Related Rates

- 1. An airplane is flying towards a radar station at a constant height of 6 km above the ground. If the distance s between the airplane and the radar station is decreasing at a rate of 400 km per hour when s = 10 km., what is the horizontal speed of the plane?
- 2. A light is on the ground 20 m from a building. A man 2 m tall walks from the light directly toward the building at 1 m/s. How fast is the length of his shadow on the building changing when he is 14 m from the building?
- 3. A conical cup is 4 cm across and 6 cm deep. Water leaks out of the bottom at the rate of 2 cm³/sec. How fast is the water level dropping when the height of the water is 3 cm?
- 4. A person 2 m tall walks towards a lamppost on level ground at a rate of 0.5 m/sec. The lamp on the post is 5 m high. How fast is the length of the person's shadow decreasing when the person is 3 m from the post?
- 5. Air is escaping from a spherical balloon at the rate of 2 cm³ per minute. How fast is the surface area shrinking when the radius is 1 cm? $V = 4/3 \pi r^3$ and $S = 4\pi r^2$ where V is the volume and S is the surface area, r is the radius.
- 6. A funnel in the shape of an inverted cone is 30 cm deep and has a diameter across the top of 20 cm. Liquid is flowing out of the funnel at the rate of 12 cm ³/sec. At what rate is the height of the liquid decreasing at the instant when the liquid in the funnel is 20 cm deep?
- 7. Find the rate of change of the area A, of a circle with respect to its circumference C.
- 8. A boat is being pulled into a dock by attached to it and passing through a pulley on the dock, positioned 6 meters higher than the boat. If the rope is being pulled in at a rate of 3 meters/sec, how fast is the boat approaching the dock when it is 8 meters from the dock?
- 9. A man 6 feet tall walks at the rate of 5 ft/sec toward a street light that is 16 ft above the ground.
 - a) At what rate is the tip of his shadow moving?
 - b) At what rate is the length of his shadow changing when he is 10 feet from the base of the light?
- 10. A water tank has the shape of an inverted right-circular cone, with radius at the top 15 meters and depth 12 meters. Water is flowing into the tank at the rate of 2 cubic meters per minute. How fast is the depth of water in the tank increasing at the instant when the depth is 8 meters?
- 11. A ladder 10 meters long is leaning against a vertical wall with its other end on the ground. The top end of the ladder is sliding down the wall. When the top end is 6 meters from the ground it is sliding down at 2 m/sec. How fast is the bottom moving away from the wall at this instant?
- 12. Gas is escaping a spherical balloon at the rate of 4 cm³ per minute. How fast is the surface area shrinking when the radius is 24 cm? For a sphere, $V = 4/3\pi r^3$ and $S = 4\pi r^2$ where V is volume, S is surface area and r is the radius of the balloon.

13. The radius of a right circular cylinder is increasing at the rate of 4 cm/sec but its total surface area remains constant at 600 kcm². At what rate is the height changing when the radius is 10 cm?

- 14. A block of ice, in the shape of a right circular cone, is melting in such a way that both its height and its radius r are decreasing at the rate of 1 cm/hr. how fast is the volume decreasing when r = h = 10 cm?
- 15. In a rig ht triangle, leg x is increasing at the rate of 2 m/s while leg y is decreasing so that the area of the triangle is always equal to 6 m². How fast is the hypotenuse z changing when x = 3 m?
- 16. A girl is flying a kite on a string. The kite is 120 ft. above the ground and the wind is blowing the kite horizontally away from her at 6 ft/sec. At what rate must she let out the string when 130 ft. of string has been let out?
- 17. A thin circular metal disk changes size (but not shape) when heated. The disk is being heated so that its radius is increasing at a rate of 0.03 mm/sec. How fast is the area of the disk changing when the radius is 200 mm?
- 18. A right circular cylinder of constant volume is being flattened. At the moment when its radius is 3 cm, the height is 4 cm and the height is decreased at the rate of 0.2 cm/sec. At that moment, what is the rate of change of the radius?
- 19. Assume that sand allowed to pour onto a level surface will form a pile in the shape of a cone, with height equal to diameter of the base. If sand is poured at 2 cubic meters per second, how fast is the height of the pile increasing when the base is 8 meters in diameters?
- 20. A boat is pulled into a dock by rope attached to it and passing through a pulley on the dock positioned 5 meters higher then the boat. If the rope is being pulled in at a rate of 2 m/sec, how fast is the boat approaching the dock when it is 12 meters away from the dock?
- 21. Jim, who is 180 cm tall, is walking towards a lamp-post which is 3 meters high. The lamp casts a shadow behind him. He notices that his shadow gets shorter as he moves closer to the lamp. He is walking at 2.4 meters per second.
 - a) When he is 2 meters from the lamp-post, how fast is the length of his shadow decreasing?
 - b) How fast is the tip of his shadow moving?

Answers: 1) - 500 k/ hr 2) - 10/9 m/s 3) - 2/
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 cm/s 4) - 1/3 m/s 5) - 4 cm²/min 6) 27/(100 Π) cm/s 7) c/(2 Π) 8) - 30/8 m/s 9a) tip -//8 ft/s b) shadow -3 ft/s must do(b) first 10) 1/(50 Π) m/s 11) 3/2 m/s 12) - 1/3 cm²/s 13) - 16 cm/s 14) - 100 Π 15) -14/15 m/s 16) 30/13 ft/s 17) 12 Π m/s 18) 3/40 cm/s 19) 1/(8 Π m/s 20)-13/6 m/s 21a) Shadow decreasing 3.6 m/s b) Tip decreasing 6 m/s