

Sols

MATH 141: QUIZ 2 SECTIONS 2.2, 2.4, 2.5

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Name: _____

No phone or calculator. You must show all work to receive full credit. Simplify your coefficients when applicable.

1. (5 points) Find the following limit:

$$\lim_{h \rightarrow 0} \frac{\sqrt{5h+4} - 2}{h}$$

$$2 \quad \frac{\sqrt{5h+4} - 2}{h} \cdot \frac{\sqrt{5h+4} + 2}{\sqrt{5h+4} + 2} = \frac{5h+4-4}{h(\sqrt{5h+4}+2)} = \frac{5h}{h(\sqrt{5h+4}+2)} \quad 2$$

$$\text{So, } \lim_{h \rightarrow 0} \frac{\sqrt{5h+4} - 2}{h} = \lim_{h \rightarrow 0} \frac{5}{\sqrt{5h+4} + 2} = \frac{5}{\sqrt{4} + 2} = \boxed{\frac{5}{4}} \quad 1$$

2. (5 points) At what points is the following function continuous?

$$y = \sqrt{4x + 28}$$

Not necessary

$$y = f(g(x)) \text{ where } g(x) = 4x + 28 \text{ and } f(x) = \sqrt{x}$$

g is a polynomial so continuous on $(-\infty, \infty)$.

$f(x)$ is continuous for all $x \geq 0$.

So, $y = f(g(x))$ is continuous when

$$g(x) \geq 0 \text{ or } 4x + 28 \geq 0 \quad 3$$

$$4x \geq -28$$

$$\boxed{x \geq -7} \quad 2$$

$$\text{or } [-7, \infty)$$