

Ensemble methods: boosting

Machine Learning and Deep Learning

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Boosting exploits the wisdom of the crowd:

- building many weak classifiers is easier than devising one complex prediction rule
- can I build a strong classifier out of a crowd of weak classifiers?

Boosting

Provides a general framework featuring:

- weak classifiers: slightly better than random chance
- cascade: each classifier is aware of previous ones errors
- the prediction rule is based on all classifiers' predictions

Boosting

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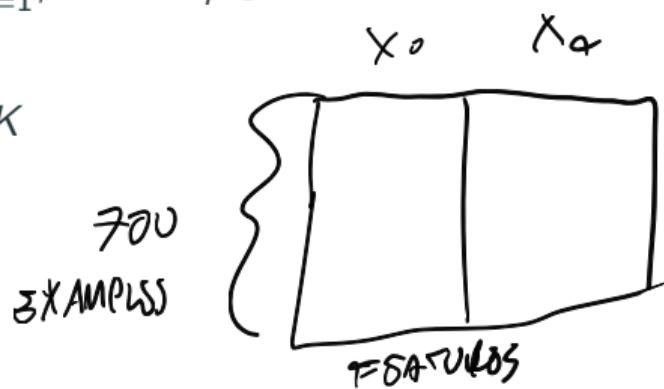
- weak classifiers: slightly better than random chance
 - How?
- cascade: each classifier is aware of previous ones errors
 - How?
- the prediction rule is based on all classifiers' predictions
 - How?

COMBINARE
DEI CLASSIFICATORI
PERCORSO

Adaboost: setting

We are given

- a dataset D of examples $\{\vec{x}_i\}_{i=1}^N \{y_i\}_{i=1}^N$, where $\vec{x}_i \in \mathbb{R}^d$ and $y_i \in \{-1, 1\} \quad \forall i = 1, \dots, N$
- a predefined number of weak learners K



Adaboost: training algorithm

1) Campione di MANTENIMENTO \rightarrow UN PESO \checkmark esempio \rightarrow metà
esempio \vee esempio

- initialize a weight w_i for each training example

- repeat for $j = 1, \dots, K$:

- from D , sample N examples with replacement and build a temporary dataset D_j .
 Each example has a probability of being sampled equal to w_i
- build a weak classifier M_j on D_j \rightarrow nuovo classificatore con un errore ϵ_j di esempio \checkmark campionato
- compute the error rate ϵ_j of M_j , and the relative *efficiency* α_j
- update weights for all samples in D_j \Rightarrow ① nuovo peso nuova efficienza.
 - if correctly classified: decrease the weight
 - if incorrectly classified: increase the weight

Adaboost: a closer look (1)

M° Fornacci - [P, 12]

AVVIO		
	x_0	x_1
1	1	1
n	1	1

II UTILIZZO SPERIMENTALE

To build a weak classifier for D_j , repeat until $\epsilon_j < 0.5$

- randomly choose a data dimension $\rightarrow \text{una dimensione}$
- randomly choose a threshold $\rightarrow \text{min e max valori verso basso in } 0.5$
- set all points above the threshold (along the chosen axis) to 1 and all points below to -1 (or viceversa)
- compute ϵ_j over D_j

• Si continua a tirare delle soglie su uno x pernies a caso finché $\epsilon_j < 0.5$

mp. UNIV. MOROGLIO
SOC 0 0 1
(le dim)
ogni passo viene
con tutti gli
esempi
ogni (tutte le classi)
sugger
 $X \in \mathbb{R}^{n \times d}$

Adaboost: a closer look (2)

PASSAGGIAMENTO DEL PESO \Rightarrow *Questa operazione serve a calcolare le classificazioni, tenendo conto dei voti di tutti i classificatori e quindi il loro errore.*

To compute the error and the efficiency of a weak classifier M_j

`error = np.sum(sample_weights[cur_idx[cur_Y != y_pred]])`

$$\epsilon_j = \sum_{M_j(x_i) \neq y_i} w_i \Rightarrow$$

Si calcola la somma delle weight per cui la classe predetta è diversa dalla vera classe.

$$\alpha_j = \frac{1}{2} \ln \left(\frac{1 - \epsilon_j}{\epsilon_j} \right)$$

Adaboost: a closer look (3)

To update w_i :

$$w_i^{(j+1)} = \frac{w_i^{(j)}}{Z^{(j)}} \begin{cases} \exp^{-\alpha_j} & \text{if } M_j(x_i) = y_i \\ \exp^{\alpha_j} & \text{if } M_j(x_i) \neq y_i \end{cases}$$

$\Rightarrow Z^{(j)}$ si calcola
per fare fine X
normalizzando
il tutto.

$Z^{(j)}$ is a normalization factor that ensures $\sum_i w_i = 1$

Adaboost: learning

Adaboost: decision rule

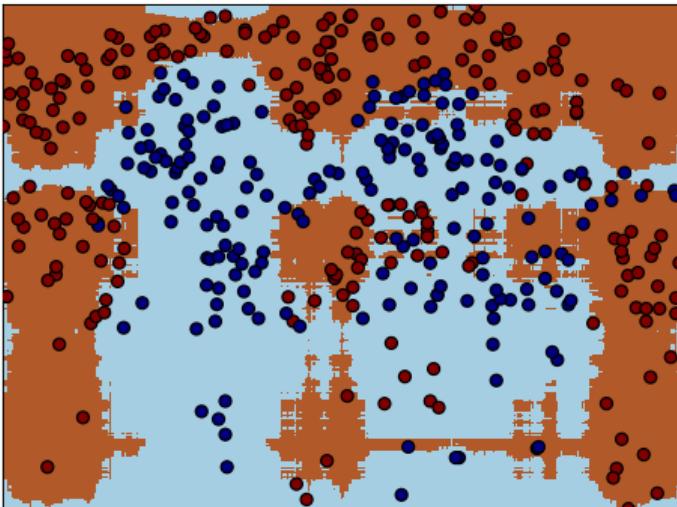
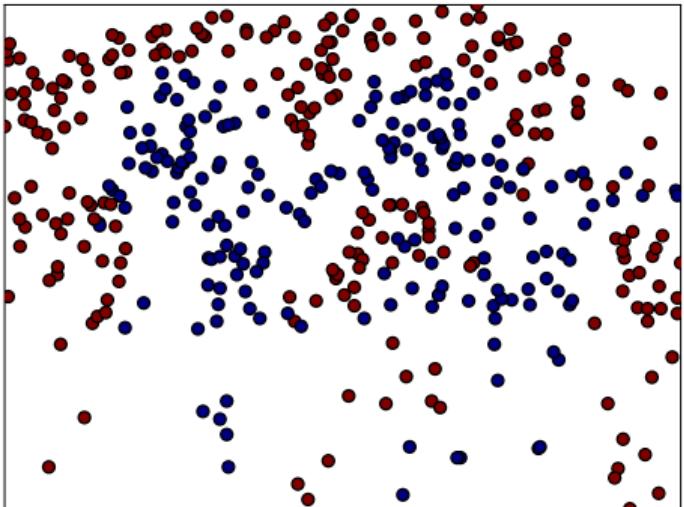
At test phase, you can classify an unknown vector \vec{u}

$$\mathcal{H}(\vec{u}) = \text{sign}\left(\sum_{j=1}^K \alpha_j M_j(\vec{u}) \right)$$

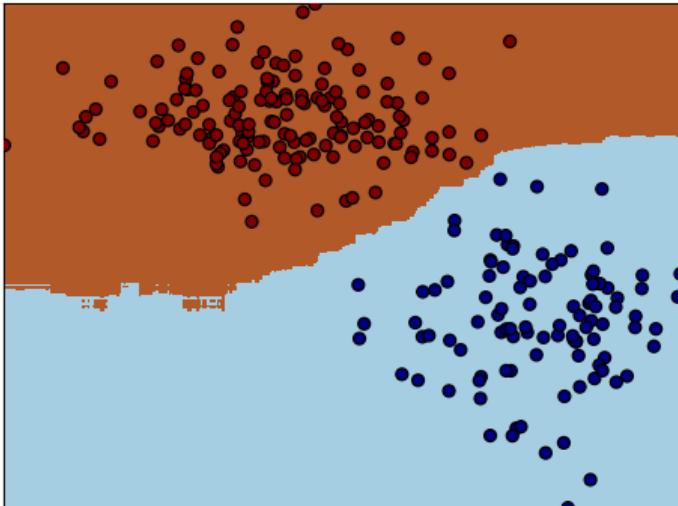
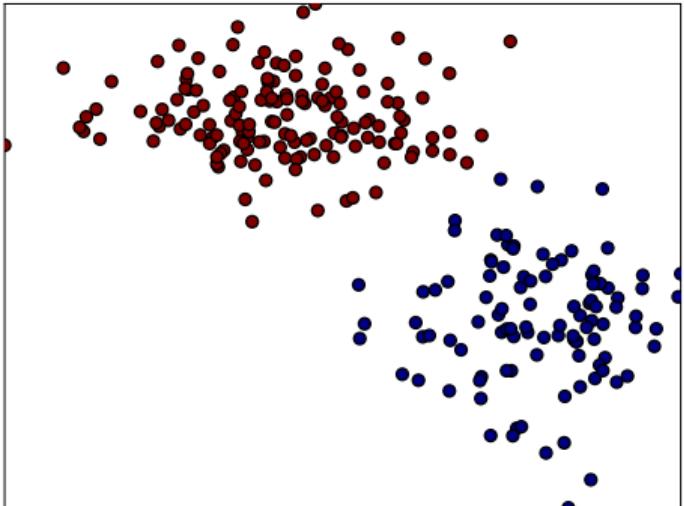
$M_j(\vec{u})$ is a classification
 \times \vec{u} vectors
 of features in \vec{u}

- CCM. FOR SU CLASSIFICATION
- SI CHIAMA DISDESS DEL CLASSIFICATORI
- SI FA IL SIGNO DEL RISULTATO
 DELLE CLASSIFICATIONS

Adaboost: example (1)



Adaboost: example (2)



Adaboost: example (3)

