GPU-based DEM code instruction

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Discrete Element Method (DEM)

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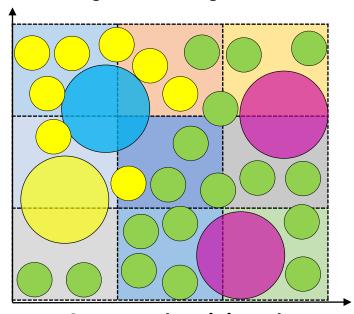
Governing equations: The normal and tangential collisional forces

$$m_i \frac{d\mathbf{v}_i}{dt} = \sum_{j=1}^{k_c} (\mathbf{f}_{c,ij} + \mathbf{f}_{d,ij}) + m_i \mathbf{g}$$

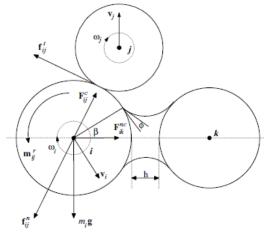
$$I_{i} \frac{d\mathbf{\omega}_{i}}{dt} = \sum_{j=1}^{k_{c}} (\mathbf{M}_{t,ij} + \mathbf{M}_{r,ij} + \mathbf{M}_{n,ij})$$

Table 1. Components of forces and torque acting on particle i

Forces and torques	Symbols	Equations
Normal elastic force	$\mathbf{f}_{\mathrm{cn,ij}}$	$-\frac{4}{3}E^*\sqrt{R^*}\boldsymbol{\delta}_n^{3/2}\mathbf{n}$
Normal damping force	$\mathbf{f}_{dn,ij}$	$-c_n(8m_{ij}E^*\sqrt{R^*\boldsymbol{\delta}_n})^{1/2}\mathbf{v}_{n,ij}$
Tangential elastic force	$\mathbf{f}_{\mathrm{ct,ij}}$	$-\mu_{s} \left \mathbf{f}_{cn,ij} \right (1 - (1 - \boldsymbol{\delta}_{t} / \boldsymbol{\delta}_{t,\text{max}})^{3/2}) \boldsymbol{\delta}_{t} (\boldsymbol{\delta}_{t} < \boldsymbol{\delta}_{t,\text{max}})$
Tangential damping force	$\mathbf{f}_{\mathrm{dt,ij}}$	$-c_{t}(6\mu_{s}m_{ij}\left \mathbf{f}_{cn,ij}\right \sqrt{1-\left \mathbf{V}_{t}\right /\boldsymbol{\delta}_{t,\max}}/\boldsymbol{\delta}_{t,\max})^{1/2}\mathbf{v}_{t,ij} (\boldsymbol{\delta}_{t}<\boldsymbol{\delta}_{t,\max})$
Coulumb friction force	$\mathbf{f}_{t,ij}$	$-\mu_{s}\left \mathbf{f}_{cn,ij}\right \mathbf{\delta}_{t}\left(\mathbf{\delta}_{t}\geq\mathbf{\delta}_{t,\max} ight)$
Torque by normal force	$\mathbf{M}_{\mathrm{n,ij}}$	$\mathbf{R}_{ij}\!\times\!(\mathbf{f}_{cn,ij}+\!\mathbf{f}_{dn,ij})$
Torque by tangential force	$\mathbf{M}_{\mathrm{t,ij}}$	$\mathbf{R}_{ij}\!\times\!(\mathbf{f}_{ct,ij}^{}+\!\mathbf{f}_{dt,ij}^{})$
Rolling friction torque	$\mathbf{M}_{\mathrm{r,ij}}$	$\mu_{r,ij}R_{i}\left \mathbf{f}_{n,ij}\right \hat{\mathbf{o}}_{t,ij}^{n}$



Computational domain



Forces acting on particle *i*

CPU-DEM and GPU-DEM

CPU-based DEM

 Number of particles < 300,000, computation time: Days to months.

2) Complex particulate systems:

Complex geometries

Complex wall movements

Particle shapes

Particle size distribution

GPU-based DEM:

- Deal with billions of particles with high efficiency
- Complex system with funcitons:

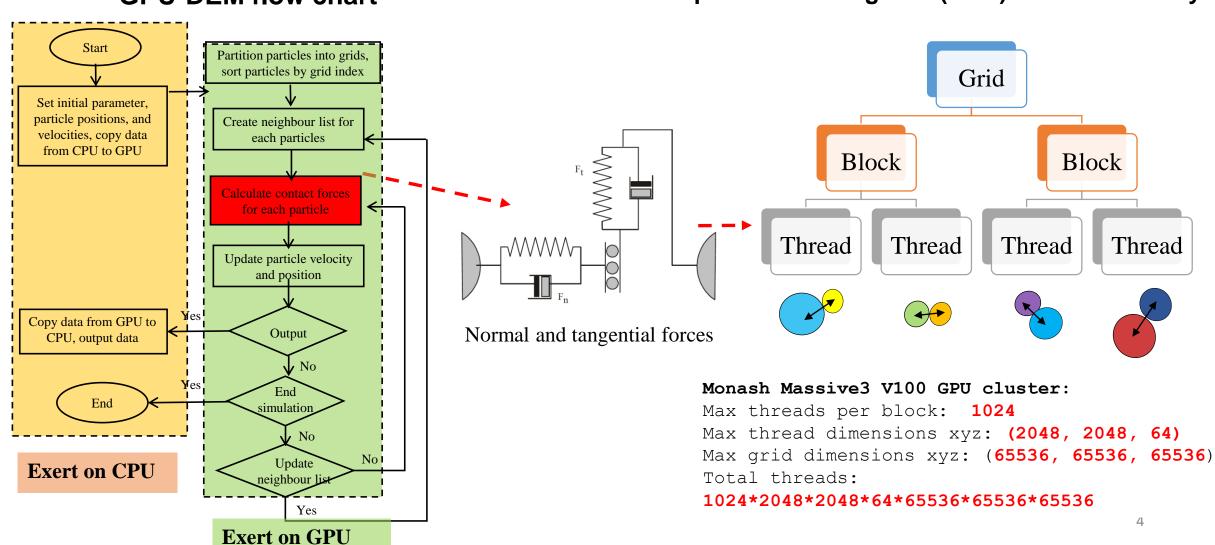
 arbitrary wall geometry, non-spherical particles,
 wide size distribution, CFD-GPU-DEM



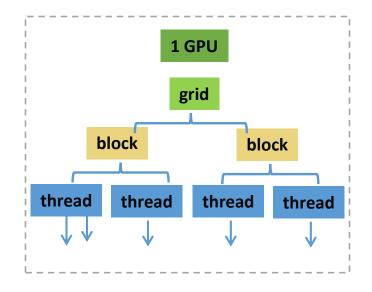
GPU-DEM

GPU-DEM flow chart

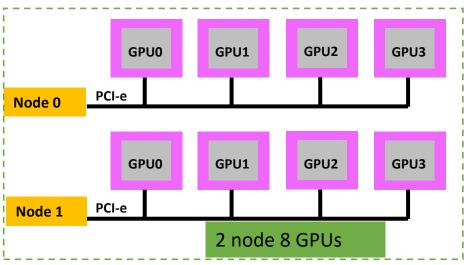
Graphic Processing Unit (GPU) thread hierarchy:



GPU Thread hierarchy:

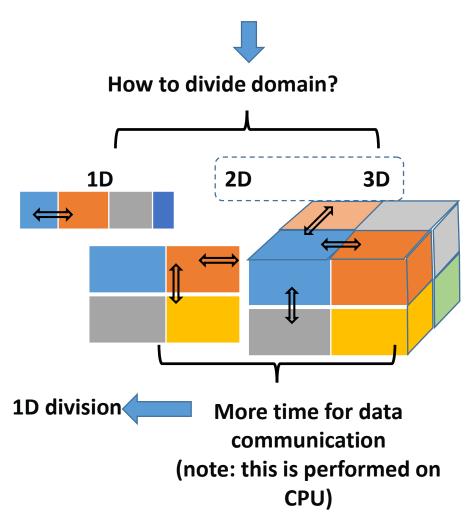


Multiple GPUs:

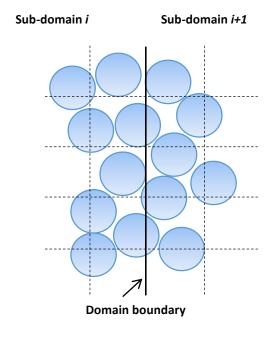


MPI-GPU-DEM (not applicable to current code)

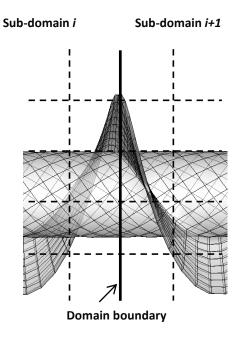
Computation domain



Particles at the domain boundary Wall surfaces at the domain boundary



Send/receive particle information: Position, velocity, temperature, etc. to/from Neighbour domain



Send/receive wall information: vertex, surface

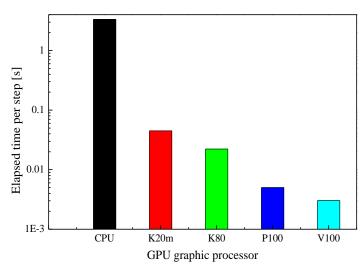
GPU - DEM

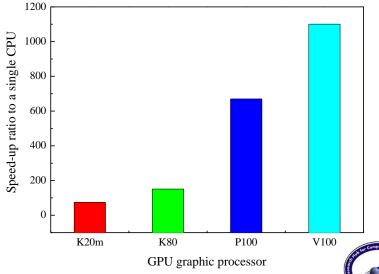
Specification of different GPU graphic processors

Model name	Tesla K20m (UNSW)	Tesla K80 (Massive 3)	Tesla P100 (Massive 3)	Tesla V100 (Massive 3)
Memory clock, GHz	2.6	5	715	876
Maximum band width,	208	480	732.2	897.0
GB/s				
Peak performance of	1.17	2.91	4.763	7.066
double precision, TFlops				

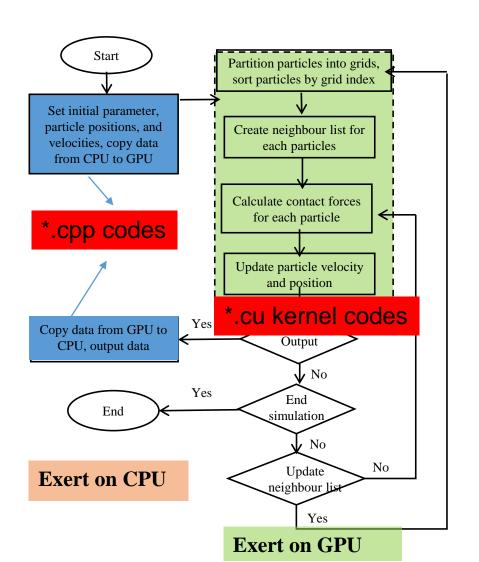
For the **homogenous** case of packing in a rectangular box with 300,000 spheres:

Speed-up ratio of V100 to a single CPU >1000 times





GDEM code implementation



Three layers:

- 1) *.cpp codes: e.g., dempacking.cpp (call other codes inside it) run on CPU for case setting: read input data, set initial variables, set material/feed stream properties. set boundary conditions (meshes). set operation conditions (mesh movements: translation, rotation and vibration) write data to output files allocate/copy data between CPU and GPU/ free data arrays 2) *.cu codes: e.g., dempacking.cu call *.cu kernel codes. 3) *.cu kernel codes: e.g. neiglist.cu
- run on GPU devices. __device__ , __global__
 to run key DEM steps,
 parallelized by particles or grids or contact pairs: e.g., each thread calculate the neighbor list of a particle, each thread calculate the

contact between a contact pair

1) Initialization DEM

```
input
// GPU start
    InitialCUDA();
    AllocateGPUArray();
                              Global GPU arrays
    AllocateCollisionArray();
                              allocation
    CopyConstantsToCUDA();
//--- treat mesh data, once for all--
    TreatMesh();
                                            CPU array allocation
    ReadRestartData();
                                            /initialization
    if(nrestart==0)
    ReadParticleData();
    AllocateGPUParticleArrays();
                              Restart simulation
    CopyDataHostToDevice();
                              from previous
m_hiall_total=1;
                               existing data
```

```
int main(int argc, char* argv[])
  MPI Init(&argc,&argv);
  StartupMPI();
   readinputparameters();
   readmaterialproperties(); //get diam
  SetMatMaxRad();
   SetConstants();
   readmeshinfo();
   SetGeometryBoundary();
   readfeedinfo();
   SetFeedArrays();
   readmovementinfo();
      SetParNumInDomain(&ntot,&m maxIlistntot);
      AllocateCPUParticleArray(ntot);
      AllocateCPUNeigListArray(m_maxIlistntot);
       InitialCPUParticleArray(ntot);
       InitialCPUNeigListArray(m maxIlistntot);
      AllocateMaterialArray();
      InitialMaterialArray();
      InitialGlobalVar();
  allocatebuf=ntot;
 m maxIlistbuf=allocatebuf*10;
 AllocateMPIParticleBuffer(allocatebuf); //newly added
```

2) Run DEM iteration

2-1): for each time step it, check if we need to add particles into domain,

if yes, add, else continue other steps.

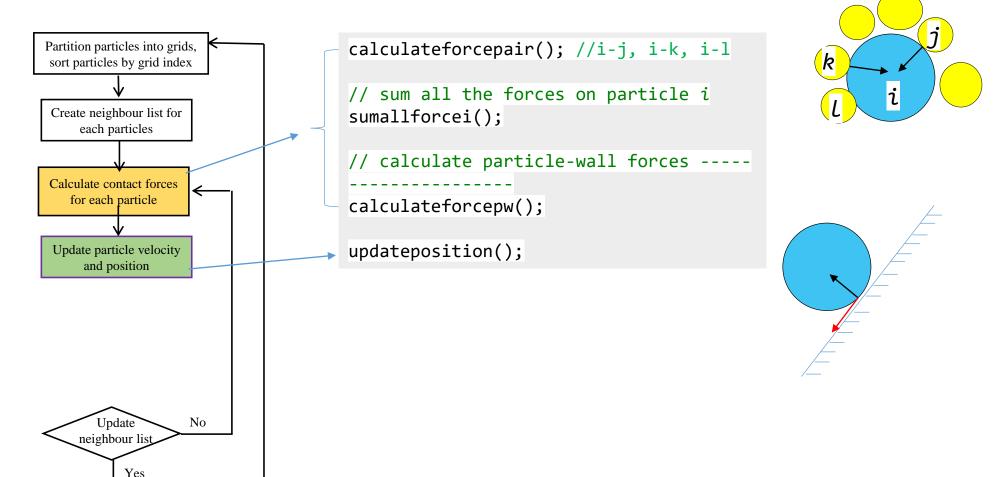
```
while( it< tstop)</pre>
     it=it+1;
     timet=dt*it;
     tsd=(it)*real dt;
// poured packing
     FeedId=IsTimeToFeed();
     if(FeedId<NumOfFeed)</pre>
// add particles to system
        itime++;
       if(it==1|| itime>tnewpar)
         itime=0;
         m_oldnumParticles=m_numParticles;
```

• 2-2) key DEM steps 1-2

```
Partition particles into grids,
                             sort particles by grid index
                              Create neighbour list for
                                   each particles
                              Calculate contact forces
                                 for each particle
Exert on GPU
                               Update particle velocity
                                    and position
                                          if(m hiall total>0)
                                      Update
                                   neighbour list
                                          Yes
```

```
if(m hiall total>0)
/// calculate hash
   calcHash();
// sort particles based on hash--
    RadixSort();
   findBoundryNum( ); //check if particles are in the boundary or halo
or inside
TreatBoundHalo();
ReOrderParticleArrays(); //if out side, remove it, and reset particle
index for others.
mpiDataSendRecv();
calculateCN(); //calculate how many particles around particle I
according particle size
prefixsumCN( ); //calculate to CN and start of totalCN for i
findBCellStart( ); //to getm dCellStart, m dCellStartB
neighborarray(); // to get m dAnei, m dnjgi, m dnjli
prefixsum( );
pairlist();
// updated neighbour list
m hiall=0;
if(idelete==1)idelete=0;
```

• 2-3) key DEM steps 3-4



• 2-4) output data for post-processing

Steps:

- 1) Set Output frequency (set in input data), important, will affect data file size
- 2) List variables to output, copy data from GPU to CPU
- 3) Output from to data file according to visualization data file format.

```
if(it==1 || (it%freqppor)==0 && m_numParticles>=0)
{
   WriteDataToPpor();
   if(m_hminhz_total<hmax-2.0 && hminflag==1)
    WriteOutEngdsp();
}
//-----
if(it==1 || it%freqparticle==0) //freqoutput
    {
    WriteParticleToTecplot();
   //exit(1);
   }</pre>
```

- 2-4) check if need to end simulation, or if reach CPU wall time,
- If need, free CPU/GPU arrays

```
if(it>=tstop)
{
    FreeGPUData();

FreeCPUData();

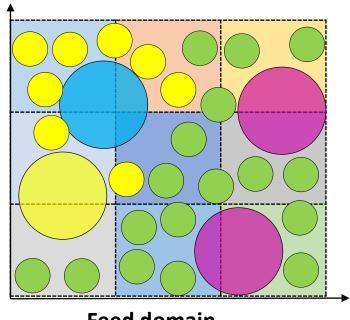
exit(1);
}
} // while, end of iteration
```

Feed.cpp

Materials with a size distribution is add in 3 size groups:

- m_NumAddH
- m_NumAddM
- m_NumAddL

First check if a feed grid is occupied with particles, if no, add Limitation: can not generate dense particle flow.

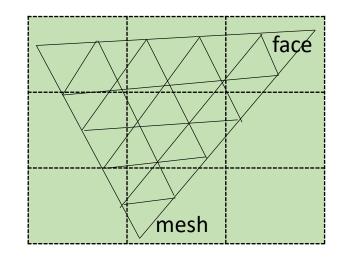


Feed domain

Boundary.cpp

- Set computation domain size and DEM grids
- Treat wall mesh:

to generate a list of possible contact wall faces of a DEM grid



Computation domain

Wall Movement: CPU level

mesh

Movement.cpp

- IsTimeToTranslateHost(),
- IsTimeToRotateHost(),
- vibration():

to check if is time to move wall

RotationPositionConvertHost()

dempacking.cuh:

```
struct Rotation
{
uint meshId;
double starttime;
double endtime;
double3 axis;
double3 pointonaxis;
double rotatespeed;
};
```

WriteData.cpp

```
Rotation
for(j=0;j<Nnode[j];j++)
                                                                  axis
 // treat particle position when they are near or inside the rotary part
   px=m hPosnode[i][j*3];
   py=m hPosnode[i][j*3+1];
   pz=m hPosnode[i][j*3+2];
    int RotateId=IsTimeToRotateHost(it, real_dt,NumOfRotation);
    if(RotateId<NumOfRotation && m hRotation[RotateId].meshId==i)
    double px1,py1,pz1;
    double rotaterate =-m hRotation[RotateId].rotatespeed*2*pi/60*real_dt/dt;
//reduced rotate rate
    double theta=rotaterate*it*dt;
    RotationPositionConvertHost(px,py,pz,m_hRotation[RotateId].axis.x,\
m_hRotation[RotateId].axis.y, m_hRotation[RotateId].axis.z,theta,&px1,&py1,&pz1);
fprintf(fp1,"%10.4f%10.4f%10.4f%2d%2d%2d%2d%2d%2d\n",px1*diam,py1*diam,pz1*d
iam,0,0,0,0,0,0);
    else
  fprintf(fp1,"%10.4f%10.4f%10.4f%2d%2d%2d%2d%2d%2d\n",
         px*diam,py*diam,pz*diam,0,0,0,0,0,0);
```

dempacking.cu

```
void calcHash(uint prehead, double* Pos, double* rad,
                    particleHash,
                                                                      Parallelized by:
             uint*
             double worldOrigin[3],
                                                                       numBodies (particles, contact pairs,
                    gridSize[3],
             uint
             double cellSize[3],
                                                                      number of DEM grids)
             uint
                    gridSizel[3],
             double cellSizel[3],
                    numBodies)
             int
   int numThreads = min(256, numBodies);
   int numBlocks = (int) ceil(numBodies / (double) numThreads);
   // execute the kernel
                                                                                        *.cu kernel code function
   calcParticleHashD<<<< numBlocks, numThreads >>>(prehead,
                                        numBodies,
                                        (double3 *) Pos,rad,
                                        (uint2 *) particleHash,
                                        make double3(worldOrigin[0],worldOrigin[1],worldOrigin[2]),
                                        make_uint3(gridSize[0], gridSize[1], gridSize[2]),
                                        make_double3(cellSize[0], cellSize[1], cellSize[2]),
                                        make_uint3(gridSizel[0], gridSizel[1], gridSizel[2]),
                                        make double3(cellSizel[0], cellSizel[1], cellSizel[2]));
```

device function:

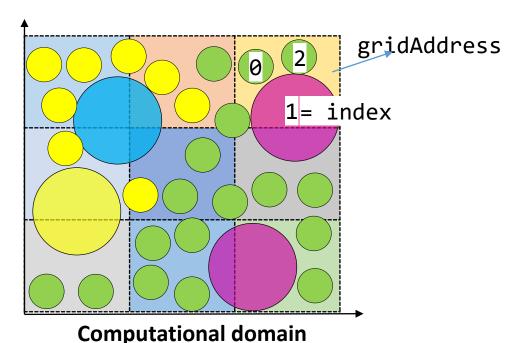
to realize a specific function

```
// calculate position in uniform grid
device int3 calcGridPos(double3 p,
                double3 worldOrigin,
                double3 cellSize
  int3 gridPos;
if(GDiv[0].x==1)
 // gridPos.x = floor((p.x - worldOrigin.x) / cellSize.x);
  gridPos.x = floor((p.x - worldOrigin.x) / cellSize.x)+1; //divide domain in x direction
  gridPos.y = floor((p.y - worldOrigin.y) / cellSize.y);
  gridPos.z = floor((p.z - worldOrigin.z) / cellSize.z);
else if(GDiv[0].z==1)
gridPos.x = floor((p.x - worldOrigin.x) / cellSize.x);
  gridPos.y = floor((p.y - worldOrigin.y) / cellSize.y);
  gridPos.z = floor((p.z - worldOrigin.z) / cellSize.z)+1; //local grid position, divide domain in z
direction
  return gridPos;
```

__global__ function

```
// calculate grid hash value for each particle
global void calcParticleHashD(uint prehead, uint numBodies,
          double3* pos,
          double* rad,
          uint2* particleHash,
           double3 worldOrigin,
                 gridSize,
          uint3
          double3 cellSize,
                 gridSizel,
          uint3
          double3 cellSizel)
   int i = blockIdx.x*blockDim.x + threadIdx.x; //check parallelized by
particles, grids, or pairs
    uint index=i+prehead;
    if(i<numBodies)</pre>
    double3 posi = pos[index];
   int3 gridPos;
    uint gridAddress;
    if(isnan(posi.x))
    gridAddress = 0xffffffff;
    // get address in grid
    if(outlimit(posi)==1) // outside boundary limit
    gridAddress=0xffffffff;
    else
    gridPos = calcGridPos(posi, worldOrigin,cellSizel);
    gridAddress = calcGridAddress(gridPos, gridSizel);
  // store grid hash and particle index
    particleHash[i] = make uint2(gridAddress, index);
```

calcParticleHashD()



Similar functions:

- calcParticleInFeedAreaHD()
- calcParticleInFeedAreaLD()

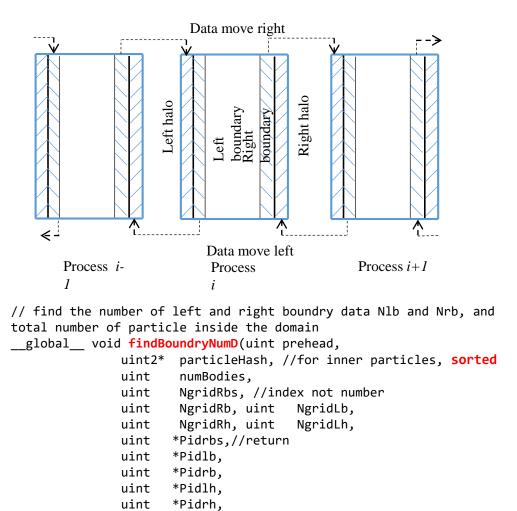
```
// calculate grid hash value for each particle
global void calcParticleHashD(uint prehead, uint numBodies,
         double3* pos,
          double* rad,
          uint2* particleHash,
            double3 worldOrigin,
                 gridSize,
          uint3
          double3 cellSize,
                 gridSizel,
          uint3
          double3 cellSizel)
    int i = blockIdx.x*blockDim.x + threadIdx.x; //check parallelized by
particles, grids, or pairs
    uint index=i+prehead;
    if(i<numBodies)</pre>
    double3 posi = pos[index];
    int3 gridPos;
    uint gridAddress;
    if(isnan(posi.x))
    gridAddress = 0xffffffff;
    // get address in grid
    if(outlimit(posi)==1) // outside boundary limit
    gridAddress=0xffffffff;
    else
    gridPos = calcGridPos(posi, worldOrigin,cellSizel);
    gridAddress = calcGridAddress(gridPos, gridSizel);
  // store grid hash and particle index
    particleHash[i] = make_uint2(gridAddress, index);
```

- RandomAddParticlesHD()
- For each grid in feed area, check
 if(NumParticleInHCell[index
]==0), no particles in the
 cell, then add particle
 position and matId

```
// calculate grid hash value for each particle
global void RandomAddParticlesHD(
          uint oldNumParticle,
          uint *NrandomH,
          uint Nallocate,
          uint Numgrids,
          uint3 gridSize,
          double* rad,
          double radHmax,
           uint FeedId,
          uint* NumParticleInHCell,
          double3* pos,
           uint* matId.
          uint* Addcount)
    // thread number= number of grids to generate in feed area
   int id= blockIdx.x*blockDim.x + threadIdx.x; //local number
    double3 p;
    int3 gridPos;
    if(id<Numgrids)
    int index=NrandomH[id]:
    if(index<Numgrids)</pre>
    if(NumParticleInHCell[index]==0) //no particles in cell
   uint icount=atomicAdd(&Addcount[0],1);
    if(icount<Nallocate)</pre>
if(GDiv[0].x==1)
gridPos.x=(int) index/(gridSize.y*gridSize.z);
    gridPos.z=(int) (index-gridPos.x*gridSize.y*gridSize.z)/gridSize.y;
    gridPos.y=index-gridPos.x*gridSize.y*gridSize.z - gridPos.z*gridSize.y;
    double3 cellSize=2.05*radHmax*make_double3(1.0);
    p.x=(gridPos.x+0.5)*cellSize.x+m dfeedlim[FeedId].xmin;
    p.y=(gridPos.y+0.5)*cellSize.y+m dfeedlim[FeedId].ymin;
    p.z=(gridPos.z+0.5)*cellSize.z+m dfeedlim[FeedId].zmin;
    pos[oldNumParticle+icount]=p;
    matId[oldNumParticle+icount]= m_dfeedlim[FeedId].matId;
    } // if(icount<Nallocate)</pre>
   } //if(NumParticleInHCell[index]==0)
```

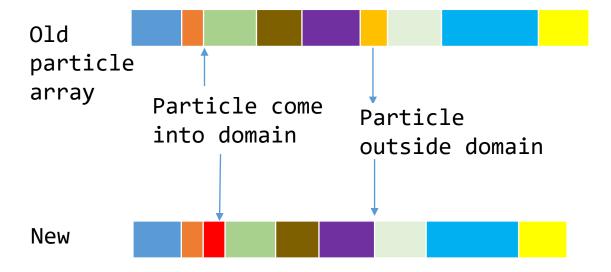
uint* Nin)

MPI



```
// find start of each cell in sorted particle list by comparing with previous hash value
// one thread per particle
__global__ void findBCellStartD(
              uint numBodies,
uint gridStart,uint Ngridlb,uint Ngridrbs,
             Nlh1, uint Nlb1, uint Nrh1, uint Nrb1,
              uint
                    Pidlh,
              uint
                    Pidrh,
                     Pidlb,
              uint
                    Pidrb,
              uint
              uint2* particleHash, //return
              uint* cellStart,//return, include the prehead
              uint* cellStartB //return
   uint i= blockIdx.x*blockDim.x + threadIdx.x; // for all particles
   if(i<numBodies)</pre>
   int cell= particleHash[i].x-gridStart;
  if(Nlh1!=0 && i < Nlh1) // left halo
     if (i > 0)
        if (cell != particleHash[i-1].x-gridStart && cell>=0) cellStartB[cell] = i;
     else
         if (cell>=0) cellStartB[cell] = i;
   else if(Nlb1!=0 && (i >=Pidlh && i < Pidlh+Nlb1)) // left boundry, write data to cellStartB
     if(i > Pidlh)
       if (cell != particleHash[i-1].x-gridStart && cell>=0) cellStartB[cell] = i;
else
        if (cell>=0) cellStartB[cell] = i;
                                              Particle index
                Grid address
```

resortParticleIdD()



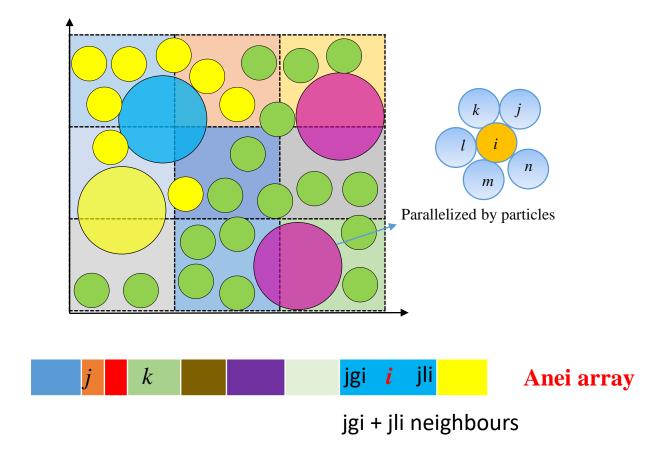
Reorder the particle index for all particle properties arrays (array length=Np)

```
// resort particle index according to cell index
// need to memset both ends of arrays
__global__ void resortParticleIdD(uint numBodies,
               maxCnPerParticle, uint prehead,
           //uint idelete,
    uint Nlh, uint Nrh,
    uint Nlh1, uint Nlb1, uint Nrb1,
           //reserve prehead for the incoming particles
           uint* oldIP,
    uint2* particleHash,uint2* particleHash0,
    double3* pos,double3* oldpos,
    double3* pdis,double3* oldpdis,
    double3* angv,double3* oldangv,
    double* rad, double* oldrad,
    double* rmass,double* oldrmass,
    double* inert,double* oldinert,
    uint *matId,uint* oldmatId,
   double3* disptw, double3* olddisptw,
   double* fricpw,double* oldfricpw,
   uint3* contactEnd, uint3* oldcontactEnd,
   double3* Engdisp, double3* oldEngdisp,
   double* Engdispw, double* oldEngdispw,
   double4* EngdispVarw, double4* oldEngdispVarw)
```

neighborarrayD()

```
global void neighborarrayD(uint prehead,
        uint numBodies,
        uint gridStart,
        uint Ngridlb, uint Ngridrbs,
        uint Ngridlh, uint Ngridrb,
        uint pidlh, uint pidrbs, uint pidrb, uint pidrh,
        uint Nlh1, uint Nlb1, uint Nrb, uint Nrh,
        double* size,
        uint* Cn,
        uint* sumCN.
                 particleHash, //gridadress is global value
        uint*
                 cellStart,
        uint*
                 cellStartB,
                 worldOrigin, //local
        uint3
                gridSizeh,
        uint3
                gridSizel,
        double3 cellSizeh.
        double3 cellSizel,
        int
                 maxCnPerParticle,
        double3* pos, //update here
        double* rad,
// return value
        uint* Anei,
        uint* njgi,
```

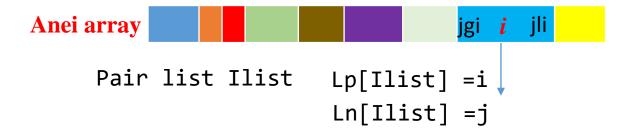
uint* njli)



For each particle i,

- 1) use particleHash to get grid address
 search the neighbor grids (>= 9 in 2D and 27 in 3D)
- 2) For each grid use cellstart to get the neighbor particle index j,k,l, etc.
- 3) Check if distance (i-k)< critical distance of the neighbor list, if yes, add to Anei
- 4) For Anei, if (j>i), add to the beginning (jgi++), else add to the end (jli++), CN[i] makes sure Anei is long enough to hold the total number of neighbor particles

- pairlistD()
- For each particles, create pair list



For each pair i -j, check oldLn[oldllist] if j appears in the oldLn list, if yes, contact in previous time step, set dispt[llist]=olddispt[oldllist]; fricp[llist]=oldfricp[oldllist]; Which will be used in force calculate for the tangential force component.

```
pairlistD(uint
                  prehead,
                                  Pidlh,
                           uint
                                  Pidrb,
                           uint
                           uint
                                 Nlb1,
                                 Nrb1,
                           uint
                           uint
                                   oldIPlength,
                         // int
                                     idelete,
                           uint* Cn,
                           uint* sumCN,
                                   oldIP,
                           uint*
                                  particleHash,
                           uint2*
                          uint*
                                   sjgi,
                           uint*
                                   oldsjgi,
                                   oldLn,// return
                          uint*
                                   Anei,
                           uint*
                           uint*
                                   njgi,
                          uint*
                                   njli,
                          double3 *olddispt,
                          double *oldfricp,
                                   maxCnPerParticle,
                          int
                                   numBodies,
                           uint
   double* oldEngdisppair,
           double* Engdisppair,
   uint* oldcontactEndpair,
   uint* contactEndpair,
                          // return value
                           uint*
                                  Lp,
                           uint*
                                  Ln,
                           double3 *dispt,// return
                           double *fricp)// return
```

• calculateforcepairD()





Parallelized by contact candidate pair

```
// cauculate force and torque for each contact particle pair

calforceij(posi,posj,pdisi,pdisj,angvi,angvj,radi,radj,
rmassi,rmassj,dispti,fricpi,matldi,matldj,
    dt,&newEngdispVarpairi,
&olddispti,&oldfricpi,&icontacti,&fi,&ti,&tj);

if(icontacti==1) //if contact, set force, torque to forcepair array index Ilist {
    forcepair[Ilist] = fi;
    torqpairi[Ilist] = ti;
    torqpairi[Ilist] = tj;
    dispt[Ilist] = olddispti;
    fricp[Ilist] = oldfricpi;
    contactpair[Ilist] = 1;
}
```

```
calculateforcepairD(uint
                              prehead,
                    int totalcontacts,
                   double3* pos,
               double3* pdis,
                double3* angv,
                double* rad,
               double* rmass,
                     uint* matId,
                   uint* Lp,
                   uint* Ln,
                   uint* oldLn,
                    double3 *dispt,
                    double *fricp,
                    double3 *olddispt,
                    double* oldfricp,
    double* oldEngdisppair,
uint* oldcontactEndpair,
   double* Engdisppair,
   double4* EngdispVarpair,//input && output
   double diam,
   double xmin,
   double hmin,
   double hmax,
                    double dt,
                   // return value
                    double3* forcepair,
                    double3* torqpairi,
     double3* torqpairj,
                   double3* pospairi,
                   double3* pospairj,
                    uint* contactpair,
   uint* contactEndpair
```

double3* Engdisp,
double* BriProb)

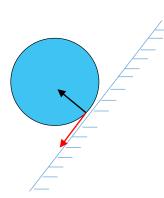
sumallforceiD

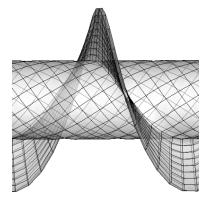
```
sumallforceiD(uint
                      prehead,
uint numBodies,
       maxParticlesPerCell,
int
         totalcontacts,
uint
uint*
       Cn,
       sumCN,
uint*
uint* njgi,
uint* njli,
double3* forcepair,
double3* torqpairi,
                                            Force pair i-j
double3* torqpairj,
uint* contactpair,
uint* Anei,
double fmat, double Wmin, double rmin, double diam,
uint* contactEndpair,
double* Engdisppairi,
double* rad,
// return value
                                            All forces on i
double3* forcei,
double3* torquei,
uint* contacti,
                               m
uint3* contactEnd,
```

```
for(i=0;i<njgi[index];i++)</pre>
 k=Anei[sumCN[index]+i];
  if(k != 0xfffffffff)
  force += forcepair[k];
  torque += torqpairi[k];
  contact += contactpair[k];
for(i=0;i<njli[index];i++)</pre>
 k=Anei[sumCN[index]+Cn[index]-1-i]-numBodies;
  if(k>=0 && k<totalcontacts)</pre>
  force -= forcepair[k];
  torque += torqpairj[k];
  contact += contactpair[k];
```

calculateforcepwD()







Wall mesh

See treatmesh.cu for details

```
uint3* meshSize,
       double3* meshOrigin,
       double3* meshEnd,
       double3 cellSize,
  double3* pos,
  double3* pdis,
  double* rad,
  double* rmass,
  double3* angv,
       // wall input -----
       uint* FaceHashStart,
       uint2* FaceHash.
       uint4* Fnodeid,
       double3* Posnode,
       uint4* sharePE,
       uint* sharePV,
       uint4* Ehead,

   uint* Vhead,

       uint* Nfacestart,
       uint* Nnodestart,
       uint* FaceHstart,
       uint* Meshstart,
        uint NumOfRotation,
        uint NumOfTranslation,
        uint NumOfVibration,
        uint it, double dt,
        double real_dt,
        double diam,
double fmat, double Wmin, double rmin,
double* Engdispw,
double4* EngdispVarw,//input && output
  double xmin,
  double hmin,
  double hmax,
       // return value-----
       double3* disptw,
       double* fricpw,
       double3* force,
       double3* torque,
       uint3* contactEnd,
       double3* Engdisp,
       double* BriProb)
```

calculateforcepwD(uint

numBodies, uint Nmesh,

prehead, uint

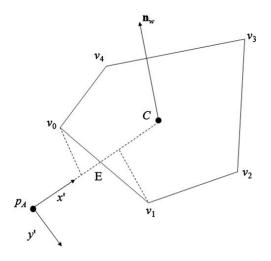
For each particle, use particle position to get grid position and grid address index:

gridPos = calcGridPos(posi,meshOri,cellSize);
gridAddress = calcGridAddress(gridPos,meshSi);

Pre-treat meshes to generate a possible contact list of mesh face index list for each grid address GridIdx, the use FaceHashStart[gridAddress+Meshstart[m]] to get the start Face index of the list, check if particle contact with this face by using hopp_hit(), If contact, calculate p-w forces using calforceiw(), and add forces and torques to particle i

•hopp_hit()

Check if particle contact with mesh face, if yes, return overlap and contact normal direction vector



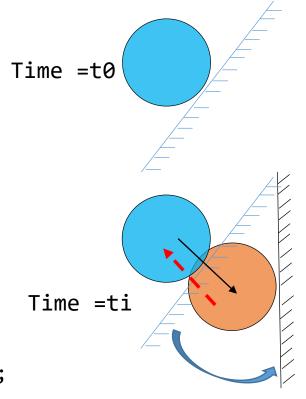
```
device void hopp hit(uint index,
              double3 posi,
              double radi,
              double radmin,
              uint edgenum,
              double3 v1, double3 v2, double3 v3, double3 v4,
              uint4 spe,
              uint4 spv,
             // uint4 spvv,
              uint4 eh,
              uint4 vh,
            // uint4 vhh,
              // return value -----
              short *ihit,
              double4 *disth,
              uint *mark)
```

Ref: Junwei Su, ZhaolinGu, XiaoYunXu. Discrete element simulation of particle flow inarbitrarily complex geometries. Chemical Engineering Science. 66 (2011): 6069-6088

Wall Movement: GPU level

In calculateforcepwD()

```
for(m=0;m<Nmesh;m++) //m=0,fix; m=1,move
// treat particle position when they are near or inside the rotary part
      RotateId=IsTimeToRotate(it, real dt,NumOfRotation);
     if(RotateId<NumOfRotation && m dRotation[RotateId].meshId==m)</pre>
     irotation=RotateId+1;
     rotaterate =-m dRotation[RotateId].rotatespeed*2*pi/60*real dt/dt;
//reduced rotate rate
     theta=rotaterate*it*dt;
     posi=RotationPositionConvert(posi,m_dRotation[RotateId].axis, theta);
     else
     irotation=0;
```



Note: Instead of moving wall, we move particle in the reverse way of wall, then detect contact of particle-wall (then treat interaction vector back), because the contact face list is pretreated in order to reduce computation time.

calforceiw()

Calculate p-w forces and torques according to equations, a wall is treated as a particle

Wall

movements

Forces and torques	Symbols	Equations
Normal elastic force	$\mathbf{f}_{\mathrm{cn,ij}}$	$-\frac{4}{3}E^*\sqrt{R^*}\boldsymbol{\delta}_n^{3/2}\mathbf{n}$
Normal damping force	$\mathbf{f}_{dn,ij}$	$-c_n(8m_{ij}E^*\sqrt{R^*oldsymbol{\delta}_n})^{1/2}\mathbf{v}_{n,ij}$
Tangential elastic force	$\mathbf{f}_{\mathrm{ct,ij}}$	$-\mu_{s} \left \mathbf{f}_{cn,ij} \right (1 - (1 - \boldsymbol{\delta}_{t} / \boldsymbol{\delta}_{t,\text{max}})^{3/2}) \boldsymbol{\delta}_{t} (\boldsymbol{\delta}_{t} < \boldsymbol{\delta}_{t,\text{max}})$
Tangential damping force	$\mathbf{f}_{\mathrm{dt,ij}}$	$-c_{t}(6\mu_{s}m_{ij}\left \mathbf{f}_{cn,ij}\right \sqrt{1-\left \mathbf{V}_{t}\right /\delta_{t,\max}}/\delta_{t,\max})^{1/2}\mathbf{v}_{t,ij}\left(\delta_{t}<\delta_{t,\max}\right)$
Coulumb friction force	$\mathbf{f}_{t,ij}$	$-\mu_{s}\left \mathbf{f}_{cn,ij}\right \mathbf{\delta}_{t}\left(\mathbf{\delta}_{t}\geq\mathbf{\delta}_{t,\max}\right)$
Torque by normal force	$\mathbf{M}_{n,ij}$	$\mathbf{R}_{ij}\!\times\!(\mathbf{f}_{cn,ij}+\!\mathbf{f}_{dn,ij})$
Torque by tangential force	$\mathbf{M}_{\mathrm{t,ij}}$	$\mathbf{R}_{ij} \times (\mathbf{f}_{ct,ij} + \mathbf{f}_{dt,ij})$
Rolling friction torque	$\mathbf{M}_{\mathrm{r,ij}}$	$\mu_{r,ij}R_i\left \mathbf{f}_{n,ij}\right \hat{oldsymbol{lpha}}_{t,ij}^n$

```
device void calforceiw(
       // input from particle index
                double3 posi,
double3 pdisi,
double radi,
double rmassi,
double3 angvi,
              double4 disth,
double3 olddptw,
double oldfcw,
// input value
double dt,
uint itranslate,
uint irotation,
uint ivibrate.
double4 *newEngdispVarw,
// return value
double3 *dptw,
double *fcw,
        double3 *forceiw,
double3 *toriw)
```

updatepositionD()

 At each time step, use updated force and torque of each particle to update the position and (translation and angular) velocity of each particle

```
__global__ void updatepositionD(uint prehead,
       uint numBodies,
       double3* pos, //input, return
       double3* pdis, //input, return
       double3* angv, //input, return
       double* rad,
       double* rmass,
       double* inert,
       double3* force,
       double3* torque,
       double3* qi,
                      //input, return
       double* keng,
       double radmin,
       double dt.
double diam,
double hmin,
       double hmax,
       double xmin,
// return value
        uint* partiall,
double* partminhz,
         double* partmaxhz,
        double* partkeng)//return
```

Data output

WriteParticleToTecplot()

Step 1) copy data from GPU to CPU, gather CPU data to host process for MPI case (not applicable to current code)

```
cpuErrchk(cudaMemcpy(outputpos,m_dpos+m_hprehead*3,m_
numParticles*3*sizeof(double),cudaMemcpyDeviceToHost)
);

MPI_CHECK(MPI_Gatherv(outputpos,m_numParticles*3,MPI_
DOUBLE,hpos_total,count,displs,MPI_DOUBLE,0,MPI_COMM_
WORLD));
    free(outputpos);
```

Step 2) write data to data file path and file name according visualization software data format _____

```
if(rank==0)
   totalNode=0;
   totalFace=0;
   for(i=0;i<Nmesh;i++)</pre>
   totalNode+=Nnode[i];
  totalFace+=Nface[i];
     if((fp1=fopen("output/particle.dat","wb+"))==NULL){
     printf("Cannot open file particle01.dat! %d\n",it);
     exit(0);
 tsd=(it)*real dt;
 sprintf(str1,"%06.3f",tsd);
      if(it==1)
     fprintf(fp1,"TITLE
                          = \"GAMBIT to Fluent File\"\n");
     fprintf(fp1, "VARIABLES = \"X\"\n");
     fprintf(fp1,"\"Y\"\n");
      fprintf(fp1,"\"Z\"\n");
  fprintf(fp1,"\"Velocity\"\n");
      fprintf(fp1,"\"Engdisp\"\n");
  fprintf(fp1,"\"Engdispiiw\"\n");
  fprintf(fp1,"\"Engdispiw\"\n");
     fprintf(fp1,"\"Radius\"\n");
     fprintf(fp1,"\"CollisionNum\"\n");
     fprintf(fp1, "DATASETAUXDATA Common.VectorVarsAreVelocity=\"TRUE\"\n");
    for(i=0;i<Nmesh;i++)</pre>
     fprintf(fp1,"ZONE T=\"ZONEW%s\"\n",m hmeshFile[i].name);
     fprintf(fp1," N=%8d, E=%8d, ZONETYPE=FEQuadrilateral\n", Nnode[i], Nface[i]);
      fprintf(fp1," DATAPACKING=POINT\n");
      fprintf(fp1," AUXDATA Common.BoundaryCondition=\"Wall\"\n");
      fprintf(fp1," AUXDATA Common.IsBoundaryZone=\"TRUE\"\n");
      fprintf(fp1," DT=(DOUBLE DOUBLE DOUBLE )\n");
```

Tecplot format

Dimensionless parameters



Parameters are reduced/dimentionless in the code, need to be vonvert to the real when output variables:

```
    Particle size, length related variables: reduced by "diam"
        m_hfeedpro[i].xmin /=diam;
        m_hfeedpro[i].xmax /=diam;
    Time step: real_dt=dt*sqrt(diam/9.81); // in initialization.cpp
    Velocity: vel_real =vel_reduced*sqrt(gg*diam)/dt;
        In WriteParticleToTecplot():
        Double velmag=sqrt(hVel_total[3*i]*hVel_total[3*i]+hVel_total[3*i+1]*hVel_total[3*i+1]+hVel_total[3*i+2]*hVel_total[3*i+2]);
        velmag=velmag*sqrt(gg*diam)/dt; //unit m/s
```

• Forces: reduced by fac

Write data for rerun

- Copy data from GPU to CPU before write.
- Write all the variables needed for rerun to data file, e.g. "preflow.dat" file

```
void WriteParticleForRerun()
                     sprintf(str1,"%02d",rank);
                     sprintf(str,"preflow%s.dat",str1);
                       if((fp1=fopen(str,"wb+"))==NULL)printf("Cannot open file %s!",str);
                       it,m numParticles,m_totalcontacts,itime, \
FeedId,m htotalout,NallocateH,NallocateM,NallocateL,Feedstart,hminflag,itstarthmin);
 if(m_numParticles>0)
     CopyParticleArrayDeviceToHost(m_hprehead, m_numParticles);
     CopyNeigListArrayDeviceToHost(m totalcontacts);
                       for(i=0;i<m_numParticles;i++){</pre>
                       fprintf(fp1, "%15.6g %15.6g %1
m_hpos[3*i], m_hpos[3*i+1], m_hpos[3*i+2],
 m hpdis[3*i], m hpdis[3*i+1], m hpdis[3*i+2],
                                   m hangv[3*i], m hangv[3*i+1], m hangv[3*i+2],
                                   m_hrad[i], m_hrmass[i], m_hinert[i], m_hmatId[i]);
                       for(i=0;i<m numParticles;i++){</pre>
                          fprintf(fp1,"%8u %15.6g %15.6g %15.6g %15.6g\n",
  m holds;gi[i],m holddisptw[3*i],m holddisptw[3*i+1],m holddisptw[3*i+2],m holdfricpw[i]);
                     for(i=0;i<m numParticles;i++){</pre>
                          fprintf(fp1,"%8u %8u %8u %15.6g %15.6
   m_hcontactEnd[3*i],m_hcontactEnd[3*i+1],m_hcontactEnd[3*i+2],m_hEngdisp[i*3],m_hEngdisp[i*3+1],m_hEngdisp[i*3+2],m_hEngdispw[i],\
  m_hEngdispVarw[4*i],m_hEngdispVarw[4*i+1],m_hEngdispVarw[4*i+2],m_hEngdispVarw[4*i+3]);
                       for(i=0;i<m totalcontacts;i++){</pre>
                       fprintf(fp1, "%8u %15.6g %15.6g %15.6g %15.6g",
m_holdLn[i],m_holddispt[3*i],m_holddispt[3*i+1],m_holddispt[3*i+2],m holdfricp[i]);
                       fprintf(fp1,"\n");
 for(i=0;i<m_totalcontacts;i++){</pre>
                       fprintf(fp1, "%8u %15.6g %15.6g %15.6g %15.6g",\
                          m holdcontactEndpair[i],m hEngdisppair[i],m hEngdispVarpair[4*i],\
   m hEngdispVarpair[4*i+1],m hEngdispVarpair[4*i+2],m hEngdispVarpair[4*i+3]);
                       fprintf(fp1,"\n");
                     cpuErrchk(cudaMemcpy(m hcontactSizepair,m dcontactSizepair,6*Nsect*sizeof(uint),
   cudaMemcpyDeviceToHost));
 for(i=0;i<6*Nsect;i++)</pre>
 fprintf(fp1,"%8u ", m_hcontactSizepair[i]);
fprintf(fp1, "\n");
                       fclose(fp1);
```

Energy dissipation

The dissipated energy is commonly calculated by integrating the normal damping force F_{dn} and the tangential damping force F_{dt} with respect to their overlaps over the entire contact period $t_{contact}$

$$E_d = \int_0^{tcontact} (|\mathbf{f}_{dn}| d\delta_n + |\mathbf{f}_{dt}| d\delta_t)$$



Force pair i-j

1) __device__ void calforceij()

contactEndpair[Ilist] = oldcontactEndpair[oldIlist];

3) Pair information, need to copy if contact in previous step,
so in pairlistD():
Engdisppair[Ilist] = oldEngdisppair[oldIlist];

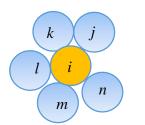
2) calforceij(&newEngdispVarpairi);

```
//---- treat energy dissipation -----
if(0.5*(posi.z+posj.z)>=hmin && 0.5*(posi.z+posj.z)//region to calculate engdisp
if(oldEngdispVarpairi.z>0.0 && newEngdispVarpairi.z>0.0 && fabs(newEngdispVarpairi.z-oldEngdispVarpairi.z)>deltas &&
(oldEndpair==5 | oldEndpair==10) ) //contact in progress
 Engdisppair[Ilist] += 0.5*(fabs(oldEngdispVarpairi.x)+fabs(newEngdispVarpairi.x))*fabs(newEngdispVarpairi.z-
oldEngdispVarpairi.z)+\
                       0.5*(fabs(oldEngdispVarpairi.y)+fabs(newEngdispVarpairi.y))*fabs(newEngdispVarpairi.w-
oldEngdispVarpairi.w);
 contactEndpair[Ilist]=oldEndpair;
 EngdispVarpair[Ilist]=newEngdispVarpairi;
else if(oldEngdispVarpairi.z<=0.0 &&newEngdispVarpairi.z>0.0 && oldEndpair==0 && fabs(newEngdispVarpairi.z-
oldEngdispVarpairi.z)>deltas) //start to contact
 Engdisppair[Ilist] = 0.5*(fabs(oldEngdispVarpairi.x)+fabs(newEngdispVarpairi.x))*fabs(newEngdispVarpairi.z-0.0)+\
                       0.5*(fabs(oldEngdispVarpairi.y)+fabs(newEngdispVarpairi.y))*fabs(newEngdispVarpairi.w-0.0);
 if(fabs(veli-veli)>3.5)
 contactEndpair[Ilist]=10; //collision with a static particle
 else if((veli>0.5 && velj>0.5))
 contactEndpair[Ilist]=5; //collision with a dynamic particle
 contactEndpair[Ilist]=0;
 EngdispVarpair[Ilist]=newEngdispVarpairi;
 else if(oldEngdispVarpairi.z>0.0 && (((oldEndpair==5 || oldEndpair==10) && newEngdispVarpairi.z<=0.0) || \
       (oldEndpair==10 && newEngdispVarpairi.z>0.0 && fabs(newEngdispVarpairi.z-oldEngdispVarpairi.z)<deltas)))</pre>
  // contact complete
 oldEngdisppair[Ilist]=Engdisppair[Ilist];
oldcontactEndpair[Ilist]=contactEndpair[Ilist];
```

^{*}newEngdisppair= make_double4(fdampn*9.81, length(fdamp)*9.81, dsnorm, dispt); $|\mathbf{f}_{dn}| \qquad |\mathbf{f}_{dt}| \qquad d\delta_n \quad d\delta_t$

Energy dissipation

 Sum Engdisppairi to get Engdispi for each particle



All forces on i

Array length of Engdisppairi =Np
Particle property, so it needs to reorder
when reorder particle index
In resortParticleIdD():
oldcontactEnd[i]=contactEnd[Pid];
oldEngdisp[i]=Engdisp[Pid];
oldEngdispw[i]=Engdispw[Pid];
oldEngdispVarw[i]=EngdispVarw[Pid];

```
global void sumallforceiD()
for(i=0;i<njgi[index];i++)</pre>
k=Anei[sumCN[index]+i];
 if(k != 0xffffffff)
 force += forcepair[k];
 torque += torqpairi[k];
 contact += contactpair[k];
 if((contactEndpair[k]==1 || contactEndpair[k]==2) &&
      !isnan(Engdisppairi[k])
 contactEndi +=1;
 Engdispi += Engdisppairi[k]*Winscale;
 if(contactEndpair[k]==2)
 Engdispiw += Engdisppairi[k]*Winscale;
 contactEndiw +=1;
```

Energy dissipation

- WriteOutEngdsp():
- Do different analysis of engdisp data: e.g.,

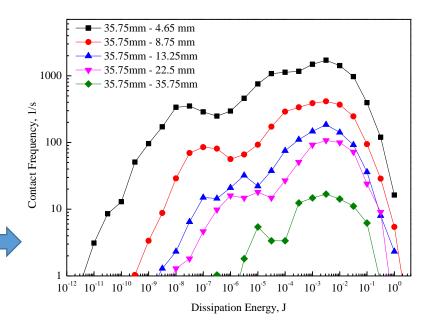
total/bulk average engdisp, engdisp at different axis position, engdisp for different size group,

Contact Frequency

```
• calculateContactFrequencyD() in cu kernel
if(fabs(radi-Size[0])<1e-6 && fabs(radj-Size[8])<1e-6)
//size i contact with size j, add to statistic of Bin
{
   atomicAdd(&contactSizepair[0*Nsect+Bin],1);
}
// Bin= (int) ((log10(Engdisppairmag)-log10(Emin))/gap);</pre>
```

WriteOutContactFrequency() in WriteData.cpp

```
for(i=0;i<Nsect;i++)
     {
     double Binstart=pow(10,i*gap+log10(Emin));
          fprintf(fp1,"%15.6g %15.6g %15
```



How to edit, build and run cases

• Edit

Try to use Visual studio to edit code

BIN

Build

Use makefile

:= ../GDEM

In winscp file path:



```
MPICC := $(MPI_PATH)/bin/mpic++ -Xlinker --allow-multiple-
definition
EXEC ?=
```

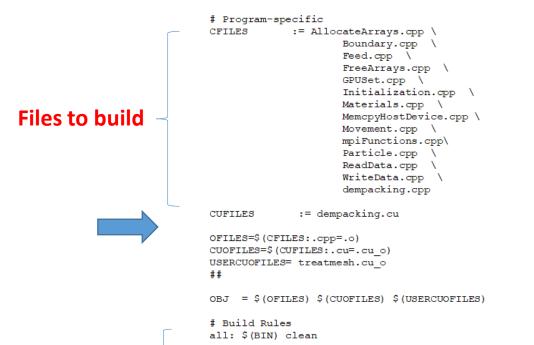
Target

In putty, cd to makefile path and then input "make" to compile:

```
[ganjq@m3-loginl ~]$ cd /projects/hi65/ganjq/mixing/ribbonmixer/colorxyz
[ganjq@m3-loginl colorxyz]$ make
```

After successfully compile, a GDEM (executive file) file should appear in the Bin path,
Otherwise, error information will appear in putty

Run DEM simulations:



\$(BIN): \$(OBJ)

%.o: %.cpp

Build rule

\$(CXX) \$(OBJ) -0 \$(BIN) \$(INCD) \$(LIBS)

\$(NVCC) \$(GENCODE FLAGS) -c \$(INCD) -o \$@ \$<

\$(CXX) -c \$(CCFLAGS) -o \$@ \$<

Run DEM simulation on Massive 3:

- 1) correctly set the input parameters, job script for wall time and memory settings
- 2) run the job script by input "sbatch case" in putty.

```
[ganjq@m3-loginl ~]$ cd /projects/hi65/ganjq/mixing/ribbonmixer/colorxyz
[ganjq@m3-loginl colorxyz]$ sbatch case
```

• 3) check job state by input "show job"

- 4) when the job shows run, check the output dat file to see the information or check if any error information file such as slurm-xxx.out file
- 5) if successfully completed, get data from output file for post-processing. For any variables, if the information of different time is needed, it should be added to the code before running the case.