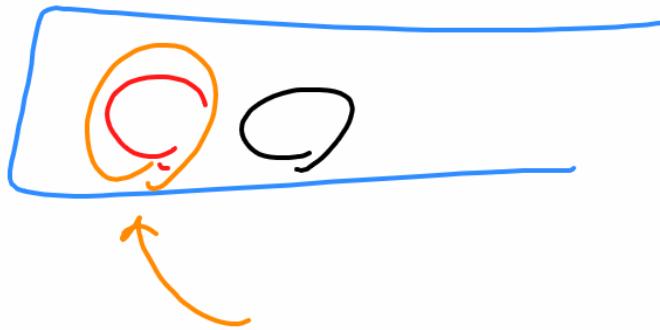
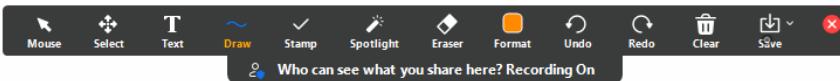
$h(n)$ is admissible

$$h(n) \leq h^*(n)$$

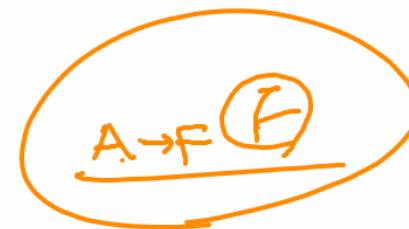
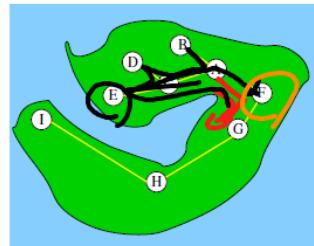


$$f(n) \leq f(G_1) < f(G_2)$$

$$f(n) < f(G_2)$$

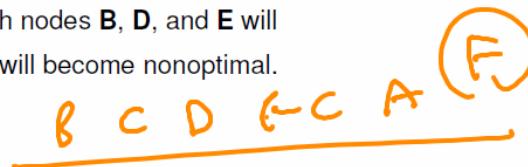


Optimality of A*: Example

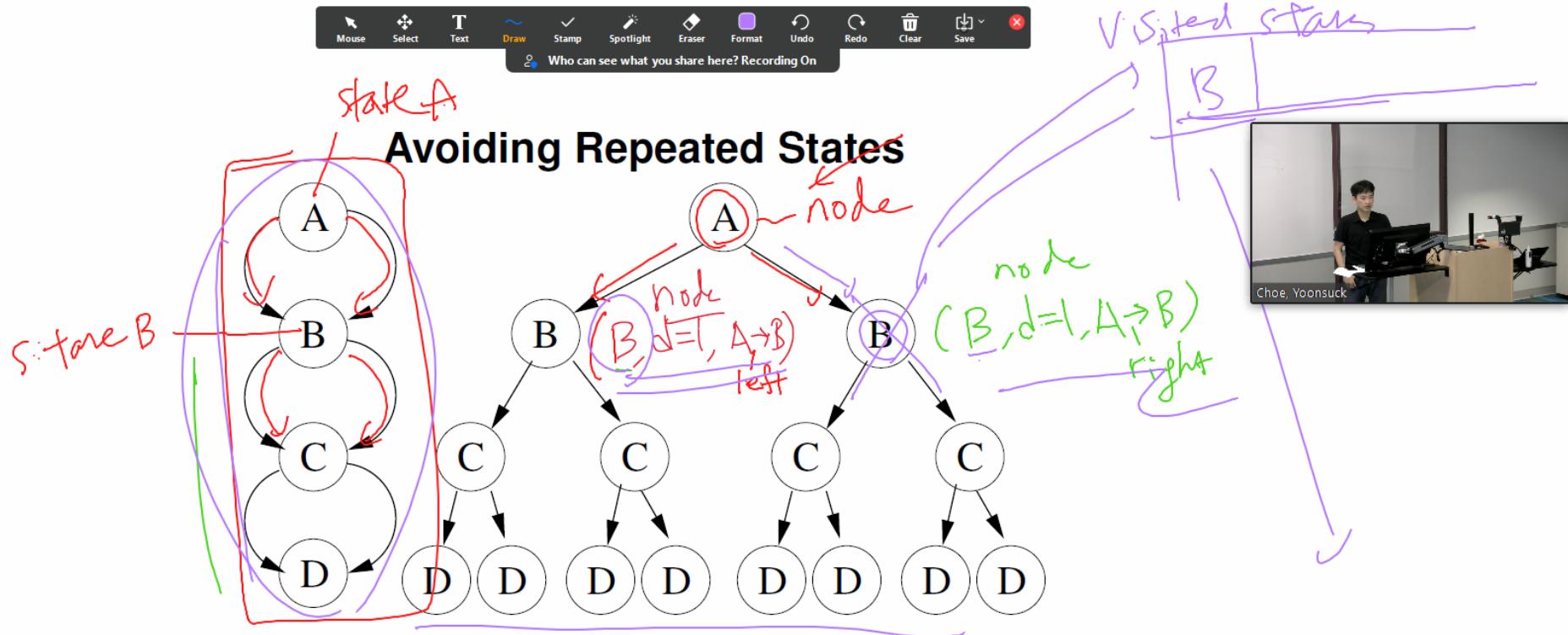


1. Visit of parent disallowed: search fails at nodes **B**, **D**, and **E**.
2. Visit of parent allowed: paths through nodes **B**, **D**, and **E** will have an inflated path cost $g(n)$, thus will become nonoptimal.

$A \rightarrow C \rightarrow E \rightarrow C \rightarrow A \rightarrow F \rightarrow \dots$
inflated path cost



So when you compare these two they're the same state,
but this is much more efficient and.

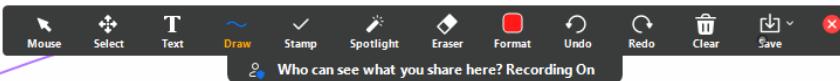


Same state can appear in different nodes.

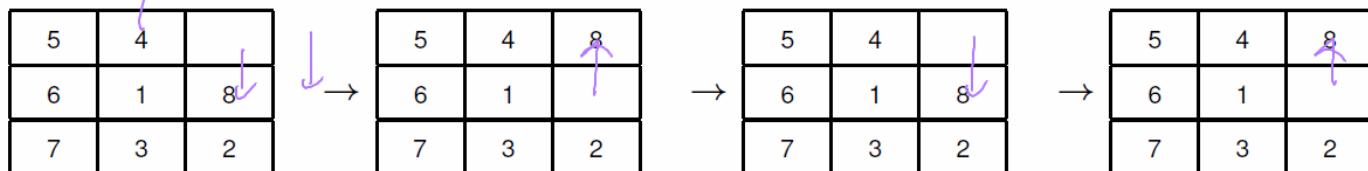
Repeated states can be devastating in search problems.

- Common cases: problems with reversible operators → search space becomes infinite
- One approach: find a spanning tree of the graph

puzzle to the next, a puzzle state. They use your pride operating backward then you can go back and forth, back and forth, we can go in.



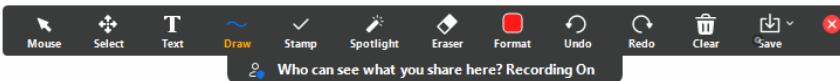
Avoiding Repeated States: Strategies



- Do not return to the node's parent
- Avoid cycles in the path (this is a huge theoretical problem in its own right)
- Do not generate states that you generated before: use a hash table to make checks efficient



How to avoid storing every state? Would using a short signature (or a checksum) of the full state description help?



Avoiding Repeated States: Strategies

The figure shows a sequence of four 3x3 state matrices, each representing a configuration of numbers:

- Matrix 1: 5, 4, ; 6, 1, 8; 7, 3, 2
- Matrix 2: 5, 4, 8; 6, 1, ; 7, 3, 2
- Matrix 3: 5, 4, ; 6, 1, 8; 7, 3, 2
- Matrix 4: 5, 4, 8; 6, , 1; 7, 3, 2

Arrows between the matrices indicate a search path. In Matrix 4, the number '1' is highlighted in red.



- Do not return to the node's parent
- Avoid cycles in the path (this is a huge theoretical problem in its own right)
- Do not generate states that you generated before: use a hash table to make checks efficient

How to avoid storing every state? Would using a short signature (or a checksum) of the full state description help?

get, get some kind of a shorter hash of that. And then just say the hash value, but.

Overview: Informed search, Iterative Improvement



Uninformed

General Search

Greedy Fn.

DF
BF

Iterate

loop

- Best-first search
- Heuristic function
- Greedy best-first search
- A*
- Designing good heuristics
- IDA*
- Iterative improvement algorithms
 1. Hill-climbing
 2. Simulated annealing

Informed

Best-first Search

Eval Fn.

iterative
loop

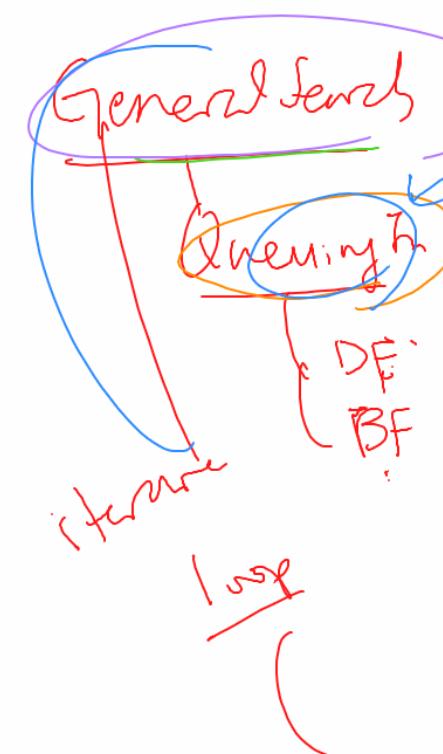
greedy Ben for
A*

IDA* = recursive

But the only thing now that is different, would be ida star was kind of similar in spirit, but Ids star is recursive Lee recursive Lee defined.

Uninformed

Overview: Informed search, Iterative Improvement



- Best-first search
- Heuristic function
- Greedy best-first search
- A*
- Designing good heuristics
- IDA*
- Iterative improvement algorithms
 1. Hill-climbing
 2. Simulated annealing

Informed

Best-first Search

Eval Fn.

General Search

greedy Ben for

A*

IDA* = recursive

So if you use this evaluation function to define King function, then that becomes informed such.

Uninformed

Overview: Informed search, Iterative Improvement



- Best-first search
- Heuristic function
- Greedy best-first search
- A*
- Designing good heuristics
- IDA*
- Iterative improvement algorithms
 1. Hill-climbing
 2. Simulated annealing

Informed

Best-first Search

Eval Fn.

General Search

greedy Ben for

A*

IDA* = recursive