## L'HOPITAL'S RULE (4.5)

NAME\_SOLS

In each problem determine if L'Hopital's Rule applies. If so, use the rule to find the limit. If not, find the limit numerically. Express your final answers in exact form.

$$1. \lim_{x \to \pi} \frac{\sin(3x)}{x - \pi}$$

$$\frac{\sin(3\pi)}{\pi - \pi} \rightarrow \frac{0}{0} \vee$$

4. 
$$\lim_{x\to\infty} \frac{e^{-x}}{1+\ln x} \to 0$$

7. 
$$\lim_{y \to 0} \frac{2^{y}}{y^{2}}$$

$$\longrightarrow \frac{1}{\sum_{n \in \mathbb{N}} \sum_{j \in \mathbb{N}} \sum_{k \in \mathbb{N}} \sum_{k \in \mathbb{N}} \sum_{j \in \mathbb{N}} \sum_{k \in \mathbb{N}} \sum_{k \in \mathbb{N}} \sum_{j \in \mathbb{N}} \sum_{j \in \mathbb{N}} \sum_{k \in \mathbb{N}} \sum_{k \in \mathbb{N}} \sum_{j \in \mathbb{N}} \sum_{k \in \mathbb{N}} \sum_{j \in \mathbb{N}} \sum_{k \in \mathbb{N}} \sum_{j \in \mathbb{N}} \sum_{k \in \mathbb{N}} \sum_{k$$

$$2. \lim_{t\to 0}\frac{e^{2t}-1}{e^t}$$

3. 
$$\lim_{\theta \to 0} \frac{\arctan \theta}{2\theta}$$

$$\lim_{\theta \to 0} \frac{1}{1+\theta^2} = \frac{1}{2}$$

$$5. \lim_{x\to\infty}\frac{(\ln x)^2}{x}$$

8. 
$$\lim_{x \to 1^+} \left( \frac{1}{\ln(1+x)} - \frac{1}{x} \right)$$

6. 
$$\lim_{u\to\infty}\frac{\sqrt{u^2+1}}{u}$$

$$\frac{\sqrt{u^{2}+1}}{u} = \frac{\sqrt{u^{2}+1}}{\sqrt{u^{2}}}$$

$$= \frac{\sqrt{u^{2}+1}}{u^{2}}$$

$$= \frac{\sqrt{u^{2}+1}}{u^{2}}$$

$$= \sqrt{1} = 1$$

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9. 
$$\lim_{\theta \to \infty} \theta \sin\left(\frac{1}{\theta}\right)$$

To apply L'H, rewrite:

$$\lim_{\theta\to\infty}\frac{\mathrm{sm}(\frac{1}{\theta})}{\frac{1}{\theta}}\to \frac{0}{0}$$

$$=\lim_{\theta\to\infty}\frac{-\frac{1}{\theta^2}\cos(\frac{1}{\theta})}{-\frac{1}{\theta^2}}$$

$$10. \lim_{z \to 0^+} \cos\left(\frac{1}{z}\right)$$

11. 
$$\lim_{t\to\infty}\cos^2\left(\frac{1}{t}\right)$$

$$= \cos^2(0)$$

$$12. \lim_{x \to 0} \frac{x^2 + 3x}{\sinh x}$$

13. 
$$\lim_{y\to 0} \frac{y}{\sqrt[3]{\sin y}} \to \frac{0}{0}$$

$$=\lim_{y\to 0} \frac{1}{3} \left( \operatorname{siny} \right)^{\frac{2}{3}} \operatorname{cusy}$$

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$$=\lim_{y\to 0} \frac{3}{3} \left( \operatorname{siny} \right)^{\frac{2}{3}} \operatorname{cusy}$$

$$=\lim_{y\to 0} \frac{3}{3$$

14. 
$$\lim_{x\to 0^+} \frac{\cot x}{\ln x} \to \frac{\infty}{-\infty} \to -\frac{\infty}{\infty}$$
 15.  $\lim_{x\to \infty} \frac{x + \sin(2x)}{x}$ 

$$\frac{L'H}{L} \lim_{x \to 0^+} \frac{-CSC^2x}{L_x} \to \frac{\infty}{\infty} = \lim_{x \to \infty} 1 + \frac{SM(2x)}{x}$$

15. 
$$\lim_{x \to \infty} \frac{x + \sin(2x)}{x}$$