

Core Course Preview

Introduction to Model Checking

<https://clegra.github.io/mc/mc.html>

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December 11, 2025

Model Checking

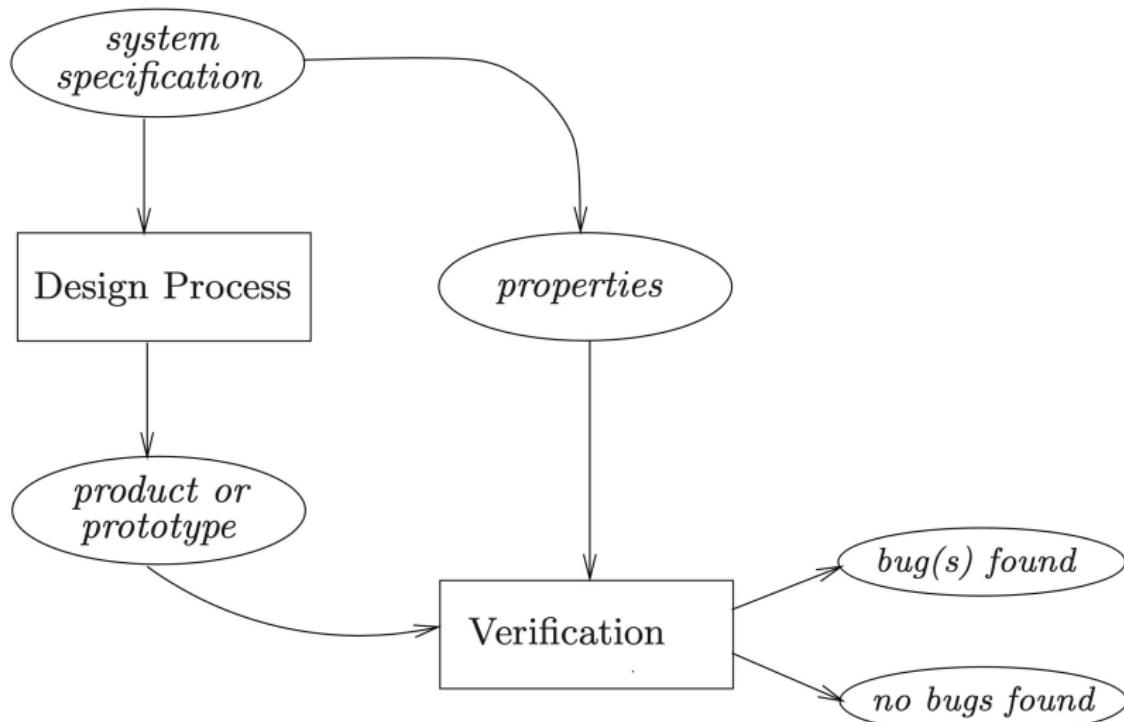
... is an effective automatable technique:

- ▶ *to expose potential software design errors;*
- ▶ *that, given a finite-state model of a system and a formal property, systematically checks whether this property holds for that model.*

Strengths:

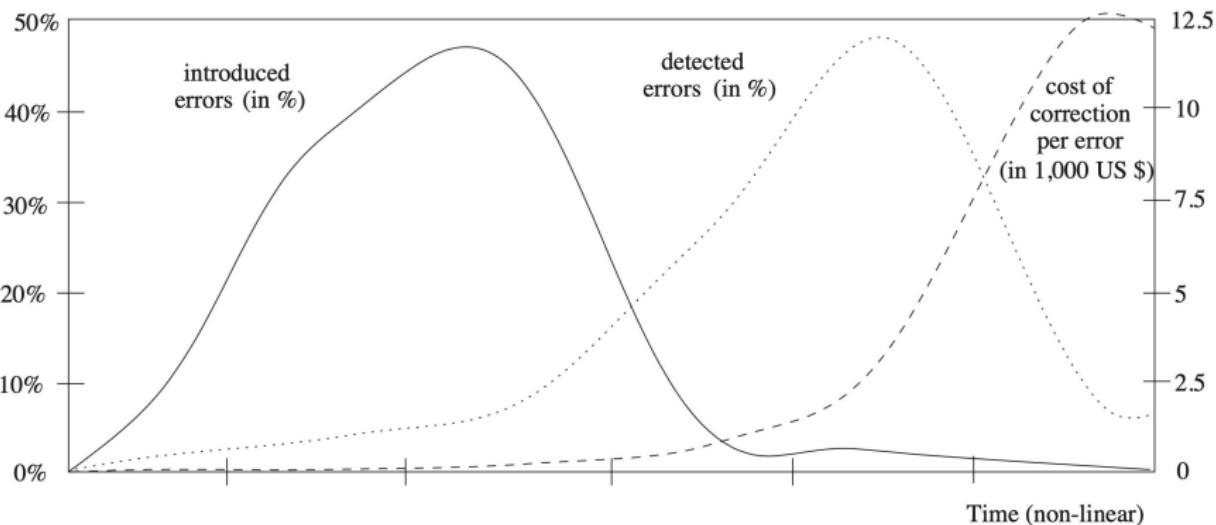
- ▶ widely applied in industry
 - for: embedded systems, software engineering, hardware design, explainable AI
- ▶ supports **partial verification** (of system parts)
- ▶ provides **diagnostic information** for debugging
- ▶ has sound **mathematical underpinning** (**logic** and **process theory**)

Hard-/Software Verification (traditionally)

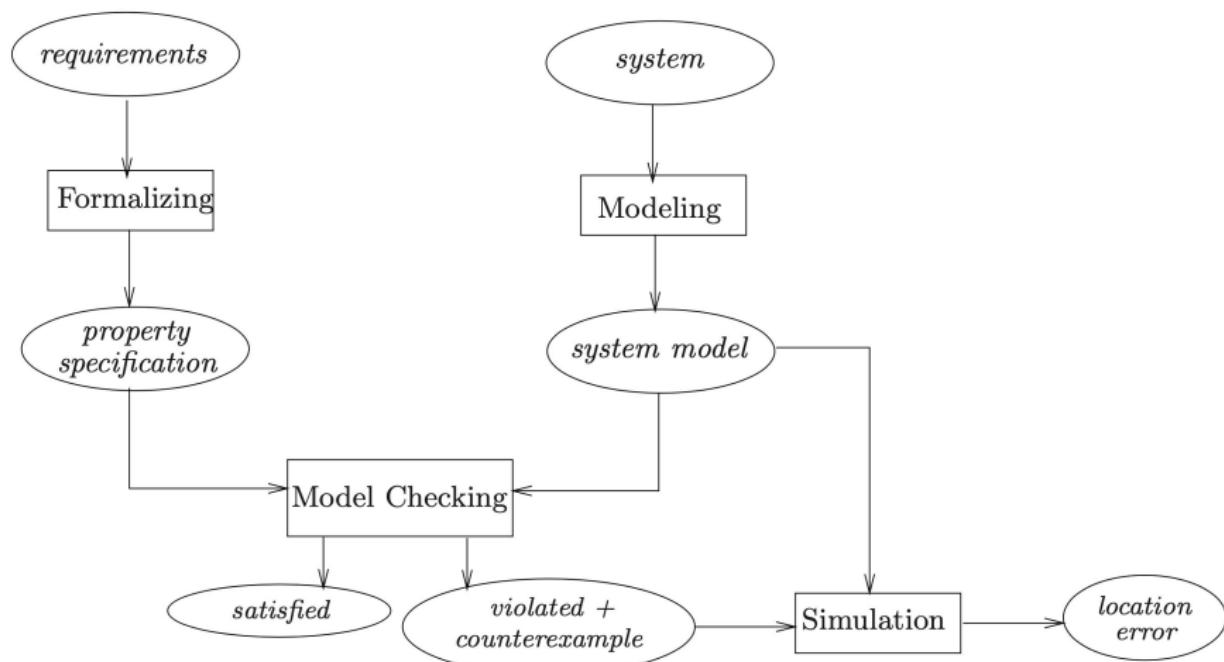


Error introduction, detection, and repair costs

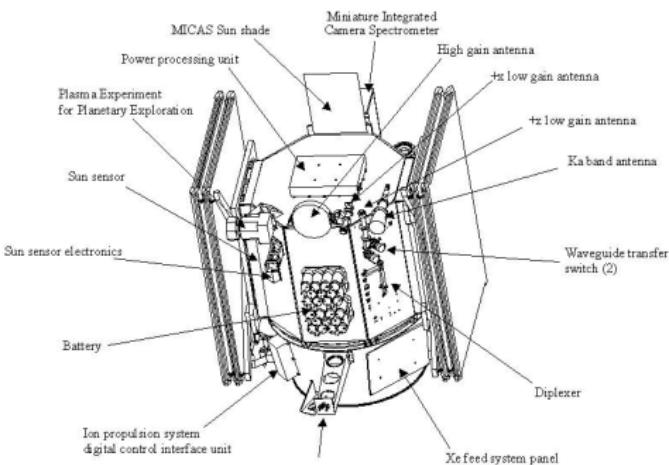
Analysis	Conceptual Design	Programming	Unit Testing	System Testing	Operation
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Model checking



Deep Space 1



- ▶ Flyby of asteroid 9969 Braille (1999)
- ▶ Entered the coma of Comet Borrelly (2001)
- ▶ Model checking discovered 5 concurrency errors

Example (program concurrency/non-determinism)

Programs `Inc`, `Dec`, and `Reset` cooperate, and use a shared variable x :

```
proc Inc
  while true
    do
      if x < 200
        then x := x + 1
      fi
    od
```

```
proc Dec
  while true
    do
      if x > 0
        then x := x - 1
      fi
    od
```

```
proc Reset
  while true
    do
      if x = 200
        then x := 0
      fi
    od
```

Example (program concurrency/non-determinism)

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```
proc Reset
  while true
    do
      if x = 200
        then x := 0
      fi
    od
```

Question: Is $0 \leq x \leq 200$ always guaranteed?

Modeling (by labeled transition systems)

proc Inc

while true

do

if $x < 200$

then $x := x + 1$

fi

od

proc Dec

while true

do

if $x > 0$

then $x := x - 1$

fi

od

proc Reset

while true

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if $x = 200$

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Modeling (by labeled transition systems)

proc Inc

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1: **if** $x < 200$

2: **then** $x := x + 1$

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while true

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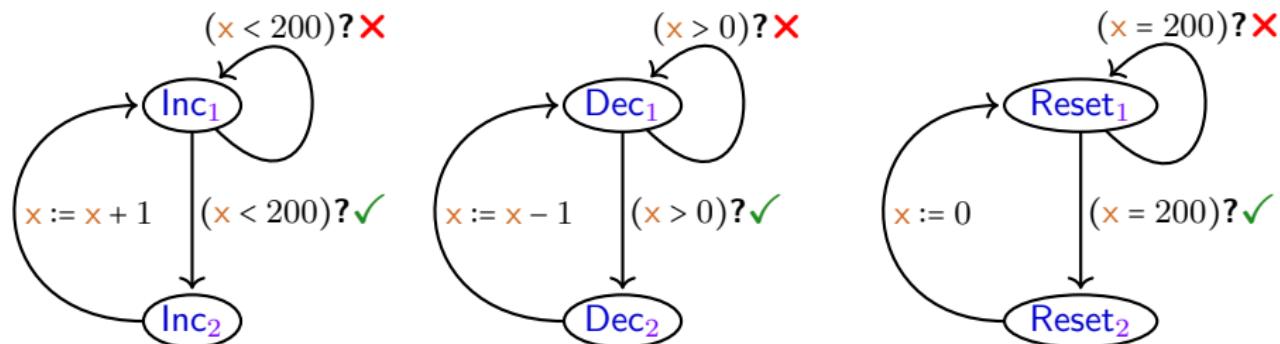
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2: **then** $x := 0$

fi

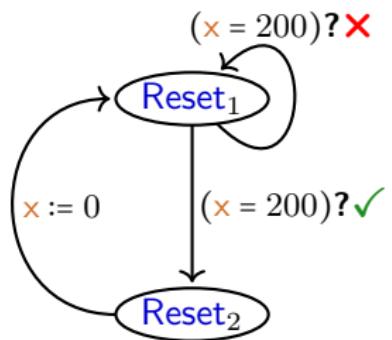
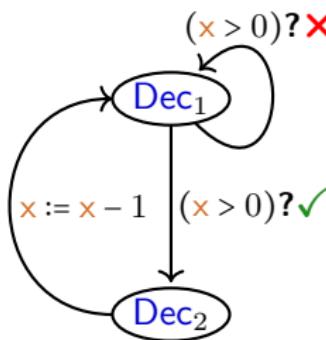
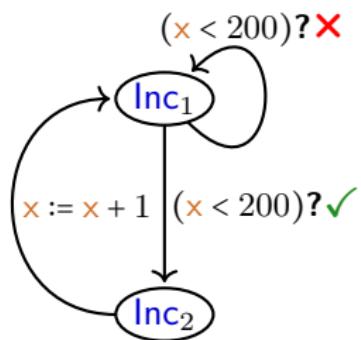
od

Modeling (by labeled transition systems)

proc Inc**while true****do**1: **if** $x < 200$ 2: **then** $x := x + 1$ **fi****od****proc Dec****while true****do**1: **if** $x > 0$ 2: **then** $x := x - 1$ **fi****od****proc Reset****while true****do**1: **if** $x = 200$ 2: **then** $x := 0$ **fi****od**

Labeled transition systems (LTSs)

Formalizing properties (in temporal logic)



$$\text{Inc}_1 \parallel \text{Dec}_1 \parallel \text{Reset}_1 \stackrel{?}{\models} \square(0 \leq x \wedge x \leq 200) \quad (\text{Linear-TL formula})$$

Counterexample (offending execution trace)

$$\langle x = 199 ; \text{Inc}_1 \parallel \text{Dec}_1 \parallel \text{Reset}_1 \rangle$$

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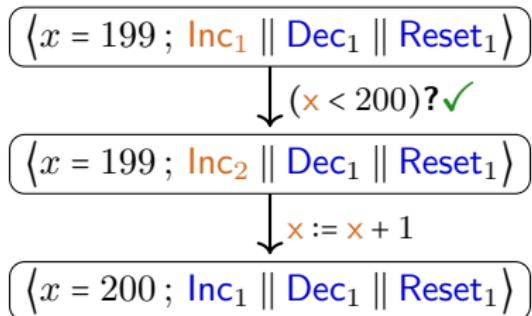
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$$\begin{array}{c} \boxed{\langle x = 199 ; \text{Inc}_1 \parallel \text{Dec}_1 \parallel \text{Reset}_1 \rangle} \\ \downarrow (\text{x} < 200)? \checkmark \\ \boxed{\langle x = 199 ; \text{Inc}_2 \parallel \text{Dec}_1 \parallel \text{Reset}_1 \rangle} \end{array}$$

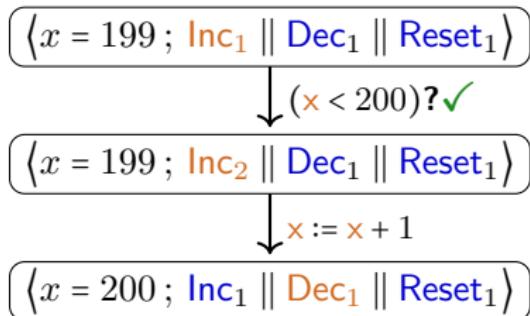
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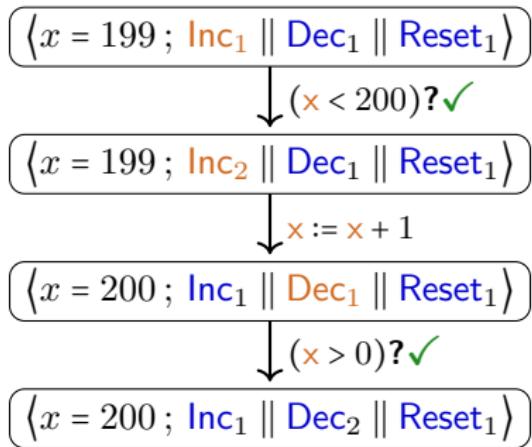
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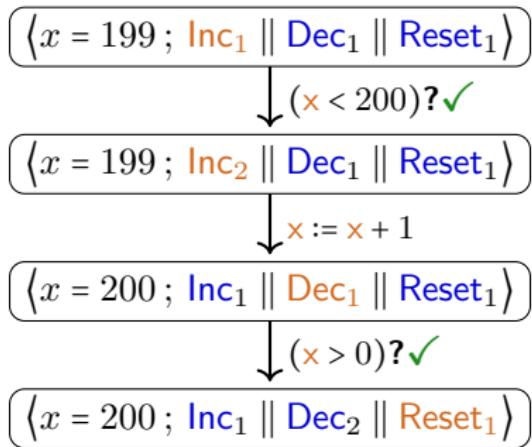
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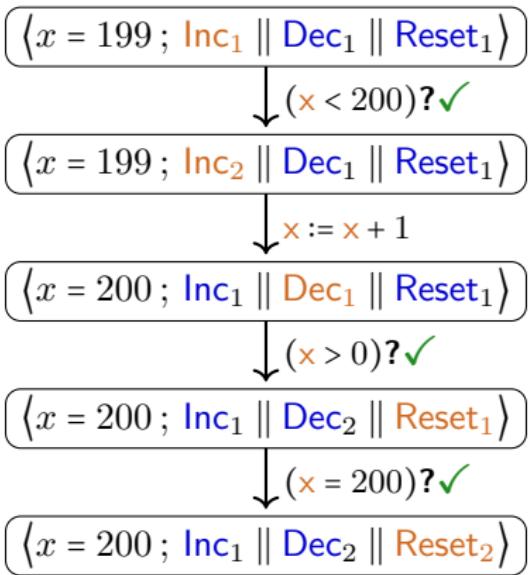
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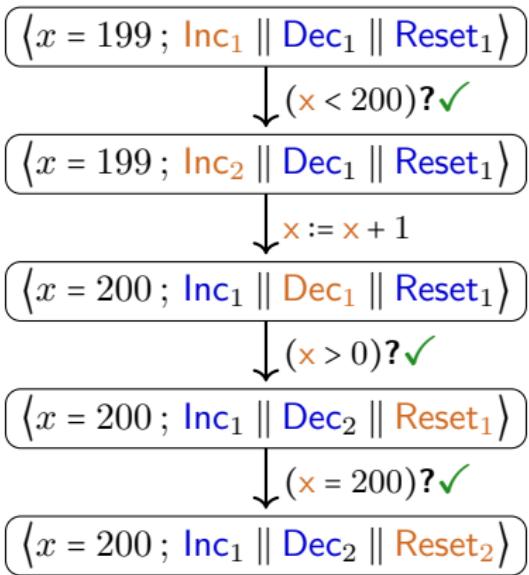
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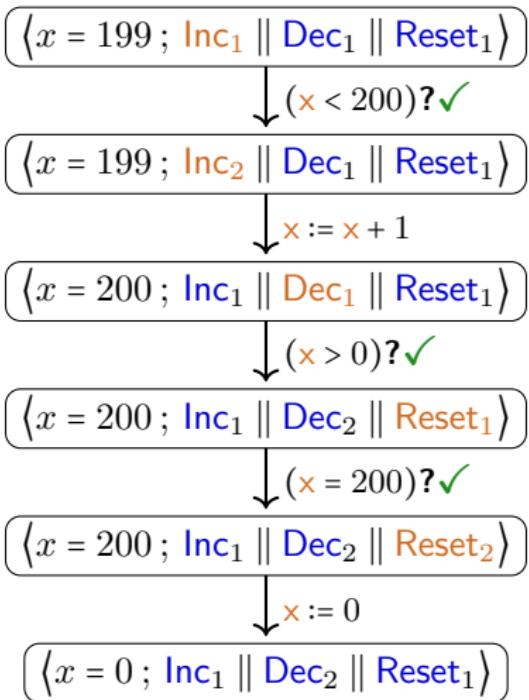
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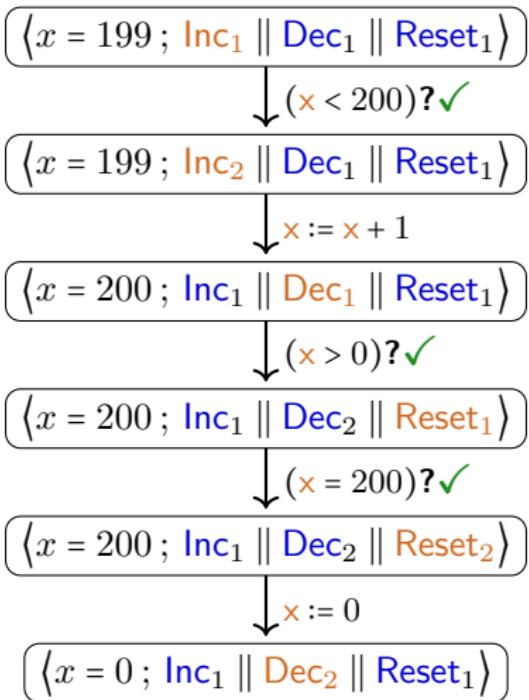
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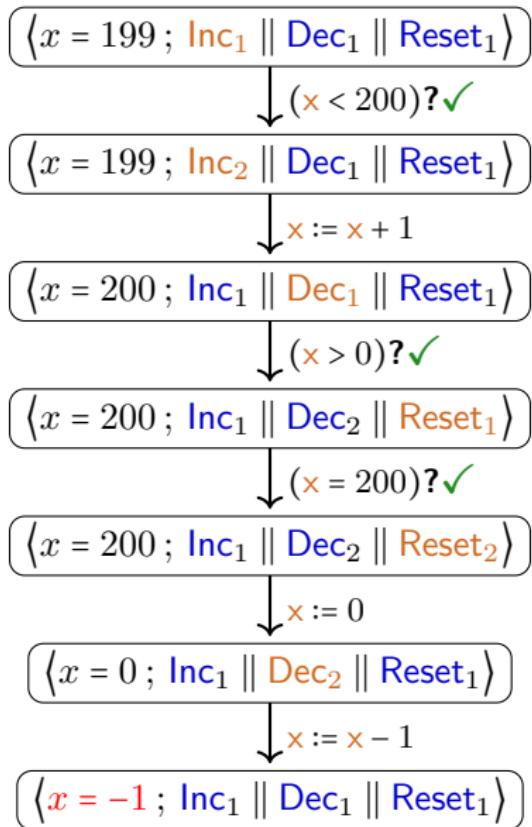
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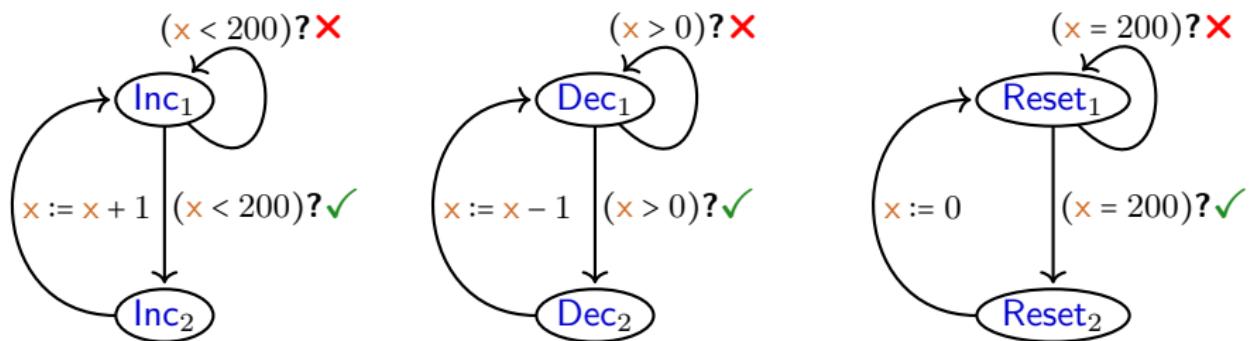
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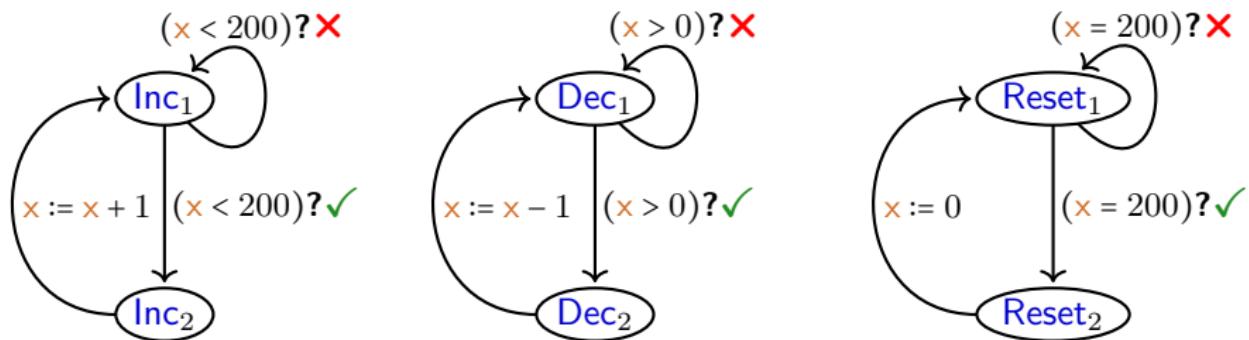


Formalizing properties (in temporal logic)



$\text{Inc}_1 \parallel \text{Dec}_1 \parallel \text{Reset}_1 \neq \square(0 \leq x \wedge x \leq 200)$ (Linear-TL formula)

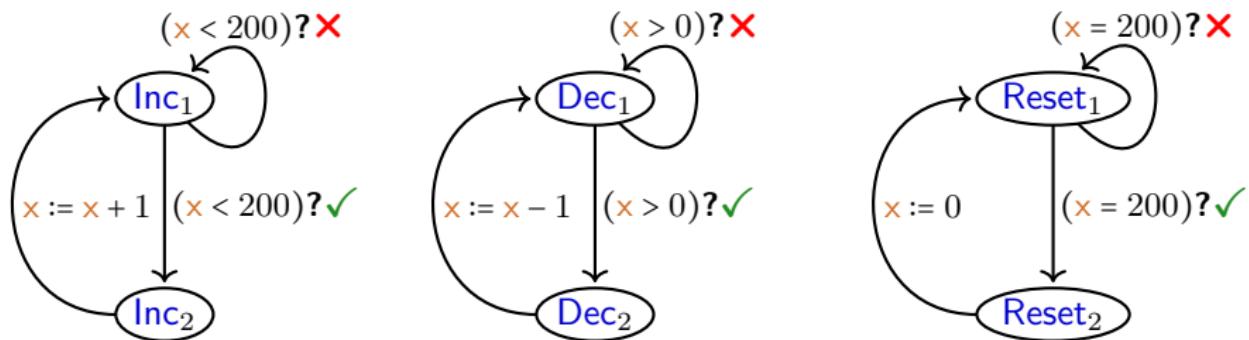
Formalizing properties (in temporal logic)



$\text{Inc}_1 \parallel \text{Dec}_1 \parallel \text{Reset}_1 \not\models \Box(0 \leq x \wedge x \leq 200)$ (Linear-TL formula)

$\text{Inc}_1 \parallel \text{Dec}_1 \parallel \text{Reset}_1 \models \Diamond(x < 0)$ (LTL formula)

Formalizing properties (in temporal logic)



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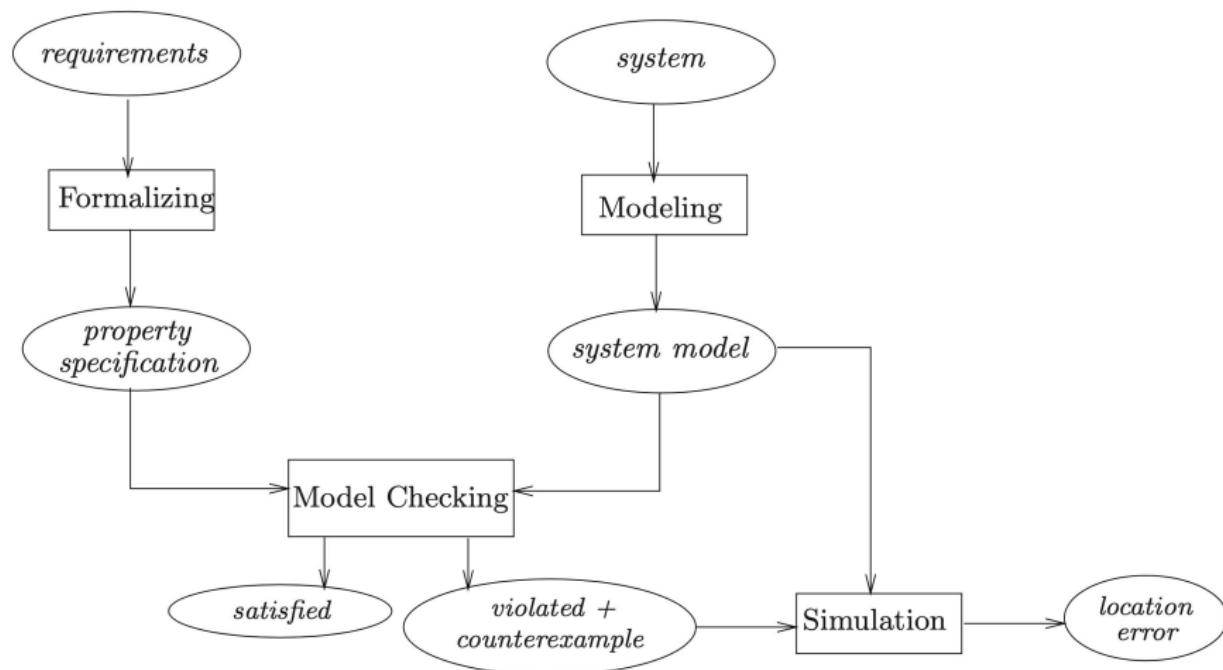
$\text{Inc}_1 \parallel \text{Dec}_1 \parallel \text{Reset}_1 \models \Diamond(x < 0)$ (LTL formula)

$\text{Inc}_1 \parallel \text{Dec}_1 \parallel \text{Reset}_1 \not\models \forall \Box(0 \leq x \wedge x \leq 200)$ (Computation-Tree-L formula)

$\text{Inc}_1 \parallel \text{Dec}_1 \parallel \text{Reset}_1 \models \exists \Box(0 \leq x \wedge x \leq 200)$ (CTL formula)

$\text{Inc}_1 \parallel \text{Dec}_1 \parallel \text{Reset}_1 \models \forall \Box \exists \Diamond(x < 0)$ (CTL formula)

Model checking

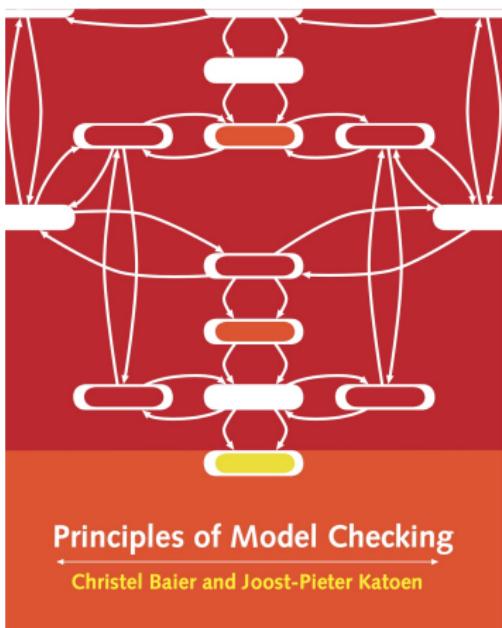


Any [such] verification is only as good as the model of the system.

Topics of the course

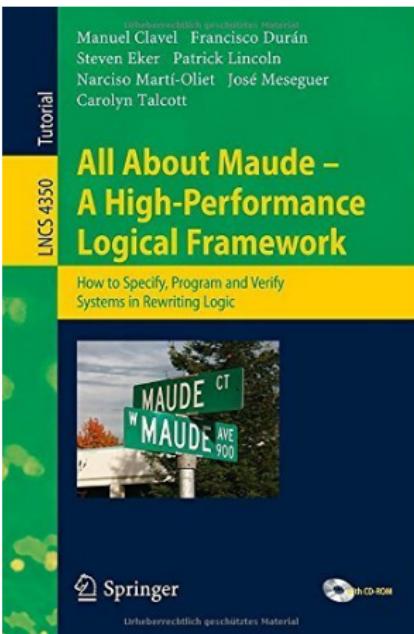
- ▶ modeling systems by labeled transition systems (LTSs)
- ▶ fairness
- ▶ Linear Temporal Logic (LTL)
 - ▶ model checking formulas
 - ▶ express properties by Büchi automata
 - ▶ model check LTSs and properties via product automata
- ▶ Computation Tree Logic (CTL)
- ▶ partial model checking
 - ▶ partially known systems (state properties/states/transitions)
- ▶ analysing system behavior with the Maude model-checker

Book



- ▶ pdf available:
https://is.ifmo.ru/books/_principles_of_model_checking.pdf

Book Maude



- ▶ pdf available:

<https://maude.cs.illinois.edu/w/images/0/0d/Maude-book.pdf>

Organization

Lectures (Emilio 3 / Clemens 4)

- ▶ presentations on blackboard
- ▶ notes after the lecture (notes 2025/26 available)
- ▶ January 19–January 28 (7 lectures)

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Exam

- ▶ options:
 - ▶ small verification project (of an algorithm, e.g. in [MaudE3](#))
 - ▶ presentation about a paper
 - ▶ written exam?

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Thank you – we are looking forward to the course!