# Project Report: Haze Removal

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#### 1 Introduction

Images of outdoor scenes are usually degraded by the turbid medium (e.g., particles, water-droplets) in the atmosphere. Haze, fog, and smoke are such phenomena due to atmospheric absorption and scattering. Haze removal1 (or dehazing) is highly desired in both consumer/computational photography and computer vision applications.

In this project, we experimentally examined approach proposed in [1], which could remove haze using single image.

# 2 Aproach

#### 2.1 Haze model

The model widely used in describing the formation of haze image is as follows:

$$I(x) = J(x)t(x) + A(1 - t(x))$$

where x is a pixel, I is the observed intensity, J is the scene radiance, A is the global atmospheric light, t is the medium transmission describing the portion of the light that is not scattered and reaches the camera. The goal of haze removal is to recover J, A, and t from I.

#### 2.2 Dark Channel Prior

Observation shows that, in foggy area of the image, the minimum RGB values of a pixel is higher than that in clear area. An intuition is that, foggy image tends to be whitish.

According to this, we can give an initial estimation of J:

$$J^{dark}(x) = \min_{c \in \{r,g,b\}} (\min_{y \in \Omega(x)} (J^c(y)))$$

where  $J^c$  is a color channel of J and  $\Omega(x)$  is a local patch centered at x. In [1], it is called dark channel prior. A typical size of the patch is 15x15, and  $\omega$  is arount 0.95.

As observation shows, nice property of  $J^{dark}$  is that, for a haze free image J,  $J^{dark} \to 0$ .

# 2.3 Estimate the Atmospheric Light

We pick the top 0.1% brightest pixels in dark channel, and pick the highest intensity in input image I as atmospheric light.

#### 2.4 Estimate the Transmission

First assume that the atmospheric light A is known, By further assuming the transmission in a local patch  $\Omega(x)$  is constant, the property of  $J^{dark}$ , after crunching equations, we get:

$$\widetilde{t}(x) = 1 - \min_{c} (\min_{y \in \Omega(x)} (\frac{I^{c}(y)}{A^{c}}))$$

where  $\widetilde{t}(x)$  is the estimation of true transmission t(x). But even in clear days, atmosphere is not absolutely free of any particle, the haze effect may still slightly appears. The catch this observation, an constant parameter  $\omega(0 < \omega <= 1)$ . The equation above then becomes:

$$\widetilde{t}(x) = 1 - \omega \min_{c} (\min_{y \in \Omega(x)} (\frac{I^{c}(y)}{A^{c}}))$$

#### 2.5 Transmission Refinement

In the original paper, the transmission is then refined using soft matting introduced in [2]. Rewriting t(x) and  $\tilde{t}(x)$  in their vector form as t and  $\tilde{t}$ , we minimize the following cost function:

$$E(t) = t^{T}Lt + \lambda(t - \bar{t})^{T}(t - \bar{t})$$

where L is the Matting Laplacian matrix proposed by [2], and  $\lambda$  is a regularization parameter.

The (i,j) element of the matrix L is defined as:

$$\sum_{k|(i,j)\in w_k} (\delta_{ij} - \frac{1}{|w_k|} (1 + (I_i - \mu_k)^T (\Sigma_k + \frac{\epsilon}{|w_k|} U_3)^{-1} (I_j - \mu_k)))$$

where  $I_i$  and  $I_j$  are the colors of the input image I at pixels i and j,  $\delta_{ij}$  is the Kronecker delta,  $\mu_k$  and  $\Sigma_k$  are the mean and covariance matrix of the colors in window  $\omega_k$ ,  $U_3$  is a 33 identity matrix,  $\epsilon$  is a regularizing parameter, and  $|w_k|$  is the number of pixels in the window  $\omega_k$ .

The optimal t can be obtained by solving the following sparse linear system:

$$(L + \lambda U)t = \lambda \widetilde{t}$$

where U is an identity matrix of the same size as L. Here, we set a small value on  $\lambda$  (10<sup>-4</sup> in our experiments) so that t is softly constrained by  $\tilde{t}$ .

#### 2.6 Recover the Scene Radience

From equation aforementioned, it is direct that we can recover J(x) by

$$J(x) = \frac{I(x) - A}{\max(t(x), t_0)} + A$$

where  $t_0$  is the minimum transmission threshold, typically around 0.1.

# 3 Result

Please see figures below to check the results.

# Reference

- [1] Kaiming He, Jian Sun, and Xiaoou Tang. Single image haze removal using dark channel prior. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2009.
- [2] Anat Levin, Dani Lischinski, and Yair Weiss. A closed form solution to natural image matting. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2004.



(a) input

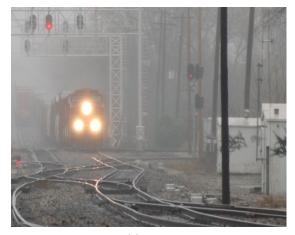


(b) before soft matting



(c) output

Figure 1: **‡**iananmen



(a) input



(b) before soft matting



(c) output

Figure 5: Train