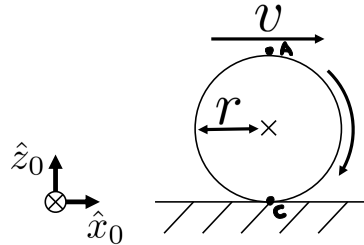


1. **Spatial Velocity:** A cylinder rolls without slipping in the  $\hat{x}_0$  direction on the  $\hat{x}_0 - \hat{y}_0$  plane. The cylinder has a radius of  $r$  and a constant forward speed of  $v$ . Let  ${}^0C=[C_x(t),0,0]^T$  be the position of the contact point at time  $t$ . Let  ${}^0A=[A_x(t),0,0]^T$  be the position of the instantaneous top of the cylinder at time  $t$ .
  - (a) What is the linear velocity of the point  $C$ ? (hint: just need to compute  $\frac{d}{dt}C_x(t)$ )?
  - (b) What is the linear velocity of the point  $A$ ?
  - (c) What is velocity of the body-fixed point currently coincides with  $C$ ?
  - (d) What is velocity of the body-fixed point currently coincides with  $A$ ?
  - (e) What is the spatial velocity of the cylinder in  $\{0\}$ -frame?
  - (f) What is the spatial velocity of the cylinder in frame  $\{C\}$ ? ( $\{C\}$  has the same orientation as  $\{0\}$ , while its origin is at the contact point  $C$ )

Note: The first 4 questions are all referring to the inertia frame  $\{0\}$



2. Modern Robotics: Exercise 3.21
3. Modern Robotics: Exercise 3.28
4. Modern Robotics: Exercise 5.5
5. Modern Robotics: Exercise 5.6