## Collaborative Filtering

Sunday, October 28, 2018 1:55 PM

2016:

## 1. [Collaborative Filtering]

- a. Two Algorithms used for Collaborative Filtering:
  - i. K nearest neighbours
  - ii. Matrix Factorization
- b. What problems are well suited for Collaborative Filtering?

Problem	Well Suited
Predicting missing values in a matrix of sensor readings from a town, where the columns correspond to sensors and the rows correspond to timestamps	Yes
Predicting the books that a user would want to read in a library, given historical records of the loans of all the users	Yes
Predicting the sentiment for a named object in a new tweet, given a large data set of annotated tweets that may not contain the named object	No
Predicting the current water level in a reservoir, given recent rainfall data and historical records of water measurements in the reservoir	No

2017:

## 2. [Collaborative Filtering]

Suppose that you are given a data set from Amazon in the form of a partially-observed matrix Y whose entry Yai represents the rating of customer a for a product i. You decide to try both the k-nearest-neighbors algorithm and matrix factorization to predict the values of unknown ratings Yai.

In k-nearest-neighbors, to predict the unbiased rating Yai-Ya where Ya is the average of all observed ratings by customer a, we use the weighted sum of the unbiased ratings of neighbors b which are nearest to a. These neighbors are ranked according to a cosine similarity function sim(a,b).

a. If we predict  $Y_{ai} = \overline{Y}_a$  using  $\sum_b w_b r_b$ , which weights  $w_b$  and values  $r_b$  should we use?

A. 
$$w_b = \frac{\sin(a,b)}{\sum_{b'}\sin(a,b')}$$
 and  $r_b = Y_{bi} - \bar{Y}_b$ 

B. 
$$w_b = \frac{|\sin(a,b)|}{\sum_{b'}\sin(a,b')}$$
 and  $r_b = Y_{bi} - \bar{Y}_b$ 



C. 
$$w_b = \frac{\sin(a,b)}{\sum_{b'}|\sin(a,b')|}$$
 and  $r_b = \mathrm{sign} \left( \sin(a,b) \right) \left( Y_{bi} - \overline{Y}_b \right)$ 

D. 
$$w_b = \frac{|\sin(a,b)|}{\sum_{b'}|\sin(a,b')|}$$
 and  $r_b = \mathrm{sign} \left( \sin(a,b) \right) \left( Y_{bi} - \overline{Y}_b \right)$