

Zoo: A framework for the verification of concurrent OCaml 5 programs using separation logic

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Abstract

The release of OCAML 5, which introduced parallelism into the language, drove the need for safe and efficient concurrent data structures. New libraries like SATURN aim at addressing this need. From the perspective of formal verification, this is an opportunity to apply and further state-of-the-art techniques to provide stronger guarantees.

We present a framework for verifying fine-grained concurrent OCAML 5 algorithms. We followed a pragmatic approach, studying OCAML code written by concurrency expert to delimit a limited but sufficient fragment of the language to express these algorithms; the outcome is a dialect of OCAML that we call ZOOLANG. We formalized its semantics carefully via a deep embedding in the ROCQ proof assistant. We provide a tool to translate source OCAML programs into ZOOLANG syntax inside ROCQ, where they can be specified and verified using the IRIS concurrent separation logic.

We verified fine-grained concurrent algorithms, along with subsets of the OCAML standard library necessary to express them: the classic Treiber stack, and a use of reference-counting for file descriptors within the Eio library. This formalization work uncovered delicate questions of programming-language semantics, around physical equality for example. In the process, we also extended OCAML to more efficiently express certain concurrent programs.

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1 Introduction

Designing concurrent algorithms, in particular fine-grained concurrent algorithms, is a notoriously difficult task. Similarly, the formal verification of such algorithms is also difficult. It typically involves finding and reasoning about non-trivial linearization points [21, 30, 55, 56, 11].

In recent years, concurrent separation logic [5] has enabled significant progress in this area. In particular, the development of IRIS [29], a state-of-the-art mechanized *higher-order* concurrent separation logic with *user-defined ghost state*, has nourished a rich and successful line of works [30, 55, 56, 11, 6, 28, 49, 38, 37, 17, 43, 41, 40], dealing with external [56] and future-dependent [30, 55, 11] linearization points, relaxed memory [38, 37, 17, 43] and automation [41, 40].

Most of these works [30, 55, 56, 6, 28, 49, 41, 40] and many others [19, 45, 54, 35] rely on HEAPLANG [52], the exemplar IRIS language. HEAPLANG is a concurrent, imperative, untyped, call-by-value functional language. To the best of our knowledge, it is currently the closest language to OCAML 5 in the IRIS ecosystem—we review the existing frameworks in Section 2. It has been extended to handle weak memory [38] and algebraic effects [18].



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Although HEAPLANG is theoretically expressive enough to represent OCAML programs, our experiments showed that it is fairly impractical when it comes to verifying large OCAML libraries. Indeed, it lacks basic abstractions such as algebraic data types (tuples, mutable and immutable records, variants) and mutually recursive functions. Verifying OCAML programs in HEAPLANG requires difficult translation choices and introduces various encodings, to the point that the relation between the source and verified programs can become difficult to maintain and reason about. It also has very few standard data structures that can be directly reused. This view, we believe, is shared by many people in the IRIS community. Our first motivation in this work is therefore to fill this gap by providing a more practical OCAML-like verification language: ZOOLANG. This language consists in a subset of OCAML 5 extended with atomic record fields and equipped with a formal semantics and a program logic based on IRIS. We were influenced by the PERENNIAL [8, 9, 10, 11] framework, which achieved similar goals for the GO language with a focus on crash-safety. As in PERENNIAL, we also provide a translator from OCAML to ZOOLANG: `ocaml2zoo`. We call the resulting framework ZOO.

Another, maybe less obvious, shortcoming of HEAPLANG is the soundness of its semantics with respect to OCAML, in other words how faithful it is to the original language. One ubiquitous—particularly in lock-free algorithms relying on low-level atomic primitives—and subtle point is *physical equality*. In Section 5, we show that (1) HEAPLANG’s semantics for physical equality is not compatible with OCAML and (2) OCAML’s informal semantics is actually too imprecise to verify basic concurrent algorithms. To remedy this, we propose a new formal semantics for physical equality and structural equality. We hope this work will influence the way these notions are specified in OCAML.

In summary, we claim the following contributions:

1. We present ZOOLANG, a convenient subset of OCAML 5 formalized in ROCQ (Sections 3 and 4). ZOOLANG comes with a program logic based on IRIS and supports proof automation through DIAFRAME [41, 40].
2. We provide a translator from OCAML to ZOOLANG: `ocaml2zoo` (Section 3), built for practical applications—it supports full projects using the `dune` build system.
3. We formalize physical equality (Section 5) and structural equality (Section 6) in a faithful way. To our knowledge this is the first detailed specification of physical equality for a practical fragment of OCAML. The careful analysis of these notions suggests a new OCAML feature: *generative constructors*.
4. We extend OCAML with *atomic record fields* and *atomic arrays* to ease the development of fine-grained concurrent algorithms (Section 7).
5. We verify realistic use cases (Section 5) involving physical equality: (1) Treiber stack [7], (2) a thread-safe wrapper around a file descriptor using reference-counting from the Eio [36] library.

2 Related work

The idea of applying formal methods to verify OCAML programs is not new. Generally speaking, there are mainly two ways:

2.1 Non-automated verification

The verified program is translated, manually or in an automated way, into a representation living inside a proof assistant. The user has to write specifications and prove them.

The representation may be primitive, like Gallina for ROCQ. For pure programs, this is rather straightforward, *e.g.* in `hs-to-coq` [50]. For imperative programs, this is more

challenging. One solution is to use a monad, *e.g.* in `coq-of-ocaml` [14], but it does not support concurrency.

The representation may be embedded, meaning the semantics of the language is formalized in the proof assistant. This is the path taken by some recent works [12, 24, 8, 16] harnessing the power of separation logic. In particular, CFML [12] and OSIRIS [16] target OCAML. However, CFML does not support concurrency and is not based on IRIS. OSIRIS, still under development, is based on IRIS but does not support concurrency.

At the time of writing, HEAPLANG is thus the most appropriate tool to verify concurrent OCAML programs. We discussed limitations of HEAPLANG in the introduction, and ZOOLANG is our proposal to improve on this. Conversely, one notable limitation of ZOOLANG today is its lack of support for OCAML’s relaxed memory model.

2.2 Semi-automated verification

In semi-automated verification approaches, the verified program is annotated by the user to guide the verification tool: preconditions, postconditions, invariants, *etc.* Given this input, the verification tool generates proof obligations that are mostly automatically discharged. One may further distinguish two types of semi-automated systems: *foundational* and *non-foundational*.

In *non-foundational* automated verification, the tool and the external solvers it may rely on are part of the trusted computing base. It is the most common approach and has been widely applied in the literature [51, 42, 26, 20, 1, 22, 34, 46], including to OCAML by CAMELEER [44], which uses the GOSPEL specification language [13] and WHY3 [22].

In *foundational* automated verification, the proofs are checked by a proof assistant like ROCQ, meaning the automation does not have to be trusted. To our knowledge, it has been applied to C [47] and RUST [23].

ZOO is a non-automated verification framework—except for our use DIAFRAME for local automation of separation logic reasoning. We would be interested in moving towards more automation in the future.

2.3 Physical equality

There is some literature in proof-assistant research on reflecting physical equality from the implementation language into the proof assistant, for optimization purposes: for example, exposing OCAML’s physical equality as a predicate in ROCQ lets us implement some memoization and sharing techniques in ROCQ libraries. However, axiomatizing physical equality in the proof assistant is difficult, and can result in inconsistencies.

The earlier discussions of this question that we know come from Jourdan’s thesis [27] (chapter 9), also presented more succinctly in [4]. This work introduces the Jourdan condition, that physical equality implies equality of values. [3] extends the treatment of physical equality in ROCQ, integrating it in an “extraction monad” to control it more safely. There is also a discussion of similar optimizations in LEAN in [48].

The correctness of the axiomatization of physical equality depends on the type of the values being compared: axiomatizations are typically polymorphic on any type *A*, but their correctness depends on the specific *A* being considered. For example, it is easy to correctly characterize physical on natural numbers, and other non-dependent types arising in ROCQ verification projects. One difficulty in HEAPLANG and ZOOLANG is that they are untyped languages, their representation of 0 and `false` has the same type. But our remark that structural equality (in OCAML) does not necessarily coincide with definitional equality (in

Rocq term	t	
constructor	C	
projection	$proj$	
record field	fld	
identifier	s, f	$\in \text{String}$
integer	n	$\in \mathbb{Z}$
boolean	b	$\in \mathbb{B}$
binder	x	$::= \langle \rangle \mid s$
unary operator	\oplus	$::= \sim \mid -$
binary operator	\otimes	$::= + \mid - \mid * \mid \text{'quot'} \mid \text{'rem'} \mid \text{'land'} \mid \text{'lor'} \mid \text{'lsl'} \mid \text{'lsr'}$ $\mid <= \mid < \mid >= \mid > \mid = \mid \neq \mid == \mid !=$ $\mid \text{and} \mid \text{or}$
expression	e	$::= t \mid s \mid \#n \mid \#b$ $\mid \text{fun: } x_1 \dots x_n \Rightarrow e \mid \text{rec: } f \ x_1 \dots x_n \Rightarrow e \mid e_1 \ e_2$ $\mid \text{let: } x := e_1 \text{ in } e_2 \mid e_1 \ ; \ ; \ e_2$ $\mid \text{let: } f \ x_1 \dots x_n := e_1 \text{ in } e_2 \mid \text{letrec: } f \ x_1 \dots x_n := e_1 \text{ in } e_2$ $\mid \text{let: 'C } x_1 \dots x_n := e_1 \text{ in } e_2 \mid \text{let: } x_1, \dots, x_n := e_1 \text{ in } e_2$ $\mid \oplus e \mid e_1 \otimes e_2$ $\mid \text{if: } e_0 \text{ then } e_1 \text{ (else } e_2 \text{)}^?$ $\mid \text{for: } x := e_1 \text{ to } e_2 \text{ begin } e_3 \text{ end}$ $\mid \S C \mid \text{'C } (e_1, \dots, e_n) \mid (e_1, \dots, e_n) \mid e.\langle proj \rangle$ $\mid [] \mid e_1 :: e_2$ $\mid \text{'C } \{e_1, \dots, e_n\} \mid \{e_1, \dots, e_n\} \mid e.\{fld\} \mid e_1 \leftarrow \{fld\} e_2$ $\mid \text{ref } e \mid !e \mid e_1 \leftarrow e_2$ $\mid \text{match: } e_0 \text{ with } br_1 \mid \dots \mid br_n \ (l_ \text{ as } s)^? \Rightarrow e \text{ end}$ $\mid e.[fld] \mid \text{Xchg } e_1 \ e_2 \mid \text{CAS } e_1 \ e_2 \ e_3 \mid \text{FAA } e_1 \ e_2$ $\mid \text{Proph} \mid \text{Resolve } e_0 \ e_1 \ e_2$
branch	br	$::= C \ (x_1 \dots x_n)^? \text{ (as } s \text{)}^? \Rightarrow e$ $\mid [] \text{ (as } s \text{)}^? \Rightarrow e \mid x_1 :: x_2 \text{ (as } s \text{)}^? \Rightarrow e$
toplevel value	v	$::= t \mid \#n \mid \#b$ $\mid \text{fun: } x_1 \dots x_n \Rightarrow e \mid \text{rec: } f \ x_1 \dots x_n \Rightarrow e$ $\mid \S C \mid \text{'C } (v_1, \dots, v_n) \mid (v_1, \dots, v_n)$ $\mid [] \mid v_1 :: v_2$

■ **Figure 1** ZOOLANG syntax (omitting mutually recursive toplevel functions)

135 ROCQ) also applies to other ROCQ types: our examples with an existential [Any](#) constructor
136 (see Section 5) can be reproduced with Σ -types.

137 3 Zoo in practice

138 3.1 Language

139 The core of ZOO is ZOOLANG: a concurrent, imperative, untyped, functional programming
140 language fully formalized in ROCQ. Its semantics has been designed to match OCAML's.

141 ZOOLANG comes with a program logic based on IRIS: reasoning rules expressed in
142 separation logic (including rules for the different constructs of the language) along with
143 ROCQ tactics that integrate into the IRIS proof mode [33, 32]. In addition, it supports
144 DIAFRAME [41, 40], enabling proof automation.

The ZOOLANG syntax is given in Figure 1¹, omitting mutually recursive toplevel functions that are treated specifically. Expressions include standard constructs like booleans, integers, anonymous functions (that may be recursive), applications, **let** bindings, sequence, unary and binary operators, conditionals, **for** loops, tuples. In any expression, one can refer to a ROCQ term representing a ZOOLANG value (of type **val**) using its ROCQ identifier. ZOOLANG is deeply embedded: variables (bound by functions and **let**) are quoted, represented as strings.

Data constructors (immutable memory blocks) are supported through two constructs: $\$C$ represents a constant constructor (e.g. $\$None$), $'C (e_1, \dots, e_n)$ represents a non-constant constructor (e.g. $'Some(e)$). Unlike OCAML, ZOOLANG has projections of the form $e.<proj>$ (e.g. $(x, y).<1>$), that can be used to obtain a specific component of a tuple or data constructor. ZOOLANG supports shallow pattern matching (patterns cannot be nested) on data constructors with an optional fallback case.

Mutable memory blocks are constructed using either the untagged record syntax $\{e_1, \dots, e_n\}$ or the tagged record syntax $'C \{e_1, \dots, e_n\}$. Reading a record field can be performed using $e.\{fld\}$ and writing to a record field using $e_1 <- \{fld\} e_2$. Pattern matching can also be used on mutable tagged blocks provided that cases do not bind anything—in other words, only the tag is examined, no memory access is performed. References are also supported through the usual constructs: **ref** e creates a reference, **!e** reads a reference and $e_1 <- e_2$ writes into a reference. The syntax seemingly does not include constructs for arrays but they are supported through the **Array** standard module (e.g. **array_make**).

Note that ZOOLANG follows OCAML in sometimes eschewing orthogonality to provide more compact memory representations: constructors are n -ary instead of taking a tuple as parameter, and the tagged record syntax is distinct from a constructor taking a mutable record as parameter. In each case the simplifying encoding would introduce an extra indirection in memory, which is absent from the ZOOLANG semantics. Performance-conscious experts care about these representation choices, and we care about faithfully modeling their programs.

Parallelism is mainly supported through the **Domain** standard module (e.g. **domain_spawn**), including domain-local storage. Special constructs (**Xchg**, **CAS**, **FAA**; see Section 4.4) are used to model atomic references.

The **Proph** and **Resolve** constructs model *prophecy variables* [30], see Section 4.5.

3.2 Translation from OCaml to ZooLang

While ZOOLANG lives in ROCQ, we want to verify OCAML programs. To connect them we provide the tool **ocaml2zoo** to translate OCAML source files² into ROCQ files containing ZOOLANG code. This tool can process entire **dune** projects, and support several libraries provided together or as dependencies of the project.

The supported OCAML fragment includes: tuples, variants, records (including inline records), shallow **match**, atomic record fields, unboxed types, toplevel mutually recursive functions.

Consider, for example, the OCAML implementation of a concurrent stack [7] in Figure 2. The **push** function is translated into:

```
Definition stack_push : val :=
  rec: "push" "t" "v" =>
```

¹ More precisely, it is the syntax of the surface language, including ROCQ notations.

² Actually, **ocaml2zoo** processes binary annotation files (**.cmt** files).

```

type 'a t = 'a list Atomic.t

let create () = Atomic.make []

let rec push t v =
  let old = Atomic.get t in
  let new_ = v :: old in
  if not (Atomic.compare_and_set t old new_) then (
    Domain.cpu_relax () ;
    push t v
  )

let rec pop t =
  match Atomic.get t with
  | [] -> None
  | v :: new_ as old ->
    if Atomic.compare_and_set t old new_ then (
      Some v
    ) else (
      Domain.cpu_relax () ;
      pop t
    )

```

■ Figure 2 Implementation of a concurrent stack

```

let: "old" := !"t" in
let: "new_" := "v" :: "old" in
if: ~ CAS "t".[contents] "old" "new_" then (
  domain_cpu_relax () ;;
  "push" "t" "v"
).

```

186 3.3 Specifications and proofs

187 Once the translation to ZOOLANG is done, the user can write specifications and prove them
 188 in IRIS. For instance, the specification of the `stack_push` function could be:

```

Lemma stack_push_spec t  $\iota$  v :
  <<< stack_inv t  $\iota$ 
  |  $\forall$  vs, stack_model t vs >>>
  stack_push t v @  $\uparrow\iota$ 
  <<< stack_model t (v :: vs)
  | RET (); True >>>.

```

Proof. ... Qed.

189 Here, we use a *logically atomic specification* [15], which has been proven [2] to be equivalent
 190 to *linearizability* [25] in sequentially consistent memory models.

191 Similarly to Hoare triples, the specification is formed of a precondition and a postcondition,
 192 represented in angular brackets. But each is split in two parts, a *public* or *atomic* condition,
 193 and a *private* condition. Following standard IRIS notations, the private conditions are on
 194 the outside (first line of the precondition, last line of the postcondition) and the atomic

195 conditions are inside.

196 For this particular operation, the private postcondition is trivial. The private condition
 197 `stack_inv t` is the stack invariant. Intuitively, it asserts that t is a valid concurrent stack.
 198 More precisely, it enforces a set of logical constraints—a concurrent protocol—that t must
 199 respect at all times.

200 The atomic pre- and post-conditions specify the linearization point of the operation:
 201 during the execution of `stack_push`, the abstract state of the stack held by `stack_model` is
 202 atomically updated from vs to $v :: vs$; in other words, v is atomically pushed at the top of
 203 the stack.

204 4 Zoo features

205 In this section, we review the salient features of ZOO, which we found lacking when we
 206 attempted to use HEAPLANG to verify real-world OCAML programs. We start with the most
 207 generic ones and then address those related to concurrency.

208 4.1 Algebraic data types

209 ZOO is an untyped language but, to write interesting programs, it is convenient to work with
 210 abstractions like algebraic data types. To simulate tuples, variants and records, we designed
 211 a machinery to define projections, constructors and record fields.

212 For example, one may define a list-like type with:

```
Notation "'Nil'" := (in_type "t" 0) (in custom zoo_tag).
Notation "'Cons'" := (in_type "t" 1) (in custom zoo_tag).
```

213 Users do not need to write this incantation directly, as they are generated by `ocaml2zoo`
 214 from the OCAML type declarations. Suffice it to say that it introduces the two tags in the
 215 `zoo_tag` custom entry, on which the notations for data constructors rely. The `in_type` term
 216 is needed to distinguish the tags of distinct data types; crucially, it cannot be simplified away
 217 by ROCQ, as this could lead to confusion during the reduction of expressions.

218 Given this incantation, one may directly use the tags `Nil` and `Cons` in data constructors
 219 using the corresponding ZOO`LANG` constructs:

```
Definition map : val :=
  rec: "map" "fn" "t" =>
    match: "t" with
    | Nil => $Nil
    | Cons "x" "t" =>
      let: "y" := "fn" "x" in
      'Cons( "y", "map" "fn" "t" )
    end.
```

220 Similarly, one may define a record-like type with two mutable fields `f1` and `f2`:

```
Notation "'f1'" := (in_type "t" 0) (in custom zoo_field).
Notation "'f2'" := (in_type "t" 1) (in custom zoo_field).
```

```
Definition swap : val :=
  fun: "t" =>
    let: "f1" := "t".{f1} in
    "t" <-{f1} "t".{f2} ;; "t" <-{f2} "f1".
```

221

4.2 Mutually recursive functions

222 ZOO supports non-recursive (`fun: $x_1 \dots x_n \Rightarrow e$`) and recursive (`rec: $f \ x_1 \dots x_n \Rightarrow e$`)
 223 functions but only *toplevel* mutually recursive functions. It is non-trivial to properly handle
 224 mutual recursion: when applying a mutually recursive function, a naive approach would
 225 replace calls to sibling functions by their respective bodies, but this typically makes the
 226 resulting expression unreadable. To prevent it, the mutually recursive functions have to
 227 know one another to preserve their names during β -reduction. We simulate this using some
 228 boilerplate that can be generated by `ocaml2zoo`. For instance, one may define two mutually
 229 recursive functions `f` and `g` as follows:

```

Definition f_g := (
  recs: "f" "x" => "g" "x"
  and:  "g" "x" => "f" "x"
)%zoo_recs.

(* boilerplate *)
Definition f := ValRecs 0 f_g.
Definition g := ValRecs 1 f_g.
Instance : AsValRecs' f 0 f_g [f;g]. Proof. done. Qed.
Instance : AsValRecs' g 1 f_g [f;g]. Proof. done. Qed.

```

230

4.3 Standard library

231 To save users from reinventing the wheel, we provide a standard library—more or less a
 232 subset of the OCAML standard library. Currently, it mainly includes standard data structures
 233 like: array (`Array`), resizable array (`Dynarray`), list (`List`), stack (`Stack`), queue (`Queue`),
 234 double-ended queue, mutex (`Mutex`), condition variable (`Condition`).

235 Each of these standard modules contains ZOO_{LANG} functions and their verified specifications.
 236 These specifications are modular: they can be used to verify more complex data structures.
 237 As an evidence of this, lists [anonymous] and arrays [anonymous] have been successfully used
 238 in verification efforts based on ZOO.

239

4.4 Concurrent primitives

240 ZOO supports concurrent primitives both on atomic references (from `Atomic`) and atomic
 241 record fields (from `Atomic.Loc`³) according to the table below. The OCAML expressions
 242 listed in the left-hand column translate into the ZOO expressions in the right-hand column.
 243 Notice that an atomic location `[%atomic.loc e.f]` (of type `_ Atomic.Loc.t`) translates
 244 directly into `e.[f]`.

³ The `Atomic.Loc` module is part of the PR that implements atomic record fields (see Section 7).

OCAML	Zoo
<code>Atomic.get e</code>	<code>!e</code>
<code>Atomic.set e₁ e₂</code>	<code>e₁ <- e₂</code>
<code>Atomic.exchange e₁ e₂</code>	<code>Xchg e₁. [contents] e₂</code>
<code>Atomic.compare_and_set e₁ e₂ e₃</code>	<code>CAS e₁. [contents] e₂ e₃</code>
<code>Atomic.fetch_and_add e₁ e₂</code>	<code>FAA e₁. [contents] e₂</code>
<code>Atomic.Loc.exchange [%atomic.loc e₁.f] e₂</code>	<code>Xchg e₁. [f] e₂</code>
<code>Atomic.Loc.compare_and_set [%atomic.loc e₁.f] e₂ e₃</code>	<code>CAS e₁. [f] e₂ e₃</code>
<code>Atomic.Loc.fetch_and_add [%atomic.loc e₁.f] e₂</code>	<code>FAA e₁. [f] e₂</code>

One important aspect of this translation is that atomic accesses (`Atomic.get` and `Atomic.set`) correspond to plain loads and stores. This is because we are working in a sequentially consistent memory model: there is no difference between atomic and non-atomic memory locations.

4.5 Prophecy variables

Lock-free algorithms exhibit complex behaviors. To tackle them, IRIS provides powerful mechanisms such as *prophecy variables* [30]. Essentially, prophecy variables can be used to predict the future of the program execution and reason about it. They are key to handle *future-dependent linearization points*: linearization points that may or may not occur at a given location in the code depending on a future observation.

ZOO supports prophecy variables through the `Proph` and `Resolve` expressions—as in HEAPLANG, the canonical IRIS language. In OCAML, these expressions correspond to `Zoo.proph` and `Zoo.resolve`, that are recognized by `ocaml2zoo`.

5 Physical equality

The notion of *physical equality* is ubiquitous in fine-grained concurrent algorithms. It appears not only in the semantics of the `==` operator, but also in the semantics of the `Atomic.compare_and_set` primitive, which atomically sets an atomic reference to a desired value if its current content is physically equal to an expected value. This primitive is commonly used to try committing an atomic operation in a retry loop, as in the `push` and `pop` functions of Figure 2.

5.1 Physical equality in HeapLang

In HEAPLANG, this primitive is provided but restricted. Indeed, its semantics is only defined if either the expected or the desired value fits in a single memory word in the HEAPLANG value representation: literals (booleans, integers and pointers⁴) and literal injections⁵; otherwise, the program is stuck. In practice, this restriction forces the programmer to introduce an indirection [53, 30, 55] to physically compare complex values, *e.g.* lists. Furthermore, when the semantics is defined, values are compared using their ROCQ representations; physical equality boils down to ROCQ equality.

⁴ HEAPLANG allows arbitrary pointer arithmetic and therefore inner pointers. This is forbidden in both OCAML and ZOOLANG, as any reachable value has to be compatible with the garbage collector.

⁵ HEAPLANG has no primitive notion of constructor, only pairs and injections (left and right).

274

5.2 Physical equality in OCaml

275 In OCAML, physical equality is more tricky and often considered dangerous. *Structural*
 276 *equality*, which we describe in Section 6, should be the preferred way of comparing values.
 277 However, structural equality is typically much slower than physical equality, as it basically
 278 compiles to only one assembly instruction. Also, the `Atomic.compare_and_set` requires the
 279 comparison to be atomic, which is the case for physical equality but not structural equality.

280 In particular, the semantics of physical equality is *non-deterministic*. To see why, consider
 281 the case of *immutable blocks* representing constructors and immutable records (as opposed to
 282 *mutable blocks* representing mutable records), *e.g.* `Some 0`. The physical comparison of two
 283 seemingly identical immutable blocks, according to the ROCQ representation (essentially a
 284 tag and a list of fields), may return `false`. Indeed, at runtime, a non-empty immutable block
 285 is represented by a pointer to a tagged memory block. In this case, physical equality is just
 286 pointer comparison. It is clear that two pointers being distinct does not imply the pointed
 287 memory blocks are. In other words, we cannot determine the result of physical comparison
 288 just by looking at the abstract values.

289 The question is then: what guarantees do we get when physical equality returns `true` and
 290 when it returns `false`? Given such guarantees, denoted by `val_physeq` and `val_physneq`,
 291 the non-deterministic semantics is reflected in the logic through the following specification:

```
Lemma physeq_spec v1 v2 :
  {{{ True }}}
  v1 == v2
  {{{ b, RET #b; ⌈(if b then val_physeq else val_physneq) v1 v2⌋ }}}
Proof. ... Qed.
```

292 The OCAML manual documents a partial specification for physical equality, which is
 293 precise for basic types such as references, but does not clearly extend to structured values
 294 containing a mix of immutable and mutable constructors. The only guarantee that it provides
 295 for all values is: if two values are physically equal, they are also structurally equal. This
 296 means we don't learn anything when two values are physically distinct.

297 In the following, we will explore both cases, looking at the optimizations that the compiler
 298 or the runtime system may perform. We will show that the aforementioned guarantee is
 299 arguably not sufficient to verify interesting concurrent programs and attempt to establish
 300 stronger guarantees.

301

5.3 When physical equality returns `true`

302 Let us go back to the concurrent stack of Figure 2 and more specifically the `push` function. To
 303 prove the atomic specification given in Section 3, we rely on the fact that, if `Atomic.compare_and_set`
 304 returns `true`, we actually observe the same list of values in the sense of ROCQ equality.
 305 However, assuming only structural equality as per OCAML's specification of physical equality,
 306 this cannot be proven. To see why, consider, *e.g.*, a stack of references (`'a ref`). As structural
 307 equality is indeed *structural*, it traverses the references without comparing their *physical*
 308 *identities*. In other words, we cannot conclude the references are *exactly* the same. Hence,
 309 we cannot prove the specification.

310 This conclusion might seem surprising and counterintuitive. Indeed, we know that physical
 311 equality essentially boils down to a comparison instruction, so we should be able to say
 312 more. Departing from OCAML's imprecise specification, let us attempt to establish stronger
 313 guarantees. We assume the following classification of values: booleans, integers, mutable
 314 blocks (pointers), immutable blocks, functions.

The easy cases are mutable blocks and functions. Each of these two classes is disjoint from the others. We can reasonably assume that, when physical equality returns `true` and one of the compared values belongs to either of these classes, the two values are actually the same in ROCQ. As far as we are aware, there is no optimization that could break this.

Booleans, integers and empty immutable blocks are represented by immediate integers through an encoding. This encoding induces conflicts: two seemingly distinct values in ROCQ may have the same encoding. For example, the following tests all return `true` (`Obj.repr` is an unsafe primitive revealing the memory representation of a value):

```
let test1 = Obj.repr false == Obj.repr 0 (* true *)
let test2 = Obj.repr None == Obj.repr 0 (* true *)
let test3 = Obj.repr [] == Obj.repr 0 (* true *)
```

The semantics of unrestricted physical equality has to reflect these conflicts. In our experience, restricting compared values similarly to typing is quite burdensome; the specification of polymorphic data structures using physical equality has to be systematically restricted. In summary, when physical equality on immediate values returns `true`, it is guaranteed that they have the same encoding.

Finally, let us consider the case of non-empty immutable blocks. At runtime, they are represented by pointers to tagged memory blocks. At first approximation, it is tempting to say that physically equal immutable blocks really are the same in ROCQ. Alas, this is not true. To explain why, we have to recall that the OCAML compiler and the runtime system (*e.g.*, through hash-consing) may perform *sharing*: immutable blocks containing physically equal fields may be shared. For example, the following tests may return `true`:

```
let test1 = Some 0 == Some 0 (* true *)
let test2 = [0;1] == [0;1] (* true *)
```

On its own, sharing is not a problem. However, coupled with representation conflicts, it can be surprising. Indeed, consider the `any` type defined as:

```
type any = Any : 'a -> any
```

The following tests may return `true`:

```
let test1 = Any false == Any 0 (* true *)
let test2 = Any None == Any 0 (* true *)
let test3 = Any [] == Any 0 (* true *)
```

Now, going back to the `push` function of Figure 2, we have a problem. Given a stack of `any`, it is possible for the `Atomic.compare_and_set` to observe a current list (*e.g.*, `[Any 0]`) physically equal to the expected list (*e.g.*, `[Any false]`) while these are actually distinct in ROCQ. In short, the expected specification of Section 3 is incorrect. To fix it, we would need to reason *modulo physically equality*, which is non-standard and quite burdensome.

We believe this really is a shortcoming, at least from the verification perspective. Therefore, we propose to extend OCAML with *generative immutable blocks*⁶. These generative blocks are just like regular immutable blocks, except they cannot be shared. Hence, if physical equality on two generative blocks returns `true`, these blocks are necessarily equal in ROCQ. At user level, this notion is materialized by *generative constructors*. For instance, to verify the expected `push` specification, we can use a generative version of lists:

```
type 'a list =
  | Nil
  | Cons of 'a * 'a list [@@generative]
```

⁶ Non-anonymous link

```

type state =
  | Open of Unix.file_descr
  | Closing of (unit -> unit)

type t =
  { mutable ops: int [@atomic];
    mutable state: state [@atomic]; }

let make fd = { ops = 0; state = Open fd }

let closed = Closing (fun () -> ())
let close t =
  match t.state with
  | Closing _ -> false
  | Open fd as prev ->
    let next = Closing (fun () -> Unix.close fd) in
    if Atomic.Loc.compare_and_set [%atomic.loc t.state] prev next then (
      if t.ops == 0
      && Atomic.Loc.compare_and_set [%atomic.loc t.state] next closed
      then close () ;
      true
    ) else false

```

■ Figure 3 Rcfid module from Eio [36] (excerpt)

348 5.4 When physical equality returns false

349 The informal OCAML specification does not give any guarantee when physical equality
 350 returns **false**. In most cases, including try loops, this is fine. However, in some specific
 351 cases, more information is needed.

352 Consider the **Rcfid** module from the Eio [36] library, an excerpt of which is given in
 353 Figure 3⁷. Thomas Leonard, its author, suggested that we verify this real-life example
 354 because of its intricate logical state. However, we found out that it is also relevant regarding
 355 the semantics of physical equality. Essentially, it consists in wrapping a file descriptor in
 356 a thread-safe way using reference-counting. At creation in the **make** function, the wrapper
 357 starts in the **Open** state. At some point, it can switch to the **Closing** state in the **close**
 358 function and can never go back to the **Open** state. Crucially, the **Open** state does not change
 359 throughout the lifetime of the data structure.

360 The interest of **Rcfid** lies in the **close** function. First, the function reads the state. If
 361 this state is **Closing**, it returns **false**; the wrapper has been closed. If this state is **Open**, it
 362 tries to switch to the **Closing** state using **Atomic.Loc.compare_and_set**; if this attempt
 363 fails, it also returns **false**. In this particular case, we would like to prove that the wrapper
 364 has been closed, or equivalently that **Atomic.Loc.compare_and_set** cannot have observed
 365 **Open**. Intuitively, this is true because there is only one **Open**.

366 Obviously, we need some kind of guarantee related to the *physical identity* of **Open** when
 367 **Atomic.Loc.compare_and_set** returns **false**. If **Open** were a mutable block, we could argue

⁷ We make use of *atomic record fields* as introduced in Section 7.1.

that this block cannot be physically distinct from itself; no optimization we know of would allow that. Unfortunately, it is an immutable block, and immutable blocks are subject to more optimizations. In fact, something surprising but allowed⁸ by OCAML can happen: *unsharing*, the dual of sharing. Indeed, any immutable block can be unshared, that is reallocated. For example, the following test may theoretically return `false`:

```
let x = Some 0
let test = x == x (* false *)
```

Going back to `Rcfd`, we have a problem: in the second branch, the `Open` block corresponding to `prev` could be unshared, which would make `Atomic.Loc.compare_and_set` fail. Hence, we cannot prove the expected specification.

To remedy this unfortunate situation, we propose to reuse the notions of generative immutable blocks, that we introduced to prevent sharing, to also forbid unsharing. More precisely, each generative block is annotated with a *logical identifier*⁹ representing its physical identity, much like a pointer for a mutable block. If physical equality on two generative blocks returns `false`, the two identifiers are necessarily distinct. Given this semantics, we can verify the `close` function. Indeed, if `Atomic.Loc.compare_and_set` fails, we now know that the identifiers of the two blocks, if any, are distinct. As there is only one `Open` block whose identifier does not change, it cannot be the case that the current state is `Open`, hence it is `Closing` and we can conclude. In practice, it suffices to patch the `state` type:

```
type state =
  | Open of Unix.file_descr [@@generative]
  | Closing of (unit -> unit)
```

6 Structural equality

Structural equality is also supported. More precisely, it is not part of the semantics of the language but axiomatized on top of it¹⁰. The reason is that it is in fact difficult to specify for arbitrary values. In general, we have to compare graphs—which implies structural comparison may diverge.

Accordingly, the specification of $v_1 = v_2$ requires the (partial) ownership of a *memory footprint* corresponding to the union of the two compared graphs, giving the permission to traverse them safely. If it terminates, the comparison decides whether the two graphs are isomorphic (modulo representation conflicts, as described in Section 5). In IRIS, this gives:

```
Axiom structeq_spec : ∀ v1 v2 footprint,
  val_traversable footprint v1 →
  val_traversable footprint v2 →
  {{{ structeq_footprint footprint }}}
  v1 = v2
  {{{ b, RET #b;
    structeq_footprint footprint *
    ⌈(if b then val_structeq else val_structneq) footprint v1 v2⌋ }}}.
```

Obviously, this general specification is not very convenient to work with. Fortunately, for abstract values (without any mutable part), we can prove a much simpler variant saying that structural equality boils down to physical equality:

⁸ This has been confirmed by OCAML experts developing the FLAMBDA backend.

⁹ Actually, for practical reasons, we distinguish identified and unidentified generative blocks.

¹⁰ We could also have implemented it in ZOOLANG, but that would require more low-level primitives.

```

Lemma structeq_spec_abstract v1 v2 :
  val_abstract v1 →
  val_abstract v2 →
  {{{ True }}}
  v1 = v2
  {{{ b, RET #b; ⌈(if b then val_physeq else val_physneq) v1 v2⌋ }}}
Proof. ... Qed.

```

7 OCaml extensions for fine-grained concurrent programming

Over the course of this work, we studied efficient fine-grained concurrent OCAML programs written by experts. This revealed various limitations of OCAML in these domains, that those experts would work around using unsafe casts, often at the cost of both readability and memory-safety; and also some mismatches between their mental model of the semantics of OCAML and the mental model used by the OCAML compiler authors. We worked on improving OCAML itself to reduce these work-arounds or semantic mismatches.

7.1 Atomic record fields

OCAML 5 offers a type `'a Atomic.t` of atomic references exposing sequentially-consistent atomic operations. Data races on non-atomic mutable locations has a much weaker semantics and is generally considered a programming error. For example, the Michael-Scott concurrent queue [39] relies on a linked list structure that could be defined as follows:

```
type 'a node = Nil | Cons of { value : 'a; next : 'a node Atomic.t }
```

Performance-minded concurrency experts dislike this representation, because `'a Atomic.t` introduces an indirection in memory: it is represented as a pointer to a block containing the value of type `'a`. Instead, they use something like the following:

```

type 'a node = Nil | Cons of { mutable next: 'a node; value: 'a }
let as_atomic : 'a node -> 'a node Atomic.t option = function
  | Nil -> None
  | (Next _) as record -> Some (Obj.magic record : 'a node Atomic.t)

```

Notice that the `next` field of the `Cons` constructor has been moved first in the type declaration. Because the OCAML compiler respects field-declaration order in data layout, a value `Cons { next; value }` has a similar low-level representation to a reference (atomic or not) pointing at `next`, with an extra argument. The code uses `Obj.magic` to unsafely cast this value to an atomic reference, which appears to work as intended.

`Obj.magic` is a shunned unsafe cast (the OCAML equivalent of `unsafe` or `unsafePerformIO`). It is very difficult to be confident about its usage given that it may typically violate assumptions made by the OCAML compiler and optimizer. In the example above, casting a two-fields record into a one-argument atomic reference may or may not be sound—but it gives measurable performance improvements on concurrent queue benchmarks. (TODO: benchmark to quantify the improvement.)

It is possible to statically forbid passing `Nil` to `as_atomic` to avoid error handling, by turning `'a node` into a GADT indexed over it a type-level representation of its head constructor. Examples of this pattern can be found in the `Kcas` [31] library by Vesa Karvonen. It is difficult to write correctly and use, in particular as unsafe casts can sometimes hide type-errors in the intended static discipline.

Note that this unsafe approach only works for the first field of a record, so it is not applicable to records that hold several atomic fields, such as the toplevel record storing

430 atomic front and back pointers for the concurrent queue.

431 7.1.1 Our atomic fields proposal

432 We proposed a design for atomic record fields as an OCAML language change proposal:
 433 RFC #39¹¹. Declaring a record field atomic simply requires an `[@atomic]` attribute—and
 434 could eventually become a proper keyword of the language.

```
(* re-implementation of atomic references *)
type 'a atomic_ref = { mutable contents : 'a [@atomic]; }

(* concurrent linked list *)
type 'a node = Nil | Cons of { value: 'a; mutable next : 'a node [@atomic]; }

(* bounded SPSC circular buffer *)
type 'a bag =
  { data : 'a Atomic.t array;
    mutable front: int [@atomic];
    mutable back: int [@atomic]; }
```

435 The design difficulty is to express atomic operations on atomic record fields. For example,
 436 if `buf` has type `'a bag` above, then one naturally expects the existing notation `buf.front` to
 437 perform an atomic read and `buf.front <- n` to perform an atomic write. But how would
 438 one express exchange, compare-and-set and fetch-and-add? We would like to avoid adding a
 439 new primitive language construct for each atomic operation.

440 Our proposed implementation¹² introduces a built-in type `'a Atomic.Loc.t` for an atomic
 441 location that holds an element of type `'a`, with a syntax extension `[%atomic.loc <expr>.<field>]`
 442 to construct such locations. Atomic primitives operate on values of type `'a Atomic.Loc.t`,
 443 and they are exposed as functions of the module `Atomic.Loc`.

444 For example, the standard library exposes

```
val Atomic.Loc.fetch_and_add : int Atomic.Loc.t -> int -> int
```

445 and users can write:

```
let preincrement_front (buf : 'a bag) : int =
  Atomic.Loc.fetch_and_add [%atomic.loc buf.front] 1
```

446 where `[%atomic.loc buf.front]` has type `int Atomic.Loc.t`. Internally, a value of type
 447 `'a Atomic.Loc.t` can be represented as a pair of a record and an integer offset for the
 448 desired field, and the `atomic.loc` construction builds this pair in a well-typed manner.
 449 When a primitive of the `Atomic.Loc` module is applied to an `atomic.loc` expression, the
 450 compiler can optimize away the construction of the pair—but it would happen if there was
 451 an abstraction barrier between the construction and its use.

452 Note: the type `'a Atomic.t` of atomic references exposes a function

```
val Atomic.make_contended : 'a -> 'a Atomic.t
```

453 that ensures that the returned atomic value is allocated with enough alignment and padding
 454 to sit alone on its cache line, to avoid performance issues caused by false sharing. Currently
 455 there is no such support for padding of atomic record fields (we are planning to work on this
 456 if the support for atomic fields gets merged in standard OCAML), so the less-compact atomic
 457 references remain preferable in certain scenarios.

¹¹Non-anonymous link

¹²Non-anonymous link

7.2 Atomic arrays

On top of our atomic record fields, we have implemented support for atomic arrays, another facility commonly requested by authors of efficient concurrent programs. Our previous example of a concurrent bag of type `'a bag` used a backing array of type `'a Atomic.t array`, which contains more indirections than may be desirable, as each array element is a pointer to a block containing the value of type `'a`, instead of storing the value of type `'a` directly in the array.

Our implementation of atomic arrays¹³ builds on top of the type `'a Atomic.Loc.t` we described in the previous section, and it relies on two new low-level primitives provided by the compiler:

```
val Atomic_array.index : 'a array -> int -> 'a Atomic.Loc.t
val Atomic_array.unsafe_index : 'a array -> int -> 'a Atomic.Loc.t
```

The function `index` takes an array and an integer index within the array, and returns an atomic location into the corresponding element after performing a bound check. `unsafe_index` omits the boundcheck—additional performance at the cost of memory-safety—and allows to express the atomic counterpart of the unsafe operations `Array.unsafe_get` and `Array.unsafe_set`. The atomic primitives of the module `Atomic.Loc` can then be used on these indices; our implementation implements a library module on top of these primitives to provide a higher-level layer to the user, with direct array operations such as:

```
val Atomic_array.exchange : 'a Atomic_array.t -> int -> 'a -> 'a
val Atomic_array.unsafe_exchange : 'a Atomic_array.t -> int -> 'a -> 'a
```

8 Conclusion and future work

We presented ZOO, a framework for the verification of concurrent OCAML 5 programs. While it is not yet available on `opam`, it can be installed and used in other ROCQ projects. We provide a minimal example¹⁴ demonstrating its use.

ZOO has already been used to verify sequential imperative algorithms [anonymous] and is currently being used to verify a library of lock-free data structures. Its main weakness so far is its memory model, which is sequentially consistent as opposed to the relaxed OCAML 5 memory model. It also lacks exceptions and algebraic effects, that we plan to introduce in the future.

Another interesting direction would be to combine ZOO with semi-automated techniques. Similarly to WHY3, the simple parts of the verification effort would be done in a semi-automated way, while the most difficult parts would be conducted in ROCQ.

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