



Exam #1 A October 4, 2017

Instructor: Ann Clifton	Name:
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Do not turn this page until told to do so.

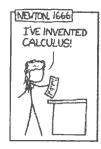
You will have a total of 1 hour and 15 minutes to complete the exam. When specified, you **must** show all work to receive full credit. NO CALCULATOR/PHONE ALLOWED. Draw a pumpkin on this page if you read this.

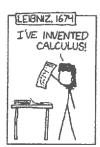
Cheating of any kind on the exam will not be tolerated and will result in a grade of 0%.



#	score	out of	#	score	out of
1		4	9		6
2		4	10		6
3		4	11		14
4		4	12		20
5		4	13		16
6		6			
7		6	EC		5
8		6	Total		100

Remember: This exam has no impact on your worth as a human being. You got this!!!











True or False. No work/explanation required. True means ALWAYS true. 4pts each.

1. If $f(x) \leq g(x)$ for all x in some open interval containing c, except possibly at x = c itself, and the limits of f and g both exist as x approaches c, then $\lim_{x\to c} f(x) \leq \lim_{x\to c} g(x)$.

True

2. If the function f is continuous at x = c and g is a function of x, then f + g is continuous at x = c.

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3. If f is continuous at c and g is continuous at f(c), then the composite $g \circ f$ is continuous at c.

True

4. If P(x) and Q(x) are polynomials, $Q(c) \neq 0$, then $\lim_{x\to c} \frac{P(x)}{Q(x)} = \frac{P(c)}{Q(c)}$

Time

5. If L and c are real numbers and $\lim_{x\to c} f(x) = L$, then $\lim_{x\to c} \sqrt[n]{f(x)} = \sqrt[n]{L} = L^{1/n}$, n a positive integer.

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Multiple Choice. No work required. 6 points each. Choose the best answer. There is only one correct answer but you may choose up to two. If you choose two and one of the answers is correct. you will receive half the points.

6. Find the average rate of change of the function over the given interval:

 $P(\theta) = \theta^2 - 4\theta + 5$, [1,2] $f(b) - f(a) = \frac{f(z) - f(1)}{z - 1}$

$$= \frac{(2^2 + 1/(2) + 5) - (1^2 + 1/(1) + 5)}{1}$$

$$= 1 - 2 = -1$$

D. 3/2**C**. 3

7. Find the limit:

 $\lim_{y \to 2} \frac{y+2}{y^2 + 5y + 6}$ = \lim_{y \to 2} \left(\frac{y+2}{y+3} \right) \left(\fra

 \mathbf{A} . 0

B. 1/5

C. 1/16

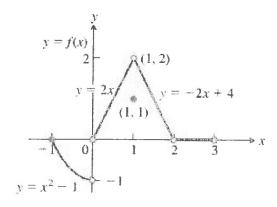
D. Does Not Exist

8. Find the limit:

$$\lim_{x\to -\infty} \left(\frac{x^2+x-1}{8x^2-3}\right)^{1/3}$$

- (A. 1/2)
- B. 1/9
- $\mathbf{C}.0$
- D. Does Not Exist

Use the graph below for questions 9 and 10.



- 9. Using the given graph, find $\lim_{x\to 1^+} f(x)$.
 - **A.** 1
- B. 2
- **C**. 0
- D. Does Not Exist
- 10. Using the given graph, determine whether the function f(x) is continuous at the point x = 2. Explain why or why not.
 - A. f(x) IS continuous at x = 2 as $\lim_{x\to 2} f(x) = f(2)$.
 - C. f(x) is NOT continuous at x = 2 as $f(2) \neq \lim_{x \to 2} f(x)$.
- B. f(x) IS continuous at x = 2 as $\lim_{x\to 2^-} f(x) = \lim_{x\to 2^+} f(x)$.
- D. f(x) is NOT continuous at x = 2 as there is a jump discontinuity there.

Short Answer. You must show all work to receive full credit. If you need more space, use the provided scrap paper and write a note indicating where to find your work.

11. (14 points) Let

$$f(x) = \frac{x^3 + x^2 - 56x}{x - 7}.$$

(a) Does f(x) have a discontinuity? If so, is it removable?

Yes, at
$$x = 7$$

 $\frac{x^3 + x^2 - S6x}{x - 7} = \frac{x(x^2 + x - S6)}{x - 7} = \frac{x(x + 8)(x - 7)}{x - 7}$
Yes, it is removable $= x(x + 8)$

(b) Use limit laws to evaluate

$$\lim_{x \to 7} \frac{x^3 + x^2 - 56x}{x - 7}$$
= $\lim_{x \to 7} \frac{x}{x - 7}$.

12. (20 points) Find the derivative, f'(x), using the limit definition, for the function $f(x) = x^2 + x$.

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h} = \lim_{h \to 0} \frac{(x+h)^2 + (x+h) - (x^2 + x)}{h}$$

13. (16 points) If

$$\lim_{x \to -3} \frac{f(x)}{x^2} = 1, \quad \text{for } f(x)$$

find (a) $\lim_{x\to -3} f(x)$

$$\frac{\left(x^{n}, f(x)\right)}{x^{n-3}} = 1$$

(b)
$$\lim_{x\to -3} \frac{f(x)}{x}$$
 $\frac{f(x)}{x^{\frac{1}{2}-3}}$

Extra Credit (5 points) No partial credit will be given for this problem.

For the given function f(x) and values of L, c, and $\epsilon > 0$ determine the largest value for $\delta > 0$ such that $0 < |x - c| < \delta \Rightarrow |f(x) - L| < \epsilon$.

$$f(x) = 6x + 4,$$
 $L = 34,$ $c = 5,$ $\epsilon = 0.6$

$$|f(x)-L| \le 2$$

 $|6x+4-34| \le 0.6$
 $-0.6 \le 6x-30 \le 0.6$
 $-0.6 \ne 6(x-5) \le 0.6$
 $-0.1 \le x-5 \le 0.1$
 $|x-5| \le 0.1$