

Python: NumPy Course Notes

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1 Learning Objectives

Concepts

- Creating and Saving NumPy ndarrays
- Using Built-in Functions to Create ndarrays
- Accessing, Deleting, and Inserting Elements Into ndarrays
- Slicing ndarrays
- Boolean Indexing, Set Operations, and Sorting
- Exercise: Manipulating ndarrays
- Arithmetic Operations and Broadcasting
- Exercise: Creating ndarrays with Broadcasting

Commands

- `np.array`
- `.shape`
- `.size`
- `np.save` and `np.load`
- `np.zeros`
- `np.ones`
- `np.eye`
- `np.diag`
- `np.arange`
- `np.linspace`
- `np.reshape`

- np.random
 - np.random.random
 - np.random.randint
 - np.random.normal
 - np.random.permutation
- np.delete
- np.append
- np.insert
- np.vstack
- np.hstack
- np.unique
- np.copy
- np.intersect1d
- np.setdiff1d
- np.union1d
- np.sort
- Mathematical Functions
 - np.add
 - np.subtract
 - np.multiply
 - np.divide
 - np.sqrt
 - np.exp
 - np.power
- Statistical Functions
 - mean
 - std
 - median
 - max
 - min

NumPy is useful in dealing with arrays of data, which can be thought of in a mathematical sense as vectors and matrices. NumPy is a powerful tool in itself, however an even more useful Python data tool, the Pandas library, is built on top of NumPy. A basic understanding of NumPy is necessary, and we'll cover some of the essential functions and uses in these notes.

2 Creating and Saving NumPy ndarrays

Not needing too much of an explanation, here's a beginning look at creating basic NumPy arrays.

Covered in this section:

- `np.array`: turn a list, or list of lists, into a NumPy array object
- `shape`: return the dimensions of an array object
- `size`: return the total number of elements in an array object
- `save` & `load`: arrays can be saved for future use

```
x = np.array([1, 2, 3, 4, 5])
print(x)
# [1 2 3 4 5]

x.shape
# (5,)
```

```
Y = np.array([[1, 2, 3], [4, 5, 6], [7, 8, 9], [10, 11, 12]])
print(Y)
"""
[[ 1  2  3]
 [ 4  5  6]
 [ 7  8  9]
 [10 11 12]]
"""

Y.shape
# (4, 3)
Y.size
# 12

# Notes Section:
# dtype changes with mixed data, and will uptype (int + floats ->
#                                     all floats)
# numpy arrays can be saved for later use

# save
np.save('my_array', x)
# load
y = np.load('my_array.npy')
```

3 Using Built-in Functions to Create ndarrays

There are several function in the NumPy library which build generalized arrays, or arrays populated by data generated following rules. For example, build an array with dimensions `nxm` that consist of all 0s, or 1s along the diagonal, etc.

Here are some of the essential generating functions:

- `zeros`: create an array populated with all 0s
- `ones`: create an array populated with all 1s
- `full`: create an array populated with a specified input
- `eye`: creates an array populated with the identity matrix (1s on the diagonals, 0s for the rest)
- `diag`: takes a list, and places the list elements on the diagonal of a matrix
- `arange`: will return a 1d array with increasing values based upon specified start, stop and spacing where the endpoint is non-inclusive: `[start, stop)`
- `linspace`: will return a 1d array with increasing values based upon start, stop and number of values desired where the endpoint is inclusive: `[start, stop]`
- `reshape`: will return an array with the elements reshaped into desired dimensions (given that the two arrays have a compatible number of elements)
- `np.random.random`: will return an array of random numbers filling specified dimensions
- `np.random.randint`: will return an array of random integers based upon a range, and filling specified dimensions
- `np.random.normal`: will return an array of normally distributed values based upon a range, and filling specified dimensions (note that this concept transfers to other common distributions)

```
# numpy zeros function
x = np.zeros((3, 4))
# can change dtype: np.zeros((3, 4), dtype = int)

# Below is what x, the object, look like:
"""
array([[0., 0., 0., 0.],
       [0., 0., 0., 0.],
       [0., 0., 0., 0.]])
"""
# For the rest of the examples, we'll be showing the print(x)
# version:
"""
[[0. 0. 0. 0.]
 [0. 0. 0. 0.]
 [0. 0. 0. 0.]]
"""
```

```

x = np.ones((4, 5))
"""
[[1.  1.  1.  1.  1.]
 [1.  1.  1.  1.  1.]
 [1.  1.  1.  1.  1.]
 [1.  1.  1.  1.  1.]]
"""

x = np.full((4, 3), 5)
"""
[[5 5 5]
 [5 5 5]
 [5 5 5]
 [5 5 5]]
"""

x = np.eye(5)
"""
[[1.  0.  0.  0.  0.]
 [0.  1.  0.  0.  0.]
 [0.  0.  1.  0.  0.]
 [0.  0.  0.  1.  0.]
 [0.  0.  0.  0.  1.]]
"""

x = np.diag([1, 2, 3, 4, 5])
"""
[[1 0 0 0 0]
 [0 2 0 0 0]
 [0 0 3 0 0]
 [0 0 0 4 0]
 [0 0 0 0 5]]
"""

x = np.arange(10)
"""
# [0 1 2 3 4 5 6 7 8 9]
"""

x = np.arange(4, 10)
"""
# [4 5 6 7 8 9]
"""

x = np.arange(1, 14, 3)
"""
# [ 1  4  7 10 13]
"""

# numpy linspace function (default = 50)
x = np.linspace(0, 25, 10)
"""
[ 0.          2.77777778  5.55555556  8.33333333 11.11111111 13.
 16.66666667 19.44444444 22.22222222 25.          ]
"""

```

```

x = np.linspace(0, 25, 10, endpoint=False)
"""
[ 0.   2.5  5.   7.5 10.  12.5 15.  17.5 20.  22.5]
"""

# numpy array methods
x = np.arange(20).reshape((4, 5))
"""
[[ 0  1  2  3  4]
 [ 5  6  7  8  9]
 [10 11 12 13 14]
 [15 16 17 18 19]]
"""

# numpy random functions
x = np.random.random((3, 3))
"""
[[0.82591877 0.69755492 0.27402617]
 [0.13409014 0.66530258 0.10349078]
 [0.22057372 0.17607417 0.98691068]]
"""

x = np.random.randint(4, 15, (3, 2))
"""
[[ 9  4]
 [14  8]
 [ 4  5]]
"""

# the 1000x1000 example is not illustrated, for formatting
# reasons
x = np.random.normal(0, 0.1, size = (1000, 1000))

```

4 Accessing, Deleting, and Inserting Elements Into ndarrays

NumPy arrays are mutable objects, meaning they can be altered following creation. We'll be going over several ways to access and change existing arrays. Some of the essential functions covered are:

- delete: specify the array and the indices for elements to be deleted
- append: add elements to the end of an array
- insert: add elements at a specified position of an array
- vstack: stack two NumPy arrays vertically
- hstack: stack two NumPy arrays horizontally

```

# Can access and change elements based on indices
x = np.arange(1, 10).reshape(3, 3)
"""
[[1 2 3]
 [4 5 6]
 [7 8 9]]
"""
# Access element
x[0, 0] = 1
# 1

# Change element
x[0, 0] = 99
"""
[[99 2 3]
 [ 4 5 6]
 [ 7 8 9]]
"""

# deleting elements
x = np.arange(1, 6)
# [1 2 3 4 5]
# delete first and last elements
x = np.delete(x, [0, -1])
# [2 3 4]

x = np.arange(1, 10).reshape(3, 3)
# for rank 2+ arrays, axis refers to dimension (row = 0, column =
1)
W = np.delete(x, 0, axis = 0)
"""
W is x with first row deleted
[[4 5 6]
 [7 8 9]]
"""
W = np.delete(x, [0, 2], axis = 1)
"""
W is x with first and last columns deleted
[[2]
 [5]
 [8]]
"""

# adding (appending) elements
x = np.arange(1, 6)
x = np.append(x, [6, 7])
# [1 2 3 4 5 6 7]
x = np.arange(1, 10).reshape(3, 3)
W = np.append(x, [[10 11 12]], axis = 0) # append row
Y = np.append(x, [[10], [11], [12]], axis = 1) # append column

# inserting elements
x = np.arange(1, 6)
# insert elements in between elements in rank 1 array
x = np.insert(x, 2, [3, 4])
print(x)
# [1 2 3 4 3 4 5]

```

```

# insert row between rows in rank 2 array
x = np.arange(1, 6)
Y = np.arange(1, 10).reshape(3, 3)
W = np.insert(Y, 1, [4, 5, 6], axis = 0)
print(W)
"""
[[1 2 3]
 [4 5 6]
 [4 5 6]
 [7 8 9]]
"""

# insert column between columns in rank 2 array
W = np.insert(Y, 1, 5, axis = 1)
print(W)
"""
[[1 5 2 3]
 [4 5 5 6]
 [7 5 8 9]]
"""

# stack arrays using vertical or horizontal stacking (pay
                                attention to dimension)
x = np.array([1, 2])
Y = np.array([[3, 4], [5, 6]])
z = np.vstack((x, Y))
print(z)
"""
[[1 2]
 [3 4]
 [5 6]]
"""

z = np.hstack((Y, x.reshape(2, 1)))
print(z)
"""
[[3 4 1]
 [5 6 2]]
"""

```

5 Slicing ndarrays

Covered briefly in the previous section, we're going to do a deeper dive into the slicing capabilities of NumPy. Aside from syntax, some essential functions covered in this section are:

- copy: this creates an entirely new array, where changes won't be mapped back to the original
- diag: another use of the diagonal function, this is used to return an array featuring the diagonal of a rank 2 array
- unique: this will find all of the unique values within an array


```

# Here are the basic ways to slice a rank 1 array:
# 1. ndarray[start:end]
# 2. ndarray[start:]
# 3. ndarray[:end]
# Also, recall that ndarray[-1] will return the last element in
# an array

# examples of slicing in rank 2 array
X = np.arange(1, 21).reshape(4, 5)
"""
[[ 1  2  3  4  5]
 [ 6  7  8  9 10]
 [11 12 13 14 15]
 [16 17 18 19 20]]
"""

# the rank 2 slice order is: rows, columns (starts are inclusive,
# ends are exclusive)
z = X[1:4, 2:5]
"""
[[ 8  9 10]
 [13 14 15]
 [18 19 20]]
"""

# by leaving either the row or column input as ":" it will select
# entire row or column
# this will return the 3rd column
z = X[:, 2]
# [ 3  8 13 18]
# however, that returns a rank 1 array (row format). Let's return
# the correct dimensions:
z = X[:, 2:3]
"""
[[ 3]
 [ 8]
 [13]
 [18]]
"""

# slicing creates a "view" of the array
# changing z will change X (keep the copy command in mind here)
z = X[1:, 2:]
z[2, 2] = 0
"""
X =
[[ 1  2  3  4  5]
 [ 6  7  8  9 10]
 [11 12 13 14 15]
 [16 17 18 19  0]]

Even though the elements were changed in the z array, there was
still a connection to the X array
.
"""

# create a brand new array (so to not change the original array)

```

```

z = X[1:, 2:].copy()
z[2, 2] = 0
"""
X =
[[ 1  2  3  4  5]
 [ 6  7  8  9 10]
 [11 12 13 14 15]
 [16 17 18 19 20]]

By using the copy function the connection to the original array
was broken.
"""

# use variable in slicing
indices = np.array([1, 3])
y = X[indices, :]
"""
[[ 6  7  8  9 10]
 [16 17 18 19 20]]
"""
z = X[:, indices]
"""
[[ 2  4]
 [ 7  9]
 [12 14]
 [17 19]]
"""

# NumPy built in slicing methods
# ex: diagonals
z = np.diag(X)
# [ 1  7 13 19]
# specify k to shift the diagonal indexing
z = np.diag(X, k = 1)
# [ 2  8 14 20]

# finding uniques
X = np.array([[1, 2, 3], [4, 5, 6], [1, 5, 6]])
# [1 2 3 4 5 6]

```

6 Boolean Indexing, Set Operations, and Sorting

Now that we have a solid understanding of elements and slicing in rank 1 and rank 2 arrays, we can move into conditionals and comparing arrays with each other. Some essentials covered in this section:

- `intersect1d`: this will find the intersection of two arrays and return the sorted, unique values
- `setdiff1d`: this will find the differences between two arrays and return the sorted, unique values

- union1d: this will find the union between two arrays and return the sorted, unique values
- sort: this will sort the values of an array

```
X = np.arange(25).reshape(5, 5)
"""
[[ 0  1  2  3  4]
 [ 5  6  7  8  9]
 [10 11 12 13 14]
 [15 16 17 18 19]
 [20 21 22 23 24]]
"""

# first look at conditional arguments
X[X > 10]
X[(X > 10) & (X < 17)]
"""
[11 12 13 14 15 16 17 18 19 20 21 22 23 24]
[11 12 13 14 15 16]
"""

# basic application of conditional arguments (other than slicing)
X[(X > 10) & (X < 17)] = -1
"""
[[ 0  1  2  3  4]
 [ 5  6  7  8  9]
 [10 -1 -1 -1 -1]
 [-1 -1 17 18 19]
 [20 21 22 23 24]]
"""

x = np.array([1, 2, 3, 4])
y = np.array([3, 4, 5, 6])
np.intersect1d(x, y)
np.setdiff1d(x, y)
np.union1d(x, y)
"""
Recall these functions return sorted, unique arrays

Intersection
[3 4]

Difference
[1 2]

Union
[1 2 3 4 5 6]
"""

x = np.random.randint(1, 11, size = (10,))
np.sort(x)
"""
np.sort(x) =
[2 2 2 2 3 5 5 5 7 9]

x =
[2 5 2 5 5 3 2 9 7 2]
```

```

"""
np.sort(np.unique(x))
"""
[2 3 5 7 9]
"""

# can also sort using x.sort()
x.sort()
"""
x =
[2 2 2 2 3 5 5 5 7 9]

Note the difference between np.sort(x) and x.sort():
- np.sort(x) creates an instance where x is sorted
- x.sort() changes the array to be sorted
"""

x = np.random.randint(1, 11, size = (5,5))
"""
[[ 9  2 10  6  6]
 [10  7  6 10  8]
 [ 3  1  1  4  2]
 [ 9  6  5  7  3]
 [10  7  5  7  7]]
"""

# can sort 2d arrays using the axis command
# sort rows with axis = 0, columns with axis = 1
np.sort(x, axis = 0)
np.sort(x, axis = 1)
"""
axis = 0 (row sort)
[[ 3  1  1  4  2]
 [ 9  2  5  6  3]
 [ 9  6  5  7  6]
 [10  7  6  7  7]
 [10  7 10 10  8]]

axis = 1 (column sort)
[[ 2  6  6  9 10]
 [ 6  7  8 10 10]
 [ 1  1  2  3  4]
 [ 3  5  6  7  9]
 [ 5  7  7  7 10]]
"""

```

It's important to note that we should be careful and deliberate when using the sort function. For instance, say we have a rank 2 array that is comprised of data entries where either each row or each column are data points referring to a specific event. If not done properly, sorting could mix the data from the events.

7 Exercise: Manipulating ndarrays

This is a quick exercise to test the combination of some of the NumPy functions we've seen so far.

The task is to create a 5x5 ndarray with consecutive integers from 1 to 25 (inclusive). Then, use Boolean indexing to pick out only the odd numbers in the array.

```
# Create a 5 x 5 ndarray with consecutive integers from 1 to 25 (
# inclusive).
X = np.arange(1, 26).reshape(5, 5)

# Use Boolean indexing to pick out only the odd numbers in the
# array
Y = X[X % 2 != 0]
```

Although a short exercise in code length, this illustrates a power conditional argument when finding even and odd values, known in mathematics as the "modulus" or "mod" for short. Essentially, the command above divides the numbers by 2, and checks to see if there is any remainder. If there is no remainder, the number is even and is accepted.

8 Arithmetic Operations and Broadcasting

9 Exercise: Creating ndarrays with Broadcasting