



School of Rock
Mathematics Department
Specialist Mathematics

2022

Task 1

Question booklet

- Answer ***all*** questions
- Write your answers in this question booklet
- Allow approximately 120 minutes
- Approved calculators may be used

Examination information

Materials

- Question booklet
- Formula sheet

Instructions

- Show appropriate working and steps of logic in the question booklets
- State all answers correct to three significant figures, unless otherwise instructed
- Use black or blue pen
- You may use a sharp dark pencil for diagrams

Total time: 120 minutes

Total marks: 12

Student Name:

Class:

Question 1 (6 marks)

(a) Write $-1 + i\sqrt{3}$ in $r \operatorname{cis} \theta$ form.

(1 mark)

(b) Consider the complex number $z_1 = x + iy$, where $x > 0$, $y > 0$, and $x > y$.

The complex number z_1 , which lies in the first quadrant of the Argand diagram, is shown in Figure 1.

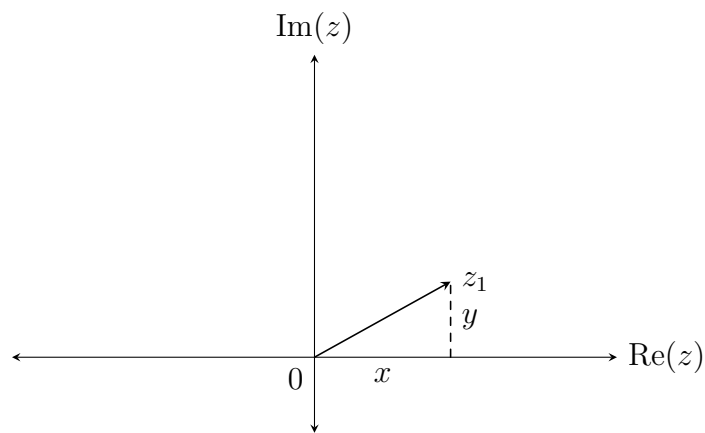


Figure 1

(i) Let $z_2 = (-1 + i\sqrt{3})z_1$.

Using part (a), show that $|z_2| = 2|z_1|$.

[illegible]

(1 mark)

(ii) On the Argand diagram in Figure 1, draw z_2 .

(2 marks)

[illegible]

(2 marks)

(ii) The area of the oil spill is expanding at a rate of $2 \text{ m}^2 \text{ s}^{-1}$ at the instant when

$$A = 12 \text{ m}^2, \quad b = 2 \text{ m}, \quad \text{and} \quad \frac{da}{dt} = 0.5 \text{ m s}^{-1}.$$

Find the **exact** value of $\frac{db}{dt}$ at this instant.

A large grid of graph paper with 20 columns and 10 rows. The grid is composed of small squares, with a slightly larger square at the top left corner, likely for a title or header. The grid is empty and ready for use.

(3 marks)