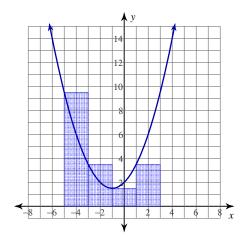
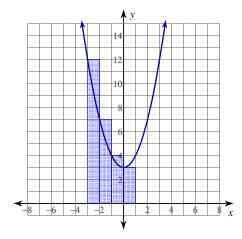
Approximating Area Under a Curve

For each problem, approximate the area under the curve over the given interval using 4 left endpoint rectangles.

1)
$$y = \frac{x^2}{2} + x + 2$$
; [-5, 3]

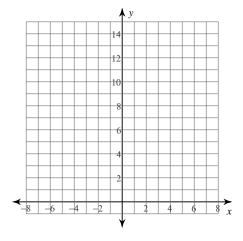


2)
$$y = x^2 + 3$$
; [-3, 1]

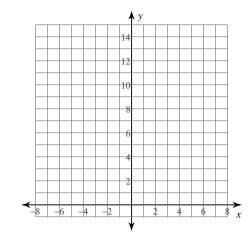


For each problem, approximate the area under the curve over the given interval using 5 right endpoint rectangles. You may use the provided graph to sketch the curve and rectangles.

3)
$$y = -\frac{x^2}{2} + 6$$
; [-3, 2]

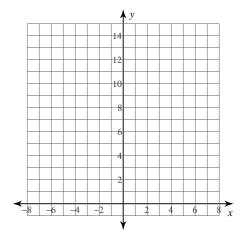


4)
$$y = -\frac{x^2}{2} + x + 5$$
; [-1, 4]

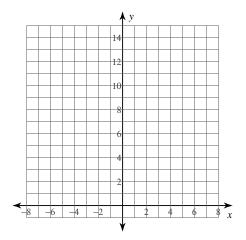


For each problem, approximate the area under the curve over the given interval using 4 inscribed rectangles. You may use the provided graph to sketch the curve and rectangles.

5)
$$y = -x + 5$$
; $[-7, -5]$

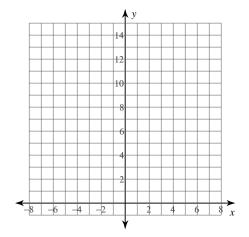


6)
$$y = \frac{2}{x}$$
; [1, 5]

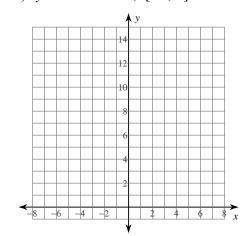


For each problem, approximate the area under the curve over the given interval using 4 midpoint rectangles. You may use the provided graph to sketch the curve and rectangles.

7)
$$y = -x^2 + 2x + 11$$
; [-1, 3]



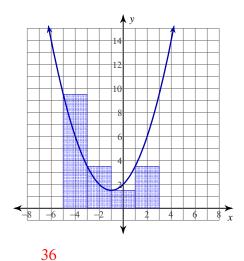
8)
$$y = x^2 - 2x + 3$$
; [-1, 3]



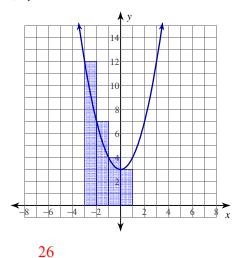
Approximating Area Under a Curve

For each problem, approximate the area under the curve over the given interval using 4 left endpoint rectangles.

1)
$$y = \frac{x^2}{2} + x + 2$$
; [-5, 3]

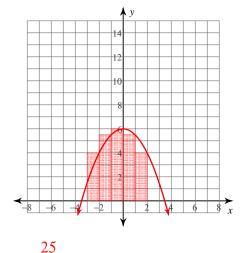


2)
$$y = x^2 + 3$$
; [-3, 1]

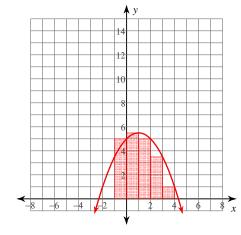


For each problem, approximate the area under the curve over the given interval using 5 right endpoint rectangles. You may use the provided graph to sketch the curve and rectangles.

3)
$$y = -\frac{x^2}{2} + 6$$
; [-3, 2]

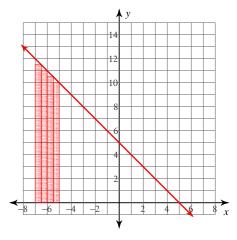


4)
$$y = -\frac{x^2}{2} + x + 5$$
; [-1, 4]



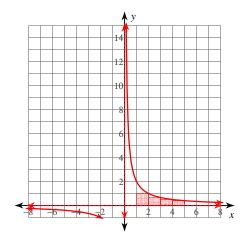
For each problem, approximate the area under the curve over the given interval using 4 inscribed rectangles. You may use the provided graph to sketch the curve and rectangles.

5)
$$y = -x + 5$$
; $[-7, -5]$



$$\frac{43}{2} = 21.5$$

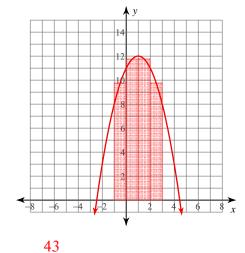
6)
$$y = \frac{2}{x}$$
; [1, 5]



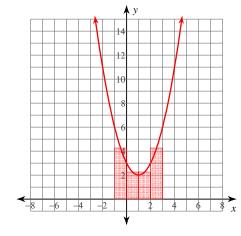
$$\frac{77}{30} \approx 2.567$$

For each problem, approximate the area under the curve over the given interval using 4 midpoint rectangles. You may use the provided graph to sketch the curve and rectangles.

7)
$$y = -x^2 + 2x + 11$$
; [-1, 3]



8)
$$y = x^2 - 2x + 3$$
; [-1, 3]



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