COMP3048: Lecture 7 Contextual Analysis: Scope II

Matthew Pike

University of Nottingham, Ningbo

This Lecture

An Illustrative Identification Algorithm in Haskell

- LTXL Syntax and Semantics, particularly scope rules.
- Abstract syntax representation
- Environment/Symbol Table representation and operations.
- The Identification Algorithm

Recap: Identification

Identification is the task of relating each applied identifier occurrence to its declaration or definition:

```
public class C {
   int x, n;
   void set(int n) { x = n; }
}
```

In the body of set, the one applied occurrence of

- x refers to the instance variable x
- n refers to the argument n.

Identification for LTXL

We are now going to study a concrete Haskell implementation of identification for LTXL:

Less Trival expression Language

- LTXL \approx TXL + typed definitions + if-expression + new operators
- Slides only show highlights: complete code available on-line.

LTXL CFG (1)

```
Exp \rightarrow Exp \mid Exp \mid Exp \mid Exp \mid Exp \mid
\mid Exp \prec Exp \mid Exp = Exp \mid Exp > Exp
\mid Exp + Exp \mid Exp - Exp
\mid Exp \star Exp \mid Exp \mid Exp
\mid PrimaryExp
```

LTXL CFG (2)

Operator precedence is used to disambiguate. In increasing order of precedence:

- 1. | |
- 2. &&
- 3. <, ==, >
- 4. +, -
- 5. *, /

LTXL CFG (3)

LTXL CFG (4)

LTXL Example 1

```
let
    int a = 10;
    bool b = a < 2
in let
    int c = a * 10;
    bool a = a == 42;
    int d = if a then 1 else 2
in
    if a && b then c else 42
```

LTXL Scope Rules

- 1. The scope of a variable is all subsequent definitions and the body of the let-expression in which the definition of the variable occurs. A variable is **not** in scope in the RHS of its own definition.
- 2. A definition of a variable hides, for the extent of its scope, any definition of a variable with the same name from an outer let-expression.
- 3. At most one definition may be given for a variable in the list of definitions of a let-expression.

LTXL Example 1 (again)

Which scope rules are used where?

```
let
    int a = 10;
    bool b = a < 2
in let
    int c = a * 10;
    bool a = a == 42;
    int d = if a then 1 else 2
in
    if a && b then c else 42
```

LTXL Example 2

What about this LTXL example?

```
let
    int a = 1;
    int b = c * 2;
    bool a = a < 1
in
    a + b</pre>
```

LTXL AST (1)

The following Haskell data types are used to represent LTXL programs.

LTXL AST (2)

```
data UnOp = Not | Neg
data BinOp = Or
             And
             Less
             Equal
              Greater
             Plus
             Minus
             Times
             Divide
```

LTXL AST (3)

Exp is a *parameterized* type. The *type*parameter a allows variables to be *annotated*with an attribute of type a. This facility is used by
the identification function.

LTXL AST (4)

Example: The LTXL program

```
let int x = 7 in x + 35
```

would be represented like this *before* identification (type Exp ()):

(After identification, type will be Exp Attr.)

LTXL Environment (1)

- An association list is used to represent the environment/symbol table to keep things simple.
- By *prepending* new declarations to the list, and searching from the beginning, we will always find an identifier in the closest containing scope. For example:

```
lookup "x" [("x", a_1), ("y", a_2), ("x", a_3)] \Rightarrow a_1
```

 No need for a "close scope" operation. We are in a pure functional setting ⇒ persistent data.

LTXL Environment (2)

The environment associates identifiers with variable attributes. Our attributes are the scope level and the declared type.

The environment is just an association list:

```
type Env = [(Id, Attr)]
```

Note: our environment does *not* store variable *definitions*.

LTXL Environment (3)

Example:

```
let
       int a = 10;
       int b = a + 42
  in let
       bool a = b < 20
  in
       if a then b else 13
Env. after (1): [("a", (1, IntType))]
Env. after (2): [ ("a", (2, BoolType)),
("b", (1, IntType)), ("a", (1, IntType))]
```

LTXL Environment (4)

enterVar inserts a variable at the given scope level and of the given type into an environment.

- Check that no variable with same name has been defined at the same scope level.
- If not, the new variable is entered, and the resulting environment is returned.
- Otherwise an error message is returned.

```
enterVar :: Id -> Int -> Type -> Env
-> Either Env ErrorMsg
```

Aside: The Haskell Type Either

The standard Haskell type Either comes in handy when one needs to represent a value that has one of two possible types:

```
data Either a b = Left a | Right b
```

A typical example is when a function needs to return one of two kinds of results:

LTXL Environment (5)

```
enterVar i l t env
  | not (isDefined i l env)
    = Left ((i,(l,t)) : env)
  | otherwise
    = Right (i ++ " already defined.")
  where
    isDefined i l [] = False
    isDefined i l((i',(l',\underline{\ })) : env)
       | l < l' = error "Should not happen!"
       | 1 \rangle 1' = False
       | i == i' = True
       | otherwise = isDefined i l env
```

LTXL Environment (6)

Let

```
env = [("y", (2, IntType)), ("x", (1, IntType))]
```

Then:

LTXL Environment (7)

lookupVar looks up a variable in an environment.

- Returns variable attributes if found.
- Returns an error message otherwise.

LTXL Environment (8)

Let

Then:

```
lookupVar "y" env

⇒ Left (2,IntType))
lookupVar "x" env

⇒ Left (2,BoolType))
lookupVar "z" env

⇒ Right "z not defined."
```

LTXL Identification (1)

Goals of LTXL identification phase:

- Annotate each applied identifier occurrence with attributes of the corresponding variable declaration.
 - I.e., map unannotated AST Exp () to annotated AST Exp Attr.
- Report conflicting variable definitions and undefined variables.

```
identification ::
    Exp () -> (Exp Attr, [ErrorMsg])
```

LTXL Identification (2)

Example: Before Identification

```
Let [("x", IntType, LitInt 7)]
(BinOpApp Plus
(Var "x" ())
(LitInt 35))
```

After identification:

LTXL Identification (3)

Main identification function:

Type signature for auxiliary identification function:

LTXL Identification (4)

Variable case:

```
identAux l env (Var i _) =
  case lookupVar i env of
  Left a -> (Var i a, [])
  Right m -> (Var i (0, UnknownType), [m])
```

LTXL Identification (5)

Binary operator application (typical recursive case):

```
identAux l env (BinOpApp op e1 e2) =
  (BinOpApp op e1' e2', ms1 ++ ms2)
  where
    (e1', ms1) = identAux l env e1
    (e2', ms2) = identAux l env e2
```

LTXL Identification (6)

Reminder: LTXL scope rules

- 1. The scope of a variable is all subsequent definitions and the body of the let-expression in which the definition of the variable occurs. A variable is *not* in scope in the RHS of its definition.
- 2. A definition of a variable hides, for the extent of its scope, any definition of a variable with the same name from an outer let-expression.
- 3. At most one definition may be given for a variable in the list of definitions of a let-expression.

LTXL Identification (7)

Block of definitions (let):

```
identAux l env (Let ds e) =
  (Let ds' e', ms1 ++ ms2)
  where
```

```
(e', ms2) = identAux l' env' e
```

LTXL Identification (8)

```
identDefs\ l\ env\ [] = ([], env, [])
identDefs\ l\ env\ ((i,t,e)\ :\ ds) =
  ((i,t,e') : ds', env'', ms1++ms2++ms3)
                            i not in scope (rule 1)
  where
    (e', ms1) = identAux l env e
    (env', ms2) = \frac{impl./checks rules 2 & 3}{}
      case enterVar i l t env of
        Left env' -> (env', [])
        Right m -> (env, [m])
    (ds', env'', ms3) = -i in scope (rule 1)
      identDefs l env' ds
```

Efficient Symbol Table Implementation

Lists don't make for very efficient symbol tables. Insertion (at head) is fast, O(1), but lookup is O(n), where n is the number of symbols.

Some more efficient options:

- Balanced trees:
 - Insertion and lookup are both $O(\log n)$.
 - One way of handling nested scopes would be a stack of trees.

Efficient Symbol Table Implementation

Hash tables:

- Insertion and lookup are both O(1) as long as the ratio between the number of symbols and the hash table size is kept below a small constant factor.
- Algorithms such as *linear hashing* allows the table to grow and shrink gracefully, guaranteeing near optimal performance.

See e.g. Aho, Sethi, Ullman (1986) for further details.