



第六章 关系数据库设计理论

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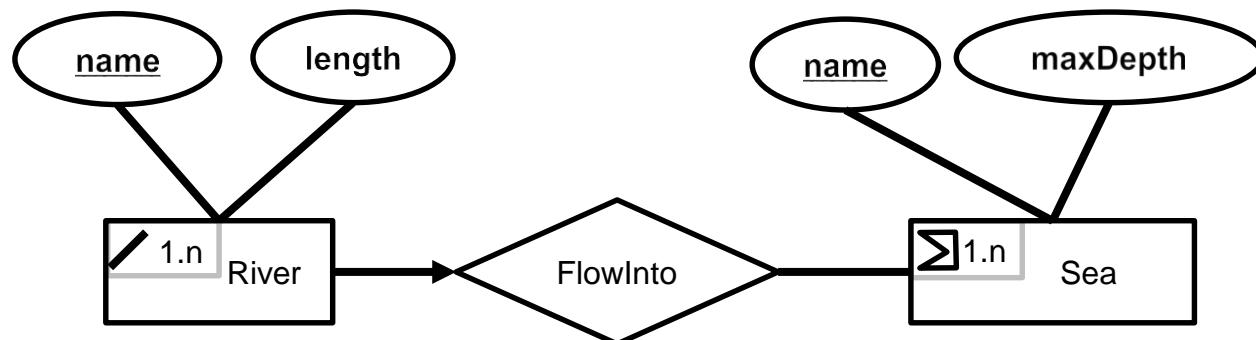
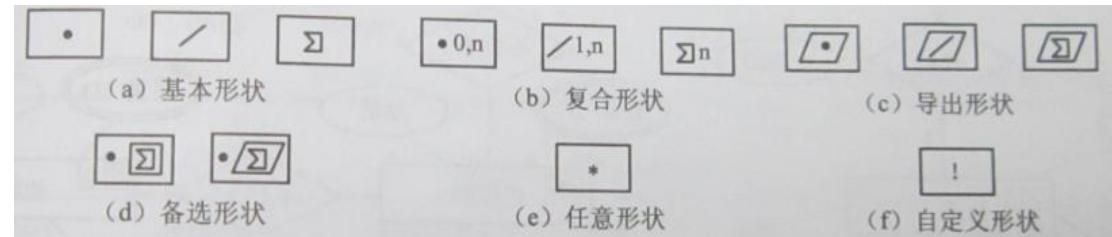
关系数据库设计

数据库设计一般要经过以下几个步骤：

- 需求分析阶段 → 数据流图和数据字典 (软工)
- 概念结构设计阶段 → E-R图/UML图
- 逻辑结构设计阶段 → 关系数据库模式 (规范化)
- 数据库物理设计阶段 → 存储方式、索引和用户权限
- 数据库实施阶段
- 数据库运行和维护阶段

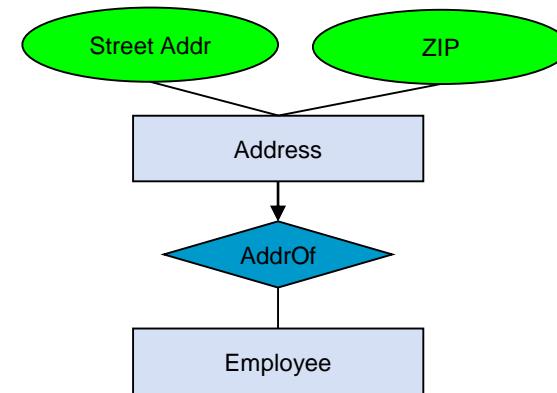
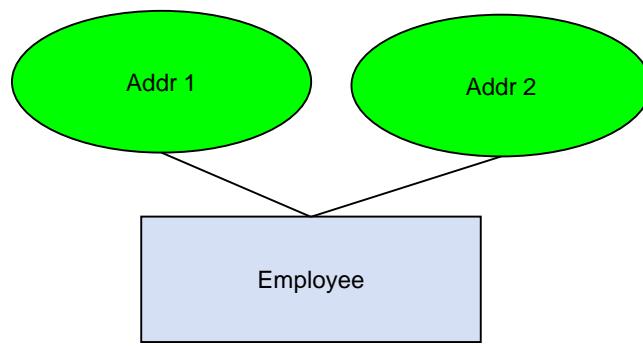
E/R 图

- Primitive units of E/R model
 - Entities sets: classes or types of objects
 - Attributes, Key
 - Pictograms
 - Relationships
 - A subset of cross-product
 - Attributes, Key
 - Multiplicity: 1:1, 1:N, M:N



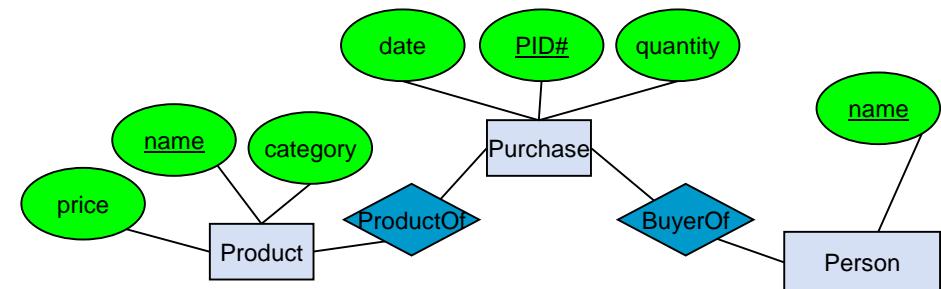
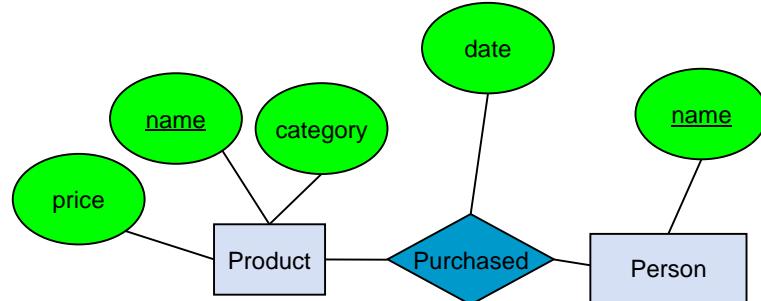
E/R 图

- Design consideration
 - Entity vs. Attributes
 - Multi-valued attributes, such as addresses, phones, and grades



E/R 图

- Design consideration
 - Entity vs. Attributes
 - Multi-valued attributes, such as addresses, phones, and grades
 - Entity vs. Relationship
 - Multiple instances of each entity combination, such as purchase



E/R 图

- Design consideration

- Entity vs. Attributes

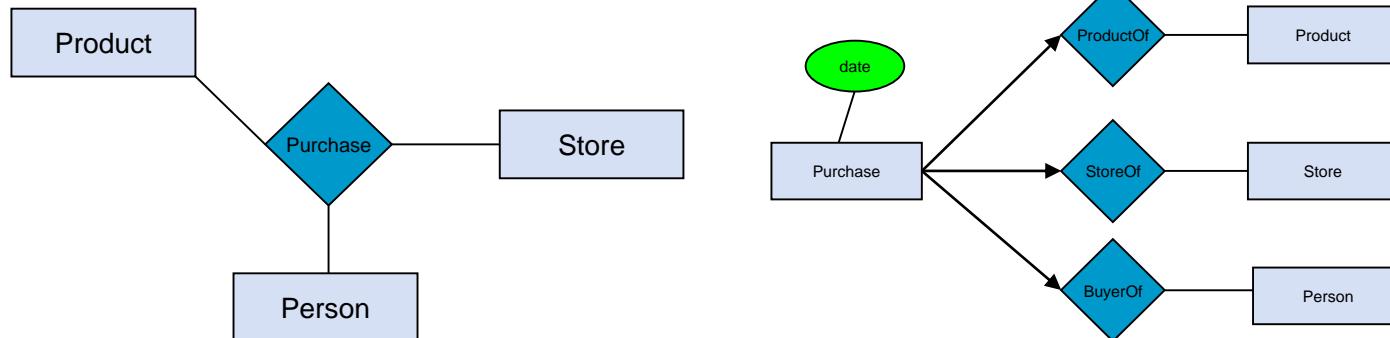
- Multi-valued attributes, such as addresses, phones, and grades

- Entity vs. Relationship

- Multiple instances of each entity combination, such as purchase

- Multi-way vs. New Entity + Binary relationships

- Multiple combination, more-fine-grained constraints



从E/R图到关系模式

- Translation rules
 - Entity becomes Relation
 - Attributes become columns in the relation
 - Multi-valued attributes become a new relation
 - Includes foreign key to link to relation for the entity
 - Relationships (1:1, 1:N, N:1) become foreign keys
 - Foreign keys enforce unique constraint for 1:1
 - M:N Relationship become a relation
 - Containing foreign keys or relations from participating entities
- Constraints in E/R diagrams
 - Keys: Implicit constraints on uniqueness of entities
 - Single-value constraints
 - Referential integrity constraints: Referenced entities must exist



从E/R图到关系模式

- 从E-R图到关系模式



方法一： Student (Sno, Sname,)

Class(ClassID, num, ...)

Class_Student (Sno, ClassID)

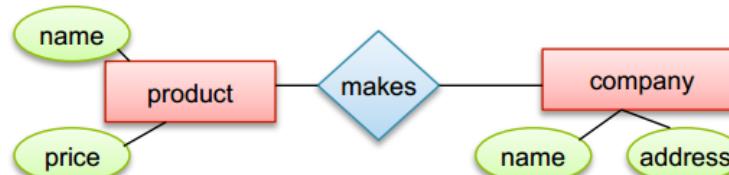
方法二： Student (Sno, Sname, ..., ClassID)

Class(ClassID, num, ...)

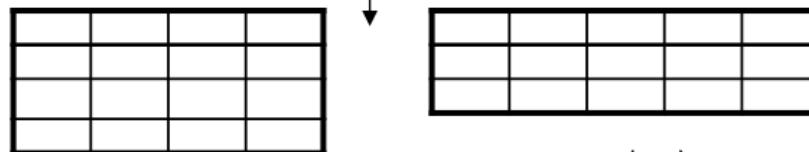
转换得到的关系模式是设计合理或“好”的关系模式？

关系数据库设计

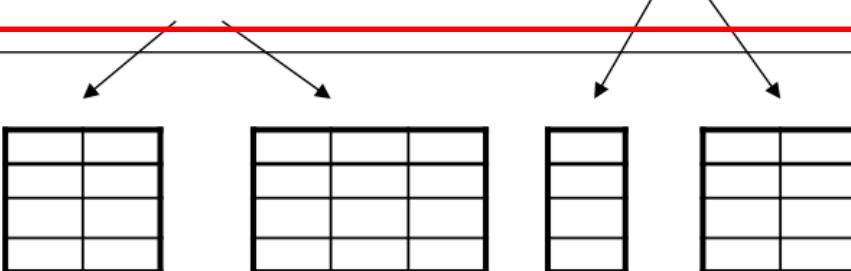
Conceptual Model:



Relational Model:
Tables + constraints
And also functional dep.



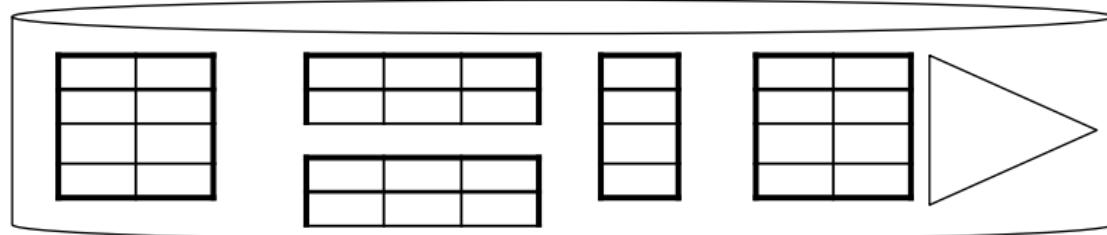
Normalization: 规范化
Eliminates anomalies



Conceptual Schema

Physical storage details

Physical Schema



第六章 关系数据库设计理论

- 6.1 数据依赖对关系模式的影响
- 6.2 函数依赖 (Functional Dependencies)
- 6.3 BC范式 (Boyce-Codd Normal Form)
- 6.4 BC范式和第4范式的局限
- 6.5 小结

参考教材：
数据库系统概念 8.1-8.9

6.1 数据依赖对关系模式的影响

- 数据依赖
 - 通过关系中属性间值的相等与否体现出的数据间的相互关系
 - 现实世界属性间相互联系的抽象
 - 数据的内在性质
 - 语义的体现
- 分类
 - 函数依赖 (Functional Dependencies)
 - 多值依赖 (Multivalued Dependencies)
 - 其他

6.1 数据依赖对关系模式的影响

- 学校数据库(举例):
 - 学生的学号 (Sno)
 - 所在系 (Sdept)
 - 系主任姓名 (Mname)
 - 课程号 (Cname)
 - 成绩 (Grade)
- E-R图中获得'mega' relation
 - Student(Sno, Sdept, Mname, Cname, Grade)
 - 属性之间的数据依赖

6.1 数据依赖对关系模式的影响

- 学校数据库的语义：
 - 一个系有若干学生， 一个学生只属于一个系
 - 一个系只有一名主任
 - 一个学生可以选修多门课程， 每门课程有若干学生选修
 - 每个学生所学的每门课程都有一个成绩
- 属性之间的函数依赖
 - $Sno \rightarrow Sdept$
 - $Sdept \rightarrow Mname$
 - $(Sno, Cname) \rightarrow Grade$

6.1 数据依赖对关系模式的影响

- 函数依赖 → 设计异常 (Design anomalies)
 - 数据冗余 (Redundancy)
 - 浪费大量的存储空间
 - 例如，每个系主任的姓名重复出现
 - 更新异常 (Update anomalies)
 - 数据冗余，更新数据时，维护数据完整性代价大
 - 例如，某系更换系主任后，系统必须修改与该系学生有关的每个元组

6.1 数据依赖对关系模式的影响

- 函数依赖 → 设计异常 (Design anomalies)
 - 插入异常 (Insert anomalies)
 - 有些数据无法正常插入
 - 例如，如果一个系刚成立，尚无学生，就无法把这个系及其系主任的信息存入数据库
 - 删除异常 (Deletion anomalies)
 - 不该删除的数据不得不删
 - 例如，如果某个系的学生全部毕业了，我们在删除该系学生信息的同时，把这个系及其系主任的信息也丢掉了

6.1 数据依赖对关系模式的影响

- 大学申请数据库(举例)
 - SSN(美国社会安全号)和name
 - Colleges applying to
 - High schools attended (with city)
 - Hobbies
- E-R图中获得'mega' relation
 - Apply(SSN, Sname, Cname, HS, HScity, hobby)
 - 属性之间的数据依赖

Cname, (HS, Hscity), hobby是多值属性 → 多值依赖

6.1 数据依赖对关系模式的影响

- Apply(SSN, Sname, Cname, HS, HScity, hobby)
 - 123 Ann from PAHS (P.A.) and GHS (P.A.) plays tennis and trumpet(喇叭) and applied to Standford, Berkely, and MIT
 - 123, Ann, Stanford, PAHS, P.A., tennis
 - 123, Ann, Berkeley, PAHS, P.A., tennis
 - 123, Ann, Berkeley, PAHS, P.A., trumpet
 -

思考：Ann在Apply关系中有多少个元组？

6.1 数据依赖对关系模式的影响

- $\text{Apply}(\text{SSN}, \text{Sname}, \text{Cname}, \text{HS}, \text{HScity}, \text{hobby})$
- 设计异常
 - 数据冗余
 - HS, HScity
 - Cname, hobby
 - 更新异常
 - Trumpet → Cornet
 - 插入异常
 - 尚未申请学校的学生信息无法插入数据库
 - 删 除 异 常

6.1 数据依赖对关系模式的影响

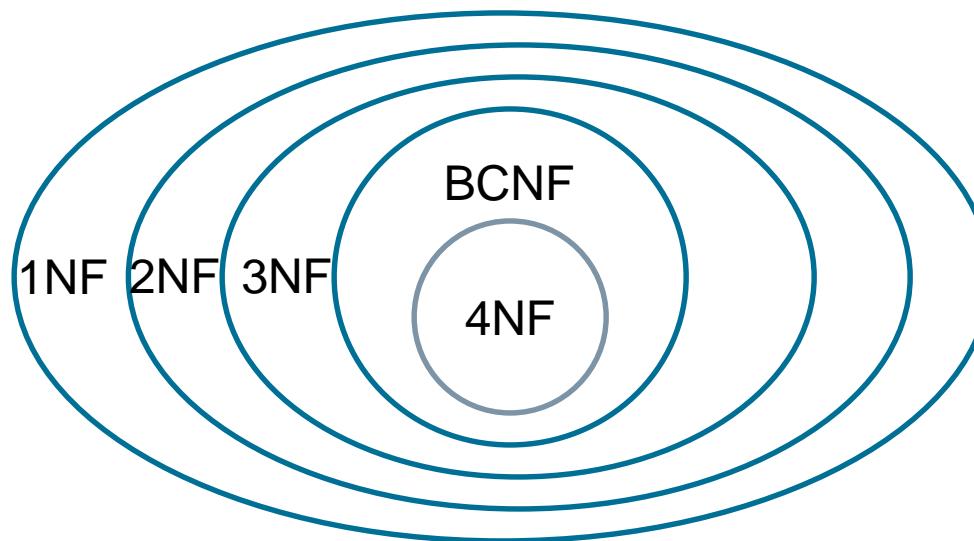
- 结论
 - Student(Sno, Sdept, Mname, Cname, Grade)
 - Apply(SSN, Sname, Cname, HS, HScity, hobby)
 - Student和Apply关系模式不是“好”的模式
 - “好”的模式不会发生插入异常、删除异常、更新异常，数据冗余应尽可能小
- 原因：关系模式中**数据依赖**
- 解决方法：通过**分解**关系模式来消除其中不合适的
数据依赖，且能重构原有模式

6.1 数据依赖对关系模式的影响

- Design by decomposition
 - Start with “mega” relations containing everything
 - Decompose into smaller, better relations with the same information
 - Can do decomposition automatically
- Automatic decomposition
 - “Mega” relations + properties of the data
 - System decomposes based on properties
 - Final set of relations satisfies normal form
 - No anomalies, no lost information

6.1 数据依赖对关系模式的影响

- Properties of the data (数据依赖) and Normal Forms (范式)
 - 函数依赖 → BC范式 (Boyce-Codd Normal Forms)
 - 多值依赖 → 第4范式 (Forth Normal Form)



6.1 数据依赖对关系模式的影响

- 1st Normal Form (1NF) = All tables are flat
 - 2nd Normal Form = disused
 - Boyce-Codd Normal Form (BCNF)
 - 3rd Normal Form (3NF)
 - 4th Normal Forms
 - 5th Normal Forms = see text books
- DB designs based on ***functional dependencies***, intended to prevent *data anomalies*
- DB designs based on ***multivalued dependencies***

6.1 数据依赖对关系模式的影响

- 1st Normal Form (1NF)

Student	Majors
Mary	{CS, EE}
Joe	{GIS, SE}
...	...

Violates 1NF

Student	Major
Mary	CS
Mary	EE
Joe	GIS
Joe	SE

In 1st NF

1NF Constraint: Types must be atomic!

6.1 数据依赖对关系模式的影响

- $\text{Apply}(\text{SSN}, \text{Sname}, \text{Cname})$ 思考: Apply 的key?
 - 数据冗余; 数据更新和删除异常
 - 每个大学都存储了 SSN-Sname 信息
- 函数依赖 $\text{SSN} \rightarrow \text{Sname}$
 - 相同的 SSN 始终得到相同的 Sname
 - $f(\text{SSN}) = \text{Sname}$
 - SSN 的 Sname 应该只存储一次
- BC范式: if $A \rightarrow B$, then A is a key
- 分解: $\text{Student}(\text{SSN}, \text{Sname})$, $\text{Apply}(\text{SSN}, \text{Cname})$

6.1 数据依赖对关系模式的影响

- Apply(SSN, Cname, HS) 思考: Apply的key?
 - 数据冗余; 数据更新和删除异常
 - Multiplicative effect
 - C 个大学, H 个高中, $C \times H$ 个元组, 期望是 $C+H$ 个元组
 - BC范式并没有解决这一问题, 无函数依赖
- 多值依赖 $SSN \rightarrow\rightarrow Cname$ ($SSN \rightarrow\rightarrow HS$)
 - Given SSN has every combination of $Cname$ and HS
 - SSN 的 $Cname$ 和 HS 应该都只存储一次
- 第4范式: if $A \rightarrow\rightarrow B$, then A is a key
- 分解: Apply($SSN, Cname$), HighSchool(SSN, HS)

思考: 如果 $C=1$ 和 $H=1$, $SSN \rightarrow\rightarrow Cname$ 还成立吗?

6.1 数据依赖对关系模式的影响

- Design by decomposition
 - “Mega” relations + properties of the data
 - System decomposes based on properties
 - Final set of relations satisfies normal form
 - No anomalies, no lost information
 - Functional dependencies → Boyce-Codd Normal Form
 - Multivalued dependences → Fourth Normal Form

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6.2 函数依赖

- 大学申请数据库(举例)

Student (SSN, Sname, address, HScode, HSname,
HScity, GPA, priority)

Apply (SSN, Cname, state, date, major)

- 假设priority取决于GPA

- $GPA > 3.8 \rightarrow priority = 1$
- $3.3 < GPA \leq 3.8 \rightarrow priority = 2$
- $GPA \leq 3.3 \rightarrow priority = 3$

- 相同GPA的两个元组具有相同的priority

6.2 函数依赖

Student (SSN, Sname, address, HScode, HSname, HScity, GPA, priority)

- 相同GPA的两个元组具有相同的priority
- 函数依赖 Functional Dependencies (FDs)
- 关系R中，属性集A和属性集B存在函数依赖的定义
(t,u是关系R的元组):

$$\forall t, u \in R: \\ t[A_1, \dots A_n] = u[A_1, \dots A_n] \Rightarrow t[B_1, \dots B_m] = u[B_1, \dots B_m]$$

6.2 函数依赖

- 函数依赖从哪儿来?
 - Based on knowledge of real word
 - 需求分析→数据流图&数据字典→E-R图→关系与依赖
 - All instances of relation must adhere
 - $R(\bar{A}, \bar{B}, \bar{C})$, $\bar{A} \rightarrow \bar{B}$

	A_1	...	A_m		B_1	...	B_n	
t_i								
t_j								

If t_1, t_2 agree here..

...they also agree here!

Given attribute sets
 $A = \{A_1, \dots, A_m\}$ and $B = \{B_1, \dots, B_n\}$ in R ,

The ***functional dependency***
 $A \rightarrow B$ on R holds if for **any**
 t_i, t_j in R :

if $t_i[A_1] = t_j[A_1]$ AND
 $t_i[A_2] = t_j[A_2]$ AND ... AND
 $t_i[A_m] = t_j[A_m]$

then $t_i[B_1] = t_j[B_1]$ AND
 $t_i[B_2] = t_j[B_2]$ AND ... AND $t_i[B_n] = t_j[B_n]$

6.2 函数依赖

- 关系 $R(A, B, C, D, E)$ 具有以下2个函数依赖
 - $A, B \rightarrow C$
 - $C, D \rightarrow E$

假设 A, B, D 分别最多有3个不同的取值， E 最多有多少个不同的取值？

6.2 函数依赖

- 关系Student (SSN, Sname, address, HScode, HSname, HScity, GPA, priority)存在哪些函数依赖?
 - $\text{SSN} \rightarrow \text{Sname}$
 - $\text{SSN} \rightarrow \text{address}$
 - $\text{HScode} \rightarrow \text{HSname}, \text{HScity}$
 - $\text{HSname}, \text{HScity} \rightarrow \text{HScode}$
 - $\text{SSN} \rightarrow \text{GPA}$
 - $\text{GPA} \rightarrow \text{priority}$
 - $\text{SSN} \rightarrow \text{priority}$
- } 函数依赖的传递性

6.2 函数依赖

- 关系Apply (SSN, Cname, state, date, major)存在哪些函数依赖?
 - $Cname \rightarrow date$
 - $SSN, Cname \rightarrow major ?$
 - $SSN \rightarrow state$

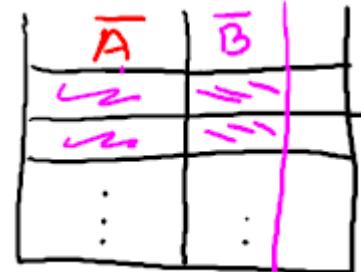
6.2 函数依赖

- 函数依赖与码(Key)的关系
 - Relations with no duplicates
 - $R(\bar{A}, \bar{B})$, suppose $\bar{A} \rightarrow$ all attributes
 - \bar{A} 是关系R的码

\bar{A}	\bar{B}
\bar{a}	\bar{b}
\bar{a}	\bar{b}

6.2 函数依赖

- 函数依赖分类
 - 平凡函数依赖 (Trivial FD)
 - If $\bar{A} \rightarrow \bar{B}$, $\bar{B} \subseteq \bar{A}$
 - 非平凡函数依赖 (Nontrivial FD)
 - If $\bar{A} \rightarrow \bar{B}$, $\bar{B} \not\subseteq \bar{A}$
 - 完全非平凡函数依赖 (Completely nontrivial FD)
 - If $\bar{A} \rightarrow \bar{B}$, $\bar{B} \cap \bar{A} = \emptyset$



6.2 函数依赖

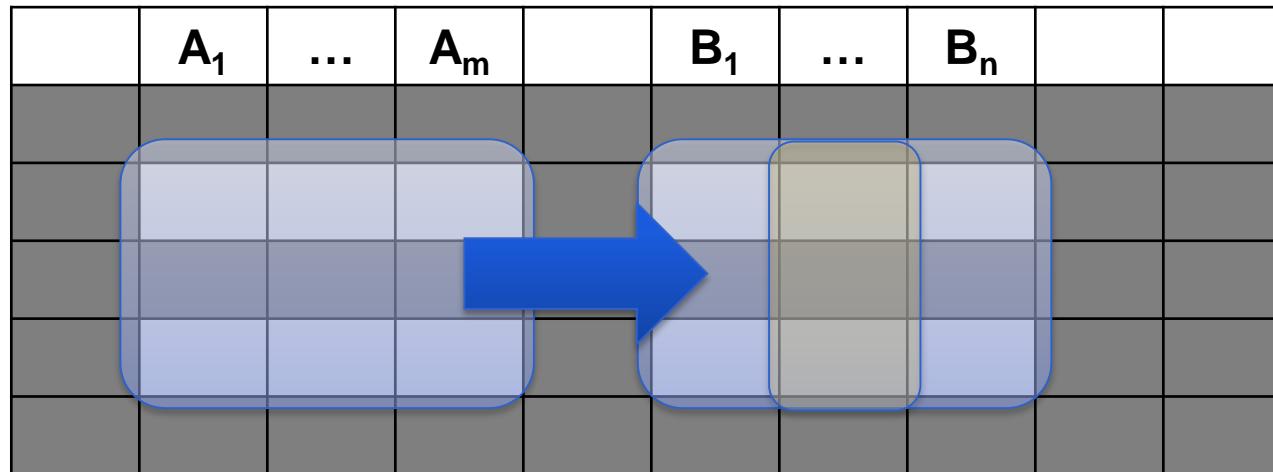
- High-level idea: why do we care about FDs?
 - Start with some relational schema
 - Find out its functional dependencies (FDs)
 - Use these to design a better schema
 - One which minimizes possibility of anomalies
 - Redundancy
 - Update anomaly
 - Delete anomaly
 - Insert anomaly

6.2 函数依赖

函数依赖规则(Armstrong's Rules)

- 分解规则(Splitting rule)

- $\bar{A} \rightarrow B_1, \dots B_m$
- $\bar{A} \rightarrow B_1, \bar{A} \rightarrow B_2, \dots, \bar{A} \rightarrow B_m$



6.2 函数依赖

函数依赖规则(Armstrong's Rules)

- 分解规则(Splitting rule)

- $\bar{A} \rightarrow B_1, \dots B_m$
 - $\bar{A} \rightarrow B_1, \bar{A} \rightarrow B_2, \dots, \bar{A} \rightarrow B_m$

- ~~— $A_1, \dots A_n \rightarrow \bar{B}$~~
 - ~~— $A_1 \rightarrow \bar{B}, A_2 \rightarrow \bar{B}, \dots, A_n \rightarrow \bar{B}$~~

- HSname, HScity \rightarrow HScode

6.2 函数依赖

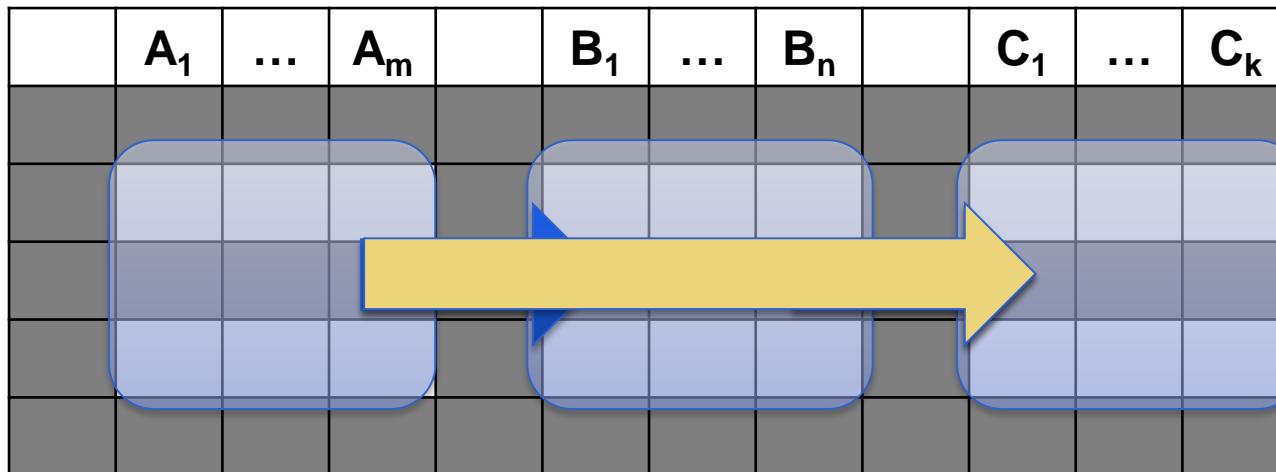
函数依赖规则

- 分解规则(Splitting rule)
- 合并规则 (Combining rule)
 - $\bar{A} \rightarrow B_1, \bar{A} \rightarrow B_2, \dots, \bar{A} \rightarrow B_m$
 - $\bar{A} \rightarrow B_1, \dots B_m$
- 平凡依赖规则 (Trivial-dependency rules)
 - If $\bar{A} \rightarrow \bar{B}, \bar{B} \subseteq \bar{A}$
 - If $\bar{A} \rightarrow \bar{B}$, then $\bar{A} \rightarrow \bar{A} \cup \bar{B}$
 - If $\bar{A} \rightarrow \bar{B}$, then $\bar{A} \rightarrow \bar{A} \cap \bar{B}$

6.2 函数依赖

函数依赖规则

- 分解规则(Splitting rule)
- 合并规则(Combining rule)
- 平凡依赖规则(Trivial-dependency rules)
- 传递规则(Transitive rule)
 - If $\bar{A} \rightarrow \bar{B}$, $\bar{B} \rightarrow \bar{C}$, then $\bar{A} \rightarrow \bar{C}$



\bar{A}	\bar{B}	\bar{C}	\bar{D}
\bar{a}	\bar{b}	\bar{c}	\bar{d}
\bar{a}	\bar{b}	\bar{c}	\bar{d}
\vdots	\vdots	\vdots	\vdots

6.2 函数依赖

- 属性的闭包 (Closure of Attributes)
 - Given relation, FDs, set of attributes \bar{A}
 - Find all B such that $\bar{A} \rightarrow B$
 - $\bar{A}^+ \{A_1, \dots, A_n\}^+$
 - 闭包计算算法
 - Start with $\{A_1, \dots, A_n\}$
 - Repeat until no change:
 - if $\bar{A} \rightarrow \bar{B}$, and \bar{A} in set
 - add \bar{B} to set

6.2 函数依赖

- Student (SSN, Sname, address, HScode, HSname, HScity, GPA, priority)
 - SSN → Sname, address, GPA
 - GPA → priority
 - HScode → HSname, HScity
- 属性闭包计算 $\{SSN, HScode\}^+ = \{SSN, HScode, Sname, address, GPA, priority, HSname, HScity\}$

思考： {SSN, HScode}是关系Student的码？

6.2 函数依赖

闭包和码

- Is \bar{A} a key for R? (Given R and FDs)
 - Compute \bar{A}^+ if $\bar{A}^+ = \text{all attributes}$, then \bar{A} is a key
- How can we find all keys given a set of FDs
 - Consider every subset of attributes as \bar{A}
 - If $\bar{A}^+ = \text{all attributes}$, then \bar{A} is a key
 - Minimum set → increasing size of the subset

6.2 函数依赖

如何为关系指定函数依赖？

- S1 and S2 sets of FDs
- S2 “follows from” S1 if every relation instance satisfying S1 also satisfies S2
 - $S1 = \{SSN \rightarrow GPA, GPA \rightarrow priority\}$
 - $S2 = \{SSN \rightarrow priority\}$
- How to test? Does $\bar{A} \rightarrow \bar{B}$ follow from S?
 - Compute \bar{A}^+ base S check if \bar{B} in set
 - Armstrong's Axioms

思考：数据库设计时，只需要保留函数依赖S1或S2，还是S1和S2？

6.2 函数依赖

- 如何为关系指定函数依赖?
 - Minimal set of completely nontrivial FDs such that all FDs that hold on the relation follow from the dependencies in the set

6.2 函数依赖

- 需求分析 → ... → 关系和函数依赖
- 函数依赖定义
 - 来源于真实世界(应用需求), 所有元组都要满足
- 函数依赖、闭包与码的关系
 - 计算属性的闭包判断是否为码(Key)
- 函数依赖分类 (三类)
- 函数依赖规则
 - splitting, combining, trivial-dependency, transitive
- 如何指定函数依赖(E-R图 → 关系, 那么FDs?)

第六章 关系数据库设计理论

- 6.1 数据依赖对关系模式的影响
- 6.2 函数依赖 (Functional Dependencies)
- 6.3 BC范式 (Boyce-Codd Normal Form)
- 6.4 BC范式和第4范式的局限
- 6.5 小结

参考教材：
数据库系统概念 8.1-8.9

6.3 BC范式

- 关系模式的分解

$$R(A_1, \dots, A_n) \quad \bar{A}$$



$$\bar{B} \cup \bar{C} = \bar{A}$$

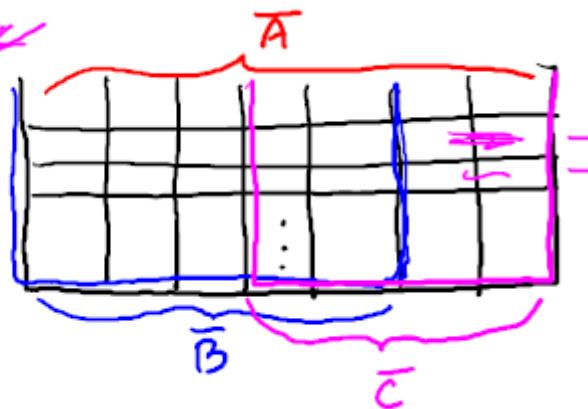
$$R1 \bowtie R2 = R$$

$$R1(B_1, \dots, B_k) \quad \bar{B}$$

$$R2(C_1, \dots, C_m) \quad \bar{C}$$

$$R_1 = \pi_{\bar{B}}(R)$$

$$R_2 = \pi_{\bar{C}}(R)$$



6.3 BC范式

$$\begin{aligned}\bar{B} \cup \bar{C} &= \bar{A} \\ R1 \bowtie R2 &= R\end{aligned}$$

例1

Student (SSN, Sname, address, HScode, HSname, HScity, GPA, priority)

以下分解正确(即没有信息丢失)?

S1 (SSN, Sname, address, HScode, GPA, priority)

S2 (HScode, HSname, HScity)

YES!

6.3 BC范式

$$\begin{aligned}\bar{B} \cup \bar{C} &= \bar{A} \\ R1 \bowtie R2 &= R\end{aligned}$$

例2

Student (SSN, Sname, address, HScode, HSname, HScity, GPA, priority)

以下分解正确(即没有信息丢失)?

S1 (SSN, Sname, address, HScode, HSname, HScity)

S2 (Sname, HSname, GPA, priority)

NO!

6.3 BC范式

- 基于分解的关系模式设计
 - “Mega” relations + properties of the data
 - System decomposes based on properties
 - “Good” decompositions only (Lossless join property)
 - Into “good” relations (即BCNF)
- A decomposition R to (R_1, R_2) is lossless if $R = R_1 \text{ Join } R_2$

6.3 BC范式

- Boyce-Codd Normal Form 定义
 - Relation R with FDs is in BCNF if:
For each $\bar{A} \rightarrow \bar{B}$, \bar{A} is a key

- BCNF violation

	\bar{A}	B	rest
C	a	b	-
	a	b	-
		:	

- \bar{A} contains a key, \bar{A} is a superkey

6.3 BC范式

- 关系Student是否属于BCNF?

Student (SSN, Sname, address, HScode, HSname, HScity, GPA, priority)

- SSN → Sname, address, GPA
- GPA → priority
- HScode → HSname, HScity

NO!

- 如何判断?
 - 每个函数依赖的左端是否都包含码?
 - Keys: {SSN, HScode}

6.3 BC范式

- 关系Apply是否属于BCNF?

Apply (SSN, Cname, state, date, major)

- SSN, Cname, state → date, major

YES!

- Cname → state
 - SSN, Cname → date, major

NO!

6.3 BC范式

BCNF decomposition algorithm

Input: relation R + FDs for R

Output: decomposition of R into BCNF relations with
“lossless join”

Compute keys for R (using FDs)

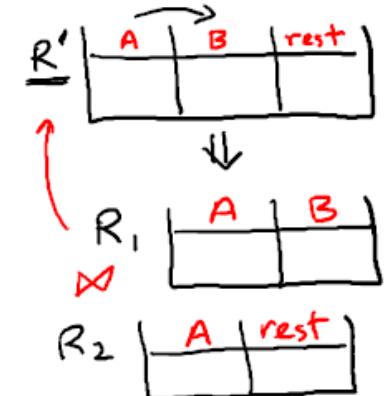
Repeat until all relations are in BCNF:

Pick any R' with $\bar{A} \rightarrow \bar{B}$ that violates BCNF

Decompose R' into $R_1(\bar{A}, \bar{B})$ and $R_2(\bar{A}, rest)$

Compute FDs for R_1 and R_2

Compute keys for R_1 and R_2



6.3 BC范式

例1

Student (SSN, Sname, address, HScode, HSname, HScity, GPA, priority)

- SSN → Sname, address, GPA
- GPA → priority
- HScode → HSname, HScity

S1 (HScode, HSname, HScity)

S2 (GPA, priority)

S3 (SSN, Sname, address, GPA)

S4 (SSN, HScode)

6.3 BC范式

- Student (SSN, Sname, address, HScode, HSname, HScity, GPA, priority)
 - FD1: SSN → Sname, address, GPA
 - FD2: GPA → priority
 - FD3: HScode → HSname, HScity
- Key: {SSN, HScode}, 违背BCNF: FD1, FD2, FD3
 - 选择FD3
 - R1 (HScode, HSname, HScity)
 - R2 (HScode, SSN, Sname, address, GPA, priority)
 - Key: {SSN, HScode}
 - FDs: FD1, FD2 (都违背BCNF)
 - 选择FD2
 - » R3 (GPA, priority)
 - » R4 (HScode, GPA, SSN, Sname, address)

6.3 BC范式

- Student (SSN, Sname, address, HScode, HSname, HScity, GPA, priority)
 - FD1: SSN → Sname, address, GPA
 - FD2: GPA → priority
 - FD3: HScode → HSname, HScity
- R1 (HScode, HSname, HScity)
- R3 (GPA, priority)
- R4 (HScode, GPA, SSN, Sname, address)
 - Key: {HScode, SSN}
 - FDs: FD1 (违背BCNF)
 - 选择FD1分解
 - R5 (SSN, Sname, address, GPA)
 - R6 (SSN, HScode)

6.3 BC范式

- Student (SSN, Sname, address, HScode, HSname, HScity, GPA, priority)
 - FD1: SSN → Sname, address, GPA
 - FD2: GPA → priority
 - FD3: HScode → HSname, HScity
- Key: {SSN, HScode}, 违背BCNF: FD1, FD2, FD3
 - 选择FD1
 - R1 (SSN, Sname, address, GPA)
 - R2 (SSN, HScode, HSname, HScity, priority)
 - Key: {SSN, HScode, priority}
 - FDs: FD3 (违背BCNF)
 - 选择FD3
 - » R3 (HScode, HSname, HScity)
 - » R4 (HScode, SSN, priority)

6.3 BC范式

- Student (SSN, Sname, address, HScode, HSname, HScity, GPA, priority)
 - FD1: SSN → Sname, address, GPA
 - FD2: GPA → priority
 - FD3: HScode → HSname, HScity
- Key: {SSN, HScode}, 违背BCNF: FD1, FD2, FD3
 - 选择FD1
 - R1 (SSN, Sname, address, GPA)
 - R2 (SSN, HScode, HSname, HScity, priority)
 - Key: {SSN, HScode, priority}
 - FDs: FD3, FD4: SSN → priority (都违背BCNF)
 - 选择FD3
 - » R3 (HScode, HSname, HScity)
 - » R4 (HScode, SSN, priority)

6.3 BC范式

- Student (SSN, Sname, address, HScode, HSname, HScity, GPA, priority)
 - FD1: SSN → Sname, address, GPA
 - FD2: GPA → priority
 - FD3: HScode → HSname, HScity
- R1 (SSN, Sname, address, GPA)
- R3 (HScode, HSname, HScity)
- R4 (HScode, SSN, priority)
 - Key: {HScode, SSN}
 - FDs: FD4: SSN → priority (违背BCNF)
 - 选择FD4分解
 - R5 (SSN, priority) → 丢失了FD2
 - R6 (SSN, HScode)

6.3 BC范式

- Student (SSN, Sname, address, HScode, HSname, HScity, GPA, priority)
 - FD1: SSN → Sname, address, GPA
 - FD2: GPA → priority
 - FD3: HScode → HSname, HScity
- Key: {SSN, HScode}, 违背BCNF: FD1, FD2, FD3
 - 选择FD1 ($A \rightarrow B$, $A \rightarrow BA^+$)
 - R1 (SSN, Sname, address, GPA, priority)
 - Key: {SSN}
 - FDs: FD2 (违背BCNF)
 - » R3 (GPA, priority)
 - » R4 (SSN, Sname, address, GPA)
 - R2 (SSN, HScode, HSname, HScity)

6.3 BC范式

- Student (SSN, Sname, address, HScode, HSname, HScity, GPA, priority)
 - FD1: SSN → Sname, address, GPA
 - FD2: GPA → priority
 - FD3: HScode → HSname, HScity
- Key: {SSN, HScode}, 违背BCNF: FD1, FD2, FD3
 - 选择FD1 ($A \rightarrow B$, $A \rightarrow BA^+$)
 - R1 (SSN, Sname, address, GPA, priority)
 - R3 (GPA, priority)
 - R4 (SSN, Sname, address, GPA)
 - R2 (SSN, HScode, HSname, HScity)
 - Key: {SSN, HScode}
 - FDs: FD3 (违背BCNF)
 - » R5 (HScode, HSname, HScity), R6(SSN, HScode)

6.3 BC范式

例2

Apply (SSN, Cname, state, date, major) B

- Cname → state
- SSN, Cname → date, major

- A. Apply(SSN,cName,state,date,major)
- B. A1(cName,state), A2(SSN,cName,date,major)
- C. A1(cName,state), A2(SSN,date,major)
- D. A1(cName,state), A2(SSN,cName,date), A3(SSN,cName,major)

6.3 BC范式

Compute keys for R (using FDs)

Repeat until all relations are in BCNF:

Pick any R' with $\bar{A} \rightarrow \bar{B}$ that violates BCNF

Decompose R' into $R_1(\bar{A}, \bar{B})$ and $R_2(\bar{A}, rest)$

Compute FDs for R_1 and R_2

Compute keys for R_1 and R_2

- 选择不同的 R' , 最终分解结果是否相同?
- Extend: $A \rightarrow B$, $A \rightarrow BA^+$
- Implied FDs closure

6.3 BC范式

- Does BCNF guarantee a good decomposition?
 - Removes anomalies? YES!
 - Can logically reconstruct original relation?
 - Too few or too many tuples?

The diagram illustrates the decomposition of a relation R into R_1 and R_2 , and the resulting Cartesian product $R_1 \bowtie R_2$.

Relation R is shown as a 4x3 grid:

A	B	C
1.	2.	3.
4.	2	5.

Handwritten annotations show two pink X's above columns B and C, indicating they are not part of the primary key. A curved arrow points from the label R to the grid.

Decomposition into R_1 and R_2 :

- R_1 (left): A 4x2 grid with columns A and B circled in pink:

A	B
1	2
4	2

- R_2 (right): A 4x2 grid with column B circled in pink:

B	C
2	3
2	5

Handwritten calculation shows the Cartesian product $R_1 \bowtie R_2$ resulting in the following 4x3 grid:

123		
125		
423		
425		

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6.4 BC范式和第4范式的局限

- BC范式
 - Relation R with FDs is in BCNF if:
For each $A \rightarrow B$, A is a key
- 4范式
 - Relation R with MVDs is in 4NF if:
For each nontrivial $A \rightarrow\rightarrow B$, A is a key

6.4 BC范式和第4范式的局限

例1

- Apply (SSN, Cname, date, major)
 - Can apply to each college once for one major
 - Colleges have non-overlapping application dates

函数依赖在分解后的关系中丢失
- FDs: $\boxed{SSN, Cname \rightarrow date, major}$ $date \rightarrow Cname$
- Keys: $SSN, Cname$
- BCNF: NO. R1(date, Cname), R2(SSN, date, major)
- Good design? Not necessarily. 3rd Normal Form

6.4 BC范式和第4范式的局限

例2

- Student (SSN, HSname, GPA, priority)
 - Multiple HS okay, priority determined from GPA
- FDs: $SSN \rightarrow GPA$ $GPA \rightarrow priority$ $SSN \rightarrow priority$
- Keys: $SSN, HSname$

选择不同函数依赖顺序会得到不同分解结果
- BCNF: NO. R1(SSN, priority), R2(SSN, GPA), R3(SSN, HSname)
- Good design? Not necessarily. 3rd Normal Form

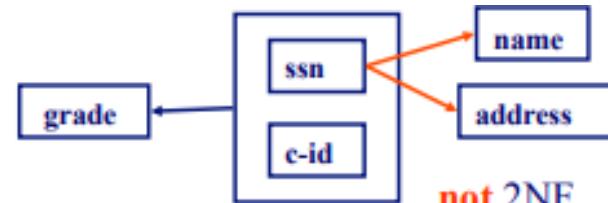
函数依赖在分解后的关系中丢失

6.4 BC范式和第4范式的局限

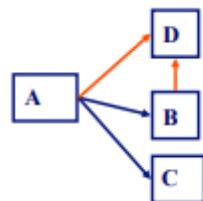
- 1st Normal Form (1NF)
 - Attributes are atomic (no set-valued attr.)
- 2nd Normal Form (2NF)
 - 1NF + non-key attributes fully depend on the key
 - Example: Takes(ssn, cid, grade, name, address)
 - ssn → name, address
 - ssn, cid → grade
- 3rd Normal Form (3NF)
 - 2NF + no transitive dependencies

Ssn	Name	Dependents
123	Smith	Peter Mary John
234	Jones	Ann Michael

not 1NF



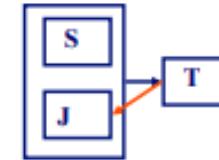
not 2NF



in 2NF, but not in 3NF

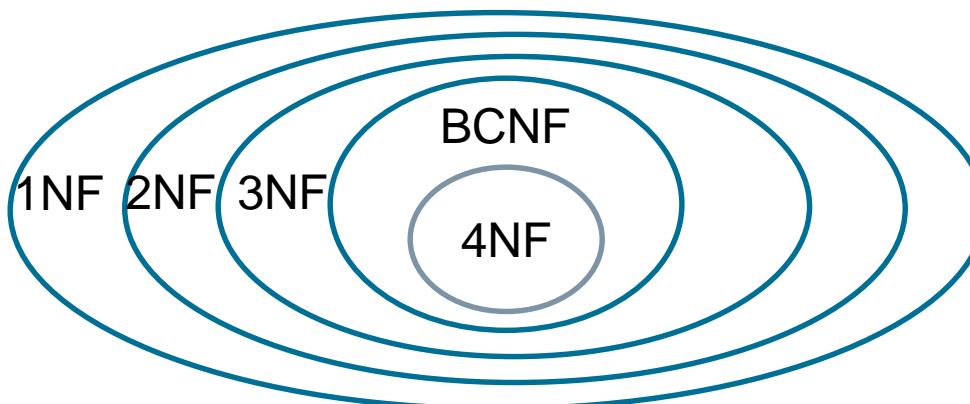
6.4 BC范式和第4范式的局限

- A relation R is in 3NF if for every FD $A \rightarrow B$
 - It is trivial (If $\bar{A} \rightarrow \bar{B}$, $\bar{B} \subseteq \bar{A}$)
 - A is a superkey (good FDs)
 - B is part of a candidate key (A may not be a superkey)
- STJ(Student, Teacher, subJect)
 - S, J \rightarrow T, T \rightarrow J
 - BCNF: R1(T, J), R2(S, T) [dependency preserving?]
 - 3NF forgives the red arrow
- In practice, aim for
 - BCNF: lossless join, dependency preservation
 - If impossible, 3NF: lossless join, dependency preservation



6.4 BC范式和第4范式的局限

- BC范式
 - Relation R with FDs is in BCNF if:
For each $A \rightarrow B$, A is a key
- 4范式
 - Relation R with MVDs is in 4NF if:
For each nontrivial $A \rightarrow\rightarrow B$, A is a key
- After decomposition, **no** guarantee dependencies can be checked on decomposed relations



6.4 BC范式和第4范式的局限

例3

“Denormalized” relation

- Scores (SSN, Sname, SAT, ACT)
 - Multiple SATs and ACTs allowed
 - All queries return name + composite score for SSN (此时更倾向于原始关系，包含所有属性)
- FDs + keys: $\text{SSN} \rightarrow \text{Sname}$. Key(SSN, SAT, ACT)
- MVDs: $\text{SSN}, \text{Sname} \rightarrow\rightarrow \text{SAT}$
- 4NF: NO. R1(SSN, Sname), R2(SSN, SAT), R3(SSN, ACT)

6.4 BC范式和第4范式的局限

例4

- College (Cname, state)
- CollegeSize (Cname, enrollment)
- CollegeScores (Cname, avgSAT)
- CollegeGrades (Cname, avgGPA)
- ...
- BCNF/4NF? Yes.
- Good design? Not necessarily.
 - 可用其他4范式关系表达，且包含信息相同

Too decomposed

6.4 BC范式和第4范式的局限

- E/R图转换关系模式时，**1:1 / 1:N**联系尽量和**弱实体 / N端实体**关系合并，减少关系数量，同时保证所有关系都属于BCNF

- River(name, length, shape(MultiLineString))

- name → length, shape



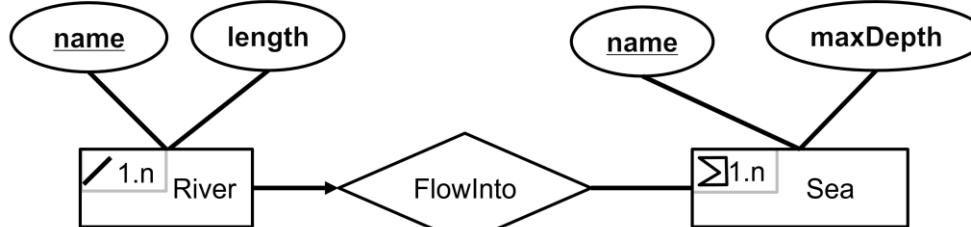
思考：几何属性适合作为主码(primary key)吗？

- FlowInto(riverName, SeaName)

- riverName → SeaName

- River(name, length, shape(MultiLineString)), seaName reference Sea)

- Sea(name, maxDepth, shape(MultiPolygon))



6.5 关系数据库设计理论小结

- Designing a database schema
 - Usually many designs possible
 - Some are (much) better than others!
 - How do we choose?
- Very nice theory for relational DB design
 - Normal forms – “good” relations
 - Design by decomposition
 - Usually intuitive and works well
 - Some shortcomings (Dependency enforcement, Query workload, Over-decomposition)

