Classical mechanics

Kinetics

velocity: $\mathbf{v} = \frac{d\mathbf{r}}{dt} = r_x'\mathbf{i} + r_y'\mathbf{j} + r_z'\mathbf{k}$ acceleration: $\mathbf{a} = \frac{d\mathbf{v}}{dt} = v_x'\mathbf{i} + v_y'\mathbf{j} + v_z'\mathbf{k}$ motion laws:

 $v = v_0 + at$ $x - x_0 = v_0 t + \frac{1}{2} a t^2$ $v^2 - v_0^2 = 2a(x - x_0)$ $x - x_0 = \frac{(v_0 + v)t}{2}$

centripetal acceleration: $a=\frac{v^2}{r}=\frac{4\pi^2r}{T^2}=4\pi^2rf^2=\omega^2r$ velocity in two frames: $\mathbf{v}_{\mathrm{PA}}=\mathbf{v}_{\mathrm{PB}}+\mathbf{v}_{\mathrm{BA}}$

same acceleration measured in all frames: $\mathbf{a}_{\mathrm{PA}} = \mathbf{a}_{\mathrm{PB}}$

Kinetics 2

Newton's second law: $\mathbf{F}_{\mathrm{T}} = m\mathbf{a}$

Newton's third law: $\mathbf{F}_{\mathrm{A \ to \ B}} = -\mathbf{F}_{\mathrm{B \ to \ A}}$

acceleration of simple pulley: $a = \frac{m_1 - m_2}{m_1 + m_2} g$

drag force (body in fluid): $D = \frac{1}{2}C\rho Av^2$ terminal speed: $v = \sqrt{\frac{2mg}{C\rho A}}$ (1) work: $W = \int \mathbf{F} \cdot d\mathbf{s} = \int_{x_i}^{x_f} F_x dx + \int_{y_i}^{y_f} F_y dy + \int_{z_i}^{z_f} F_z dz$ Hooke's law: $\mathbf{F} = -k\mathbf{x}$

work by spring: $W = \frac{1}{2}kx_i^2 - \frac{1}{2}kx_f^2$

kinetic energy: $K = \frac{1}{2}mv^2$

work-kinetic energy theorem: $W = K_f - K_i = \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2$ power: $P = \frac{dW}{dt} = \mathbf{F} \cdot \mathbf{v}$

Kinetics 3

definition of change in potential energy: $\Delta U = -W$ change in mechanical energy: $\Delta K + \Delta U = 0$ total mechanical energy: E = U + K (isolated)

U-x graph:

external force: $F(x) = -\frac{d}{dx}U(x)$ neutral equilibrium: E = Uunstable equilibrium: U'' < 0, U' = 0stable equilibrium: U'' > 0, U' = 0

total m.energy of block-spring system: $E = \frac{1}{2}kx^2 + \frac{1}{2}mv^2$ total m.energy of particle-earth system: $E = may + \frac{1}{\pi}mv^2$

total m.energy of particle-earth system: $E = mgy + \frac{1}{2}mv^2$ conservation of energy:

 $^{(1)}$ C: drag coefficient, A: effective cross-sectional area, ρ : air density.

A formula summary for physics

 $\Delta K + \Delta U + \Delta E_{\text{internal}}$ (+other forms) = 0 (isolated) external work done: $W = \Delta K + \Delta U + \Delta E_{\text{internal}}$ change in energy: $\Delta E = \Delta K + \Delta U$ loss in mechanical energy (friction): $\Delta E = -fd$ energy loss due to emitted light: $E_x - E_y = hf$

System kinetics

centre of mass: $\mathbf{r}_{\text{CM}} = \frac{1}{M} \sum_{i} m_{i} \mathbf{r}_{i}$ continuous: $\mathbf{r}_{\text{CM}} = \frac{1}{M} \int \mathbf{r} \rho dV = \frac{1}{V} \int \mathbf{r} dV$ relation: $dm = \rho dV$

linear momentum: $\mathbf{p} = m\mathbf{v}$ relation: $K = \frac{p^2}{2m}$ net force: $\mathbf{F}_{\mathrm{T}} = \frac{d\mathbf{p}}{dt}$

Newton's second law: $\sum \mathbf{F}_{\text{external}} = M \mathbf{a}_{\text{CM}} = \frac{d\mathbf{P}}{dt}$ conservation of linear momentum: $\mathbf{P} = \text{constant}$

циолковский's rocket formula:

 $\mathbf{F} = (\mathbf{v} - \mathbf{u}) \frac{dm}{dt} + m \frac{d\mathbf{v}}{dt}$ or $\frac{d}{dt} m \mathbf{v} = \mathbf{F} + \mathbf{u} \frac{dm}{dt}$ v: rocket's velocity in earth, u: fuel's velocity in earth

change in translational k. energy: $\Delta K_{\rm CM}=F_{\rm ext}d_{\rm CM}$ König's theorem: $K=K_{\rm related~to~CM}+\frac{1}{2}mv_{\rm CM}^2$

Collisions

impulse: $\mathbf{J} = \Delta \mathbf{p} = \int \mathbf{F} dt$

elastic collision:

$$\begin{array}{l} v_1' = \frac{m_1 - m_2}{m_1 + m_2} v_1 + \frac{2m_2}{m_1 + m_2} v_2 \\ v_2' = \frac{m_2 - m_1}{m_1 + m_2} v_2 + \frac{2m_1}{m_1 + m_2} v_1 \\ v_{\mathrm{CM}} = \frac{P}{m_1 + m_2} \end{array}$$

complete inelastic collision: $m_1v_1 + m_2v_2 = (m_1 + m_2)V_{\rm CM}$ heat of reactions: $Q = -\Delta mc^2$ (+Q: exothermic, -Q: endothermic)

Rotation

angular position: $\theta = s/r$ angular velocity: $\omega = \frac{d\theta}{dt}$ angular acceleration: $\alpha = \frac{d\omega}{dt}$ motion laws: $\omega = \omega_0 + \alpha t$ $\theta = \omega_0 t + \frac{1}{2}\alpha t^2$

$$\omega^2 - \omega_0^2 = 2\alpha\theta$$
$$\theta = \frac{(\omega_0 + \omega)t}{2}$$

linear-angular relation: $s=\theta r,\,v=\omega r$

tangent acceleration: $a_t = \alpha r$ radial acceleration: $a_r = \frac{v^2}{r} = \omega^2 r$

rotational inertia: $I = \sum_{i} m_i r_i^2$

r.i. for continuous objects: $I = \int r^2 dm$

total rotational inertia: $I_{\text{whole}} = \sum_{i} I_{i}$ (all to one axis)

parallel-axis theorem: $I = I_{\rm CM} + Mh^2$

perpendicular-axis theorem: $I_P = I_x + I_y$ (no thickness)

rotational kinetic energy: $K = \frac{1}{2}I\omega^2$

torque: $\boldsymbol{\tau} = \mathbf{r} \times \mathbf{F}$

Newton's second law: $\tau_T = I\alpha$ work: $W = \int F_t r d\theta = \int \tau d\theta$

power: $P = \frac{dW}{dt} = \tau \omega$

work-kinetic energy theorem: $W = \Delta K = \frac{1}{2}I\omega_f^2 - \frac{1}{2}I\omega_i^2$

Rotational inertia

hoop, central axis: $I = MR^2$

hoop, diameter: $I = \frac{1}{2}MR^2$

annular cylinder, central axis: $\frac{1}{2}M\left(R_1^2+R_2^2\right)$

annular cylinder, central diameter, $\frac{1}{4}M\left(R_1^2+R_2^2\right)$

solid cylinder/disk, central axis: $\frac{1}{2}MR^2$

solid cylinder/disk, central diameter: $I=\frac{1}{4}MR^2+\frac{1}{12}ML^2$

rod, centre of length: $I = \frac{1}{12}ML^2$

rod, one end: $I = \frac{1}{3}ML^2$

triangle, parallel to base a (whose height is h, through CM):

 $I = \frac{1}{18}Mh^2$

solid sphere, diameter: $I = \frac{2}{5}MR^2$

spherical shell, diameter: $I = \frac{2}{3}MR^2$

slab, centre: $I = \frac{1}{12}M(a^2 + b^2)$

slab, along edge $b:I = \frac{1}{3}Ma^2$

Rolling

CM displacement/distance rolled: $x_{\rm CM} = \theta R$, $v_{\rm CM} = \omega R$ kinetic energy: $K = K_{\rm rot} + K_{\rm tra} = \frac{1}{2}I_{\rm CM}\omega^2 + \frac{1}{2}mv_{\rm CM}^2$ accleration of ideal yoyo: $a = -g(\frac{1}{1+I/MR^2})$ angular momentum: $\boldsymbol{\ell} = \mathbf{r} \times \mathbf{p} = \mathbf{r} \times m\mathbf{v}$ a.m. for rigid, fixed axis: $L = I\omega$ angular impulse: $\Delta L = \int \tau dt$

angular impulse: $\Delta L = \int \boldsymbol{\tau} dt$ Newton's second law: $\boldsymbol{\tau}_{\mathrm{T}} = \frac{dL}{dt}$

conservation of angular momentum: L = constant

Elasticity

static equilibrium: $\mathbf{P} = 0, \mathbf{L} = 0$ requirements of equilibrium: $\sum \mathbf{F}_{\text{ext}} = 0, \sum \boldsymbol{\tau}_{\text{ext}} = 0$ tensile stress: $\frac{F}{A} = E \frac{\Delta L}{L}$, E: Young's modulus sheering stress: $\frac{F}{A} = G \frac{\Delta x}{L}$, G: sheer modulus hydraulic compression: $p = B \frac{\Delta V}{V}$, B: Bulk modulus

Oscillation

simple harmonic motion $(F = -m\omega^2 x)$: $\omega = \frac{2\pi}{T} = 2\pi f$ $x(t) = x_m \cos(\omega t + \phi)$ $v(t) = -\omega x_m \sin(\omega t + \phi)$ $a(t) = -\omega^2 x(t)$ linear oscillator definition: $\frac{d^2x}{dt^2} + \omega^2x = 0$

angular frequency: $\omega = \sqrt{\frac{k}{m}}$ period: $T = 2\pi \sqrt{\frac{m}{k}}$ potential energy: $U(t) = \frac{1}{2}kx_m^2\cos^2(\omega t + \phi)$ kinetic energy: $K(t) = \frac{1}{2}kx_m^2\sin^2(\omega t + \phi)$ total energy: $E = \frac{1}{2}kx_m^2$ series spring: $\frac{1}{K} = \sum_{j} \frac{1}{k_j}$, two: $K = \frac{k_1 k_2}{k_1 + k_2}$ parallel spring: $K = \sum_{i} k_{i}$

simple pendulum period: $T = 2\pi \sqrt{\frac{L}{a}}$ restoring force: $F \approx -(\frac{mg}{T})s$

torsion pendulum period: $T = 2\pi \sqrt{\frac{I}{\kappa}}$ restoring torque: $\tau = -\kappa \theta$

physical pendulum period: $T = 2\pi \sqrt{\frac{I}{mah}}$

restoring torque: $\tau = -(mq\sin\theta)h$ damped simple harmonic motion damping force: $F_d = -bv$, b: damping constant definition: $\frac{d^2x}{dt^2} + \frac{b}{m}\frac{dx}{dt} + \frac{k}{m}x = 0$ displacement: $x(t) = x_m e^{-bt/2m} \cos(\omega_d t + \phi)$ angular frequency: $\omega_d = \sqrt{\frac{k}{m} - \frac{b^2}{4m^2}}$ total energy: $E(t) \approx \frac{1}{2} k x_m^2 e^{-bt/m}$

Gravitation

Newton's law of gravitation: $F = \frac{GMm}{r^2}$ gravitational constant: $G = 6.67 \cdot 10^{-11} \,\mathrm{N \cdot m^2/kg^2}$ differential: $dF = \frac{Gm_1}{r^2}dm$ gravitational field: $g = \frac{GM}{r^2}$ gravitational potential energy: $U = \int_{\infty}^{r} \frac{GMm}{r^2} dx = -\frac{GMm}{r}$ escape speed: $v = \sqrt{\frac{2GM}{r}}$

orbits:

path of planet: $r = \frac{p}{1 + e \cos \theta}$ $p = \frac{L^2}{GMm^2}, e = \sqrt{1 + \frac{2EL^2}{G^2M^2m^3}}$ net angular momentum: $L = mr^2\dot{\theta}$ net mechanical energy: $E = \frac{1}{2} m (\dot{r}^2 + r^2 \dot{\theta}^2) - \frac{GMm}{r} = \frac{1}{2} m \dot{r}^2 + (\frac{L^2}{2mr^2} - \frac{GMm}{r})$ total energy of satellite-earth ellipse system: $E = -K = -\frac{GMm}{2r}$ perihelion: $r_1 = a - c$ aphelion: $r_2 = a + c$ $a = \frac{r_1 + r_2}{2} = -\frac{GMm}{2E}, c = \frac{r_2 - r_1}{2},$ $b = \sqrt{a^2 - c^2} = \sqrt{r_1 r_2} = \frac{L}{\sqrt{-2mE}}$ total energy of satellite-earth hyperbola system: $E = \frac{GMm}{2r}$

total energy of satellite-earth parabola system: E=0law of periods: $\frac{T^2}{r^3} = \frac{4\pi^2}{GM}$

Fluids

pressure: $p = \frac{\Delta F}{\Delta A}$ (all direction) pressure in liquid: $p = p_0 + \rho q h$ Pascal's principle: $\Delta p_{\rm int} = \Delta p_{\rm ext}$ Archimede's principle: $F_{\text{buoyancy}} = G_{\text{displaced water}}$ equation of continuity: volume flow rate R = Av = constantmass flow rate $m = Av\rho = \text{constant}$ Bernoulli's equation: $p + \frac{1}{2}\rho v^2 + \rho qy = \text{constant}$

Transverse waves

transverse displacement: $y(x,t) = y_m \sin(kx - \omega t)$ angular wave number: $k = \frac{2\pi}{\lambda}$ waver number: $\kappa = \frac{1}{\lambda}$ angular frequency: $\omega = \frac{2\pi}{T}$ frequency: $f = \frac{1}{T} = \frac{\omega}{2\pi}$ wave speed: $v = \frac{\omega}{k} = \lambda f$ material expression: $v = \sqrt{\frac{\tau(\text{tension})}{\mu(\text{density of media})}}$ transverse speed: $u = \frac{\partial y}{\partial t}$ average power: $\overline{P} = \frac{1}{2}\mu v\omega^2 y_m^2$

adding waves superposition: $y = y_1 + y_2 = y_m \sin(kx - \omega t + \phi) + y_m \sin(kx - \omega t)$ new wave: $y = (2y_m \cos \frac{1}{2}\phi)\sin(kx - \omega t + \frac{1}{2}\phi)$ new amplitude: $2y_m\cos\frac{1}{2}\phi$ phase shift: $+\frac{1}{2}\phi$ standing waves superposition: $y = y_1 + y_2 = y_m \sin(kx - \omega t) + y_m \sin(kx + \omega t)$ new wave: $y = [(2y_m)\sin kx]\cos \omega t$ new amplitude: $2y_m \sin kx$ nodes: $x = n \frac{\lambda}{2}, n = 0, 1, 2, ...$ antinodes: $x = (n + \frac{1}{2})\frac{\lambda}{2}, n = 0, 1, 2, ...$ resonant frequency: $f_r = \frac{v}{\lambda} = \frac{v}{2l}n, n = 1, 2, 3, \dots$

Longitudinal waves

speed of sound: $v = \sqrt{\frac{B}{a}}$ bulk modulus: $B = -\frac{\Delta p}{\Delta V/V} (= \rho v^2)$ longitudinal displacement: $s = s_m \cos(kx - \omega t)$ air pressure: $\Delta p = \Delta p_m \sin(kx - \omega t)$ relation: $\Delta p_m = (v \rho \omega) s_m$

interference

phase shift: $\phi = \frac{\Delta d}{\lambda} 2\pi$ fully constructive: $\phi = m2\pi, m = 0, 1, 2, ...$ fully destructive: $\phi = (m + \frac{1}{2})2\pi, m = 0, 1, 2, ...$

sound intensity: $I = \frac{1}{2}\rho v\omega^2 s_m^2$ sound level: $\beta = (10 \text{ dB})\log(\frac{I}{I_0})$ standard reference intensity: $I_0 = 10^{-12} \text{W/m}^2$

resonant frequency

pipe, two opens: $f_r = \frac{v}{\lambda} = \frac{v}{2L}n, n = 1, 2, 3$ pipe, one open: $f_r = \frac{v}{\lambda} = \frac{v}{4L}n, n = 1, 3, 5, ...$ beat frequency: $f_{beat} = f_1 - f_2$

doppler effect: $f' = f \frac{v \pm v_L}{v \mp v_S}$ cone angle at supersonic speed: $\sin \theta = \frac{v}{v}$

Heat, Second law of thermodynamics

Heat

coefficient of linear expansion: $\alpha = \frac{\Delta L/L}{\Delta T}$ area expansion: $\beta = 2\alpha$ volume expansion: $\gamma = 3\alpha$ heat capacity: $Q = cm(T_f - T_i) = C(T_f - T_i)$ heat of transformation: Q = Lmvolume work: $W = \int_{V_i}^{V_f} p dV$

first law of thermodynamics: $\Delta E_{\rm int} = E_{\rm int,f} - E_{\rm int,i} = Q - W$ rate of heat transfer: $H = \frac{Q}{t} = kA \frac{T_H - T_C}{L}$ (2) multiple slabs: $H = A \frac{T_H - T_C}{\sum (L/k)}$

Kinetic theory of gases

ideal gas law: pV = nRT

gas constant $R = 8.31 \text{J/mol} \cdot \text{K}$

volume work of expansion at constant pressure:

$$W = \int \frac{nRT}{V} dV = nRT \ln(\frac{V_f}{V_i})$$

gas pressure: $p = \frac{nMv_{\rm rms}^2}{3V}$

translational kinetic energy: $\overline{K} = \frac{3}{2}kT$

Boltzman constant $k = R/N_A$

mean free path: $\lambda = \frac{1}{\sqrt{2\pi}dN/V}$ (3) Maxwell's speed distribution:

$$P(v) = 4\pi (\frac{M}{2\pi RT})^{3/2} v^2 e^{-Mv^2/2RT}$$

most propable speed: $v_p = \sqrt{\frac{2RT}{M}}$

average speed: $\overline{v} = \sqrt{\frac{8RT}{\pi M}}$

rms speed: $v_{\rm rms} = \sqrt{\frac{3RT}{M}}$

internal energy of monoatomic gas: $E_{\text{int}} = (nN_A)\overline{K} = \frac{3}{2}nRT$ monoatom: 3/2 (f = 1)

diatom: $5/2 \ (f = 2)$

5-atom: 3 (f = 5)

molar specific heat of monoatomic gas at constant volume:

 $C_v = \frac{3}{2}R = 12.5 \,\text{J/molK}$

constant volume, change in internal energy:

 $\Delta E_{\rm int} = Q = nC_v(T_f - T_i)$

molar specific heat of monoatomic gas at constant pressure:

 $C_p - C_v = R$

heat: $Q = nC_p(T_f - T_i)$

work: $W = nR(T_f - T_i)$

law of adiabatic expansion: $pV^{\gamma} = \text{constant}$, or

 $TV^{\gamma-1} = \text{constant}$

$$\gamma = C_p/C_v = 1 + 2/f$$

(2) k: media's thermal conductivity. (3) d: diameter, N: number of molecules. (4) n: number of carriers per unit volume. (5) ρ : temperature coefficient of resistivity.

Second law of thermodynamics

thermal efficacy of engine: $e = \frac{|W|}{|Q_H|} = \frac{|Q_H| - |Q_C|}{|Q_H|}$ $\max: e_{\text{Car}} = \frac{T_H - T_C}{T_H}$ coefficient of performance of refrigerator:

$$\begin{split} e &= \frac{|Q_C|}{|W|} = \frac{|Q_C|}{|Q_H| - |Q_C|} \\ \text{max: } e_{\text{Car}} &= \frac{T_C}{T_H - T_C} \end{split}$$

first law of thermodynamics in closed system:

 $|W| = |Q_H| - |Q_C|$

entropy: $dS = \frac{dQ}{T}$ and $\oint dS \leq 0$

reversible process: $S_f - S_i = \int_i^f dS = \int_i^f \frac{dQ}{T}$

free expansion: $S_f - S_i = \frac{1}{T} \int_i^f dQ = nR \ln \frac{V_f}{V_i}$

irreversible heat transfer: $S_f - S_i = cm \ln \frac{T^2}{T^2 - \Delta T^2}$

Electricity and Magnetism

Electrostatic forces

Coulomb's law: $F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$ permitivity constant in vacuum: $\epsilon_0 = 8.85 \cdot 10^{-12} \, \mathrm{C}^2 / \mathrm{N} \cdot \mathrm{m}^2$ charge is quantized: q = neelementary charge $e = 1.6 \cdot 10^{-14} \,\mathrm{C}$

Electric field

electric field: $\mathbf{E} = \frac{\mathbf{F}}{q_0}$ differential: $d\mathbf{E} = \frac{1}{4\pi\epsilon_0} \frac{dq}{r^3} \mathbf{r}$ (r from dq to point) point charge: $E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$ straight rod (perpendicular): $E = \frac{\lambda a}{2\pi\epsilon_0 r} \frac{1}{\sqrt{4r^2 + a^2}}$ arc (to centre): $E = \frac{\lambda}{4\pi\epsilon_0 r} (2\sin\frac{\theta}{2})$ ring (perpendicular): $E = \frac{qz}{4\pi\epsilon_0(z^2+R^2)^{3/2}}$ round disk (perpendicular): $E = \frac{\sigma}{2\epsilon_0}(1-\frac{z}{\sqrt{z^2+R^2}})$ electrostatic force in a field: $\mathbf{F} = q\mathbf{E}$ (signed)

Gauss' law

Gauss' law: $\Phi_E = \oiint \mathbf{E} \cdot d\mathbf{S} = \frac{q}{\epsilon_0}$ conducting surface: $E = \frac{\sigma}{\epsilon_0}$ nonconducting surface: $E = \frac{\sigma}{2\epsilon_0}$ straight rod: $\frac{\lambda}{2\pi r\epsilon_0}$ two conducting plates (+ greater): $|E_L| = |E_R| = |E_{(+)} - E_{(-)}|, |E_{\rm in}| = E_{(+)} + E_{(-)} = \frac{\sigma_1 + \sigma_2}{\epsilon_0}$ shell: $E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$ (outside), E = 0 (inside) sphere: $E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$ (outside), $E = \left(\frac{q}{4\pi\epsilon_0 R^3}\right) r$ (inside) cylinder: $E = \frac{R^2 \rho}{2\epsilon_0 r}$ (outside), $E = \frac{\rho}{2\epsilon_0} r$ (inside)

Potential

work: $W = \int \mathbf{F} \cdot d\mathbf{s} = q_0 \int \mathbf{E} \cdot d\mathbf{s}$ electric potential difference: $\Delta V = -\frac{W_{if}}{q_0} = \frac{\Delta U}{q_0}$ E-V relation: $\mathbf{E} = -\nabla V$, $V = -\int_{i_0}^{f} \mathbf{E} \cdot d\mathbf{s}$ electric field of parallel plates: $E = \frac{\Delta V}{\Delta d}$ point charge: $V = \frac{1}{4\pi\epsilon_0} \frac{q}{r}$ (signed) discrete points: $V = \frac{1}{4\pi\epsilon_0} \sum_i \frac{q_i}{r_i}$ continuous charge: $V = \frac{1}{4\pi\epsilon_0} \int \frac{dq}{r}$ rod (perpendicular to one end): $V = \frac{\lambda}{4\pi\epsilon_0} \ln(\frac{L + (L^2 + d^2)^{1/2}}{d})$ arc (to centre): $V = \frac{\lambda \theta}{4\pi\epsilon_0}$ ring (perpendicular): $V = \frac{q}{4\pi\epsilon_0 \sqrt{z^2 + R^2}}$ disk (perpendicular): $V = \frac{\sigma}{2\epsilon_0}(\sqrt{z^2 + R^2} - z)$

Current and circuits

current: $i = \frac{dq}{dt}$ current density: J = i/Arelation: $i = \iint \mathbf{J} \cdot d\mathbf{A}$ draft speed: $\mathbf{v}_{\rm d} = \mathbf{J}/(ne)^{(4)}$ resistance law: $R = \frac{V}{4}$ isotropic resistivity: $\rho = E/J$ relation: $\mathbf{E} = \rho \mathbf{J}$ conductivity: $\sigma = 1/\rho$ resistance: $R = \rho \frac{L}{A}$ variation with temperature: $\rho - \rho_0 = \rho_0 \alpha (T - T_0)^{(5)}$ $T_0 = 293 \,\mathrm{K}, \, \rho_0 = 1.69 \,\mu\Omega \cdot \mathrm{cm}$ rate of electricity supply: P = iVresistive dissipation: $P = i^2 R = \frac{V^2}{R}$ electromotive force: $\varepsilon = \frac{dW}{da}$ supplying current: $i = \frac{\varepsilon}{R}$

Kirchhoff's circuit laws

resistance rule: $\Delta V = -iR$ (current), $\Delta V = +iR$ (opposite) emf rule: $\Delta V = +\varepsilon$ (current), $\Delta V = -\varepsilon$ (opposite)

series charge: $q = q_1 = q_2 = \dots$ parallel charge: $q = \sum_{i} q_{i}$ series current: $i = i_1 = i_2 = \dots$ parallel current: $i = \sum_{i} i_{i}$ series voltage: $V = \sum_{i} V_{i}$ parallel voltage: $V = V_1 = V_2 = ...$ series resistance: $R = \sum_{i} R_{i}$ parallel resistance: $\frac{1}{R} = \sum_{j} \frac{1}{R_{i}}$, two: $R = \frac{R_{1}R_{2}}{R_{1} + R_{2}}$

Capacitance

capacitance: $C=\frac{q}{V}$ parallel-plate: $C=\epsilon_0\frac{A}{d}$ cylindrical: $C=2\pi\epsilon_0L\frac{1}{\ln(\mathrm{b/a})}$ spherical: $C=4\pi\epsilon_0\frac{ab}{b-a}$ isolated sphere: $C=4\pi\epsilon_0R$ series capacitor: $\frac{1}{C}=\sum_j\frac{1}{C_j}$ parallel capacitor: $C=\sum_jC_j$ potential energy: $U=\frac{q^2}{2C}=\frac{1}{2}CV^2$ volume energy density: $u=\frac{1}{2}\epsilon_0E^2$ q unchanged: $U_f=U_i/\kappa$ V unchanged: $U_f=\kappa U_i$

RC circuit

charging equation: $R\frac{dq}{dt} + \frac{q}{C} = \varepsilon$ charge function: $q = C\varepsilon(1 - e^{-t/\tau_C})$ current function: $i = (\frac{\varepsilon}{R})e^{-t/\tau_C}$ discharging equation: $R\frac{dq}{dt} + \frac{q}{C} = 0$ charge function: $q = q_0e^{-t/\tau_C}$ current function: $i = -i_0e^{-t/\tau_C}$ capacitive time constant $\tau_C = RC$

Magnetism

force due to moving charge: $\mathbf{F}_B = q\mathbf{v} \times \mathbf{B}$ force due to current-carrying wire: $\mathbf{F}_B = i\mathbf{L} \times \mathbf{B}$ L along direction of conventional i circular motion under F_B : $qvB = m\frac{v^2}{r}$ period: $T = \frac{2\pi m}{qB}$ Hall effect, density of carriers: $n = \frac{Bi}{Vle}$ l = A/d: thinkness of strip Biot-Savart law: $d\mathbf{B} = \frac{\mu_0}{4\pi} \frac{id\mathbf{s} \times \mathbf{r}}{r^3}$ vacuum permeability: $\mu_0 = 4\pi \cdot 10^{-7} \mathrm{T} \cdot \mathrm{m/A}$ (H/m) arc (to centre): $B = \frac{\mu_0 i\theta}{4\pi R}$

Ampere's circuital law: $\oint \mathbf{B} \cdot d\mathbf{s} = \mu_0 i$ long straight wire: $B = \frac{\mu_0 i}{2\pi r}$ solid wire: $B = \frac{\mu_0 i}{2\pi r}$ (outside), $B = (\frac{\mu_0 i}{2\pi R^2})r$ (inside) ideal solenoid: $B = \mu_0 i_0 n$, n = N/L: turns per unit length ideal toroid: $B = \frac{\mu_0 i_0 N}{2\pi r}$

induced emf: $\varepsilon = -\frac{d\Phi_B}{dt} = -\frac{d}{dt} \iint \mathbf{B} \cdot d\mathbf{S}$ for coils: $\varepsilon = -N\frac{d\Phi_B}{dt}$ Maxwell-Faraday equation: $\oint \mathbf{E} \cdot d\mathbf{s} = -\frac{d}{dt} \iint \mathbf{B} \cdot d\mathbf{S}$ induced electrodynamic field, circle: $E = \frac{R^2}{2} \frac{dB}{dt} \frac{1}{r} \text{ (outside)}, E = \frac{1}{2} \frac{dB}{dt} r \text{ (inside)}$

Inductance

 $\begin{array}{l} \text{inductance: } L = \frac{N\Phi_B}{i} \\ \text{solenoid: } L/l = \mu_0 n^2 A \\ \text{toroid: } L = \frac{\mu_0 N^2 h}{2\pi} \ln \left(\frac{b}{a}\right) \\ \text{self-induced emf: } \varepsilon_L = -L \frac{di}{dt} \\ \text{potential energy: } U_B = \frac{1}{2} L i^2 \\ \text{energy density: } u_B = \frac{B^2}{2\mu_0} \end{array}$

LR circuit

rise in current: $iR + L\frac{di}{dt} = \varepsilon$ current function: $i = \frac{\varepsilon}{R}(1 - e^{-t/\tau_L})$ decay in current: $iR + L\frac{di}{dt} = 0$ current function: $i = i_0 e^{-t/\tau_L}$ inductive time constant: $\tau_L = L/R$

series inductance: $L = \sum_j L_j$ parallel inductance: $\frac{1}{L} = \sum_j \frac{1}{L_j}$ mutual induction, two coils: $\varepsilon_2 = -M \frac{di_1}{dt}, \ \varepsilon_1 = -M \frac{di_2}{dt}$

LC oscillation definition: $\frac{d^2q}{dt^2} + \frac{1}{LC}q = 0$

charge function: $q=Q\cos(\omega t+\phi)$ angular frequency: $\omega=\frac{1}{\sqrt{LC}}$ electric potential energy: $U_E=\frac{Q^2}{2C}\cos^2(\omega t+\phi)$ magnetic potential energy: $U_B=\frac{Q^2}{2C}\sin^2(\omega t+\phi)$ total energy: $U=\frac{Q^2}{2C}$

series RLC oscillation

net energy dissipation: $\frac{dU}{dt} = -i^2 R$ definition: $\frac{d^2q}{dt^2} + \frac{1}{LR} \frac{dq}{dt} + \frac{1}{LC} q = 0$ charge function: $q = Q e^{Rt/2L} \cos(\omega' t + \phi)$ angular frequency: $\omega' = \sqrt{\omega^2 - (R/2L)^2}$

Electromagnetic waves

magnetic field induced by electric field: $\oint \mathbf{B}_E \cdot d\mathbf{s} = +\mu_0 \epsilon_0 \frac{d\Phi_E}{dt} = +\mu_0 \epsilon_0 \frac{d}{dt} \iint \mathbf{E} \cdot d\mathbf{S}$ "displacement current"between parallel plates, circle: $B = \frac{\mu_0 \epsilon_0 R^2}{2} \frac{dE}{dt} \frac{1}{r} \text{ (outside)}, \ \frac{\mu_0 \epsilon_0}{2} \frac{dE}{dt} r \text{ (inside)}$ displacement current: $i_d = \epsilon_0 \frac{d\Phi_E}{dt}$

Electromagnetic waves

B and E are in phase: $E = E_m \sin(kx - \omega t)$ $B = B_m \sin(kx - \omega t)$ magnitude ratio: $\frac{E_m}{B_m} = c$ speed of light: $c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$ direction of wave/poynting vector: $\mathbf{S} = \frac{1}{\mu_0} \mathbf{E} \times \mathbf{B}$ plane wave's instantaneous flow rate: $S = \frac{1}{c\mu_0} E^2$ (S = P/A) wave intensity: $I = \overline{S} = \frac{1}{c\mu_0} E_{\mathrm{rms}}^2$ momentum of light:

 $\Delta p=\frac{\Delta U}{c}$ (total absorption), $\Delta p=\frac{2\Delta U}{c}$ (total reflection) radiation pressure:

 $p_r=\frac{I}{c}$ (total absorption), $p_r=\frac{2I}{c}$ (total reflection) law of Malus: $I=I_m\cos^2\theta$

\mathbf{AC}

resistive circuit: $V_R = I_R R$ capacitive circuit: $V_C = I_C X_C$ capacitive reactance: $X_C = \frac{1}{\omega C}$ inductive circuit: $V_L = I_L X_L$ inductive reactance: $X_L = \omega L$

series RLC circuit

wave speed: $c = \frac{\omega}{k}$

where RLC circuit current: $i = I \sin(\omega t - \phi)$ voltage: $\varepsilon = v_R + v_C + v_L$ current amplitude: $I = \frac{\varepsilon_m}{Z}$ impedance $Z = \sqrt{R^2 + (X_L - X_C)^2}$ phase constant: $\tan \phi = \frac{V_L - V_C}{V_R} = \frac{X_L - X_C}{R}$ average power: $\overline{P} = I_{\rm rms}^2 R = \varepsilon_{\rm rms} I_{\rm rms} \cos \phi$ I is in phase with v_R ; leads v_C by 90°, lags hehind v_L by 90°

ideal transformer (rms)

voltage: $\frac{V_s}{V_p} = \frac{N_s}{N_p}$ (AC supply at p end, sends to s end) current: $\frac{I_s}{I_p} = \frac{N_p}{N_s}$ resistances: $R_{eq} = (\frac{N_p}{N})^2 R$ (R at s)

Dipoles

electric dipole electric dipole $\begin{array}{l} \text{electric dipole} \\ \text{electric field produced: } E = \frac{1}{2\pi\epsilon_0} \frac{p}{z^3} \text{ (dipole axis)} \\ \text{electric potential: } V(\theta) = \frac{1}{4\pi\epsilon_0} \frac{p\cos\theta}{r^2} \\ \text{net torque: } \boldsymbol{\tau} = \mathbf{p} \times \mathbf{E} \\ \text{potential energy: } U(\theta) = -\mathbf{p} \cdot \mathbf{E} \\ \text{dipole moment: } \mathbf{p} = q\mathbf{d} \text{ (-to +)} \\ \end{array}$

magnetic dipole/current loop magnetic field produced: $\mathbf{B} = \frac{\mu_0}{2\pi} \frac{\mu}{z^3}$ net torque: $\boldsymbol{\tau} = \boldsymbol{\mu} \times \mathbf{B}$

potential energy: $U(\theta) = -\mu \cdot \mathbf{B}$ magnetic dipole moment: $\mu = Ni\mathbf{A}, N$: turns

Maxwell's equations

Gauss' law: $\oiint \mathbf{E} \cdot d\mathbf{S} = q/\epsilon_0$ Gauss' law: $\nabla \cdot \mathbf{E} = \rho/\epsilon_0$

Gauss' law for magnetism: $\oiint \mathbf{B} \cdot d\mathbf{S} = 0$ Gauss' law for magnetism: $\nabla \cdot \mathbf{B} = 0$

Maxwell-Faraday equation: $\oint \mathbf{E} \cdot d\mathbf{s} = -\frac{d}{dt} \iint \mathbf{B} \cdot d\mathbf{S}$

Maxwell-Faraday equation: $\nabla \times \mathbf{E} = -\frac{d\mathbf{B}}{dt}$

Ampere's circuital law: $\oint \mathbf{B} \cdot d\mathbf{s} = \mu_0 i + \mu_0 \epsilon_0 \frac{d}{dt} \iint \mathbf{E} \cdot d\mathbf{S}$

Ampere's circuital law: $\nabla \times \mathbf{B} = \mu_0 \mathbf{J} + \mu_0 \epsilon_0 \mathbf{E}$

electric displacement: $\mathbf{D} = \epsilon \mathbf{E}$ magnetic field: $\mathbf{H} = \mathbf{B}/\mu$

Magnets

magnetism due to spinning electron spin angular momentum: $S=\frac{h}{4\pi}=5.2729\times 10^{-35} {\rm J/s}$ spin magnetic moment: $\mu_S=\mu_B=\frac{eh}{4\pi m}=9.27\times 10^{-24} {\rm J/T}$ magnetism due to orbital motion orbital angular momentum: $L_{\rm orb}=mvr$ orbital magnetic moment: $\mu_{\rm orb}=\frac{1}{2}evr$ negative charge: $\mu_{\rm orb}=-\frac{e}{2m}L_{\rm orb}$

Optics

Geometric optics

law of reflection: $\theta_1 = \theta_2$ law of refraction: $n_1 \sin \theta_1 = n_2 \sin \theta_2$ total internal refraction, critical angle: $\theta_c = \sin^{-1}(\frac{n_2}{n_1})$ (incident from greater n_1) Brewster angle: $\theta = \tan^{-1}(\frac{n_2}{n_1})$ (incident from n_1)

spherical mirror (Real side is where reflected) focus: $f = \frac{r}{2}$ (+: concave, -: convex) relationship of object, image distance: $\frac{1}{p} + \frac{1}{i} = \frac{1}{f}$ (+: Real side, upright; -: Virtual side, inverted) (p is +) lateral magnification: $|m| = \frac{h_{\text{image}}}{h_{\text{obj}}}, m = -\frac{i}{p}$ (+: same orientation; -: opposite) spherical refracting surface (Real side is where refracted)

spherical refracting surface (Real side is where refracted) relationship: $\frac{n_1}{p}+\frac{n_2}{i}=\frac{n_2-n_1}{r}$ (p is +)

thin lens

relation 1:
$$\frac{1}{p} + \frac{1}{i} = \frac{1}{f}$$

relation 2: $\frac{1}{f} = (n-1)(\frac{1}{r_1} - \frac{1}{r_2})$
 $(n = n_{\text{lens}}/n_{\text{medium}}, r_1$: first side light goes through)

angular magnification, simple magnifer: $m_{\theta} = \frac{15 \text{ cm}}{f}$ angular magnification, refracting telescope: $m_{\theta} = -\frac{f_{\text{ob}}}{f_{\text{eye}}}$ magnification, compound microscope: $M = -\frac{|f'_{\text{ob}} - f_{\text{eye}}|}{f_{\text{ob}}} \frac{15 \text{ cm}}{f_{\text{eye}}}$

Interference and diffraction

index of refraction: $n=\frac{c}{v}$ wavelength in medium: $\lambda_n=\frac{\lambda}{n}$ two mediums, same light, number of wavelength difference: $N_2-N_1=\frac{L}{\lambda}(n_2-n_1)$

double-slit interference

fully constructive: $d\sin\theta = m\lambda, m = 0, 1, 2, ...$ fully destructive: $d\sin\theta = (m + \frac{1}{2})\lambda, m = 0, 1, 2, ...$ illumination intensity: $I = 4I_0\cos^2(\frac{1}{2}\phi), \ \phi = \frac{2\pi d}{\lambda}\sin\theta$ (I_0 : intensity of one slit when the ohter covered, d: separation of slits), $\overline{I} = 2I_0$

real double-slit

intensity:
$$I = I_m \underbrace{\left(\cos^2 \beta\right)}_{\text{intfr}} \underbrace{\left(\sin \alpha/\alpha\right)^2}_{\text{diffr}}$$

$$\beta = \left(\frac{\pi d}{\lambda}\right) \sin \theta, \ \alpha = \left(\frac{\pi a}{\lambda}\right) \sin \theta$$

multiple slits (N slits)

grating maxima: $d\sin\theta = m\lambda, m = 0, 1, 2, ...$ line width: $\Delta\theta = \frac{\lambda}{Nd\cos\theta}$ dispersion/seperation of lines: $D = \frac{\Delta\theta}{\Delta\lambda} = \frac{m}{d\cos\theta}$ resolving power: $R = Nm = \frac{\lambda}{\lambda\lambda}$

thin film, $n_1, n_3 > n_2$ (incident at n_1) (every larger n of refraction side causes phase change of $\lambda/2$) fully constructive: $2n_2L = (m + \frac{1}{2})\lambda, m = 0, 1, 2, ...$ fully destructive: $2n_2L = m\lambda, m = 0, 1, 2, ...$

single-slit diffraction

intensity minima: $a \sin \theta = m\lambda, m = 1, 2, 3, ...$ intensity maximum: I_m at centre intensity: $I = I_m (\frac{\sin \alpha}{\alpha})^2, \ \alpha = (\frac{\pi a}{\lambda}) \sin \theta \ (a$: width)

Rayleigh's criteria: $\theta_R=1.22\frac{\lambda}{d}$ (d: lens' diameter) seperation of two sources: $\Delta x\approx f\theta$ (f: may be viewing distance)

Modern physics

Special relativity

speed parameter: $\beta=v/c$ Lorentz factor: $\gamma=\frac{1}{\sqrt{1-\beta^2}}$ time dilation: $\Delta t=\gamma\Delta t_0$ length contraction: $L=\frac{L_0}{\gamma}$

conservation of space-time interval:

construction of space-time interval.
$$(\Delta s)^2 = c^2 (\Delta t)^2 - (\Delta x)^2 - (\Delta y)^2 - (\Delta z)^2 = \text{constant}$$
 relation of proper time: $\Delta s = c \Delta \tau$ 4-displacement: $x^\mu(\tau) = [ct(\tau), x(\tau), y(\tau), z(\tau)]$ 4-velocity: $u^\mu = \frac{d}{d\tau} x^\mu = \gamma(v)[c, v]$ magniture of velocity: $|u^\mu| = \sqrt{(u^0)^2 - (u^1)^2} = c$ accleration: $a^\mu = \frac{d}{d\tau} u^\mu \perp u^\mu$ 4-momentum: $p^\mu = mu^\mu = m\gamma[c, v] = [\frac{E}{c}, \gamma mv]$ relativistic kinetic energy: $K = mc^2(\gamma - 1)$ total energy: $E = \gamma mc^2 = mc^2 + K$ rest E kinetic E relations: $E^2 = (pc)^2 + (mc^2)^2, (pc)^2 = K^2 + 2Kmc^2$

Quantum

Photons, particles

single slit experiment:

distance between central and first max: $y = \frac{\lambda L}{d}$ width of central max: $w = 2y = \frac{2\lambda L}{d}$ De Braglie relation: $h = \lambda p = \lambda \sqrt{2mK}$ Planck's constant: $h = 6.626 \cdot 10^{-34} \, \text{m}^2 \cdot \text{kg/s}$ energy of photon: $E = cp = c\frac{h}{\lambda} = hf$ photoelectric effect: $K_{\text{max}} = hf - \phi$ Compton scattering: electron stationary: $\lambda' - \lambda = \frac{h}{mc}(1 - \cos\phi)$ electron head-on: $\lambda' \approx \frac{hc}{E^c} \left[1 + \frac{m_e^2 c^4 \lambda}{4hcE^c} \right]$

blackbody radiation (low frequency)

distribution finding entities with energy E:

$$p_E(E) = \frac{1}{KT}e^{-E/kT}$$

average energy: $\overline{E} = kT$

distribution of number of standing waves per unit volume:

$$p_N(f) = \frac{N(f)}{V} = \frac{8\pi}{c^2} f^2$$

distribution of energy per unit volume

$$p_{E/V}(f) = \frac{E(f)}{V} = \frac{8\pi}{c^3} f^2 kT$$

number of photons in standing wave: $n \approx \frac{kT}{h}$

ultraviolet catastrophe (high frequency)

energy of photons: E = nhf

average energy:
$$\overline{E}(f) = \frac{hf}{e^{hf/kT}-1}$$

distribution of number of standing waves per unit volume:

$$p_N(f) = \frac{8\pi f^2}{c^3} \frac{hf}{e^{hf/kT} - 1}$$
$$p_N(\lambda) = \frac{8\pi hc}{\lambda^5} \frac{1}{e^{hc/\lambda kT} - 1}$$

confining standing waves

probability distribution of finding particle: $p(x) = |\Psi(n)|^2$

wavelength, ground state: $\lambda_0 = 2L$

momentum, ground state: $p_0 = \frac{h}{2L}$

energy, ground state: $E_0 = \frac{h^2}{8L^2m}$

wavelength, excited state: $\lambda_n = \frac{\lambda_0}{n}$, n = 1, 2, ...

momentum, excited state: $p_n = np_0$, n = 1, 2, ...energy, excited state: $E_n = n^2 E_0$, n = 1, 2, ...

Heisenberg uncertainty principle: $\Delta x \Delta p \geq \frac{h}{4\pi} = \frac{\hbar}{2}$

corollary: $\Delta E \Delta t \propto \hbar$

particle diffraction, max angle: $\Delta \theta_{\text{max}} = \frac{\lambda_0}{I}$

Waves 1

orbit of hydrogen atoms

constructive interference: $2\pi r = n\lambda, n = 1, 2, ...$

Bohr radius: $r_n = a_0 n^2$, $a_0 = \frac{4\pi\epsilon_0 \hbar^2}{me^2} = 0.529 \text{ Å}$

original quantization condition: $p_n = \frac{\hbar}{a_0} \frac{1}{n}, L_n = \hbar n$

total energy: $E_n = -K_n = -\frac{\hbar^2}{2ma_0} \frac{1}{n^2} = -\frac{E_1}{n^2}$

ground state energy: $E_1 = 13.6 \,\text{eV}$

free particle, 2D complex wave: $\Psi(x,t) = Ae^{\frac{1}{\hbar}(px-Et)}$

general Schrödinger equation:

 $i\hbar \frac{\partial}{\partial t} \Psi(x,y,z,t) = -\frac{\hbar^2}{2m} \nabla^2 \Psi(x,y,z,t) + U(x,y,z) \Psi(x,y,z,t)$

time-independent Schrödinger equation:

 $E\Psi(x,y,z) = -\frac{\hbar^2}{2m}\nabla^2\Psi(x,y,z) + U(x,y,z)\Psi(x,y,z)$

probability flux: $\mathbf{J} = \frac{p}{m} \nabla s$

normalisation: $\int |\Psi(x,y,z,t)|^2 dv = 1$

particle bounded by nodes 0, L

potential function: $V(x) = \begin{cases} 0, & 0 \le x \le L \\ \infty, & x < 0 \lor x > L \end{cases}$

momentum: $p_n = \frac{h}{2L}n, n = 1, 2, ...$ energy: $E_n = \frac{h^2}{8mL^2}n^2, n = 1, 2, ...$

wave function, time-independent:

$$\psi_n(x) = \sqrt{\frac{2}{L}} \sin(\frac{n\pi x}{L}), n = 1, 2, ...$$

wave function, time-dependent:
$$\Psi_n(x,t) = \sqrt{\frac{2}{L}} \sin(\frac{n\pi x}{L}) \cdot e^{-\frac{i}{\hbar}E_n t}, n = 1, 2, \dots$$

wave function, time-independent, 3D:

$$\psi_n(x,y,z) = \sqrt{\frac{2}{L}}\sin(\frac{n_x\pi x}{L})\cdot\sqrt{\frac{2}{L}}\sin(\frac{n_y\pi y}{L})\cdot\sqrt{\frac{2}{L}}\sin(\frac{n_z\pi z}{L}), n_i = 1,2,...$$
energy assuming constant time: $E = \frac{\hbar}{2m}\frac{\pi^2}{L^2}(n_x^2 + n_y^2 + n_z^2)$

finite potential well

momentum in regions:

$$p_x = \begin{cases} \pm \sqrt{2mE}, & 0 \le x \le L \\ \pm \sqrt{2m(E - U_0)}, & x < 0 \lor x > L \end{cases}$$
 momentum amplitude: $|p_x| = \hbar k = \sqrt{2m(U_0 - E)}$ tunneling probability: $P_T \approx \alpha e^{-2kL}, \; \alpha = 16 \frac{E}{U_0} (1 - \frac{E}{U_0})$

harmonic oscillator

zero-point energy: $E_0 = \frac{1}{2}hf$

energy at nth level:

$$E_n = (n + \frac{1}{2})hf = \underbrace{nhf}_{\text{number of photons}} + \underbrace{\frac{1}{2hf}}_{\text{zero-point energy}}$$

energy in vacuum: $E_{\text{vac}} = -\frac{hc}{40}L$

quantum numbers

total energy:
$$E_n = -(\frac{1}{4\pi\epsilon_0})^2 \frac{me^4}{2\hbar} \frac{1}{n^2} = -\frac{13.6 \text{ eV}}{n^2}, n = 1, 2, ...$$

magnitude of **L**: $L = \sqrt{\ell(\ell+1)\hbar}, \ell = 1, 2, ..., n-1$
z-projection of **L**: $L_z = m_\ell \hbar, m_\ell = 0, \pm 1, \pm 2, ..., \pm \ell$

End of formula sheet

Version 1.0.1

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