

Probabilistic Short-Term Low-Voltage Load Forecasting using Bernstein-Polynomial Normalizing Flows

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Marcel Arpogaus¹ Marcus Voss² Beate Sick³ Mark Nigge-Uricher⁴ Oliver Dürr¹

¹HTWG Konstanz - University of Applied Sciences

²Technische Universität Berlin (DAI-Lab)

³EBPI, University of Zurich & IDP, Zurich University of Applied Sciences

⁴Bosch.IO GmbH

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Probabilistic Short-Term Low-Voltage Load Forecasting

- ▶ Energy sector is the major contributor to greenhouse gas emissions [6]
- ▶ Utilization of renewable energy can be increased by short-term load forecast [3]
- ▶ Especially at the low level the distributions are complex and multimodal
- ▶ Probabilistic forecasts estimate the distribution to quantify uncertainty for more informed decision-making [4]

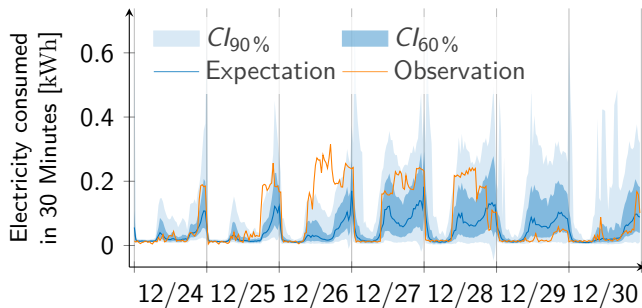
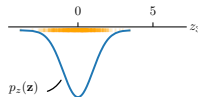
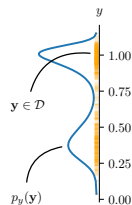


Figure: Exemplary load forecast in Christmas week based on data from [1].

Bernstein-Polynomial Normalizing Flows (BNF)



In a Nutshell

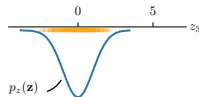
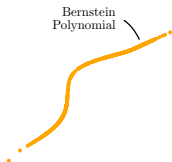
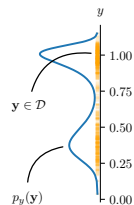
Normalizing Flows fit a parametric bijective function f that transforms between a complex target distribution $p_y(y)$ and a simple distribution $p_z(z)$, often $p_z(z) = N(0, 1)$.

Change of Variable Formula

Evaluate the probability $p_y(y)$ from the simple probability $p_z(z)$ as follows:

$$p_y(\mathbf{y}) = p_z(f(\mathbf{y})) |\det \nabla f(\mathbf{y})|^{-1} \quad (1)$$

Bernstein-Polynomial Normalizing Flows (BNF)

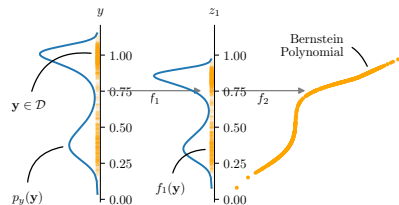


- ▶ Bernstein polynomials h^M of order M , approximate any function on $y \in [0, 1]$ [2].
- ▶ M controls the flexibility at no cost to the training stability [5].

$$h^M(y) = \frac{1}{M+1} \sum_{i=0}^M \text{Be}_i^M(y) \vartheta_i(\mathbf{x})$$

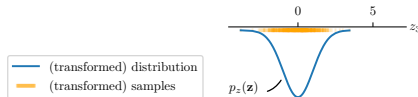
With covariates \mathbf{x} such as lagged power consumption at earlier time steps, holiday indicator and calendar variables.

Bernstein-Polynomial Normalizing Flows (BNF)



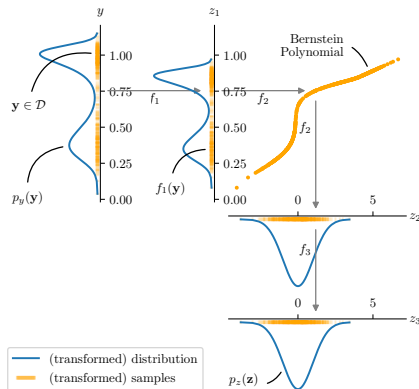
$$f_1 : z_1 = a_1(\mathbf{x}) \cdot y - b_1(\mathbf{x})$$

$$f_2 : z_2 = \frac{1}{M+1} \sum_{i=0}^M \text{Be}_i^M(z_1) \vartheta_i(\mathbf{x})$$



With covariates \mathbf{x} such as lagged power consumption at earlier time steps, holiday indicator and calendar variables.

Bernstein-Polynomial Normalizing Flows (BNF)



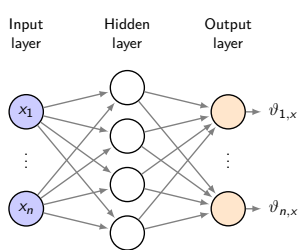
$$f_1 : z_1 = a_1(\mathbf{x}) \cdot y - b_1(\mathbf{x})$$

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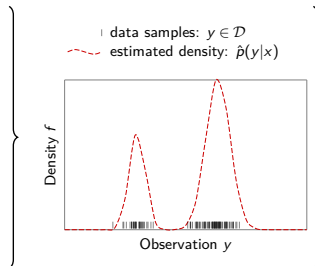
$$f_3 : z_3 = a_2(\mathbf{x}) \cdot y$$

With covariates \mathbf{x} such as lagged power consumption at earlier time steps, holiday indicator and calendar variables.

Maximum Likelihood Estimation



Neural Network:
 $n(\mathbf{x}, \omega) = \theta_x$ with $\mathbf{x} = [x_1, \dots, x_n]^T \in \mathcal{D}$



Conditioned probability density:
 $\hat{p}(y, \theta_x)$ with $\theta_x = [v_{1,x}, \dots, v_{n,x}]^T \in \Theta$

Choose the parameters of the model so that the observed data has the *highest likelihood*.

$$\mathcal{L}(\mathcal{D}|\omega) = \prod_{i=1}^m \hat{p}(y_i, n(\mathbf{x}_i, \omega))$$

$$\hat{\omega} = \arg \max_{\omega \in \Omega} \{ \mathcal{L}(\mathcal{D}|\omega) \}$$

Maximum likelihood estimation

Results of empiric experiments

Architecture	Model	CRPS	NLL	MAE	MSE
FC	BNF (ours)	0.021	-123.157	0.414	9.430
FC	GMM	0.026	-114.892	0.360	0.464
FC	GM	1.314	-75.101	1.027	53.203
FC	QR	0.026	-	0.415	4.351
1DCNN	BNF (ours)	0.017	-132.089	0.342	0.429
1DCNN	GMM	0.019	-125.933	0.384	0.450
1DCNN	GM	0.018	-101.290	0.347	0.366
1DCNN	QR	0.017	-	0.321	0.399

Abbreviations

- FC Fully connected neural network
- 1DCNN dilated 1D-Convocational neural network
- BNF Bernstein-Polynomial Normalizing Flow
- GM Gaussian model
- GMM Gaussian mixture model
- QR Quantile regression

- CRPS Continuous ranked probability score
- NLL Negative logarithmic likelihood
- MAS Mean absolute Error
- MSE Mean Squared Error

Summary

- ▶ BNFs are a powerful and stable method to express complex distributions, with almost no regularization or special tuning.
- ▶ This makes them a preferential choice over quantile regression or mixture models for probabilistic load forecasts.
- ▶ BNFs allow sampling from the learned distribution to generate synthetic load data for research or scenarios used for grid planning.

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Thanks for your interest, especially also on behalf of my colleagues:

- ▶ Marcus Voss
- ▶ Beate Sick
- ▶ Mark Nigge-Uricher
- ▶ Oliver Dürr

Marcel Arpogaus

PhD Student at the University of Applied Sciences Konstanz

[eMail](mailto:marcel.arpogaus@htwg-konstanz.de) marcel.arpogaus@htwg-konstanz.de

[GitHub](#) /MArpogaus/stplf-bnf

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