

Py2: Bases of programming in Python

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General comments

Assignments. How did it go?

Please try to pass homework exercises during tutorials, as much as possible!

Plan. 0. Feedback on last week's exercises

1. Built-in data structures

2. Loop and notions of algorithmic complexity

3. Functions

Books.

A Whirlwind Tour of Python, by Jake VanderPlas (O'Reilly). Available online [here](#).

0 -

This week's exercises

This week's exercises

H1: Information [here](#)

on how floating point numbers are encoded and on subnormal number

H3: Be careful with the units! Advices:

- write down units as comments near the definition of variables and near the functions
- Check unites quantities, try to use appropriate units
- defines intermediate variables

Scientific notations:

- powers of 10? $1.5e4$
- Print with scientific notation: —> see Tips section of "Py1_Lab"

H3: precision limit!

- $1 + u^2 = 1 + 1e-32$
- > what happens? How can you still compute the difference in Dx?

Sqrt with complex type: `cmath.sqrt()`

Part 1

Built-in Data Structure

List, Tuple, Dictionary, Set

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Type Name	Example	Description
list	[1, 2, 3]	Ordered collection
tuple	(1, 2, 3)	Immutable ordered collection
dict	{'a':1, 'b':2, 'c':3}	Unordered (key,value) mapping
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ordered Access the element by indexing / slicing

Immutable Element can't be changed

Lists

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List: **ordered** and **mutable** collection of objects.

```
# define a list:  
fruits = ['orange', 'apple', 'pear', 'banana', 'kiwi', 'apple', 'banana']
```

Mixed types

```
# Example of a list mixing types:  
L = [1, 'two', 3.14, [0, 3, 5]]
```

Lists

Type Name	Example	Description
list	[1, 2, 3]	Ordered collection
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List: **ordered** and **mutable** collection of objects.

```
# define a list:  
fruits = ['orange', 'apple', 'pear', 'banana', 'kiwi', 'apple', 'banana']
```

Indexing

```
# Indexing: access an element:  
print(fruits[4])
```

Access an element:

Lists

Type Name	Example	Description
list	[1, 2, 3]	Ordered collection
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```
# define a list:  
fruits = ['orange', 'apple', 'pear', 'banana', 'kiwi', 'apple', 'banana']  
0 1 2 3 4 5 6
```

Indexing

Access an element:

```
kiwi
```

```
# Indexing: access an element:  
print(fruits[4])
```

Lists

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# define a list:  
fruits = ['orange', 'apple', 'pear', 'banana', 'kiwi', 'apple', 'banana']  
0 1 2 3 4 5 6
```

Indexing

```
# Indexing: access an element:  
print(fruits[-1])
```

Access an element:

Lists

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# define a list:
fruits = ['orange', 'apple', 'pear', 'banana', 'kiwi', 'apple', 'banana']

      0      1      2      3      4      5      6
      -7     -6     -5     -4     -3     -2     -1
```

```
# Indexing: access an element:
print(fruits[-1])
```

Access an element:

banana

Indexing

Lists

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```

```
# Indexing: access an element:
print(fruits[4])
print(fruits[-1])
```

Modify an element:

```
# Modify an element via indexing:
fruits[0]='ananas'
```

Indexing

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# define a list:
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      0      1      2      3      4      5      6
      -7     -6     -5     -4     -3     -2     -1
```

```
# Indexing: access an element:
print(fruits[4])
print(fruits[-1])
```

```
# Modify an element via indexing:
fruits[0]='ananas'
```

```
# Slicing: access several elements:
fruits[2:5]
```

Access several elements:

Slicing

Lists

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```

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# Indexing: access an element:
print(fruits[4])
print(fruits[-1])
```

```
# Modify an element via indexing:
fruits[0]='ananas'
```

```
# Slicing: access several elements:
fruits[2:5]           5 is excluded!
['pear', 'banana', 'kiwi']
```

Modify an element:

Slicing

Access several elements:

Lists

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# Modify an element via indexing:
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```
# Slicing: access several elements:
fruits[2:5]

['pear', 'banana', 'kiwi']

fruits[::-2]
```

Slicing

Access several elements:

```
['pear', 'banana', 'kiwi']

fruits[::-2]
```

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```
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fruits[0]='ananas'
```

```
# Slicing: access several elements:
fruits[2:5]
```

```
['pear', 'banana', 'kiwi']
```

```
fruits[::-2] # equivalent to fruits[0:len(fruits):2]
```

```
['orange', 'pear', 'kiwi', 'banana']
```

```
fruits[::-1]
```

```
['banana', 'apple', 'kiwi', 'banana', 'pear', 'apple', 'orange']
```

Indexing

Modify an element:

Slicing

Access several elements:

Lists

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# Slicing: access several elements:
fruits[2:5]
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```
# The addition '+' concatenates lists:
veggies = ['aubergine', 'carrot', 'potato']
fruits + veggies
```

Slicing

Operations

Lists

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fruits + veggies
```

```
# Check membership:
'carrot' in fruits
'carrot' not in fruits
```

Indexing

Modify an element:

Slicing

Operations

Membership

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fruits + veggies
```

```
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'carrot' not in fruits
```

```
# Count how many times the element 'apple' occurs in the fruits list:
fruits.count('apple')
```

>>> Q1

Modify an element:

Slicing

Operations

Membership

Methods

Lists — Summary

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List: **ordered** and **mutable** collection of objects.

```
# define a list:
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```

Mixed types

```
# Example of a list mixing types:
L = [1, 'two', 3.14, [0, 3, 5]]
```

Indexing

```
# Indexing: access an element:
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print(fruits[-1])
```

Modify an element:

```
# Modify an element via indexing:
fruits[0]='ananas'
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Slicing

```
# Slicing: access several elements:
fruits[2:5]
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Operations

```
# The addition '+' concatenates lists:
veggies = ['aubergine', 'carrot', 'potato']
fruits + veggies
```

Membership

```
# Check membership:
'carrot' in fruits
'carrot' not in fruits
```

Methods

```
# Count how many times the element 'apple' occurs in the fruits list:
fruits.count('apple')
```

Small exercise!

>>> Q3

Elements in a list are **Mutable**

Question: Can you guess and explain the outputs of the following statements:

```
x = [1, 10, 3, 4, 5, 6, 7, 8]  
y = x  
y[1] = 2
```

```
print(x)      ???
```

Small exercise!

>>> Q3

Question: Can you guess and explain the outputs of the following statements:

```
x = [1, 10, 3, 4, 5, 6, 7, 8]  
y = x  
y[1] = 2
```

```
print(x)      ???
```

```
[1, 2, 3, 4, 5, 6, 7, 8]
```

x points to a list of elements that are mutable

y points to the same list (y=x)

as the elements of a list are mutable y[1] modify the list where both x and y are pointing

Small exercise!

>>> Q3

Question: Can you guess and explain the outputs of the following statements:

```
x = [1, 10, 3, 4, 5, 6, 7, 8]  
y = x  
y[1] = 2
```

```
print(x)      ???
```

[1, 2, 3, 4, 5, 6, 7, 8]

```
x = 10  
y = x  
y = y + 20
```

```
print(x)      ???
```

Small exercise!

>>> Q3

Question: Can you guess and explain the outputs of the following statements:

```
x = [1, 10, 3, 4, 5, 6, 7, 8]  
y = x  
y[1] = 2
```

```
print(x)      ???
```

[1, 2, 3, 4, 5, 6, 7, 8]

```
x = 10  
y = x  
y = 20
```

```
print(x)      ???
```

10

x is a pointer to an immutable object (integer 10)
when doing y = x; y = 20; the value 10 in x is not changed;
instead a new object is created and y points to that new object

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Tuple: **ordered** and **immutable** collection of objects.

Tuples are similar to lists, main difference is that elements are immutable.

Immutable: this means that once a tuple is created, its size and content can't be changed anymore

```
# define a tuple:  
t = (1,2,3)
```

```
# like lists: access an element via indexing:  
t[0]
```

```
# Unlike lists: modifying a tuple is not allowed:  
t[2] = 5
```

TypeError: 'tuple' object does not support item assignment

```
# convert a tuple to a list:  
l=list(t)
```

>>> Q5

Tuple: example

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Tuple: **ordered** and **immutable** collection of objects.

Use of Tuples: a common use is in function that returns multiple values

Ex. `as_integer_ratio()`

is a method of float that returns a numerator and a denominator as a tuple

```
x = 0.125
x.as_integer_ratio()
```

(1, 8)

>>> Q7

Tuple: example

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Use of Tuples: a common use is in function that returns multiple values

Ex. `as_integer_ratio()`

is a method of float that returns a numerator and a denominator as a tuple

```
x = 0.125
x.as_integer_ratio()
```

(1, 8)

```
numerator, denominator = x.as_integer_ratio()
```

>>> Q7

Dictionary

Type Name	Example	Description
list	[1, 2, 3]	Ordered collection
tuple	(1, 2, 3)	Immutable ordered collection
dict	{'a':1, 'b':2, 'c':3}	Unordered (key,value) mapping
set	{1, 2, 3}	Unordered collection of unique values

Dictionary: collection of maps between keys and values.

Elements are of the form pairs of **key:value**.

Elements are not ordered; the value of any item can be access with the key.

```
# define a dictionary :
shopping = {'carrot': 10, 'mango': 3}

{'carrot': 10, 'mango': 3}
```

```
# access a value via the indexing syntax using the key:
shopping['mango']
```

3

```
# set a new value via the indexing syntax using the key:
shopping['mango'] = 6

{'carrot': 10, 'mango': 6}
```

```
# add a new item (pair key:value) via the indexing syntax:
shopping['orange'] = 5

{'carrot': 10, 'mango': 6, 'orange': 5}
```

```
# check membership: check if 'orange' is in shopping:
'orange' in shopping
```

True

Set

Type Name	Example	Description
list	[1, 2, 3]	Ordered collection
tuple	(1, 2, 3)	Immutable ordered collection
dict	{'a':1, 'b':2, 'c':3}	Unordered (key,value) mapping
set	{1, 2, 3}	Unordered collection of unique values

Set: Unordered collections of unique items.

As for sets in mathematics, you can perform operations such as union, intersection, difference, and symmetric difference.

```
# define two sets:  
primes = {2, 3, 5, 7}  
odds = set(range(1,10,2))
```

Set

Type Name	Example	Description
list	[1, 2, 3]	Ordered collection
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# define two sets:  
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{2, 3, 5, 7}  
{1, 3, 5, 7, 9}
```

```
primes | odds
```

Bitwise OR

Set

Type Name	Example	Description
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{2, 3, 5, 7}  
{1, 3, 5, 7, 9}
```

```
# union: union of the two sets, primes and odds:  
primes | odds  
  
{1, 2, 3, 5, 7, 9}
```

```
primes & odds
```

Bitwise OR

Bitwise AND

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{1, 3, 5, 7, 9}
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# union: union of the two sets, primes and odds:  
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{1, 2, 3, 5, 7, 9}
```

Bitwise OR

```
# intersection: items appearing in both set  
primes & odds  
  
{3, 5, 7}
```

Bitwise AND

```
# difference: items in odds but not in primes  
odds - primes
```

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{2, 3, 5, 7}  
{1, 3, 5, 7, 9}
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{1, 2, 3, 5, 7, 9}
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```
# intersection: items appearing in both set  
primes & odds  
  
{3, 5, 7}
```

```
odds - primes  
  
{1, 9}
```

>>> Q9

Bitwise OR

Bitwise AND

Part 2

Loops and algorithmic complexity

List, Tuple, Dictionary, Set

For Loop

Way to repeatedly execute the same code statement.

In python: `for` loop can iterate over any object that is *iterable*

Ex. `Lists, Strings, Tuples, Range, etc...`

```
# iteration over the characters of a string:  
for l in 'words':  
    print(l)
```

w
o
r
d
s

```
# iteration over the elements of a list:  
for word in ['cat', 'mouse', 'elephant']:  
    print(word, len(word))
```

cat 3
mouse 5
elephant 8

For Loop

Way to repeatedly execute the same code statement.

In python: `for` loop can iterate over any object that is *iterable*

Ex. Lists, Strings, Tuples, `Range`, etc...

Range object: generates a sequence of numbers.
syntax similar to slicing for lists.

By convention, exclude the last element:

```
for i in range(5,10):
    print(i, end=' ')
```

5 6 7 8 9

By convention, start from 0:

```
for i in range(10):
    print(i, end=' ') # print all on same line
```

0 1 2 3 4 5 6 7 8 9

By steps of 2:

```
list(range(0, 10, 2))
```

[0, 2, 4, 6, 8]

>>> Q10

while Loop

Iterates until some condition is met.

The argument of the `while` loop is evaluated as a boolean statement, and the loop is executed until the statement evaluates to `False`.

```
i = 0
while i < 10:
    print(i, end=' ')
    i += 1
```

0 1 2 3 4 5 6 7 8 9

break: comment

List comprehensions

Nice feature of Python that allows you to build list from loops in a compact way.

Ex.

```
L = []
for n in range(12):
    L.append(n ** 2)
L
```

```
[0, 1, 4, 9, 16, 25, 36, 49, 64, 81, 100, 121]
```

The list comprehension equivalent is:

```
[n ** 2 for n in range(12)]
```

```
[0, 1, 4, 9, 16, 25, 36, 49, 64, 81, 100, 121]
```

List comprehensions

Nice feature of Python, that allows you to build list from loops in a compact way.

Ex. **Multiple iterations:**

```
[(i, j) for i in range(2) for j in range(3)]
```

```
[(0, 0), (0, 1), (0, 2), (1, 0), (1, 1), (1, 2)]
```

List comprehensions

Nice feature of Python, that allows you to build list from loops in a compact way.

Ex. **Multiple iterations:**

```
[(i, j) for i in range(2) for j in range(3)]
```

```
[(0, 0), (0, 1), (0, 2), (1, 0), (1, 1), (1, 2)]
```

Note that the second for acts as the interior index:

```
L=[]
for i in range(2):
    for j in range(3):
        L.append((i,j))
```

```
[(0, 0), (0, 1), (0, 2), (1, 0), (1, 1), (1, 2)]
```

List comprehensions

Nice feature of Python, that allows you to build list from loops in a compact way.

Ex. **Conditionals on iterator:**

```
[i for i in range(20) if i % 3 > 0]
```

List comprehensions

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Ex. **Conditionals on iterator:**

```
[i for i in range(20) if i % 3 > 0]
```

```
[1, 2, 4, 5, 7, 8, 10, 11, 13, 14, 16, 17, 19]
```

Works for lists, sets, tuples, dictionaries

Functions

Way of creating more readable and reusable code.

Syntax: using `def`

Ex. function returning a list of the first N values of the Fibonacci sequence:

$$F_0 = 0, \quad F_1 = 1,$$
$$F_n = F_{n-1} + F_{n-2} \quad \text{for } n > 1.$$

```
def fibonacci(N):
    L = []
    a, b = 0, 1
    while len(L) < N:
        a, b = b, a + b
        L.append(a)
    return L

fibonacci(10)
```

[1, 1, 2, 3, 5, 8, 13, 21, 34, 55]

Algorithmic Complexity

Factoriel(n):

```
fact=1
for i in range(1,n+1):
    fact=fact*i
print(fact)
```

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O(n) simple operations

N_choose_K (N, K):

```
def NchooseK(N,K):
    result=1
    # intermediate prints:
    #print(N, 'choose 0 =', result)
    for k in range(K):
        # intermediate prints to observe what's happening during the loop:
        # These prints should be removed from the final function.
        result=(result*(N-k))//(k+1)
        #print(N, 'choose', k+1, '=', result)
    return(result)
```

Algorithmic Complexity

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    return(result)
```

O(K) simple operations

```
def NchooseK_bis(N,K):
    if K > N//2:
        return NchooseK(N,N-K)
    else:
        return NchooseK(N,K)
```

Algorithmic Complexity

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    return(result)
```

O(K) simple operations

```
def NchooseK_bis(N,K):
    if K > N//2:
        return NchooseK(N,N-K)
    else:
        return NchooseK(N,K)
```

min(K, N-K) simple operations

Int32 and int64

```
def factFn(n):
    fact=1
    for i in range(1,n+1):
        fact=fact*i
    return fact

import numpy as np
n=12

print("\n", factFn(n))
print(" 12!=", np.prod(np.arange(1,n+1, dtype='int32')))
print("2^31=", 2**31)

n=13
print("\n", factFn(n))
print(" 13!=", np.prod(np.arange(1,n+1, dtype='int32'),dtype='int32'))
print("2^31=", 2**31)
```

```
479001600
12!= 479001600
2^31= 2147483648
```

```
6227020800
13!= 1932053504
2^31= 2147483648
```