

# 50.039 – Theory and Practice of Deep learning

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Week 03

[The following notes are compiled from various sources such as textbooks, lecture materials, Web resources and are shared for academic purposes only, intended for use by students registered for a specific course. In the interest of brevity, every source is not cited. The compiler of these notes gratefully acknowledges all such sources. ]

Due: week4 Wednesday, 6pm

## 1 Task 1:

Consider the loss:

$$(-1) \cdot \sum_{i=1}^n y_i \log(h(x_i)) + (1 - y_i) \log(1 - h(x_i))$$

Prove that The gradient with respect to  $w$  will be:

$$\begin{aligned}\nabla_w L &= \nabla_w \left( (-1) \cdot \sum_{i=1}^n y_i \log(s(w \cdot x_i)) + (1 - y_i) \log(1 - s(w \cdot x_i)) \right) \\ \nabla_w L &= \sum_{i=1}^n x_i (s(w \cdot x_i) - y_i) = \sum_{i=1}^n x_i (h(x_i) - y_i)\end{aligned}$$

You can use

$$\begin{aligned}\frac{\partial \log(s(a))}{\partial a} &= 1 - s(a) \\ \frac{\partial \log(1 - s(a))}{\partial a} &= -s(a)\end{aligned}$$

and we know  $h(x) = s(w \cdot x)$

## 2 Task 2:

Which einsum notation is required to implement the following operations? Remember it is a pair

$$indices_1, indices_2, indices_3, \dots, indices_n - > indices_r, [t_1, t_2, t_3, \dots, t_n]$$

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$$C_{j,k} = \sum_i A_{ijk} b_i$$

- 

$$C_j = \sum_{i,k} A_{ijk} b_{ik}$$

- 

$$A_{ik} = \sum_{j,l} A_{ijkl}$$

- yes this is not the same as before, note the change in index ordering

$$A_{ki} = \sum_{j,l} A_{ijkl}$$

- 

$$C_i = \sum_{j,k} A_{ijk} A_{ijk}$$

- 

$$C = x^\top A x, x \in \mathbb{R}^d, \text{ 1-tensor}, A \in \mathbb{R}^{d \times d}, \text{ 2-tensor},$$

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$$C = A G^\top B, A \in \mathbb{R}^{d \times e}, \text{ 2-tensor}, G \in \mathbb{R}^{f \times e}, \text{ 2-tensor}, B \in \mathbb{R}^{f \times l}, \text{ 2-tensor},$$

The result is a tensor of what order here ? in any case there is more than one possible output index ordering in the sense of  $C_{ijk}$  vs  $C_{jki}$  vs  $C_{kij}$  and so on . any output index ordering is okay here

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$$C_{????} = \sum_{cd} A_{abcd} B_{bcde} E_{cdef}$$

any output index ordering is okay here again

### 3 Task 3:

which of these pairs of tensor shapes are broadcastable ? If they are, what is the final result shape ?

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$$(3, 1, 2, 3)$$

$$(5, 3)$$

•

$(3, 2, 1, 3, 4)$   
 $(5, 3, 4)$

•

$(3, 2, 1, 3, 4)$   
 $(5, 1, 4)$

•

$(3, 2, 1, 3, 2)$   
 $(5, 3, 1)$

•

$(3, 2, 1, 3, 2)$   
 $(1, 3, 1, 2)$

•

$(7, 1)$   
 $(7)$