Math 170: Section 7.2, 7.3 Lecture

Section 7.2

Definition: When an experiment is performed a number of times, the **Leguency** or **L**

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$$P(E) = \frac{fr(E)}{N}.$$

The number fr(E) is called the P(E) of E. N, the number of times that the experiment is performed, is called the number of **trials** or the **sample size**. If E consists of a single outcomes s, then we refer to P(E) as the relative frequency or estimated probability of the outcomes s, and we write P(s).

The collection of the estimated probabilities of all the outcomes is the relative frequency distribution or estimated probability distribution.

Example 1 In a survey of 250 hybrid vehicles sold in the United States, 125 were Toyota Prii, 30 were Honda Civics, 20 were Toyota Camrys, 15 were Ford Escapes, and the rest were other makes. What is the relative frequency that a hybrid vehicle sold in the United States is not a Toyota Camry?

E = 2 Toyota Prius, Honda Civic, Ford Escape, Other 3 11 Complement of theset 2 Toyota Canry 3 = FE = F'

$$N=250$$
 fr(E)=?

$$=250-20$$

$$C_{c}(F)$$
 220 $n(F)$

$$P(E) = \frac{fr(E)}{N} = \frac{230}{250} = .92$$

Bid Price	\$0-\$9.99	\$10-\$49.99	\$50-\$99.99	≥\$100
Frequency	6	23	15	6
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Example 2 The above chart shows the results of a survey of the bid prices for 50 paintings on eBay with the highest number of bids.

Consider the experiment in which a painting is chosen and the bid price is observed.

- (a) Find the relative frequency distribution.
- (b) Find the relative frequency that a painting in the survey had a bid price of less than \$50.

(a) Bid Price 0-9.99 10-49.99
$$|SO-9.99.99| \ge 100$$

Rel. Frequency $\frac{6}{50} = .12$ $\frac{23}{50} = .46$ $\frac{15}{50} = .30$ $\frac{6}{50} = .12$

(b) Method I Compute Directly
$$E = \frac{50-9.99}{50}, 10-49.99$$
 P(E) = $\frac{fr(E)}{10} = \frac{6+23}{50} = \frac{29}{50} = .58$

Method 2 Use Rel. Frez.

$$P(E) = P(F) + P(G)$$

= $\frac{6}{50} + \frac{23}{50}$
= $\frac{6+23}{50}$

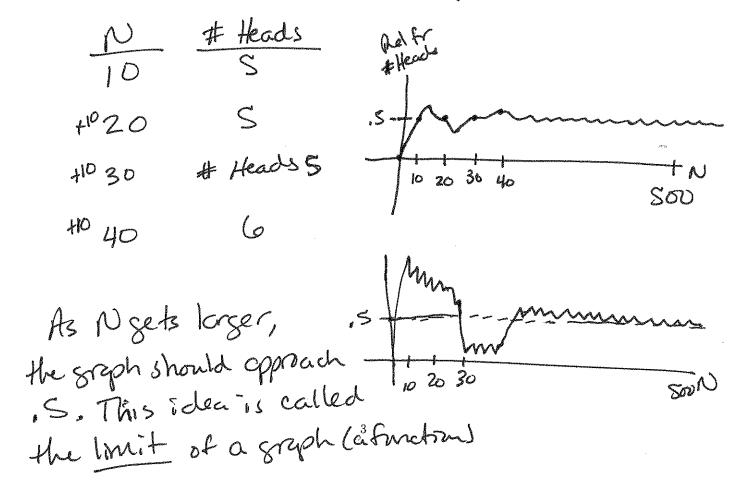
Some Properties of Relative Frequency Distribution Let $S = \{s_1, s_2, \dots, s_n\}$

be a sample space and let $P(s_i)$ be the relative frequency of the event $\{s_i\}$. Then

- 1. $0 \le P(s_i) \le 1$
- 2. $P(s_1) + P(s_2) + \cdots + P(s_n) = 1$ 3. If $E = \{e_1, e_2, \dots, e_r\}$ then $P(E) = P(e_1) + P(e_2) + \cdots + P(e_r)$.

- 1. The relative frequency of each outcome is a number between 0 and 1(inclusive).
- 2. The relative frequencies of all the outcomes add up to 1.
- 3. The relative frequency of an event E is the sum of the relative frequencies of the individual outcomes of E.

Relative Frequency and Increasing Sample Size A "fair" coin is one that is as likely to come up heads as it is to come up tails. In other words, we expect heads to come up 50% of the time if we toss such a coin many times. Put more precisely, we expect the relative frequency to approach .5 as the number of trials gets larger. Let's graph the behavior of the relative frequency for a sequence of coin tosses. For each N we will plot what fraction of times the coin comes up heads in the first N tosses.



Outcome	1	2	3	4	5	6
Probability	.3	.3		.1	.2	

Table 1: Example 3

Section 7.3: Probability and Probability Models

Probability Distribution; Probability
(Compare with the properties of relative frequency.)
A (finite) Scopability dismovis in assignment of a number
$P(s_i)$, the probability of s_i , to each outcome of a finite
sample space $S = \{s_1, s_2, \dots, s_n\}$. The probabilities must satisfy
$1. \ 0 \le P(s_i) \le 1$
2. $P(s_1) + P(s_2) + \cdots + P(s_n) = 1$.
We find the probabilities of the outcomes in E , written $P(E)$, by adding up the probabilities of the outcomes in E . If $P(E) = 0$, we call E an impossible event \emptyset is always impossible, since something must happen.
Examples
1. Let us take $S = \{H, T\}$ and make the assignments $P(H) = .5$ and
P(T) =
2. We can instead make the assignments $P(H) = .2$ and $P(T) =$
3. The table at the top of this page gives a probability distribution for
the sample space $S = \{1, 2, 3, 4, 5, 6\}.$
It follows that $P(\{1,6\}) = 1$
$P(\{2,3\}) =$
P(3) =
Probability Models
A for a particular experiment is a prob-
ability distribution that predicts the relative frequency of each outcome if
the experiment is performed a number
of times. Just as we think of relative frequency as estimated probability, we
can think of modeled probability as