## Math 141: Practice Problems for Exam 3 Sections 4.5-5.6

## Questions to Guide Your Review:

- 1. Describe l'Hôpital's Rule. How do you know when to use it and when to stop? Give an example.
- 2. How can you sometimes handle limits that lead to indeterminate forms  $\infty/\infty$ ,  $\infty \cdot 0$ , and  $\infty \infty$ ? Given examples.
- 3. How can you sometimes handle limits that lead to indeterminate forms  $1^{\infty}$ ,  $0^{0}$ , and  $\infty^{\infty}$ ? Give examples.
- 4. Can a function have more than one antiderivative? If so, how are the antiderivatives related? Explain.
- 5. What is an indefinite integral? How do you evaluate one? What general formulas do you know for finding indefinite integrals?
- 6. What is an initial value problem? How do you solve one? Give an example.
- 7. If you know the acceleration of a body moving along a coordinate line as a function of time, what more do you need to know to find the body's position function? Give an example.
- 8. How can you sometimes estimate quantities like distance traveled, area, and average value with finite sums? Why might you want to do so?
- 9. What is sigma notation? What advantage does it offer? Give examples.
- 10. What is a Riemann sum? Why might you want to consider such a sum?
- 11. What is the norm of a partition of a closed interval?
- 12. What is the definite integral of a function f over a closed interval [a, b]? When can you be sure it exists?
- 13. What is the Fundamental Theorem of Calculus? Why is it so important? Illustrate each part of the theorem with an example.
- 14. How is integration by substitution related to the Chain Rule?
- 15. How does the method of substitution work for definite integrals?
- 16. How do you define and calculate the area of the region between the graphs of two continuous functions? Give an example.

## **Practice Exercises:**

- 17. Evaluate the limit:  $\lim_{x \to \infty} \sqrt{4x^2 + 3x} 2x$ .
- 18. A student turns in the incorrect solution to the problem below. Explain the student's mistake in words, using complete sentences. Then work out the correct solution.

$$\lim_{x \to -\infty} x^2 + 5x = (-\infty)^2 + 5(-\infty) = \infty - \infty = 0$$

- 19. If  $30,000 \text{ } cm^2$  of material is available to make a box with a square base and an open top, find the largest possible volume of the box.
- 20. Find f(x) if  $f'(x) = 12x^2 + 6x 4$  and f(1) = 1.
- 21. Evaluate using the Fundamental Theorem of Calculus, Part I.

$$\frac{d}{dx} \int_{1}^{x^2} \sec(t) dt$$

22. Evaluate the following definite integral using (a) the limit (Riemann sum) definition and (b) the Fundamental Theorem of Calculus.

$$\int_0^2 (7-x^2)dx$$

23. Evaluate the indefinite integral.

$$\int \csc\theta(\sin\theta - \csc\theta)d\theta$$

- 24. Find  $\int_{5}^{10} f(x)dx$  if  $\int_{0}^{5} f(x)dx = -12$  and  $\int_{0}^{10} f(x)dx = 2$ .
- 25. Evaluate the indefinite integral.

$$\int \frac{\sin x}{\cos^2 x} dx$$

- 26. The velocity function (in meters per second) for a particle moving along a line is given by  $v(t) = t^2 2t 24$ ,  $1 \le t \le 3$ . Find the displacement of the particle and the total distance traveled by the particle.
- 27. Find the area bounded by the curves  $y = 2 x^2$  and y = -x.