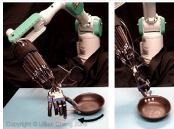


The role of intrinsic motivations in learning vocal mappings

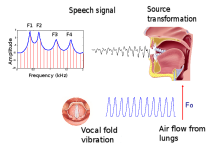
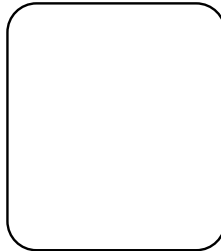
a developmental robotics study

Clément Moulin-Frier and Pierre-Yves Oudeyer
Flowers-team, Inria/ENSTA-Paritech
`flowers.inria.fr`

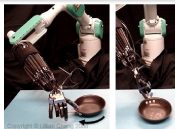
Why exploration strategies?



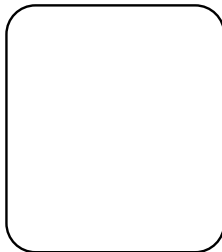
Space of motor
controllers



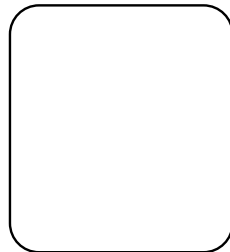
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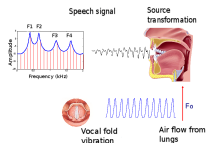
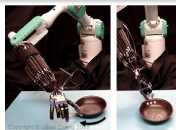
Space of motor controllers



Space of sensory effects

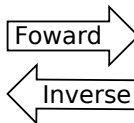


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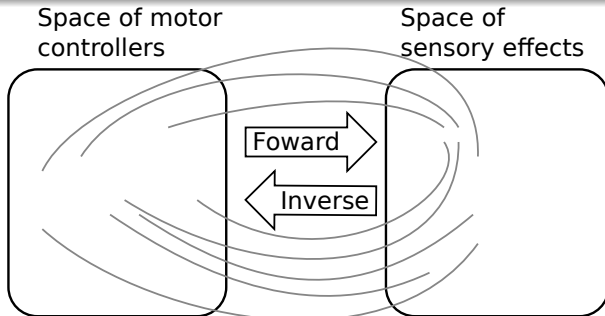
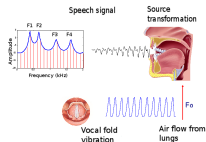
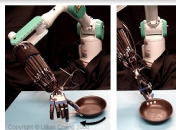
Space of motor controllers

Space of sensory effects



Objective: Learning forward and/or inverse sensorimotor models

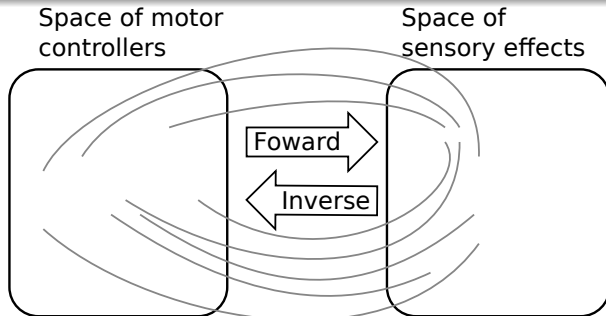
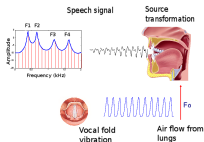
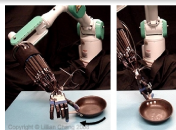
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Solution: Need to drive the learning process \Rightarrow exploration strategies

Two important principles

- Goal babbling

- Intrinsically-motivated (or active) exploration

- (Schmidhuber, 2006; Oudeyer and Kaplan, 2007; Baldassare and Miroili, 2013; Barto et al., 2004, ...)

⇒ Combining both principles in a unified probabilistic model

⇒ Relevance for infant (early vocal) development

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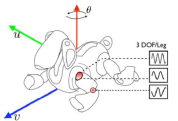
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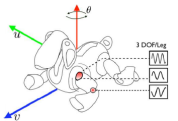
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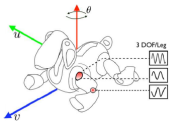
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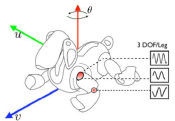
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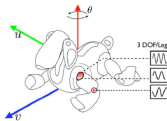
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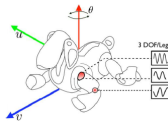
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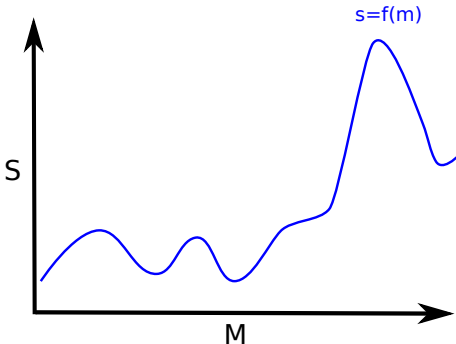
⇒ Relevance for infant (early vocal) development

Illustrative example



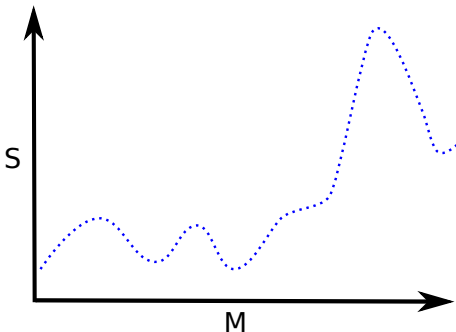
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 - Sample $m \in M$
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 - Sample $s_g \in S$
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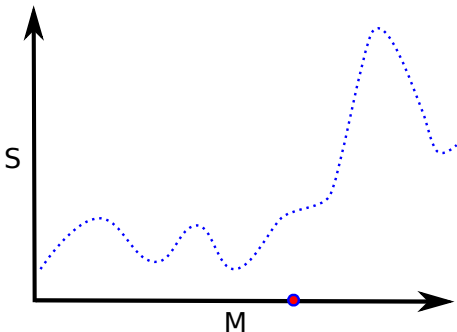
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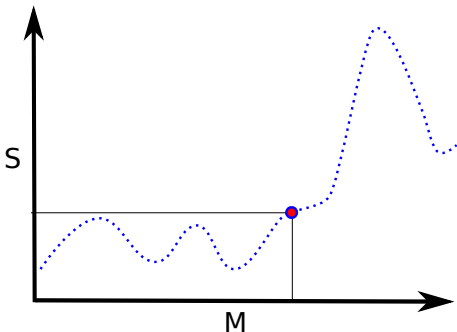
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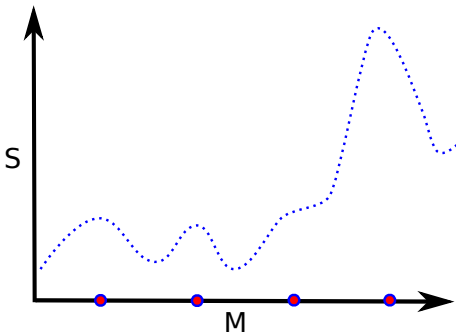
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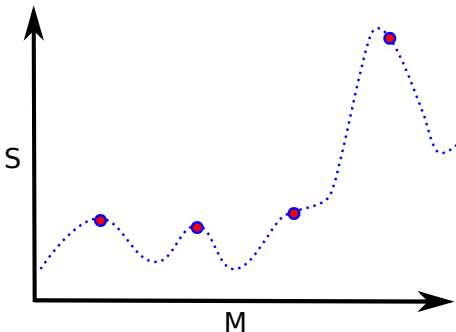
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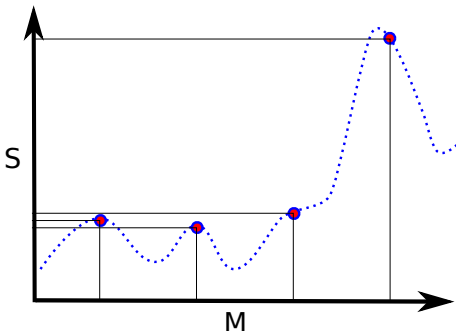
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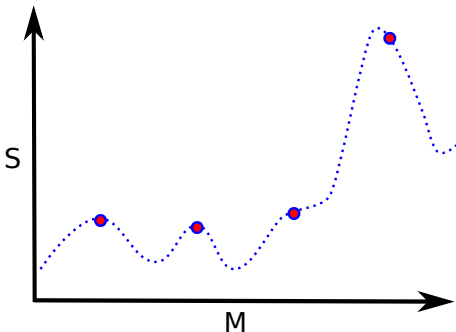
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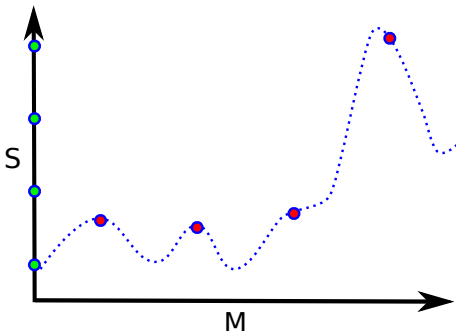
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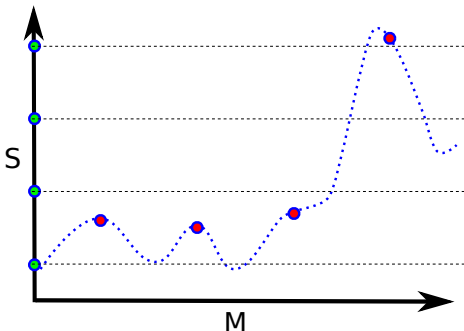
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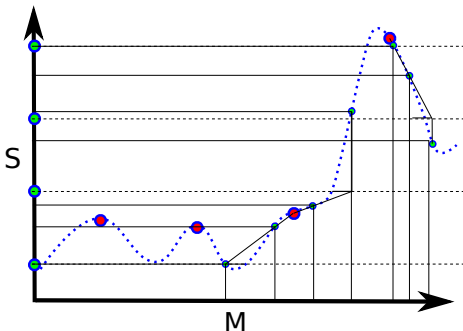
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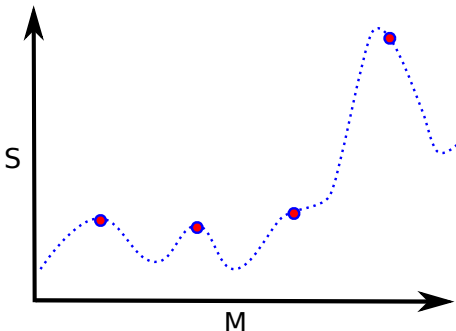
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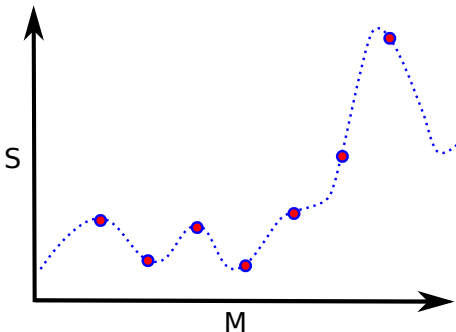
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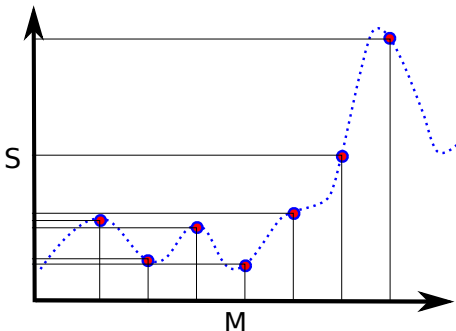
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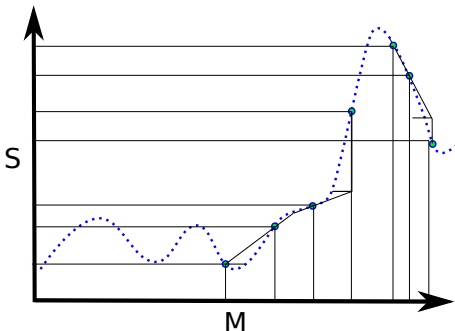
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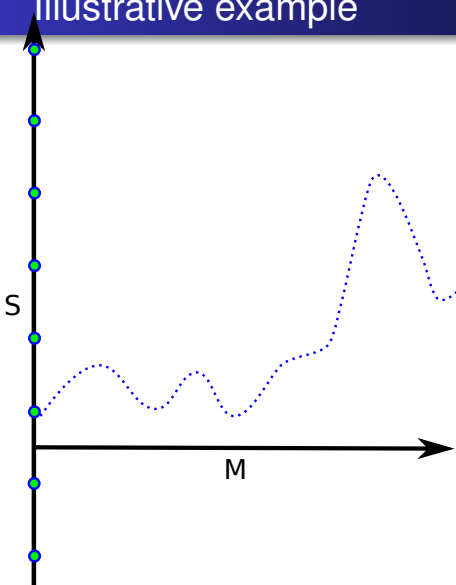
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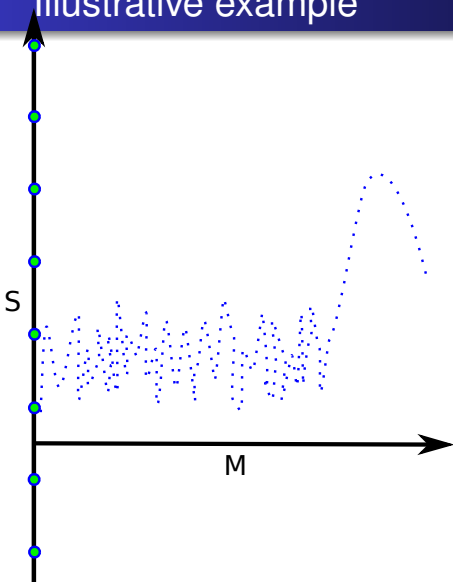
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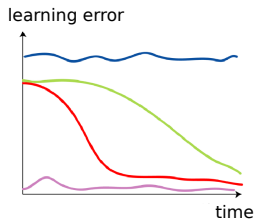
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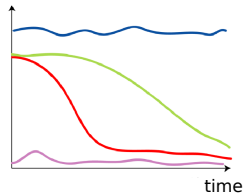
Maximizing the learning progress

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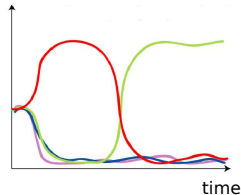


Maximizing the learning progress

learning error



time spent in each task when maximizing learning progress



Outline

- 1 Probabilistic unification
- 2 Results

A generic exploration algorithm

Choice space X	Interest distribution $p(X)$	
	Random exploration	Active exploration
Motor babbling: $X = M, Y = S$	Random motor exploration (ACTUATOR-RANDOM)	Active motor exploration (ACTUATOR-RIAC)
Goal babbling: $X = S, Y = M$	Random goal exploration (SAGG-RANDOM)	Active goal exploration (SAGG-RIAC)

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5:    $s = f(m) + \epsilon$ 
6:    $e = \text{distance}(S(x, y), s)$ 
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(Baranes and Oudeyer, 2010, 2013)

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Motor babbling: $X = M, Y = S$	Random motor exploration (ACTUATOR-RANDOM)	Active motor exploration (ACTUATOR-RIAC)
Goal babbling: $X = S, Y = M$	Random goal exploration (SAGG-RANDOM)	Active goal exploration (SAGG-RIAC)

(Baranes and Oudeyer, 2010, 2013)

```

1: while true do
2:    $x \sim p(X)$ 
3:    $y \sim p(Y | x)$ 
4:    $m = M((x, y))$ 
5:    $s = f(m) + \epsilon$ 
6:    $e = \text{distance}(S(x, y), s)$ 
7:    $\text{update}(p(M|S), (m, s))$ 
8:    $\text{update}(p(X), (x, e))$ 
9: end while
    
```

A generic exploration algorithm

Choice space X	Interest distribution $p(X)$	
	Random exploration	Active exploration
Motor babbling: $X = M, Y = S$	Random motor exploration (ACTUATOR-RANDOM)	Active motor exploration (ACTUATOR-RIAC)
Goal babbling: $X = S, Y = M$	Random goal exploration (SAGG-RANDOM)	Active goal exploration (SAGG-RIAC)

(Baranes and Oudeyer, 2010, 2013)

```

1: while true do
2:    $x \sim p(X)$ 
3:    $y \sim p(Y | x)$ 
4:    $m = M((x, y))$ 
5:    $s = f(m) + \epsilon$ 
6:    $e = \text{distance}(S(x, y), s)$ 
7:    $\text{update}(p(M|S), (m, s))$ 
8:    $\text{update}(p(X), (x, e))$ 
9: end while
    
```

A generic exploration algorithm

Choice space X	Interest distribution $p(X)$	
	Random exploration	Active exploration
Motor babbling: $X = M, Y = S$	Random motor exploration (ACTUATOR-RANDOM)	Active motor exploration (ACTUATOR-RIAC)
Goal babbling: $X = S, Y = M$	Random goal exploration (SAGG-RANDOM)	Active goal exploration (SAGG-RIAC)

(Baranes and Oudeyer, 2010, 2013)

```

1: while true do
2:    $x \sim p(X)$ 
3:    $y \sim p(Y | x)$ 
4:    $m = M((x, y))$ 
5:    $s = f(m) + \epsilon$ 
6:    $e = \text{distance}(S(x, y), s)$ 
7:    $\text{update}(p(M|S), (m, s))$ 
8:    $\text{update}(p(X), (x, e))$ 
9: end while
    
```

A generic exploration algorithm

Choice space X	Interest distribution $p(X)$	
	Random exploration	Active exploration
Motor babbling: $X = M, Y = S$	Random motor exploration (ACTUATOR-RANDOM)	Active motor exploration (ACTUATOR-RIAC)
Goal babbling: $X = S, Y = M$	Random goal exploration (SAGG-RANDOM)	Active goal exploration (SAGG-RIAC)

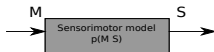
Sensorimotor model
 $p(M|S)$

```

1: while true do
2:    $x \sim p(X)$ 
3:    $y \sim p(Y | x)$ 
4:    $m = M((x, y))$ 
5:    $s = f(m) + \epsilon$ 
6:    $e = \text{distance}(S(x, y), s)$ 
7:    $\text{update}(p(M|S), (m, s))$ 
8:    $\text{update}(p(X), (x, e))$ 
9: end while
    
```

A generic exploration algorithm

Choice space X	Interest distribution $p(X)$	
	Random exploration	Active exploration
Motor babbling: $X = M, Y = S$	Random motor exploration (ACTUATOR-RANDOM)	Active motor exploration (ACTUATOR-RIAC)
Goal babbling: $X = S, Y = M$	Random goal exploration (SAGG-RANDOM)	Active goal exploration (SAGG-RIAC)

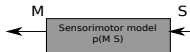
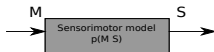


```

1: while true do
2:    $x \sim p(X)$ 
3:    $y \sim p(Y | x)$ 
4:    $m = M((x, y))$ 
5:    $s = f(m) + \epsilon$ 
6:    $e = \text{distance}(S(x, y), s)$ 
7:    $\text{update}(p(M|S), (m, s))$ 
8:    $\text{update}(p(X), (x, e))$ 
9: end while
    
```


A generic exploration algorithm

Choice space X	Interest distribution $p(X)$	
	Random exploration	Active exploration
Motor babbling: $X = M, Y = S$	Random motor exploration (ACTUATOR-RANDOM)	Active motor exploration (ACTUATOR-RIAC)
Goal babbling: $X = S, Y = M$	Random goal exploration (SAGG-RANDOM)	Active goal exploration (SAGG-RIAC)

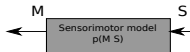
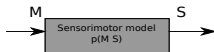


```

1: while true do
2:    $x \sim p(X)$ 
3:    $y \sim p(Y | x)$ 
4:    $m = M((x, y))$ 
5:    $s = f(m) + \epsilon$ 
6:    $e = \text{distance}(S(x, y), s)$ 
7:    $\text{update}(p(M | S), (m, s))$ 
8:    $\text{update}(p(X), (x, e))$ 
9: end while
    
```

A generic exploration algorithm

Choice space X	Interest distribution $p(X)$	
	Random exploration	Active exploration
Motor babbling: $X = M, Y = S$	Random motor exploration (ACTUATOR-RANDOM)	Active motor exploration (ACTUATOR-RIAC)
Goal babbling: $X = S, Y = M$	Random goal exploration (SAGG-RANDOM)	Active goal exploration (SAGG-RIAC)

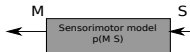
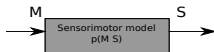


```

1: while true do
2:    $x \sim p(X)$ 
3:    $y \sim p(Y | x)$ 
4:    $m = M((x, y))$ 
5:    $s = f(m) + \epsilon$ 
6:    $e = \text{distance}(S(x, y), s)$ 
7:    $\text{update}(p(M | S), (m, s))$ 
8:    $\text{update}(p(X), (x, e))$ 
9: end while
    
```

A generic exploration algorithm

Choice space X	Interest distribution $p(X)$	
	Random exploration	Active exploration
Motor babbling: $X = M, Y = S$	Random motor exploration (ACTUATOR-RANDOM)	Active motor exploration (ACTUATOR-RIAC)
Goal babbling: $X = S, Y = M$	Random goal exploration (SAGG-RANDOM)	Active goal exploration (SAGG-RIAC)

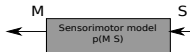
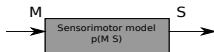


```

1: while true do
2:    $x \sim p(X)$ 
3:    $y \sim p(Y | x)$ 
4:    $m = M((x, y))$ 
5:    $s = f(m) + \epsilon$ 
6:    $e = \text{distance}(S(x, y), s)$ 
7:    $\text{update}(p(M S), (m, s))$ 
8:    $\text{update}(p(X), (x, e))$ 
9: end while
    
```

A generic exploration algorithm

Choice space X	Interest distribution $p(X)$	
	Random exploration	Active exploration
Motor babbling: $X = M, Y = S$	Random motor exploration (ACTUATOR-RANDOM)	Active motor exploration (ACTUATOR-RIAC)
Goal babbling: $X = S, Y = M$	Random goal exploration (SAGG-RANDOM)	Active goal exploration (SAGG-RIAC)

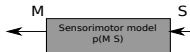
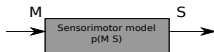


```

1: while true do
2:    $x \sim p(X)$ 
3:    $y \sim p(Y | x)$ 
4:    $m = M((x, y))$ 
5:    $s = f(m) + \epsilon$ 
6:    $e = \text{distance}(S(x, y), s)$ 
7:    $\text{update}(p(M S), (m, s))$ 
8:    $\text{update}(p(X), (x, e))$ 
9: end while
    
```

A generic exploration algorithm

Choice space X	Interest distribution $p(X)$	
	Random exploration	Active exploration
Motor babbling: $X = M, Y = S$	Random motor exploration (ACTUATOR-RANDOM)	Active motor exploration (ACTUATOR-RIAC)
Goal babbling: $X = S, Y = M$	Random goal exploration (SAGG-RANDOM)	Active goal exploration (SAGG-RIAC)

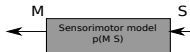
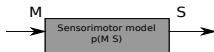


```

1: while true do
2:    $x \sim p(X)$ 
3:    $y \sim p(Y | x)$ 
4:    $m = M((x, y))$ 
5:    $s = f(m) + \epsilon$ 
6:    $e = \text{distance}(S(x, y), s)$ 
7:    $\text{update}(p(M | S), (m, s))$ 
8:    $\text{update}(p(X), (x, e))$ 
9: end while
    
```

A generic exploration algorithm

Choice space X	Interest distribution $p(X)$	
	Random exploration	Active exploration
Motor babbling: $X = M, Y = S$	Random motor exploration (ACTUATOR-RANDOM)	Active motor exploration (ACTUATOR-RIAC)
Goal babbling: $X = S, Y = M$	Random goal exploration (SAGG-RANDOM)	Active goal exploration (SAGG-RIAC)



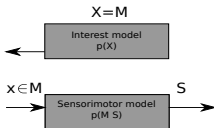
```

1: while true do
2:    $x \sim p(X)$ 
3:    $y \sim p(Y | x)$ 
4:    $m = M((x, y))$ 
5:    $s = f(m) + \epsilon$ 
6:    $e = \text{distance}(S(x, y), s)$ 
7:    $\text{update}(p(M | S), (m, s))$ 
8:    $\text{update}(p(X), (x, e))$ 
9: end while
    
```

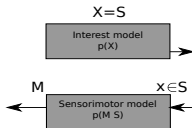
A generic exploration algorithm

Choice space X	Interest distribution $p(X)$	
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Motor babbling: $X = M, Y = S$	Random motor exploration (ACTUATOR-RANDOM)	Active motor exploration (ACTUATOR-RIAC)
Goal babbling: $X = S, Y = M$	Random goal exploration (SAGG-RANDOM)	Active goal exploration (SAGG-RIAC)

Motor babbling



Goal babbling



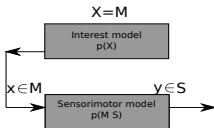
```

1: while true do
2:    $x \sim p(X)$ 
3:    $y \sim p(Y | x)$ 
4:    $m = M((x, y))$ 
5:    $s = f(m) + \epsilon$ 
6:    $e = \text{distance}(S(x, y), s)$ 
7:    $\text{update}(p(M|S), (m, s))$ 
8:    $\text{update}(p(X), (x, e))$ 
9: end while
    
```

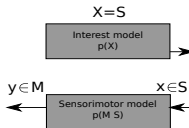
A generic exploration algorithm

Choice space X	Interest distribution $p(X)$	
	Random exploration	Active exploration
Motor babbling: $X = M, Y = S$	Random motor exploration (ACTUATOR-RANDOM)	Active motor exploration (ACTUATOR-RIAC)
Goal babbling: $X = S, Y = M$	Random goal exploration (SAGG-RANDOM)	Active goal exploration (SAGG-RIAC)

Motor babbling



Goal babbling



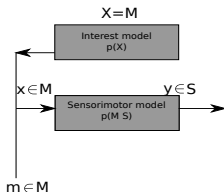
```

1: while true do
2:    $x \sim p(X)$ 
3:    $y \sim p(Y | x)$ 
4:    $m = M((x, y))$ 
5:    $s = f(m) + \epsilon$ 
6:    $e = \text{distance}(S(x, y), s)$ 
7:    $\text{update}(p(M|S), (m, s))$ 
8:    $\text{update}(p(X), (x, e))$ 
9: end while
    
```

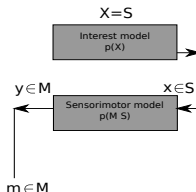

A generic exploration algorithm

Choice space X	Interest distribution $p(X)$	
	Random exploration	Active exploration
Motor babbling: $X = M, Y = S$	Random motor exploration (ACTUATOR-RANDOM)	Active motor exploration (ACTUATOR-RIAC)
Goal babbling: $X = S, Y = M$	Random goal exploration (SAGG-RANDOM)	Active goal exploration (SAGG-RIAC)

Motor babbling



Goal babbling



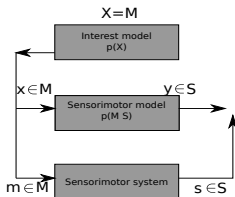
```

1: while true do
2:    $x \sim p(X)$ 
3:    $y \sim p(Y | x)$ 
4:    $m = M((x, y))$ 
5:    $s = f(m) + \epsilon$ 
6:    $e = \text{distance}(S(x, y), s)$ 
7:    $\text{update}(p(M|S), (m, s))$ 
8:    $\text{update}(p(X), (x, e))$ 
9: end while
    
```

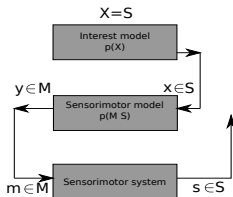
A generic exploration algorithm

Choice space X	Interest distribution $p(X)$	
	Random exploration	Active exploration
Motor babbling: $X = M, Y = S$	Random motor exploration (ACTUATOR-RANDOM)	Active motor exploration (ACTUATOR-RIAC)
Goal babbling: $X = S, Y = M$	Random goal exploration (SAGG-RANDOM)	Active goal exploration (SAGG-RIAC)

Motor babbling



Goal babbling



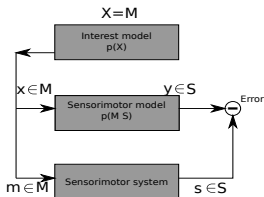
```

1: while true do
2:    $x \sim p(X)$ 
3:    $y \sim p(Y | x)$ 
4:    $m = M((x, y))$ 
5:    $s = f(m) + \epsilon$ 
6:    $e = \text{distance}(S(x, y), s)$ 
7:    $\text{update}(p(M|S), (m, s))$ 
8:    $\text{update}(p(X), (x, e))$ 
9: end while
    
```

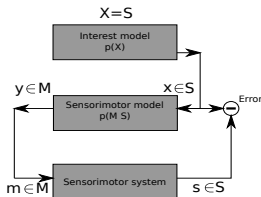
A generic exploration algorithm

Choice space X	Interest distribution $p(X)$	
	Random exploration	Active exploration
Motor babbling: $X = M, Y = S$	Random motor exploration (ACTUATOR-RANDOM)	Active motor exploration (ACTUATOR-RIAC)
Goal babbling: $X = S, Y = M$	Random goal exploration (SAGG-RANDOM)	Active goal exploration (SAGG-RIAC)

Motor babbling



Goal babbling



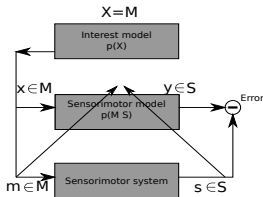
```

1: while true do
2:    $x \sim p(X)$ 
3:    $y \sim p(Y | x)$ 
4:    $m = M((x, y))$ 
5:    $s = f(m) + \epsilon$ 
6:    $e = \text{distance}(S(x, y), s)$ 
7:    $\text{update}(p(M|S), (m, s))$ 
8:    $\text{update}(p(X), (x, e))$ 
9: end while
    
```

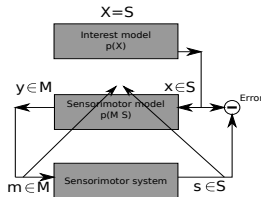
A generic exploration algorithm

Choice space X	Interest distribution $p(X)$	
	Random exploration	Active exploration
Motor babbling: $X = M, Y = S$	Random motor exploration (ACTUATOR-RANDOM)	Active motor exploration (ACTUATOR-RIAC)
Goal babbling: $X = S, Y = M$	Random goal exploration (SAGG-RANDOM)	Active goal exploration (SAGG-RIAC)

Motor babbling



Goal babbling



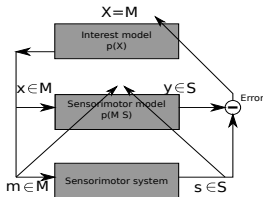
```

1: while true do
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3:    $y \sim p(Y | x)$ 
4:    $m = M((x, y))$ 
5:    $s = f(m) + \epsilon$ 
6:    $e = \text{distance}(S(x, y), s)$ 
7:    $\text{update}(p(M|S), (m, s))$ 
8:    $\text{update}(p(X), (x, e))$ 
9: end while
    
```

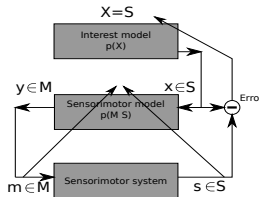
A generic exploration algorithm

Choice space X	Interest distribution $p(X)$	
	Random exploration	Active exploration
Motor babbling: $X = M, Y = S$	Random motor exploration (ACTUATOR-RANDOM)	Active motor exploration (ACTUATOR-RIAC)
Goal babbling: $X = S, Y = M$	Random goal exploration (SAGG-RANDOM)	Active goal exploration (SAGG-RIAC)

Motor babbling



Goal babbling



```

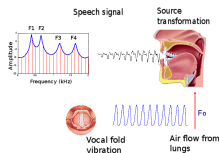
1: while true do
2:    $x \sim p(X)$ 
3:    $y \sim p(Y | x)$ 
4:    $m = M((x, y))$ 
5:    $s = f(m) + \epsilon$ 
6:    $e = \text{distance}(S(x, y), s)$ 
7:    $\text{update}(p(M|S), (m, s))$ 
8:    $\text{update}(p(X), (x, e))$ 
9: end while
    
```

Outline

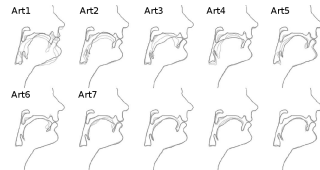
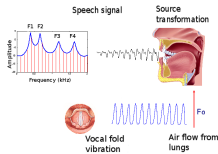
1 Probabilistic unification

2 **Results**

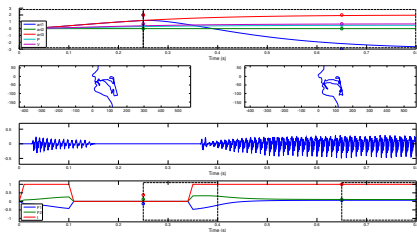
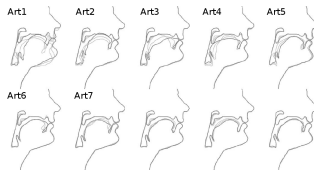
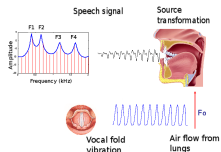
Sensorimotor system: articulatory synthesizer of Guenther (2006)



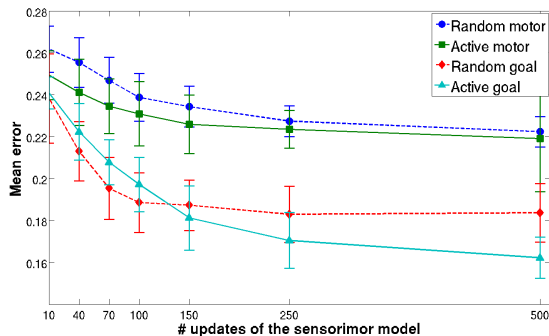
Sensorimotor system: articulatory synthesizer of Guenther (2006)



Sensorimotor system: articulatory synthesizer of Guenther (2006)

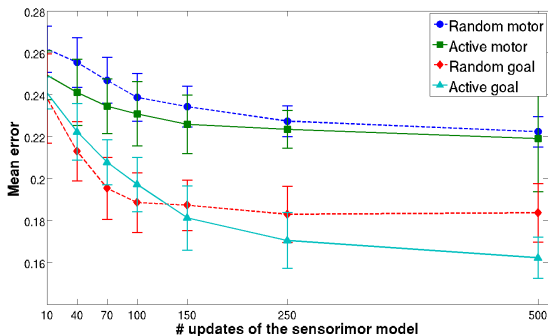


Performance comparison



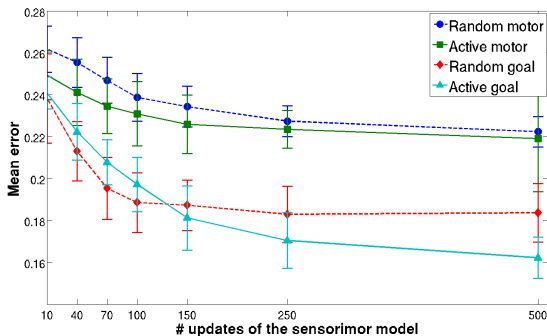
- To learn an inverse model:
 - Goal exploration strategies outperform motor exploration strategies
 - Active goal exploration outperforms random goal exploration

Performance comparison



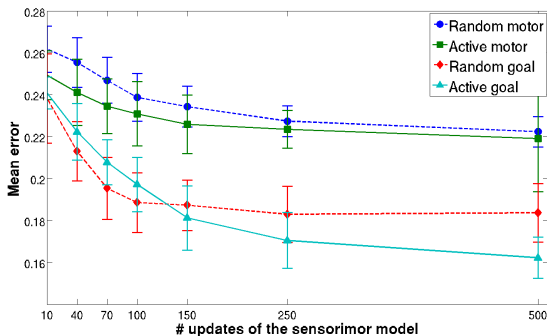
- To learn an inverse model:
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Performance comparison



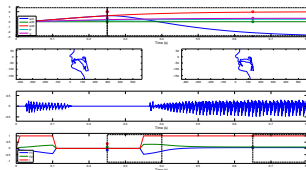
- To learn an inverse model:
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Performance comparison



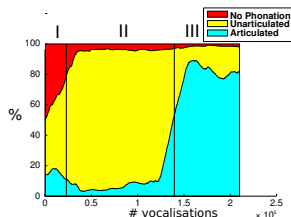
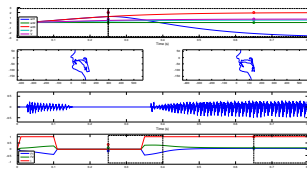
- To learn an inverse model:
 - Goal exploration strategies outperform motor exploration strategies
 - Active goal exploration outperforms random goal exploration

Self organization of early vocal development



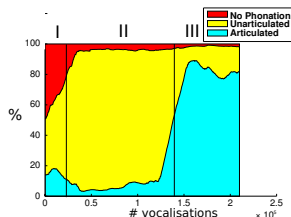
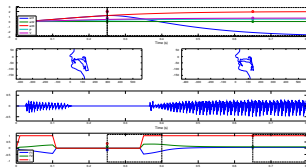
- Active goal exploration enables the self-organization of a developmental sequence, from simple to complex

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Conclusions

Take-home messages

- Developmental robotics studies algorithmic principles that allows robots to efficiently explore and learn sensorimotor mappings
- These principles (e.g. goal babbling and intrinsically-motivated exploration, but also maturations, social guidance ...) are grounded in developmental psychology
- The interest they present for speech acquisition models has not been studied significantly but could yield important contributions to the field

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- Active choice of sensorimotor dimensions X and Y to explore
- Extending the unification to more developmental robotics principles, e.g. social guidance and maturations.
- Using a physical model of the vocal tract

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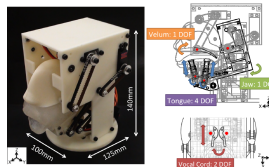
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(Yuki et al., ICDL-Epirob 2013)

Thank you for your attention. Any question?

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