ECE 4802, Project 2

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Versioning

```
$ gcc --version
gcc (Ubuntu 5.4.0-6ubuntu1~16.04.2) 5.4.0 20160609
$ python3 --version
Python 3.5.2
$ julia --version
julia version 0.4.5
```

Usage

```
$ ./q1c.j1
$ ./q2b.j1
$ gcc q2c.c && ./a.out
$ gcc q3.c && ./a.out
$ ./q4.py
```

Packages

The program q4.py requires the packages pycrypto and joblib, installed as below.

```
$ pip3 install pycrypto==2.6.1 joblib==0.10.3
```

1a

XOR the plaintext and ciphertext to obtain the LFSR sequence. The sequence length is 7, so the degree is L=3.

1b

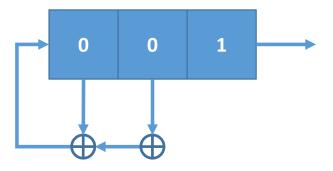
The first L=3 bits of the LFSR sequence are the initialization vector $\{0,0,1\}$.

1c

Find the LFSR coefficients by solving the linear system below, created from the first 6 bits of the LFSR sequence. The script q1c.j1 returns $\{1,1,0\}$. The LSFR is also pictured below.

$$\begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 1 \end{bmatrix} \begin{bmatrix} p_0 \\ p_1 \\ p_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix}$$

\$./q1c.jl [1.0,1.0,0.0]



1d

The key is the feedback coefficients of the LFSR. The initial content of the LFSR can't be used as a key, because you need to "warmup" the LFSR before the output has good statistical properties.

2a

XOR the plaintext and ciphertext headers to obtain the LFSR behavior. The first m=6 bits are the initialization vector: $\{1,1,1,1,1,1\}$.

2b

Find the LFSR coefficients by solving the linear system below, created from the first 12 bits of the LFSR sequence. The script q2b.j1 returns $\{1,1,0,0,0,0,0\}$.

```
$ ./q2b.jl
[1.0,1.0,0.0,0.0,0.0]
```

2c

The program q2c.c outputs "WPIWOMBAT" as the plaintext.

2d

Wombats live in Australia and Tasmania.

2e

This was a known-plaintext attack.

3a

The program q3.c implements DES S-box S_2 using the function out_S2(). Verification is below.

```
$ gcc q3.c && ./a.out
problem 3a, verify DES S_2
x out_S2(x)
4 8
8 6
24 12
56 9
```

3b

The program q3.c also computes the SAC for S_2 , for i=0...5. The SAC is fulfilled by S_2 .

```
$ gcc q3.c && ./a.out
problem 3b, compute SAC
         SAC_coef:
0
         20
                  16
                           16
                                    20
1
         28
                  44
                           56
                                    52
2
                  40
                                    44
         44
                           40
3
         36
                  44
                           28
                                    48
4
         36
                  52
                           36
                                    36
5
         44
                           44
                                    44
                  36
```

The script q4.py implements an exhaustive key search for DES. Verification is below.

```
$ ./q4.py
$ cat answer.txt
0x00000000c2445aee
```

Problem 5 - Bonus

The script q4.py can solve Problem 5 by changing line 11 to "keyspace = 1 << 64". However, it failed to find a key within a reasonable time frame. As a benchmark, the script takes 1.682 seconds to exhaust a keyspace of 2^{20} . We can find the upper and lower bound by assuming 1 or 31 leading zero bits respectively.

$$t_{exhaust} < 2^{63} \left(\frac{1.682 \text{s}}{2^{20}} \right) = 468840 \text{yr}$$

 $t_{exhaust} > 2^{33} \left(\frac{1.682 \text{s}}{2^{20}} \right) = 3\text{h}49\text{m}$

Source Code

q1c.jl

q2b.jl

q2c.c

```
#include <stdio.h>
#include <stdint.h>
#define MSG_BITLEN 45 // 45 bits in the message
#define MSG_SYMLEN 9
                       // 9 symbols in the message
#define SYM_BITLEN 5
                      // 5 bits per symbol
#define LFSR_DEGREE 6
#define LFSR_INIT 0x3f
const uint8_t bit_rev[32] = {
0x00, 0x10, 0x08, 0x18, 0x04, 0x14, 0x0c, 0x1c,
0x02, 0x12, 0x0a, 0x1a, 0x06, 0x16, 0x0e, 0x1e,
0x01, 0x11, 0x09, 0x19, 0x05, 0x15, 0x0d, 0x1d,
0x03, 0x13, 0x0b, 0x1b, 0x07, 0x17, 0x0f, 0x1f
};
uint8_t stob(char s)
    return (s >= 'A') ? s - 65: s - 22;
}
char btos(uint8_t b)
    return (b < 26) ? b + 65: b + 22;
}
int main(void)
    /* Generate a sufficiently-long LFSR sequence */
    uint64_t lfsr = LFSR_INIT; // sequence
    uint64_t bit;
    uint8_t state = LFSR_INIT;
    int offset = LFSR_DEGREE;
    do {
        bit = (state ^ (state >> 1)) & 1; // coefs: {1, 1, 0, 0, 0, 0}
        state = (state >> 1) | (bit << (LFSR_DEGREE-1));</pre>
        lfsr += (bit << offset++);</pre>
    } while (offset < MSG_BITLEN);</pre>
    /* Convert the ciphertext into plaintext */
    char ct_s[MSG_SYMLEN] = "J5AOEDJ2B";
    char pt_s[MSG_SYMLEN];
    uint64_t ct_b = 0;
    uint64_t pt_b;
    for (int i=0; i<MSG_SYMLEN; i++) {</pre>
        ct_b += (uint64_t) bit_rev[stob(ct_s[i])] << i*SYM_BITLEN;</pre>
        pt_b = ct_b ^ lfsr; // sub-optimal :(
        pt_s[i] = btos(bit_rev[pt_b >> (i*SYM_BITLEN) & 0x1f]);
        printf("%c", pt_s[i]);
    puts("");
    return 0;
```

q3c.c

```
#include <stdio.h>
#include <stdlib.h>
#define LBIT 0b00100000
#define MBITS Ob00011110
#define RBIT 0b0000001
#define OUTER2(x) ((x & LBIT) >> 4 + (x & RBIT))
#define INNER4(x) ((x & MBITS) >> 1)
static const char S2[4][16] =
     {15, 1, 8, 14, 6, 11, 3, 4, 9, 7, 2, 13, 12, 0, 5, 10},
    { 3, 13, 4, 7, 15, 2, 8, 14, 12, 0, 1, 10, 6, 9, 11, 5}, { 0, 14, 7, 11, 10, 4, 13, 1, 5, 8, 12, 6, 9, 3, 2, 15}, {13, 8, 10, 1, 3, 15, 4, 2, 11, 6, 7, 12, 0, 5, 14, 9}
};
char out_S2(char x)
     return S2[OUTER2(x)][INNER4(x)];
}
int main(void)
    printf("problem 3a, verify DES S_2\n");
     printf("x\tout_S2(x)\n");
    printf("%d\t%d\n", 4, out_S2(4));
printf("%d\t%d\n", 8, out_S2(8));
printf("%d\t%d\n", 24, out_S2(24));
    printf("%d\t%d\n", 56, out_S2(56));
    printf("problem 3b, compute SAC\n");
     int i, j, k, sum, SAC_coef[6][4] = {0};
     /* fill SAC_coef */
     for (i = 0; i < 64; i++) {
         for (j = 0; j < 6; j++) {

sum = out_S2(i) ^ out_S2(i ^ (1 << j));
                   for (k = 0; k < 4; k++)
                        SAC_coef[j][k] += (sum >> k) & 1;
         }
     }
     /* print SAC_coef */
     printf("i\tSAC_coef:\n");
     for (i = 0; i < 6; i++) {
         printf("%d\t", i);
         for (j = 0; j < 4; j++) {
    printf("%d\t", SAC_coef[i][j]);</pre>
          printf("\n");
     return 0;
```

q4.py

```
#!/usr/bin/env python3
from Crypto.Cipher import DES
from joblib import Parallel, delayed
import binascii
import struct
pt = binascii.unhexlify('48656c6c6f212121')
ct = binascii.unhexlify('d52bd481f21e25a1')
keyspace = 1 << 32
n_{cpus} = 8
chunk_size = int(keyspace/n_cpus)
def check(cpu):
    for k in range(chunk_size * cpu, chunk_size * (cpu+1)):
        if DES.new(struct.pack('>Q',k), DES.MODE_ECB).encrypt(pt) == ct:
            return k
keys = Parallel(n_jobs=n_cpus)(delayed(check)(cpu) for cpu in range(n_cpus))
for k in keys:
    if k is not None:
        with open('answer.txt', 'w') as f:
            f.write(str(hex(k))+'\n')
        break
```